

Two-sample t-test: $T = \frac{(\bar{X} - \bar{Y}) - (\mu_x - \mu_y)}{\sqrt{s_p^2 \left(\frac{1}{n_x} + \frac{1}{n_y} \right)}} \sim t_{n_x + n_y - 2}.$

$$(\bar{x} - \bar{y}) \pm t_{\frac{\alpha}{2}, n_x + n_y - 2} \times s_p \sqrt{\frac{1}{n_x} + \frac{1}{n_y}}$$

$$s_p^2 = \frac{\sum (x - \bar{x})^2 + \sum (y - \bar{y})^2}{n_x + n_y - 2} = \frac{(n_x - 1)s_x^2 + (n_y - 1)s_y^2}{n_x + n_y - 2}$$

p-Values: The **p-value** of the data is the probability of obtaining a test statistic at least as extreme as the one actually observed, assuming H_0 is correct. In other words, **the p-value is the maximum significance level at which we still reject the null hypothesis H_0 for that sample.** Thus, if we are given a fixed α , the null hypothesis H_0 is rejected if the p-value is less than or equal to α .

Rule: Smaller p-values suggest stronger evidence against H_0 .