

# Deep Illumination-Driven Light Probe Placement

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**ΤΜΗΜΑ ΜΗΧ. Η/Υ & ΠΛΗΡΟΦΟΡΙΚΗΣ**

**ΠΑΝΕΠΙΣΤΗΜΙΟ ΙΩΑΝΝΙΝΩΝ**

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# **Dedication**

To my mother, father, and brother, who always helped me achieve my goals.

# Acknowledgments

First and foremost, I would like to express my sincere gratitude to my supervisor, Prof. Ioannis Fudos, for his invaluable guidance, feedback, and support. As an advisor, he always made time, was extraordinarily patient, and his suggestions were instrumental in the completion of this thesis.

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I dedicate this thesis to them.

# Abstract

Realistic lighting is a cornerstone of visually compelling 3D graphics. Unity’s LightProbe system offers an efficient way to capture and interpolate baked Global Illumination (GI) data across dynamic objects in scenes. However, manual placement of light probes in complex scenes is both time-consuming and error-prone, greatly delaying the iteration process when making 3D applications. This thesis presents an automated, deep learning-based approach that predicts per-point importance scores for light probe placement using a PointNet-inspired neural network.

We first generate a regular 3D point grid that conforms to the user-defined arbitrarily-shaped bounds of the scene. We sample per-point lighting information, including spherical harmonics, light-, normal-, and RGB- variance, and occlusion factor as well. These features capture important information that drive GI accuracy. The data is then converted into a concise feature vector at each location, used to then train the PointNet-style AI model that consumes an arbitrary-length list of such feature vectors and outputs a probability in the range 0-1, depicting how vital it is to place a light probe at each point on the grid.

To deploy in Unity, the trained model is then exported to an .ONNX file and imported via Sentis, the official Unity package for handling AI models inside a Unity Runtime; at edit-time, it ingests per-point scene data and returns per-point importance values. Predicted high-importance locations are then used to populate a Unity LightProbeGroup object, giving developers immediate, visually appropriate probe distributions, with easy to control thresh-holding if higher- or lower-importance locations are desired.

We demonstrate that our AI model generalizes across grid sizes and shapes without retraining, as well as giving immediate results for any scene. Although our evaluation remains mostly qualitative, based on visual inspection of GI results and light-probe placement across a variety of indoor and outdoor scenes, we consistently observe that the generated probe layouts capture important scene light-data with minimal or no manual tweaking. By replacing manual probe placement with a simpler AI-based workflow, artists and developers save time and achieve a faster iteration process throughout the development of a 3D application.

# Περίληψη

Ο αληθινόφανής φωτισμός είναι ο ακρογωνιαίος λίθος των οπτικά ελκυστικών τρισδιάστατων γραφικών. Το σύστημα φωτο-ανιχνευτών (Light-Probe) της μηχανής γραφικών Unity παρέχει έναν αποδοτικό τρόπο καταγράφης και να παρεμβολής προπαρασκευασμένων δεδομένων παγκόσμιου φωτισμού (Global Illumination) προς όλα τα δυναμικά αντικείμενα μιας σκηνής. Πάραντα, η χειροκίνητη τοποθέτηση των φωτο-ανιχνευτών σε πολύπλοκες σκηνές είναι μια χρονοβόρα διαδικασία, αλλά και επιρρεπής σε λάθη, δημιουργώντας μεγάλες καθυστερήσεις κατά την διάρκεια κατασκευής τρισδιάστατων εφαρμογών. Η διπλωματική αυτή παρουσιάζει μία αυτοματοποιημένη μέθοδο βαθιάς μάθησης η οποία προβλέπει τον βαθμό σημαντικότητας ανά σημείο για τα σημεία τοποθέτησης των φωτο-ανιχνευτών, χρησιμοποιώντας ένα νευρωνικό δίκτυο εμπνευσμένο από το PointNet.

Αρχικά δημιουργούμε ένα κανονικό τρισδιάστατο πλέγμα σημείων το οποίο προσαρμόζεται στα αυθαίρετα δομημένα όρια της σκηνής, ορισμένα από τον χρήστη. Δειγματολειπούμε πληροφορίες φωτισμού ανά σημείο, συμπεριλαμβάνοντας σφαιρικές αρμονικές, διακυμάνσεις φωτισμού, κανονικών επιφάνειας, και RGB, όπως και παράγωντα απόφραξης. Τα χαρακτηριστικά αυτά εμπεριέχουν σημαντικές πληροφορίες που ωθούν την ακρίβεια του παγκόσμιου φωτισμού. Στην συνέχεια τα δεδομένα δειγματοληψίας μετατρέπονται σε ένα συνεκτικό διάνυσμα χαρακτηριστικών ανά σημείο, και χρησιμοποιούνται για την εκπαίδευση του PointNet-τύπου μοντέλου τεχνητής νοημοσύνης. Το μοντέλο αυτό καταναλώνει μία αυθαίρετου μήκους λίστα από συνεκτικά διανύσματα χαρακτηριστικών και εξάγει μια πιθανότητα σε εύρος 0 έως 1, η οποία αναπαριστά την κρισιμότητα τοποθέτησης ενός φωτο-ανιχνευτή σε κάθε σημείο στο πλέγμα.

Στην μηχανή Unity, το εκπαίδευμένο μοντέλο εξάγεται σε ένα αρχείο τύπου .ONNX και εισάγεται μέσο του Sentis, του επίσημου πακέτου της Unity για χειρισμό μοντέλων τεχνητής νοημοσύνης εντός του εκτελέσιμου της Unity κατά την επεξεργασία, καταναλώνει δεδομένα σκηνής ανά σημείο και επιστρέφει τιμές χρισμότητας ανά σημείο. Οι προβλεπόμενες τοποθεσίες υψηλής σημασίας χρησιμοποιούνται για να συμπληρώσουν μια ομάδα φωτο-ανιχνευτών, αντικείμενο της Unity, παρέχοντας στους χρήστες άμεση και οπτικά κατάλληλη κατανομή των φωτο-ανιχνευτών, με ευκολόχρηστη κατωφλίωση όταν υψηλότερης ή χαμηλότερης σημασίας τοποθεσίας είναι επιθυμητές.

Επιδεικνύουμε ότι το τεχνητής νοημοσύνης μοντέλο μας γενικεύει ανάμεσα σε πλέγματα με διάφορα μεγέθη και σχήματα, χωρίς την ανάγκη επανεκπαίδευσης, όπως και ότι παρέχει άμεσα αποτελέσματα για κάθε σκηνή. Παρόλο που η αξιολόγησή μας παραμένει κυρίως ποιοτική, βασιζόμενη στον οπτικό έλεγχο του αποτελέσματος παγκόσμιου φωτισμού, όπως και τα σημεία τοποθέτησης των φωτο-ανιχνευτών σε ένα εύρος από εσωτερικών και εξωτερικών χώρων, παρατηρούμε συστηματικά πως η παραγόμενη διάταξη των φωτο-ανιχνευτών περιλαμβάνει σημαντικά δεδομένα φωτισμού της σκηνής με ελάχιστη ή μηδενική χειροκίνητη προσαρμογή. Αντικαθιστώντας την χειροκίνητη τοποθέτηση των προβες με την απλή χρήση ενός μοντέλου τεχνητής νοημοσύνης, οι καλιτέχνες και οι προγραμματιστές κερδίζουν χρόνο και επιταχύνουν την διαδικασία ανάπτυξη μιας τρισδιάστατης εφαρμογής.

