# A Curve and Surface Fitting Tool for Octave

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#### 1 Goal

Create a tool similar to the cftool in MATLAB seen in Figure 1. Essential features:

- Create a simple GUI, such that simple regression problems can be solved without the command line.
- The GUI should allow to define arbitrary functions, apply regression and display numerical and graphical results.
- Do not try to create an exact copy of cftool(), since there would be too many features to implement.

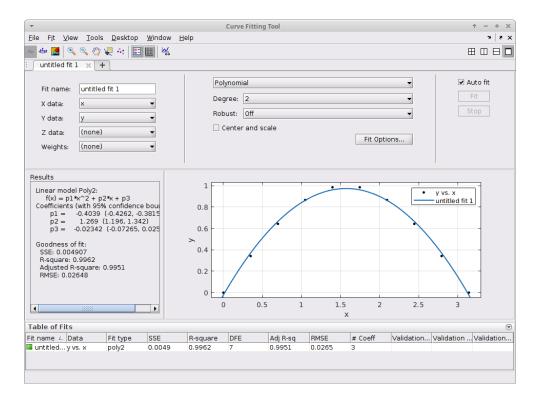


Figure 1: The very popular curve fitting tool cftool in MATLAB

#### 2 The first versions of FitTool.m and FitToolNL.m

Currently the functions LinearRegression(), nonlin\_curvefit() and curvefit\_stat() are used to perform linear or nonlinear regression. The commands are part of the package optim in *Octave*. On Win\* systems this is most often already installed and on Linux systems apply the commands pkg install -forge optim.

The code for LinearRegression.m can be downloaded from the web site of your author at AndreasStahel.github.io/Octave.html.

#### 2.1 General usage of the functions FitTool() and FitToolNL()

The tools FitTool and FitToolNL will

FitTool: use linear regression to determine the best fitting linear combination of the selected basis functions to approximate the given data, depending on one or two independent variables.

FitToolNL: use a nonlinear regression to attempt to find the best parameters to fit the given function to the given data, depending on one or two independent variables.

#### 2.1.1 Perform a linear regression, using FitTool()

• Generate some random data and start FitTool().

```
Cotave
x_in = 1.5 + 0.3*randn(10,1); y_in = sin(x_in) + 0.01*randn(10,1);
FitTool("1D")
```

- Since the variables in the base context are called x\_in and y\_in their values are used inside the function FitTool and have to be entered in the boxes on the top left in Figure 2. Once the names of the variables are entered the raw data will be displayed.
- The expressions in the input boxes for x and y are evaluated in the base context. Thus one may apply simple operations, e.g. to read in the values of y use  $sin(x_in)$  in the y-box.
- The help button on the top right provides an elementary help description.
- The 1D/2D button switches between the versions for one or two independent variables.
- The export/import button allows to export or import some of the fitting data to the base context. A dialog box will ask for the name of the variable to be exported or imported. The result is a cell array with three or four entries:
  - 1. The first entry is the string with the formula for the regression matrix **M** of the function f(x)
  - 2. The second entry is a column vector with the optimal values of the parameters  $p_i$ .
  - 3. The third entry is a column vector with the estimated values of the standard deviations of the parameters  $p_i$ .
  - 4. For FitToolNL() the forth entry is a row vector with the initial values of the parameters used.

On import the formula for the regression matrix M or the function f(x) is copied into the corresponding box in the GUI, but not evaluated. Hit the Enter key in the box to evaluate.

• For FitToolNL() the the optimal values of the parameters will used as new initial values for the parameters. This allows the iteration to be run with other initial values for the parameters.

#### 2.1.2 Linear regression with one independent variable

• Within FitTool select a quadratic polynomial  $f(x) = p_1 x^0 + p_2 x^1 + p_3 x^2$  leading to the string 1

$$\mathbf{M} = [x. \wedge 0, x. \wedge 1, x. \wedge 2]$$

in the box for the matrix M to be used for the linear regression.

- You may edit the box with the regression matrix. Hit the Enter key in the box and the linear regression will be performed.
- In Figure 2 the raw data and the best fitting parabola are displayed.

<sup>&</sup>lt;sup>1</sup>The silly trick of  $x^0$  generates a vector of the correct size filled with numbers 1.

- On the left find the numerical results:
  - The mean residual

$$r_{\text{mean}} = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (y_i - f(x_i))^2}$$
.

