

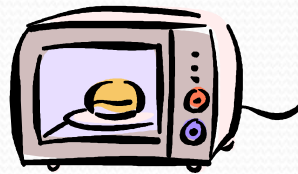
# Logică computațională

## Curs 13

Lector dr. Pop Andreea-Diana

# Circuite logice

- circuite electronice simple



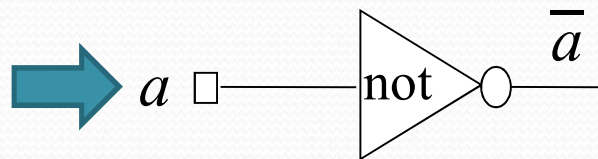
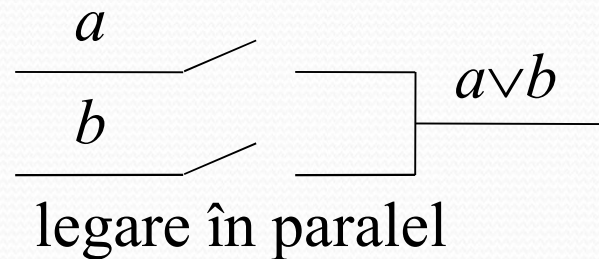
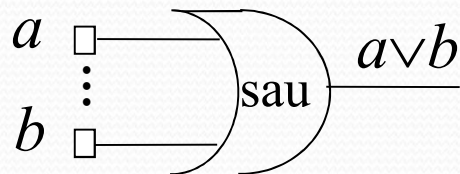
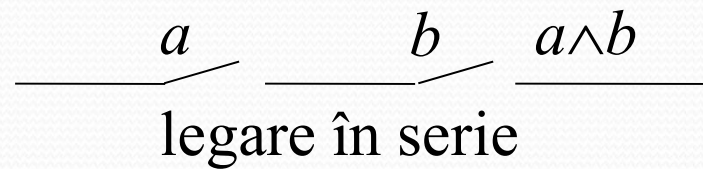
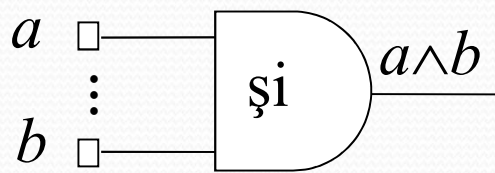
- modelarea – se face cu ajutorul *funcțiilor booleene* și a *circuitelor logice* care descriu algebric și grafic funcționarea acestora.



# Porțile logice

- sunt elementele de bază ale unui circuit logic
- sunt utilizate pentru modelarea circuitelor
- **Definiție:** O *poartă* este un minicircuit logic care realizează una dintre operațiile logice de bază:  $\wedge$  ,  $\vee$  ,  $\overline{\phantom{x}}$  .

# Porțile logice – conform standardelor IEEE



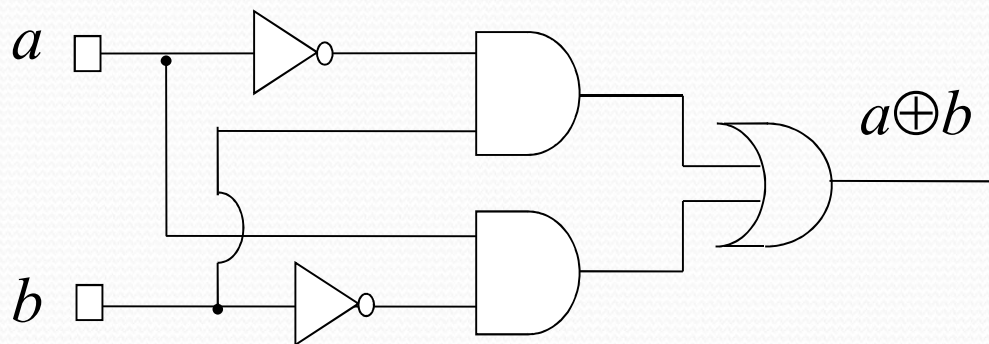
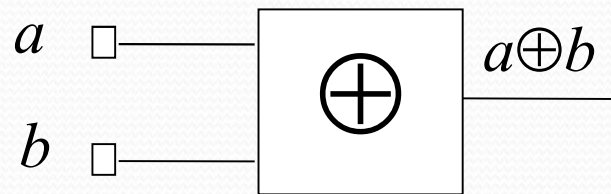