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# Chapter 1

## Introduction

Modern interactive 3D applications, like video games, VR/AR apps, simulators etc., depend on believable lighting interactions with the objects of a 3D scene to achieve the desired visual goals, while trying to maintain real-time frame-rate budgets, typically above 30 Frames per Second (FPS). Achieving visual fidelity and performance can be a difficult task and sometimes impossible with the given hardware specifications of the device. For that reason, modern real-time rendering engines, e.g. Unity, Unreal Engine, Godot and others, depend on a number of methods to balance those metrics.

The illumination of any scene can be split into two very simple categories. Direct Illumination, the light that travels unoccluded from a light source to a surface of an object, is typically handled with techniques like shadow-mapping or screen-space shadows, yielding crisp, high-framerate-capable shadows, but lack in inter-surface light transport situations. In contrast, Indirect Illumination, or Global Illumination (GI), captures light that has bounced or refracted off one or more surfaces, producing soft shadows, color bleeding, and contextually rich shading.

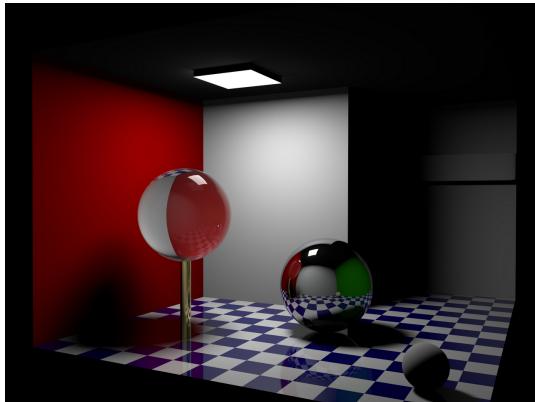


Figure 1.1: Scene lighting with direct illumination only. By Barahag - Own work, CC BY-SA 4.0

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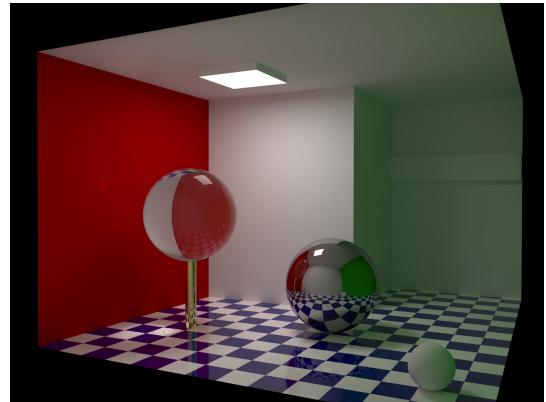


Figure 1.2: Scene lighting with Global illumination. By Barahag - Own work, CC BY-SA 4.0

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The field-standard for accurate lighting and shadows in a scene is Path-Tracing, a method that tracks every light ray and any interactions it has with the objects of a 3D scene and calculates the resulting color for each pixel of the screen. Such approach remains prohibitively expensive for most interactive applications, so real-time systems employ pre-computation and approximation of the illumination of the scene; static geometry is baked into lightmaps that store per-texel irradiance, while dynamic elements sample from irra-

diance volumes or light probes, sparse 3D points whose spherical-harmonic coefficients are interpolated at runtime.

Screen-space GI methods typically approximate a limited number of light-ray bounces directly from the camera’s depth buffer, but suffer from missing contextual information outside the camera’s view frustum and temporal instability. Voxel-based approaches (e.g., cone-tracing through a low resolution 3D grid) enable more dynamic multi-bounce effects at the cost of memory, processing cost and potential blurring of fine detail.

Across all these techniques, the central challenge is allocating a strict millisecond-scale budget to indirect illumination while maintaining consistency across static and dynamic scene content, avoiding visible seams when blending baked and runtime solutions and fitting within GPU memory constraints.

Light probes, in particular, represent a compelling middle-ground, flexible enough to illuminate moving objects without rebaking yet compact enough for real-time evaluation, making their optimal placement a critical factor in any high-quality GI pipeline.

## 1.1 Related Work

There is an abundance of work in the literature addressing the problem of Global Illumination. These studies aim to achieve realistic lighting in 3D scenes by employing various approaches and techniques, each offering unique advantages and disadvantages, but they share a common goal: to maximize visual fidelity while minimizing computational costs.

### 1.1.1 Offline Methods

Offline Illumination methods refer to techniques that are not viable for real-time applications and are therefore used only in situations where the importance of high visual fidelity far outweighs the need for computational speed, typically in non-interactive 3D renders, most commonly in movies or pre-rendered scenes. Classic Path-Tracing, first introduced in 1986 (Kajiya 1986), tracks the movement of a photon ray emitted from a source, typically the camera, and simulates physics interactions to calculate the color of each screen pixel accurately. The immense computational cost of path-tracing led to the development of performance improvements, such as the Metropolis Light Transport (MLT) method introduced in 1997 (Veach and Guibas 1997), and variants like bi-directional Path-Trace (Lafortune and Willem 1993), which build on Monte-Carlo algorithms (Lafortune 1996).

### 1.1.2 Online Methods

In contrast, online methods aim to calculate GI interactions in real-time, most commonly used in interactive applications like video games or simulations. They try to balance performance and accuracy, a task that is often difficult due to the processing cost of the calculations for a realistic result. Therefore, these methods take shortcuts, either approximating the GI interactions to a certain degree to maintain framerate budgets, or by precomputing some of the data, wherever possible.

## Traditional Methods

Techniques that precompute the illumination of a scene only do so for static geometry; objects in the scene that will never change their position, rotation or scale. The algorithms “bake” the required information onto texture maps, which are rendered as such when needed. Light-mapping is one such technique. It precomputes surface brightness and

has a low runtime cost. The game Quake was the first interactive application that used lightmaps for rendering GI (Wikipedia contributors 2025).

Another early technique is the Irradiance Volumes algorithm (Greger et al. 1998), which scatters spherical-harmonic (SH) irradiance samples on a 3D grid on the scene. At runtime, lighting is interpolated from the nearest SH cells; this underlies many probe systems, like Unity’s light-probe system that implicitly implements a sparse irradiance volume.

More recent static-GI algorithms include Light Field Probes (McGuire et al. 2017). Light Field Probes extend standard irradiance probes by additionally storing per-texel visibility for each probe. Furthermore, (Xu et al. 2022) introduce Discrete Visibility Fields for static ray-traced lighting. The method precomputes occlusion masks stored in a uniform voxel grid, and at runtime, rays that hit a cell use the stored precomputed masks to quickly cull visibility, skipping geometry already known to be occluded.

Unity’s new Adaptive Probe Volumes (APV) build on irradiance volumes by automatically populating a grid, with density matched to local geometry. APV then performs per-pixel probe sampling; each pixel blends from the eight nearest probes (Unity 2025).

Additionally, there are methods that don’t focus on Probes for GI. A prevalent example is Unreal Engine’s Lumen, a dynamic GI and reflections system that uses a hybrid tracing approach; It starts with a cheap screen-space or signed-distance-field ray cast, and then falls back to more expensive methods like hardware ray tracing (EpicGames 2025).