- The square or the Pearson correlation coefficient R2.
- The values of the optimal parameters and their estimated standard deviation. In the above example

$$p_1 = -0.0743 \pm 0.0239$$
  
 $p_2 = +1.3372 \pm 0.0512$ .  
 $p_3 = -0.4160 \pm 0.0208$ 

• In the drop down selection of functions only polynomials are provided. The box with the regression matrix  $\mathbf{M}$  can be edited and thus any linear regression can be performed. To fit a function  $f(x) = p_1 \sin(3x) + p_2 \cos(3x) + p_3 \exp(x)$  use the string

$$\mathbf{M} = [\sin(3*x), \cos(3*x), \exp(x)].$$

This string could also be used to import a cell structure into the GUI FitTool. In the base context create FitExpTrig.

```
Octave

FitExpTrig{1} = "[ sin(3*x), cos(3*x), exp(x) ]" ;

FitExpTrig{2} = [ 0, 0, 0] ;

FitExpTrig{3} = [ 0, 0, 0] ;
```

Then import FitExpTrig into the GUI, using export/import, and perform the regression by using the Enter key in the matrix box.

#### 2.1.3 Linear regression with two independent variables

- By clicking on the 1D/2D button the GUI switches between one or two independent variables.
- Obviously values of x, y and z are required now. In the base context (i.e. the usual command window of Octave) create the data.

```
x = 2*randn(5); y = 2 + randn(5);
z = 1 + x - y + 0.5*x.*y;
```

• Then select a quadratic polynomial of two variables to obtain Figure 3. The numerical results confirm the best fit

$$f(x,y) = 1 + x - y + 0.5 x \cdot y$$

with outstanding accuracy. This is no surprise, since exact data was used.

For functions of two variables fewer functions are predefined, see Table 1.
 By editing the box with the regression matrix M any linear combination of functions can be used.

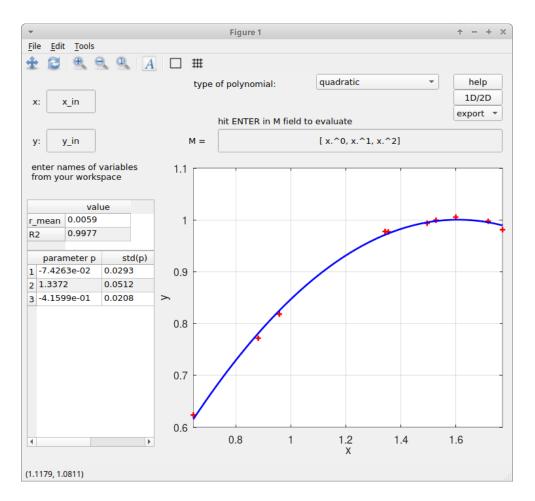


Figure 2: The curve fitting tool FitTool, using one independent variable

```
Constant f(x,y) = p_1

Linear f(x,y) = p_1 + p_2 x + p_3 y

Quadratic f(x,y) = p_1 + p_2 x + p_3 y + p_4 x^2 + p_5 x y + p_6 y^2

Cubic f(x,y) = p_1 + p_2 x + p_3 y + p_4 x^2 + p_5 x y + p_6 y^2 + p_7 x^3 + p_8 x^2 y + p_9 x y^2 + p_{10} y^3
```

Table 1: Predefined functions for linear regression with two variables

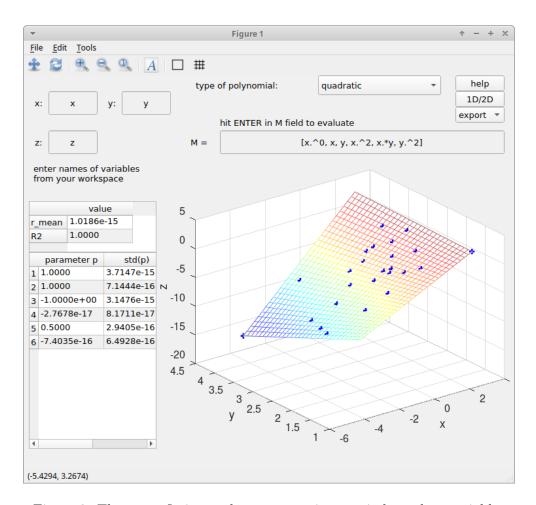


Figure 3: The curve fitting tool FitTool, using two independent variables

#### 2.1.4 Nonlinear regression with one independent variable, using FitToolNL()

There is a second tool FitToolNL.m to perform a nonlinear regression with respect to one or two independent variables. It is using the commands nonlin\_curvefit() and curvefit\_stat() from the package optim. Thus the package has to be available.

The usage of FitToolNL() is very similar to the above FitTool().

• First generate the data and then launch the tool.

```
x = linspace(0,1,20);
FitToolNL()
```

- To work with the generated data  $y = \exp(-x^2)$  enter the string  $\exp(-x \cdot \lambda^2)$  into the y-box.
- Then select a rational function of the type

$$f(x) = \frac{p_1 + p_2 x}{1 + p_3 x + p_4 x^2} .$$

The parameters  $p_i$  are all initialized to 0. Using the box with the function and hitting the Enter key in the "f(x) =" field leads to Figure 4.

