```
restart
with(Gym):
with(LinearAlgebra):
with(MTM, svd):
```

## Robot to table calibration

Input points as vectors in the lists.

$$p_{i, \, robot} \coloneqq \begin{bmatrix} -0.05907 \\ -0.31838 \\ 0.17 \end{bmatrix}, \begin{bmatrix} 0.06377 \\ -0.48364 \\ 0.17 \end{bmatrix}, \begin{bmatrix} 0.23051 \\ -0.36235 \\ 0.17 \end{bmatrix} :$$

$$p_{i, \, world} \coloneqq \begin{bmatrix} 0.65 \\ 0.55 \\ 0.205 \end{bmatrix}, \begin{bmatrix} 0.45 \\ 0.5 \\ 0.205 \end{bmatrix}, \begin{bmatrix} 0.5 \\ 0.3 \\ 0.205 \end{bmatrix} :$$

#### Compute centroid (Center of a figure)

$$N := nops(p_{i,robot})$$
:

$$\begin{split} C_{p, \, robot} &:= \frac{1}{N} \cdot \sum_{i=1}^{N} \left( p_{i, \, robot}[i] \right) : \\ C_{p, \, world} &:= \frac{1}{N} \cdot \sum_{i=1}^{N} \left( p_{i, \, world}[i] \right) : \end{split}$$

The two sets of points with zero centroid

$$\begin{array}{l} \textbf{for } i \textbf{ from } 1 \textbf{ by } \hat{1} \textbf{ to } N \textbf{ do } q_{i,robot}[i] \coloneqq p_{i,robot}[i] - C_{p,robot} \textbf{ end do} \text{:} \\ \textbf{for } i \textbf{ from } 1 \textbf{ by } 1 \textbf{ to } N \textbf{ do } q_{i,\ world}[i] \coloneqq p_{i,\ world}[i] - C_{p,robot} \textbf{ end do} \text{:} \end{array}$$

# Compute SVD (singular value decomposition)

 $unassign(\, 'i')$ 

for 
$$i$$
 from  $1$  by  $1$  to  $N$  do  $Q[i] := q_{i,robot}[i] \cdot Transpose(q_{i,world}[i])$  end do:  $H := add(Q[i], i = 1..N)$ : 
$$U, \Sigma, V := svd(H)$$
:

## Compute rotation matrix and translation vector

$$R^{\hat{}} := V \cdot Transpose(U) :$$
 $T^{\hat{}} := C_{p, world} - R^{\hat{}} \cdot C_{p, robot} :$ 

#### **Define transformation matrix**

# Computation of the coordinates

Compute the point seen from {W} in {R}

Inverse transformation matrix

$$\begin{split} H_{W,\,R}[\,1\,..3,\,1\,..3\,] &:= Transpose\big(H_{R,\,W}[\,1\,..3,\,1\,..3\,]\big): \\ P_{W,\,R_{org}} &:= H_{R,\,W}[\,1\,..3,\,4\,]: \\ H_{W,\,R}[\,1\,..3,\,4\,] &:= -\big(Transpose\big(H_{R,\,W}[\,1\,..3,\,1\,..3\,]\big)\big) \cdot P_{W,\,R_{org}}: \end{split}$$

### **Computation of the point**

Input point coordinates of a point in {W}.

$$x := 0.3 :$$
  
 $y := 0.4 :$   
 $z := 0.205 :$ 

$$\begin{split} P_{World} &:= \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} : \\ P_{Robot} &:= H_{W, R} \bullet P_{World} : \end{split}$$

$$P_{Robot, xyz} := P_{Robot}[1..3] = \begin{bmatrix} 0.213241296324387 \\ -0.585006974555421 \\ 0.17000000000000000 \end{bmatrix}$$