NVIDIA has also developed RTXGI, a GPU-accelerated library implementing Dynamic Diffuse GI, using a volumetric grid of irradiance probes, which update every frame using hardware-accelerated ray tracing, creating accurate results at the cost of hardware-restricted algorithms and a relatively escalated cost of calculation (Nvidia 2024).

In 2011 (Crassin et al. 2011) , a Voxel Cone Tracing (VCT) technique was introduced to approximate real-time GI. In VCT, the scene’s static geometry and lighting are ”voxelized” into a 3D texture with multiple levels of mipmapping, containing radiance and opacity. At runtime, indirect illumination is approximated by tracing a few low-resolution ”cones” from each surface sample into the aforementioned voxel grid, summing the values from regions of voxels.

Even though there are numerous methods trying to solve real-time GI issues, a big percentage of them tend to revolve around probes of various types; most commonly calculating irradiance values among other high-importance metrics. Therefore, it is vital for a 3D scene to have proper probe placement for best results. There are a few methods that try to automate that process, often by placing the probes in a regular grid and only removing the probes that are inside objects, but that can lead to over-sampling, leading to performance costs, mainly in memory usage budgets. Furthermore, some techniques try to remove additional probes using heuristic methods, therefore approaching optimal placement, but with a significant precomputational cost.

In (Wang et al. 2019), an automatic non-uniform placing scheme is introduced, which uses 3D scene skeletons and gradient-descent refinement to cover important locations without redundant probes. A very recent work formulates geometry-based optimization of probe placement using various mesh features, to further improve the lighting in VR/AR scenarios (Teuber et al. 2024).

Similarly, (Vardis, Vasilakis, and Papaioannou 2021b) approach the problem by starting with a probe set on a dense grid and iteratively removing the least-important probes using radiance error tests, preserving the global light field while minimizing probe count.

## AI-based Methods

Recently, AI-assisted methods have started to be developed in order to improve GI in 3D applications, specifically in probe-based solutions. In (Guo et al. 2022), they propose a hybrid neural probe GI. They use a gradient-based search to re-project stored probe radiance for any view, therefore eliminating parallax, and then apply a small neural network to reconstruct high-quality images from low-resolution probe data. Related, a Neural Light Field Probes method has been introduced (You, Geiger, and Chen 2024), which works by decomposing a scene into a grid of trainable light field probes. Each of these probes encodes local radiance and visibility in a compact feature map. Finally, a neural network optimizes these probes so that the summation of their contributions reproduces the full scene lighting.

## 1.2 Thesis Structure

The structure of the remainder of this thesis will be described shortly. Chapter 2, titled Background, covers important information about light probes and their implementation, describes the AI model basis that was used for our implementation, and introduces the tools and technologies that were used in this thesis. Chapter 3, titled Our Approach, presents our method, describes the implementation of the algorithms used, and explains how each part is combined to create the Light-Probe Neural Network (LPNN), our neural network system that attempts to speed up light probe placement in Unity 3D scenes by predicting importance values for the given grid set and placing only the most vital light probes, affected by a user-controlled threshold value. Each grid position gathers samples of a few metrics, which are then used by the neural network to decide whether or not it is vital to place a light probe in each individual cell of the 3D grid. A step-by-step process of creating the grid, getting the features out of the grid cells, and placing the probes and baking the global illumination inside Unity. Additionally, the feature set can be used to retrain the AI model, we explain how to create the labels needed for the process, and how to import the new model to Unity using Sentis for usage. Chapter 4, titled Experiments, presents an experimental comparative and qualitative evaluation between the proposed method and some of the already introduced algorithms. Finally, Chapter 5, titled Conclusions and Future Works, concludes the thesis and proposes directions for future work based on this thesis.

# Chapter 2

## Background

In this chapter we introduce some basic, required background for this thesis. First, we introduce light probes and the mathematical equations that define them. Then, we present the AI architecture that was the basis of our AI model. Finally, the tools and technologies used for this thesis are presented.

### 2.1 Light Probes

As mentioned previously, the idea of using discrete probes to capture scene lighting data traces back to early GI research. In the paper (Greger et al. 1998) introduced the irradiance volume, a 3D grid of sample points storing the irradiance field to approximate GI in complex scenes. A light probe samples the incident radiance at a point in empty space from all directions. Often just the diffuse component of the radiance is captured, since it most commonly varies smoothly, so it can be compactly represented by projecting the lighting onto a truncated spherical harmonic (SH) basis. Third-order SH is most commonly used, storing 9 coefficients per color channel, abbreviated to L2-SH.

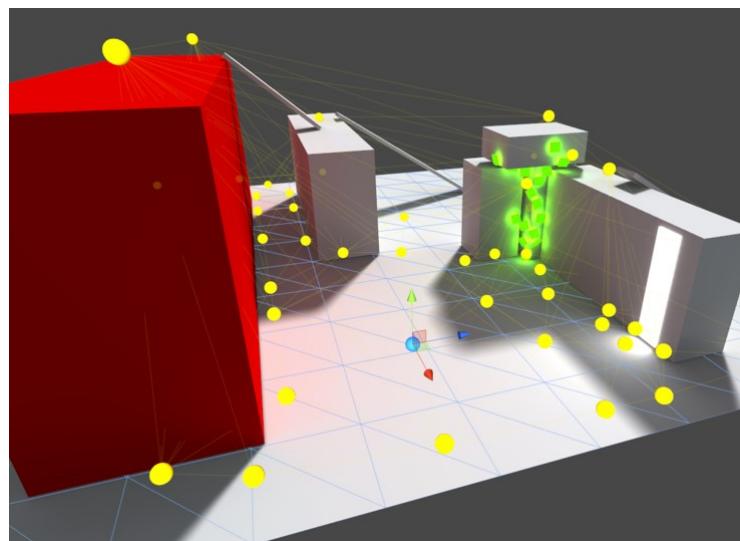


Figure 2.1: A 3D Scene showing a few light probes placed in important locations (Unity 2016).

## 2.2 Spherical Harmonics

Spherical Harmonics (SH), first introduced by Pierre Simon de Laplace, are a method of storing information on a point in space. They are categorized in structures called orders. We are interested in third-order SH, since they represent a good middle ground between storage size, computational cost and accuracy. SH are often described as the Fourier Series of functions on the surface of a sphere, breaking down any pattern of light on a sphere into a set of basis frequencies. The order of SH depicts the amount of data we capture, third-order SH, noted as L2 SH, store the first three bands of data, resulting in 9 coefficients per color channel. Bands represent the individual frequencies; the Zeroth band captures the overall average lighting present in that position in space, the First band captures simple directional gradients, and the Second band captures quadratic variations, e.g. gentle light gradients and their shadows.

## 2.3 PointNet

PointNet (Qi et al. 2017) is a neural-network architecture designed to work directly on unordered 3D point-clouds; a collection of points without any required grid connectivity. Each point passes through a small MultiLayer Perceptron (MLP), extracting a feature vector that describes its local attributes, e.g. color and normal. After per-point features are computed, PointNet aggregates them into a global descriptor by applying a symmetric operation, usually max-pooling across all points, capturing the strongest signal from the features. Then, the global descriptor is concatenated back to the per-point features, resulting in every point having knowledge about both its characteristics and the broader context. Finally, a per-point MLP refines these combined values into task-specific outputs, commonly classification scores or per-point importance metrics.

