# Bayesian Rogers-Castro models for migration

## BMSS, October 16 2024

## Monica Alexander

## **Table of contents**

| 1 | Overview                       | 1 |
|---|--------------------------------|---|
| 2 | What is a Rogers-Castro model? | 2 |
| 3 | Read in data                   | 2 |
| 4 | Fit model                      | 2 |
| 5 | Plot                           | 2 |
| 6 | Extensions                     | 2 |

## 1 Overview

This Quarto document illustrates how to fit Rogers-Castro models to age-specific migration rates using the rcbayes R package. Here's a paper that gives some more information the package.

Load in the required packages:

```
library(tidyverse)
library(rcbayes)
```

## 2 What is a Rogers-Castro model?

The Rogers-Castro model (1981) for migration age schedules is multi-exponential parametric model that aims to capture the non-linear characteristic non-linear shape of migration. It has the form:

$$\begin{split} m(x) = & a_1 \exp\left\{-\alpha_1 x\right\} + \\ & a_2 \exp\left\{-\alpha_2 \left(x - \mu_2\right) - \exp\left[-\lambda_2 \left(x - \mu_2\right)\right]\right\} + \\ & a_3 \exp\left\{-\alpha_3 \left(x - \mu_3\right) - \exp\left[-\lambda_3 \left(x - \mu_3\right)\right]\right\} + \\ & a_4 \exp\left\{\alpha_4 x\right\} + \\ & c \end{split}$$

where m(x) is the migration rate (in- or out-) for age x. The successive additive components of the model represent pre-working, working, retirement, post-retirement, and overall migration, respectively. Various versions of the model can be estimated; for example, a simpler version would remove the components related to retirement and post-retirement peaks. The rcbayes package has a built-in interaction Shiny application that you can use to explore how different parameter values affect the shape of the migration age curve:

```
rcbayes::interact_rc()
```

### 3 Read in data

XX todo

## 4 Fit model

XX todo

#### 5 Plot

XX todo

#### 6 Extensions

The rcbayes package was designed for users to be able to fit Rogers-Castro models to a single population. The Stan code for the models in the packages is here. These could be extended to fit, for example, hierarchical models for multiple areas at a time.