

Part II: Integral Calculus

6. Antiderivatives & Riemann Intgrl.

↳ YES (everything in 6.)

^{7/11} Riemann Sum, LEIBNIZ-NEWTON etc.

7. Measurable sets & multiple integral

§ 7.1. NO

§ 7.2. YES (= Jordan Measurability)
↳ everything

§ 7.3. The multiple Integral: YES

8. Computation of multiple integrals

YES & NO → no theory questions

↳ you need it for exercises

Jacobi Matrix: YES

Polar coords: YES, spherical: NO

9. The Riemann Integral: Related topics

§ 9.1. Numerical computation of $\int_a^b f(x) dx$

Trapezoidal & composite trapez. rule YES

§ 9.2. Integrals & Probability: NO

Buffon needle: NO

§ 9.3. Monte-Carlo Integration: NO
& Manhattan Project

10. Extensions of the Riemann Integral

§ 10.1. Improper \int (CAUCHY) YES

§ 10.2. Testing (CONV): YES

~~Additional~~

§ 10.3. Improper \int w. parameter
only Def, No Thms.

Part III: Sequences & Series

11. Series of real numbers

§ 11.1 Sequences YES (all)

§ 11.2 Series YES

especially CAUCHY'S Integral Crit' YES

Applications: $\sum 2^n$, $\sum \frac{1}{n}$, $\sum \frac{1}{n^2}$ YES

§ 11.3. CONV Criteria /
additional material (Files) YES

12. Sequences & Series of functions

§ 12.1 Sequences of functions

Def & Example YES

\mathbb{N} 's (1, 2, 3)

NO

§ 12.1.4 (WEIERSTRASS) YES (Rest: NO)

§ 12.2. Power series

13. Fourier series

§ 13.1 Recap: NO (just def)

§ 13.2. Fourier Series & 13.3 Convergence: YES

§ 13.4. $\sum \frac{1}{n^2} = \frac{\pi^2}{6}$ YES

Gibbs (Idea) YES

Part I: Diff. Calculus

1. Diff. Calc for $f: [a, b] \rightarrow \mathbb{R}$ & Taylor

§ 1.1. Limits & continuity

ϵ - δ Defs NO

☒ Weierstrass YES

§ 1.2. Diff. calc. & Mean Value ☒s

All ☒s YES (with geom. interpr.)

Examples YES

§ 1.3. Taylor's Formula

☒ Taylor YES (Proof: YES)

2. Calculus for $f: \mathbb{R}^d \rightarrow \mathbb{R}$ I

§ 2.1. Geometry of \mathbb{R}^d YES (all) ^{def, etc.}

§ 2.2. Partial derivatives — (✓!!!)

3. Calculus \mathbb{R}^d II

☒ CHAIN YES (HW/Proof: NO !!!)

☒ Lagrange YES (Proof: YES)

☒ Schwarz YES

§ 3.3. Fréchet diff

Linear & Quadratic functions YES

Def of F-diff: NO!

4. Optimization I: Least Squares & ML

§ 4.1. Optimization for $f: \mathbb{R}^d \rightarrow \mathbb{R}$

☒ Fermat \mathbb{R}^d YES

☒ 4 & ☒ Sylvester YES

Examples: YES

§ 4.2. Least Squares Meth

Formal statement: YES

(up to $E(q, b) = \dots$)

Rest: NO

§ 4.3. Deep Learning: NO

5. Constraint Optimization

§ 5.1. Planar curves & Implicit F Thm

Curves: YES

☒ Implicit Fct. Thm: NO

§ 5.2. Level Sets YES (everything)

§ 5.3. The Lagrange Multiplier Meth

☒ 3 YES (= Lagr. Multipl. Meth.)

Geometric Insight: YES

Proof: NO (contains typo?)
 $\nabla f(x^*) = \lambda^* \nabla g(x^*)$

Box of minimal surface: YES

↖ (see also Exercises)