Since there is no fixed grid, meaning the points are assumed to be unordered and irregular, traditional CNNs can't be applied directly. Additionally, since PointNet predicts values per-point, it can be used to handle point clouds of any shape and point amount without retraining, limited only by the system's memory. This makes PointNet a fitting candidate to base our model on, with the implementation being the only varying factor.

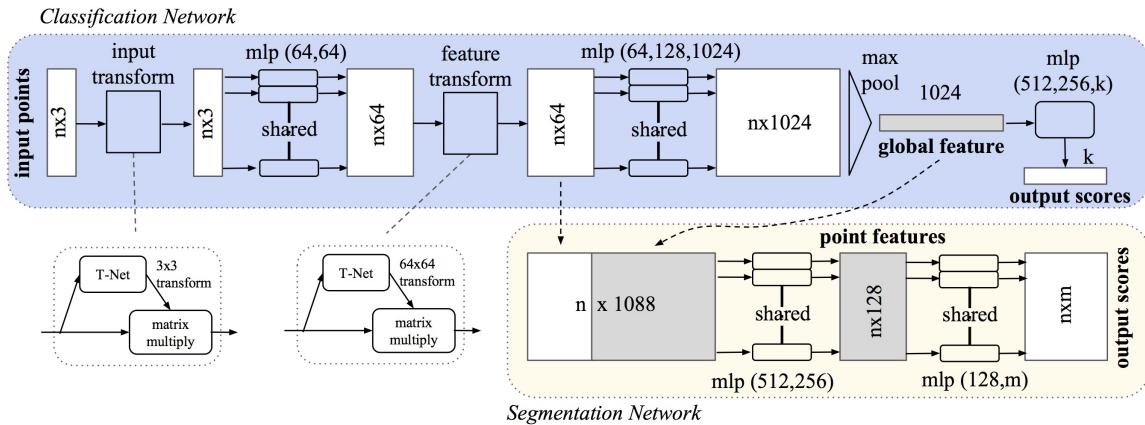


Figure 2.2: PointNet architecture. Image from Qi et al. 2017.

## 2.4 Tools

In this section, technologies, tools, and assets used throughout this thesis will be briefly presented.

### 2.4.1 Graphics Engine

For the implementation of this thesis, a stable and well-documented engine with a variety of capabilities, especially supporting light probe features, was necessary. For that reason, we decided to use the Unity Engine. Unity is used globally for computer applications, ranging from 2D and 3D interactive applications like video games, simulations of physics interactions like liquid simulations, and cinematic films with realistic or stylized visuals. Unity additionally supports light probes internally, under the name Light Probe Groups, an object that contains all individual light probes of a scene and handles the interpolation and mapping of dynamic objects passing through the scene that are affected by GI.

### 2.4.2 Sentis

For the purposes of this thesis, a tool that allows us to run AI models inside Unity was needed. For that purpose, we used Sentis, a neural-network inference library for Unity. It is able to detect and import pre-trained AI models into Unity as assets, run them both in runtime and edit time, and utilize the end-user's device compute, CPU or GPU. Sentis is able to capture an .onnx file containing the AI model, and then exposes a variety of functions via programming code to allow the developer to send data to the model and capture the output of the model.

### 2.4.3 3D Scenes

For training and testing the AI model, we used the Sponza scene (McGuire 2017), the Office scene (CG AUEB 2021), and the Corridor scene (Vardis, Vasilakis, and Papaioannou 2021a). The scenes underwent some manual editing to make them better suit our needs, remove assets deemed unnecessary for our goals, or to import them properly inside Unity along with their textures and required objects. These edits are minimal and not vital to the thesis. Therefore, they will not be explicitly described.

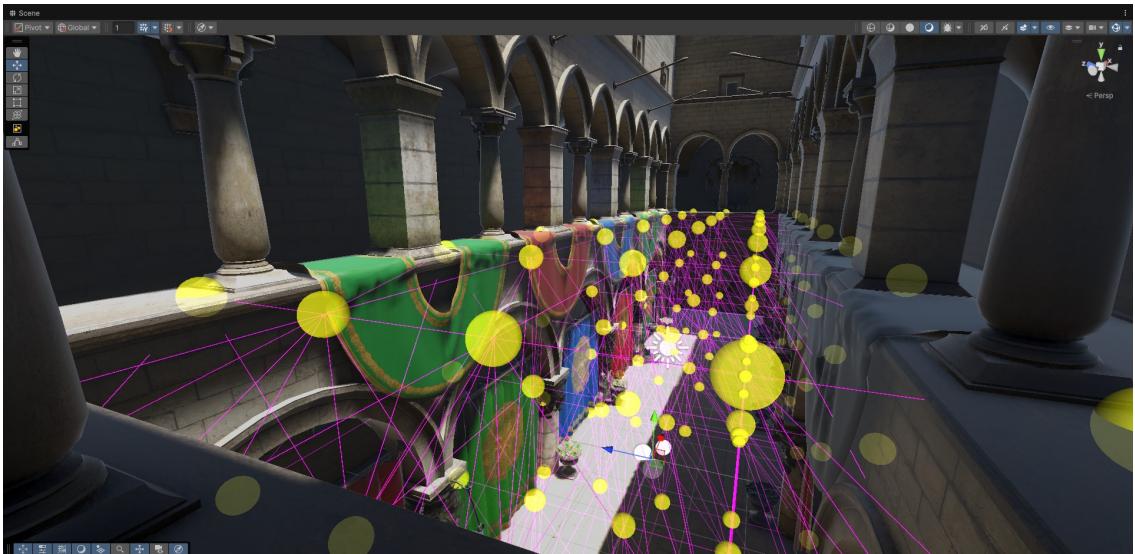


Figure 2.3: The Sponza Unity Scene showing light probes placed on a grid (McGuire 2017).

#### 2.4.4 Python and TensorFlow

For this thesis, Python was used as the language of choice for the creation of our Deep Learning AI Model. Python is an interpreted programming language. Its high-level nature makes it ideal for general purpose scenarios and easy to work with. Python was used for its simplicity, making the reading, preparation, post-processing, and saving of the data a fast process during the development of LPNN.

TensorFlow is a free and open-source software library used for machine-learning and artificial-intelligence applications. It supports a variety of well-known programming languages, but for this thesis we used the Python version for creating and training our model.

# Chapter 3

## Our Approach

In this chapter, we will present the pipeline of the tool and its implementation. The chapter will be split into five parts, describing the process of collecting the features, how labels are created, LPNN training in python, and predicting light probe positions using the trained model accordingly. Lastly, we will present the tool inside the Unity Editor.

### 3.1 Feature Collection

A necessary step before collecting scene and lighting features is to first place points in the scene to collect data per-point. We decided to create an algorithm that places those points, called Evaluation Points (EP) henceforth, inside a collection of user-defined scene bounds of arbitrary shape. As shown in algorithm 1, we begin by placing the Evaluation Points on a volume that surrounds the collection of bounds the user defined, then we remove the points that are not within the bounds, as seen in figure 3.1.

