

9.3.2.7.Simplificați următoarele funcții booleene de patru variabile, date prin formele canonice disjunctive, utilizând diagrame Veitch:

$$f_7(x_1, x_2, x_3, x_4) = x_1x_2x_3x_4 \vee \bar{x}_1x_2\bar{x}_3x_4 \vee \bar{x}_1x_2x_3x_4 \vee x_1x_2\bar{x}_3\bar{x}_4 \vee x_1\bar{x}_2x_3\bar{x}_4 \vee x_1\bar{x}_2\bar{x}_3\bar{x}_4 \vee x_1\bar{x}_2x_3x_4 \vee \bar{x}_1\bar{x}_2\bar{x}_3x_4 \vee \bar{x}_1\bar{x}_2x_3x_4$$

		$x_2$	$\bar{x}_2$	
$x_1$	m15		m11	$x_4$
		m12	m8	m10
				$\bar{x}_4$
$\bar{x}_1$	m7	m5	m1	m3
	$x_3$	$\bar{x}_3$	$x_3$	$x_4$

1. Se afla  $M(f)$  (multimea monoamelormaximale). Se grupeaza 2 la k, k natural, mintermi adiacenti, k-cat mai mare:

$$\text{max1} = m_1 \vee m_3 \vee m_5 \vee m_7 =$$

$$\bar{x}_1\bar{x}_2\bar{x}_3x_4 \vee \bar{x}_1\bar{x}_2x_3x_4 \vee \bar{x}_1x_2\bar{x}_3x_4 \vee \bar{x}_1x_2x_3x_4$$

$$\text{max2} = m_3 \vee m_7 \vee m_{11} \vee m_{15} =$$

$$\bar{x}_1\bar{x}_2x_3x_4 \vee \bar{x}_1x_2x_3x_4 \vee x_1\bar{x}_2x_3x_4 \vee x_1x_2x_3x_4$$

$$\text{max3} = m_8 \vee m_{10} =$$

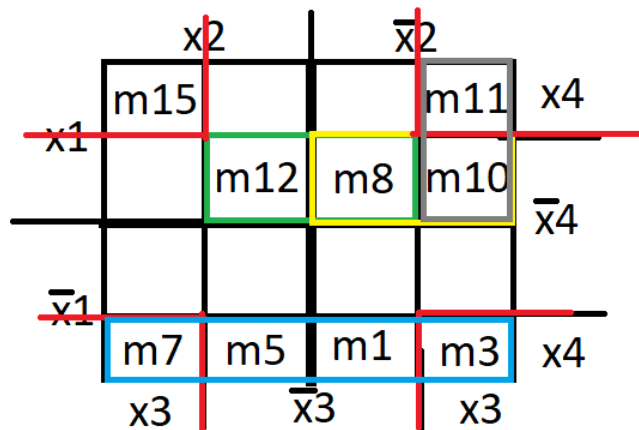
$$x_1\bar{x}_2\bar{x}_3\bar{x}_4 \vee x_1\bar{x}_2x_3\bar{x}_4$$

$$\text{max4} = m_8 \vee m_{12} =$$

$$x_1\bar{x}_2\bar{x}_3\bar{x}_4 \vee x_1x_2\bar{x}_3\bar{x}_4$$

$$\max 5 = m_{10} \vee m_{11} =$$

$$x_1\bar{x}_2x_3\bar{x}_4 \vee x_1\bar{x}_2x_3x_4$$



2. Se afla  $C(f)$  ( multimea monoamelor centrale ):

$$\max 1 =$$

$$\bar{x}_1\bar{x}_2\bar{x}_3x_4 \vee \bar{x}_1\bar{x}_2x_3x_4 \vee \bar{x}_1x_2\bar{x}_3x_4 \vee \bar{x}_1x_2x_3x_4$$

$$\max 2 =$$

$$\bar{x}_1\bar{x}_2x_3x_4 \vee \bar{x}_1x_2x_3x_4 \vee x_1\bar{x}_2x_3x_4 \vee x_1x_2x_3x_4$$

$$\max 3 =$$

$$x_1\bar{x}_2\bar{x}_3\bar{x}_4 \vee x_1x_2\bar{x}_3\bar{x}_4$$

Aflam cazul de simplificare:

$$M(f) \neq C(f)$$

$$C(f) \neq \text{multimea vida}$$

=> Intram pe cazul 2 al algoritmului de simplificare:

Functiile simplificate:

$$g(x_1, x_2, x_3, x_4) = \max_1 \vee \max_2 \vee \max_3 =$$

$$\bar{x}_1 x_4 \vee x_3 x_4 \vee x_1 \bar{x}_3 \bar{x}_4$$

$$f_7(x_1, x_2, x_3, x_4)'_1 = \bar{x}_1 x_4 \vee x_3 x_4 \vee x_1 \bar{x}_3 \bar{x}_4 \vee x_1 \bar{x}_2 x_3$$

$$f_7(x_1, x_2, x_3, x_4)'_2 = \bar{x}_1 x_4 \vee x_3 x_4 \vee x_1 \bar{x}_3 \bar{x}_4 \vee x_1 \bar{x}_2 \bar{x}_4$$