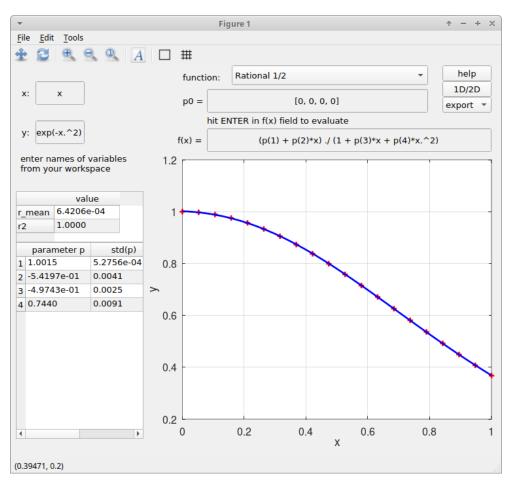


Figure 4: The nonlinear curve fitting tool FitToolNL, using one independent variable

- Since you can edit the function f(x) freely any type of nonlinear regression can be performed. The critical part is most often the choice of good initial values for the parameters  $p_i$ . The tool only provides naive initial guesses.
- The tool provides a few prototypes for functions for nonlinear regression with one independent variable, see Table 2.

```
f(x) = p_1 + p_2 x
Polynomial, linear
                                     f(x) = p_1 + p_2 x + p_3 x^2
Polynomial, quadratic
                                     f(x) = p_1 + p_2 x + p_3 x^2 + p_4 x^3
Polynomial, cubic
                                     f(x) = p_1 \cos(p_3 x) + p_2 \sin(p_3 x)
Trigonometric
                                     f(x) = p_1 \cos(p_3 x) + p_2 \sin(p_3 x) + p_4 + p_5 x
Trigonometric and linear
Exponential
                                     f(x) = p_1 \exp(p_2 x)
                                     f(x) = p_1 + p_2 \exp(p_3 x)
Exponential and constant
                                     f(x) = p_1 + p_2 x + p_3 \exp(p_4 x)
Exponential and linear
                                     f(x) = p_1 \exp(p_2 x) + p_3 \cos(p_5 x) + p_4 \sin(p_5 x)
Exponential and trigonometric
Double exponential
                                     f(x) = p_1 \exp(p_2 x) + p_3 \exp(p_4 x)
                                     f(x) = p_1 \exp(\frac{(x-p_2)^2}{2p_3^2})
Gaussian
Rational 1/2
Rational 2/2
```

Table 2: Predefined functions for nonlinear regression with one variable

#### 2.1.5 Nonlinear regression with two independent variables

The procedure is similar to FitToolNL() with one independent variable. Create some data and launch the GUI.

```
Cotave
x = 2 + randn(6); y = 2*randn(6);
z = 1 - x + x.^2 - 3*x.*y + 0.1*randn(6);
FitToolNL("2D")
```

Then select a quadratic polynomial of two variables to obtain Figure 5.

For functions of two variables fewer functions are predefined, see Table 3. By editing the

```
Polynomial, linear f(x,y) = p_1 + p_2 x + p_3 y

Polynomial, quadratic f(x,y) = p_1 + p_2 x + p_3 y + p_4 x^2 + p_5 x y + p_6 y^2

Trigonometric f(x,y) = p_1 \cos(p_3 x) + p_2 \sin(p_3 x) + p_4 \cos(p_6 y) + p_5 \sin(p_6 y)

Exponential f(x,y) = p_1 \exp(p_2 x + p_3 y)

Exponential and constant f(x,y) = p_1 + p_2 \exp(p_3 x + p_4 y)

Gaussian f(x,y) = p_1 \exp(-(p_4 (x - p_2)^2 + p_5 (x - p_2)(y - p_3) + p_6 (y - p_3)^2))
```

Table 3: Predefined functions for nonlinear regression with two variables

function f(x,y) a nonlinear regression with any type of function can be attempted.

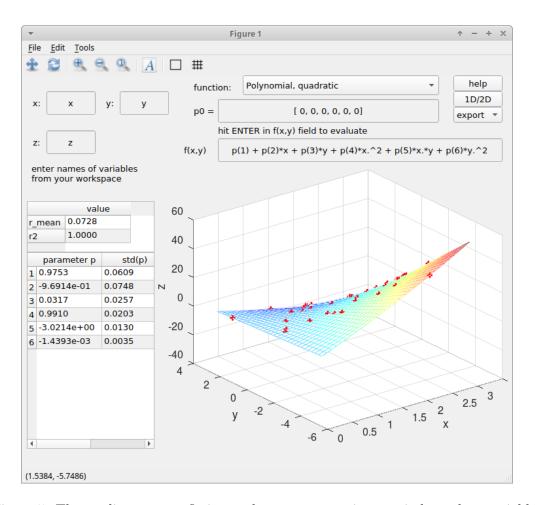


Figure 5: The nonlinear curve fitting tool FitToolNL, using two independent variables