---

**Algorithm 1** Placement of Evaluation Points on a grid-like layout

---

**Require:**  $cellsize > 0$

```
1:  $EP = \emptyset$ 
2: for all  $points \in volume$  do
3:   if  $point \in bounds$  then
4:      $EP \leftarrow EP + point$                                  $\triangleright$  Append point to the set
5:   end if
6: end for
7: return  $EP$ 
```

---

In algorithm 1,  $cellsize$  is the distance between each EP, and a value of 0 or negative values do not apply, therefore it is vital to require a  $cellsize$  bigger than 0.  $Cellsize$  is not directly shown inside the algorithm, but for the C# implementation it is necessary and the value is used often, therefore we show the requirement here.  $Bounds$  is the collection of 3D areas defined by the user, and  $volume$  are the bounds of that collection. As seen in figure 3.1, the rectangles shown in pink are three distinct areas defined by the user, defining where they want EP placed. Seen in red is the surrounding volumes of those bounds. We clearly see the EP, shown as yellow dots. They are present only inside the areas of the user defined bounds, but in a grid layout, regardless of the position of those bounds. The EP intentionally "overshoot" the bounds for completeness when calculating the feature data for each point, making sure we cover the entirety of the bounds given by the user.

After placing the EP, we use each point to calculate the data needed for the feature vectors. The aim of the LPNN model is to give an importance value to each of those EP

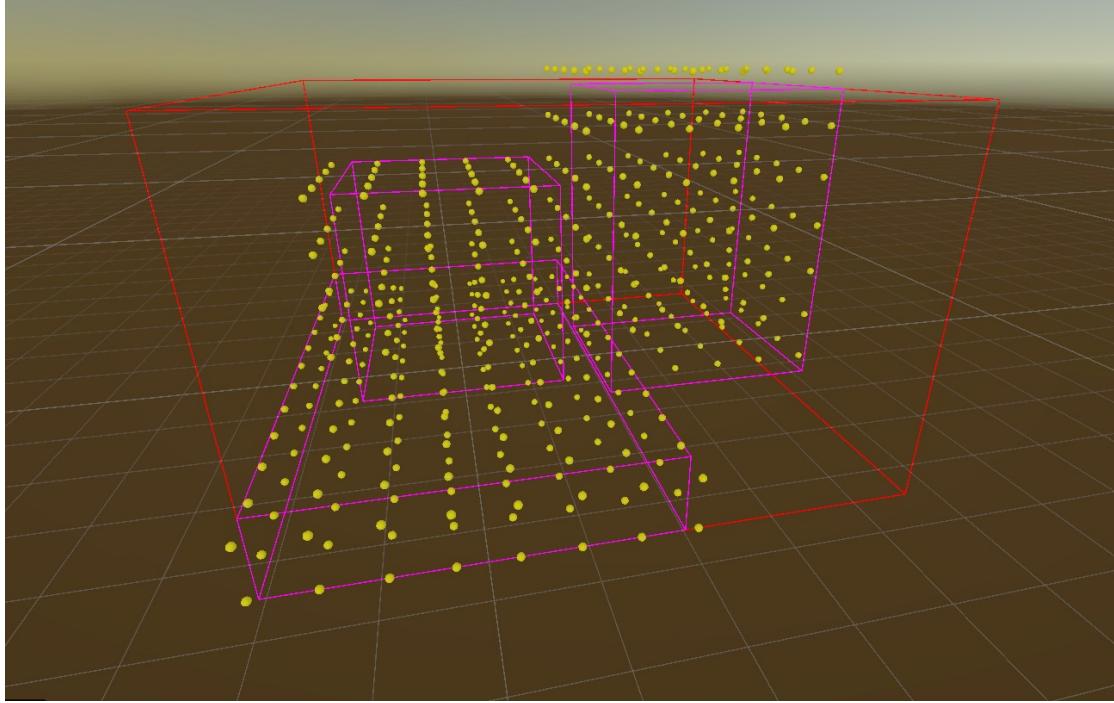


Figure 3.1: A 3D Scene showing the placement of Evaluation Points (shown in yellow) inside the user defined bounds (shown in pink), contained within the calculated volume (shown in red).

that it is given. Therefore, it is vital that it understands what defines a significant point via the features that it is trained on. Our knowledge dictates that an important location for a light probe is one that has great variance in illumination. Therefore, we include light-, RGB- and normal-variance as features for each point. Light-Variance dictates how much the light intensity changes around a point. RGB-Variance is similar, since it shows the change in Red, Green, and Blue light around each point, each channel being independent from the others. Normal-Variance is a value that makes locations like corners distinct from empty areas or from locations near a wall. Similarly, we also calculate Occlusion-Factor, a feature that gives each point a value depending on how empty or cluttered the area around it is. Normal-Variance together with Occlusion-Factor inform the model of areas that are enclosed or close to complex geometry. This makes the model able to distinguish these locations, even when all other values are identical, making it able to give different importance values to those distinct locations.

Along with the features mentioned above, we additionally include a vector that contains the spherical-harmonic values for a small amount of distinct directions around each point. The implementations of each feature collection method are shown in 2, 3, 4, 5, and 6.

---

**Algorithm 2** Feature Extraction: Spherical Harmonics around a point

---

**Require:**  $EP \neq \emptyset$

```

1:  $values = \emptyset$ 
2: for all  $points \in EP$  do
3:    $value \leftarrow evaluateSH(point)$ 
4:    $values \leftarrow values + value$                                  $\triangleright$  Append SH to the list
5: end for
6: return  $values$ 

```

---

In line 3.7, to convert from RGB channel values to perceived light intensity of the

---

**Algorithm 3** Feature Extraction: Light Variance around a point

---

**Require:**  $EP \neq \emptyset$

**Require:**  $samples \geq 1$  ▷ The amount of directions

1:  $radius \leftarrow 1$  ▷ How far around the point to check

2: **for all**  $points \in EP$  **do**

3:      $luminances = \emptyset$

4:     **for**  $n = 1, \dots, samples$  **do**

5:          $direction \leftarrow$  random point on sphere with  $radius$

6:          $sh \leftarrow evaluateSH(direction)$

7:          $luminance \leftarrow sh.R * 0.2126 + sh.G * 0.7152 + sh.B * 0.0722$  ▷ From RGB to luminance value

8:          $luminances \leftarrow luminances + luminance$  ▷ Add luminance to the list

9:     **end for**

10:     $mean \leftarrow mean(luminances)$  ▷ Get the mean value of the luminances

11:     $variance \leftarrow (luminances - mean)^2 \div samples$  ▷ Get the total variance of luminances

12: **end for**

13: **return**  $variance$  per point

---

pixel, also known as luminance, we use the formula shown in ITU-R 2015, under section 3 item 3.2. This formula is used to calculate how bright a pixel in regards to the RGB channel values it currently shows.

Similarly, we collect the RGB-Variance independently for each channel. The formula is similar to Light-Variance, with the exception of line 3.7, since it is not applicable. We need each channel RGB value to be unaffected by any conversion. This is seen in algorithm 4.

---

**Algorithm 4** Feature Extraction: RGB Variance around a point

---

**Require:**  $EP \neq \emptyset$

**Require:**  $samples \geq 1$  ▷ The amount of directions

1:  $radius \leftarrow 10$  ▷ How far around the point to check

2: **for all**  $points \in EP$  **do**

3:      $count \leftarrow 0$

4:     **for**  $n = 1, \dots, samples$  **do**

5:          $direction \leftarrow$  random point on sphere with  $radius$

6:          $sh \leftarrow evaluateSH(direction)$

7:     **end for**

8:      $meanRGB \leftarrow mean(sh.RGB)$

9:      $RGBvariance \leftarrow (sh.RGB - meanRGB)^2 \div samples$

10: **end for**

11: **return**  $RGBvariance.R, RGBvariance.G, RGBvariance.B$  per point

---

In line 5.12, we want the higher values to define the areas with more complex geometry. The dot product of vectors is a value between 0 and 1, therefore we subtract the dot product from 1, to invert the range of the variance.

After collecting all the features, we compact them into a feature vector per-EP, and save them into a file for use during training, or directly for light probe placement, as we will see shortly. As shown in section 3.5, it is also possible to collect feature vectors from multiple scenes at different times, as well as labels, to make the model more accurate by providing more input data.

**Algorithm 5** Feature Extraction: Normal Variance around a point

---

**Require:**  $EP \neq \emptyset$

**Require:**  $samples \geq 1$  ▷ The amount of directions

- 1:  $radius \leftarrow 1$  ▷ How far around the point to check
- 2: **for all**  $points \in EP$  **do**
- 3:    $normals = \emptyset$
- 4:   **for**  $n = 1, \dots, samples$  **do**
- 5:      $direction \leftarrow$  random point on sphere with  $radius$
- 6:      $hit \leftarrow castRay(direction)$
- 7:     **if**  $hit == True$  **then**
- 8:        $normals \leftarrow normals + hit.normal$
- 9:     **end if**
- 10:   **end for**
- 11:    $mean \leftarrow mean(normals)$  ▷ Get the mean direction of the normals
- 12:    $variance \leftarrow (1 - dot(normals, mean)) \div samples$  ▷ Get the total variance of normals
- 13: **end for**
- 14: **return**  $variance$  per point

---

**Algorithm 6** Feature Extraction: Occlusion Factor around a point

---

**Require:**  $EP \neq \emptyset$

**Require:**  $samples \geq 1$  ▷ The amount of directions

- 1:  $radius \leftarrow 10$  ▷ How far around the point to check
- 2: **for all**  $points \in EP$  **do**
- 3:    $count \leftarrow 0$
- 4:   **for**  $n = 1, \dots, samples$  **do**
- 5:      $direction \leftarrow$  random point on sphere with  $radius$
- 6:      $hit \leftarrow castRay(direction)$
- 7:     **if**  $hit == True$  **then**
- 8:        $count \leftarrow count + 1$
- 9:     **end if**
- 10:   **end for**
- 11:    $factor \leftarrow count \div samples$  ▷ Percentage of hits versus misses.
- 12: **end for**
- 13: **return**  $factor$  per point

---

## 3.2 Label Collection

The supervised-learning approach we decided on for this thesis requires that the model also receives labels as an input. Labels are values for each of the input feature vectors that describe the correct output for that feature vector. It is therefore vital to collect labels for each EP that we have also collected features for. For this purpose, we use LumiProbes (Vardis, Vasilakis, and Papaioannou 2021b) to collect labels by returning a True or False value, depending on if the cell of each Evaluation Point contains a probe placed by LumiProbes. The use of LumiProbes as the ground-truth was arbitrary. The system is constructed in a way that allows any method of ground-truth light probe placement to be used for label extraction, even manual placement. In algorithm 7 we check every EP with every light probe in the ground-truth list and set the label to True if there exists a light probe around a *cellsize* radius of that Evaluation Point.

---

**Algorithm 7** Label Extraction per-EP

---

```

Require:  $EP \neq \emptyset$ 
Require:  $cellsize > 0$ 
1: for all  $points \in EP$  do
2:   for all  $probes \in groundTruth$  do
3:     if  $probe \in cellsize$  around  $point$  then
4:        $label \leftarrow True$ 
5:     else
6:        $label \leftarrow False$ 
7:     end if
8:   end for
9: end for
10: return  $labels$  per point

```

---

The nature of this label extraction method beckons for the ground-truth light probe placement to be close to the optimal placement, determined by the user's intuition, experience, and demands for the specific scene.

After collecting the labels into a list, they are saved into a file on the hard disk for use in training of the model, as seen in section 3.3. As mentioned previously, it is possible to collect labels from multiple scenes, creating a bigger dataset for the model to train on.

## 3.3 Model Training

The model basis for LPNN, as described in section 2.3, was a PointNet architecture (Qi et al. 2017). We followed the style loosely, mainly focusing on making a model that is able to predict importance scores per-point, and able to handle an arbitrary amount of input points without retraining.

### 3.3.1 Data Preparation

The feature vectors that were created from the previous steps are read from the files stored on the hard disk. For the labels, we convert each True or False line into numerical 1 or 0, respectively. Then, a Numpy array is created, containing all the values in order of appearance. For the feature vectors, a similar method is used. Additional logic is needed since there are multiple values per line, but the features are finally converted into an array of arrays. Each sub-array contains the values per-point, in order of appearance.

### 3.3.2 Model Architecture & Training

The architecture is as follows; First, three Convolution1D layers followed by three Batch Normalization layers expand the input from a feature vector of length 30 to 256. Each of these 6 layers are used one after the other, first a Convolution1D with dimensions  $64 \times 30 \times 1 \times 1$  and a ReLu activation, followed by a Batch Normalization layer, then the next Convolution1D layer with dimensions  $128 \times 64 \times 1 \times 1$  with the same activation function, etc. Then, in order for the model to have some knowledge of the global context, we use a Global Max Pooling 1D layer and a Global Average Pooling Layer 1D, concatenated together with each per point local context, resulting in a 512 dimensional feature layer. In order to avoid averaging all neurons together, we tile the global context, using a custom tiling function, making each neuron have knowledge of only the surrounding points, instead of every point in the scene. This ensures that each point's significance will only be affected by the surrounding lighting data of itself and the nearby points.

Finally, another Convolution1D and Dropout sequence is used to reduce the high-dimensional hidden layers into a single importance score  $i \in [0, 1]$ . The Dropout layers are important to reduce learning error rates by randomly deactivating a small set of neurons and their connections during the training process. The probability for drop-out is set to 0.3, meaning 30%. This sequence of layers are then directed into another Convolution1D layer with Sigmoid activation function, and trained for 50 epochs. The model is then compiled and saved in an .onnx file for import back into the Unity engine.

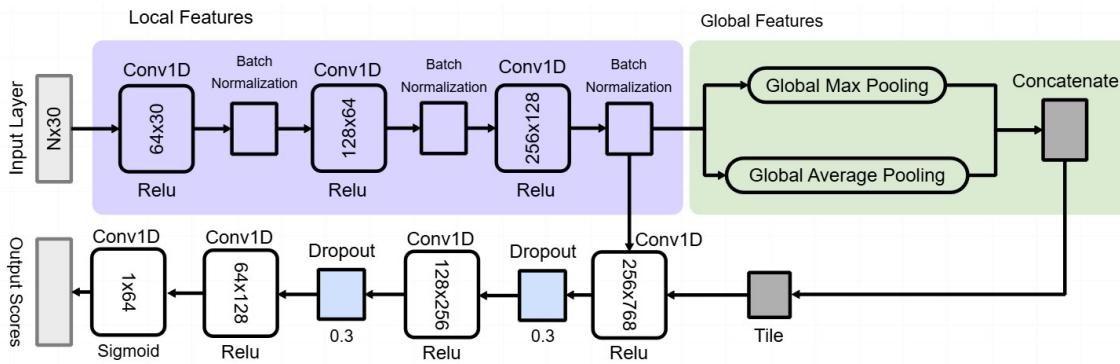


Figure 3.2: Neural Network architecture of our LPNN model.

## 3.4 Light Probe Prediction

In order to use the model to infer importance scores for the EP, we need to import it to Unity. For this purpose, we use Sentis. After model import, it can be used for our goals. First,

## 3.5 LPNN inside Unity Editor

# Chapter 4

# Experiments

In this chapter, we present experimental results of the LPNN approach. The evaluation is qualitative, since the nature of light probes and their optimal placement is subjective to the user and the needs of the application. We focus mainly on speed in relation to light probe layout given by the tool. We compare performance results to LumiProbes (Vardis, Vasilakis, and Papaioannou 2021b). All experiments were conducted in Unity 6 version 6000.0.38f1, on a system comprising of an NVIDIA RTX2060M GPU, 16GB DDR4 RAM and an Intel i7-9750H CPU, on a Windows 10 Operating System.

## 4.1 Performance

Since the focus of the thesis was to speed up the placement of light probes in this stage of any 3D application development iteration process, we will focus on the execution time of the tool and also critique the results and their qualitative properties, to make sure the placements are correct. Indeed, as seen in table 4.1, the LPNN approach speeds up light probe placement by orders of magnitude faster than other approaches, but it may suffer from occasional misplacement; probes that were placed in positions that are not vital, leading to oversampling, which we will show shortly. In experiments where LumiProbes and LPNN were requested to place close to the same amount of light probes in the same scene, LPNN time stayed close to constant, typically up to a few seconds, regardless of the scenario or the amount requested. Results for various amounts of light probes and scenes are presented in table 4.1. Times are averaged over multiple runs. Units are represented in minutes (m), seconds (s), or milliseconds (ms). Where applicable, we also append the settings used for each tool. For LumiProbes, settings include the grid parameters and the evaluation-point count. All other settings are as follows: Evaluation point placement type is set to Poisson, Decimation type is set to Medium, Decimation directions are averaged, Decimation metric is set to Chrominance, Minimum LP set is disabled, and Maximum Error is set to 3. For LPNN, settings include the threshold value used for the specific result and the cell size of the 3D grid, in order. Figures for the results are shown in section 4.2. Memory requirements for this tool are strictly dependent on the amount of light probes present in the scene, since all information needed by the tool are either already present in Unity and are needed regardless of the presence of the tool, e.g. Global Illumination data, or are stored on the Hard Disk of the system as files with storage sizes dependent on the amount of probes placed before the execution of the tool. File sizes for 150 probes were less than 2KB. Typically, the tool creates files needed for placing the light probes with size-scaling 1KB per approximately 100 probes.

Execution time					
Method	Scene	Time	P. Count	P. Present (& Removed)	Settings
LumiProbes	Sponza	22.443s	105	34 (75)	(7,3,5), 128
	Office	51.059s	144	84 (60)	(12,3,4), 128
		919.134s	288	182 (106)	(12,3,8), 256
	Corridor	161.151s	180	120 (60)	(20,3,3), 256
Ours	Sponza	<b>5.3ms</b>	90	54 (36)	0.4, 2.0
		<b>17.8ms</b>	400	40 (360)	0.9, 1.3
	Office	<b>7.8ms</b>	140	34 (106)	0.758, 1.87
		<b>25.2ms</b>	832	117 (715)	0.859, 1.10
	Corridor	<b>10.9ms</b>	186	84 (102)	0.549, 1.94
		<b>15.7ms</b>	246	95 (151)	0.615, 1.50

Table 4.1: Execution time for LPNN and LumiProbes on a select number of scenes and probe counts. *P. count* represents the total amount of probes in the scene, before simplification. *P. Present* depict the final amount of probes after running the tools. The number in parenthesis is the amount of probes removed by the tool, in respect to the settings. Fastest times are shown in **bold**.

## 4.2 Quality

The tools were tested on the aforementioned edited Sponza scene (McGuire 2017), Corridor scene (Vardis, Vasilakis, and Papaioannou 2021a) and Office scene (CG AUEB 2021). We will present the qualitative results. As we will see shortly, LPNN correctly places light probes in areas of high variance.

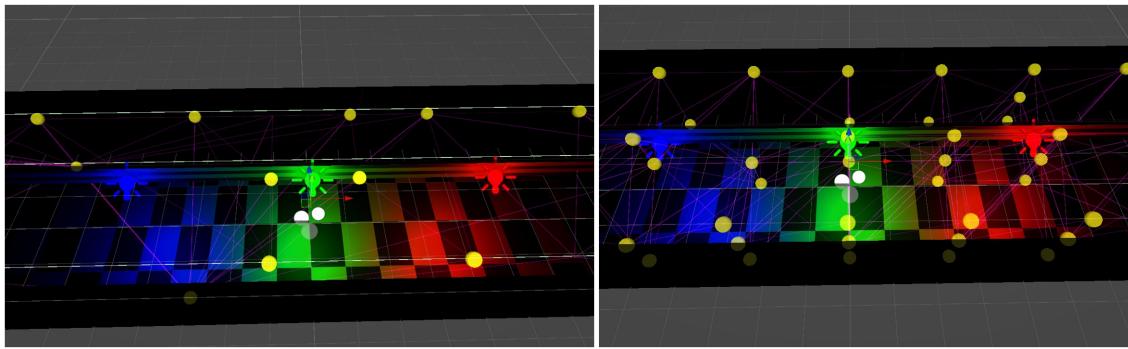


Figure 4.1: A 3D Scene showing a comparison of light probe placement in a **high** color-variance scenario, between LPNN (left) and LumiProbes (right) with settings 0.549, 1.94 and (27,3,3), 256 respectively, in the Corridor scene.

As shown in figure 4.1, we can clearly see that the LPNN tool has correctly placed light probes between the blue and green light sources, as well as between the green and red light sources, locations with great variance in Chrominance. It has additionally kept the amount of probes at a minimum, only placing one probe at each location mentioned. This result is close to optimal placement, since the distance between the light sources is only 4 units, making additional probes unnecessary in most scenarios. It should be noted that the tool did correctly place probes on the edges of the bounds, seen as light-green colored lines. This ensures that any dynamic object that moves outside the bounds set by the user continues to have some light-probes information for its illumination.

Furthermore, in figure 4.2 we can see a similar result. The light probe between the

two white light sources is vital. The areas left and right from the two light sources have light probes only in the dark areas, making the light transition when a dynamic object moves within this section of the scene smooth. Additionally, the light sources are next to an opaque wall, meaning no light present on the other side of the wall. Therefore, the model decided that placing light probes is only important on the edges of the wall, which is what we see in the example. It is important to note that on the left side of the corridor, as seen in the left image of figure 4.2, the model has placed a great amount of light probes, even though there is low light variance since that section of the scene is not illuminated. Additionally, as seen in figure 4.3, the model suffers from under-sampling in certain scenarios; placing fewer light probes than necessary, resulting in partially incorrect lighting. However, this can be resolved in two immediate ways; the user can execute the tool again with different parameters, as seen in figure 4.4, or the user can manually place a small number of light probes in locations they deem vital. The tool has placed only 2 light probes on the lower section of the scene, resulting in elongated tetrahedrons and incorrect lighting for dynamic objects placed low. Additionally, the light probes placed on the dark side of the wall in figure 4.3 require one more row of light probes placed next to the wall, making any object inside that section of the scene completely dark due to the lack of light in that section. With the settings present in figures 4.1, 4.2, and 4.3, the tool doesn't have enough light probes in the desired locations to correct this issue. This can be fixed by decreasing the cell size parameter.

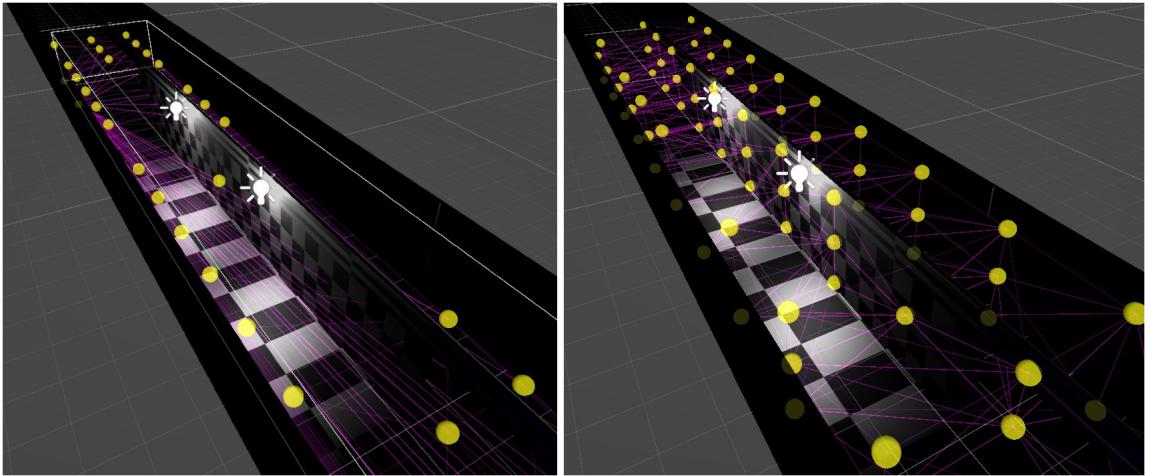


Figure 4.2: A 3D Scene showing a comparison of light probe placement in a **low** color-variance scenario, but **high** luminance variance, between LPNN (left) and LumiProbes (right) with settings 0.615, 1.5 and (27,3,3), 256 respectively, in the Corridor scene.

With different settings, as seen in figure 4.4, we can resolve the under-sampling issue from figure 4.3. By increasing the cell size but reducing the threshold, the tool has placed more probes on the lower section of the scene, from just 2 to 8, leading to better results overall.

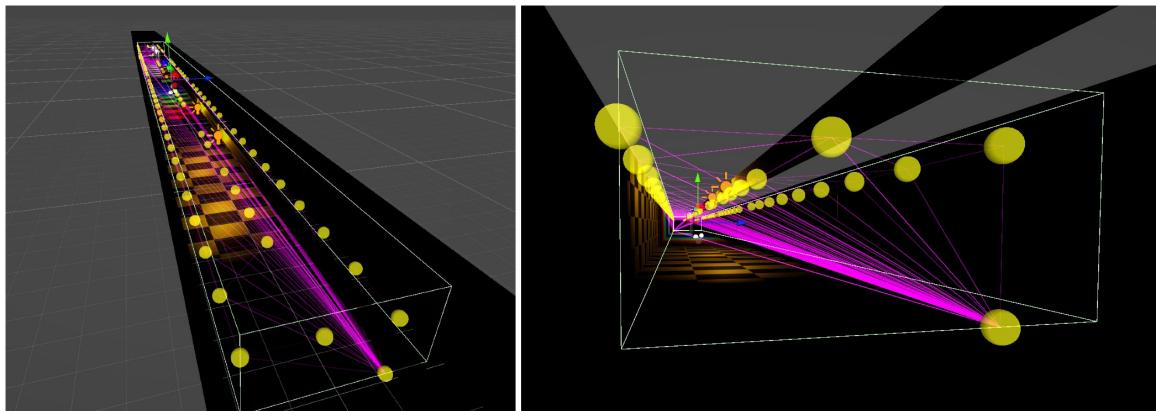


Figure 4.3: A 3D Scene showing under-sampling of light probe placement in the Corridor scene. The example was captured with LPNN with settings 0.615, 1.5.

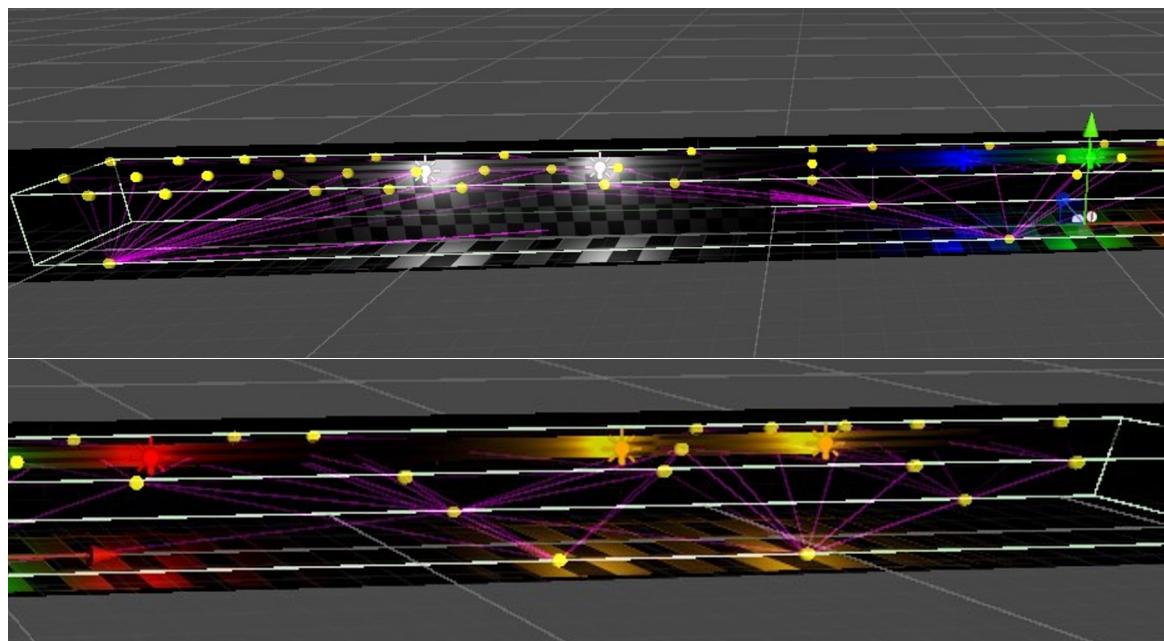


Figure 4.4: A 3D Scene showing improved light probe placement in the Corridor scene. The example was captured with LPNN with settings 0.549, 1.94.

## Chapter 5

# Conclusions and Future Work

conclusions and future works

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