# Circuite integrate

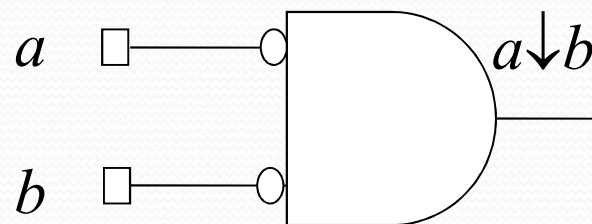
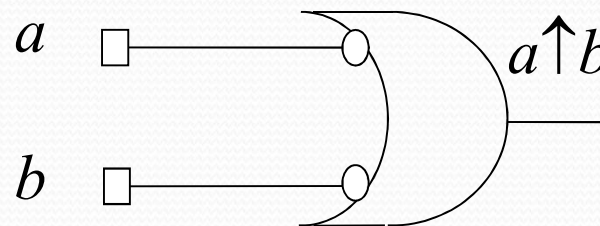
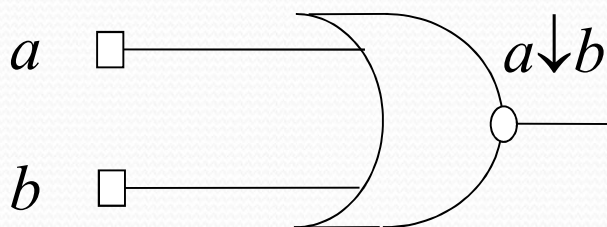
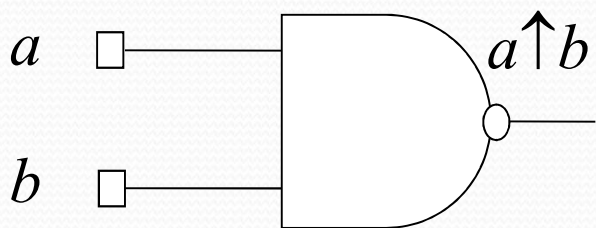
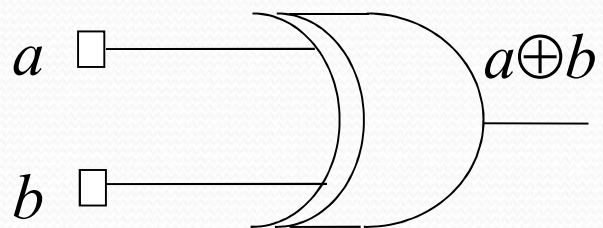
- 14-16 ”pini”
  - o parte porți de intrare
  - o parte sunt utilizate pentru conexiunea la curent
- Observație: forma disjunctivă este cel mai simplu de realizat

# Exercițiu – desenați circuitul



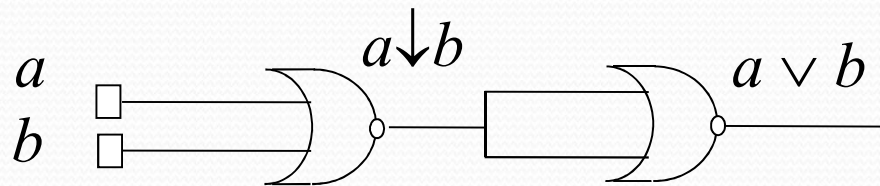
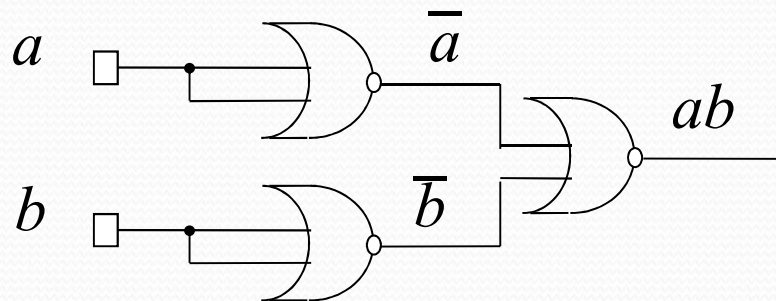
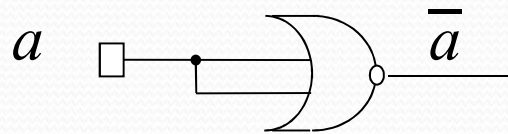


# Porți derivate



# Exercițiu

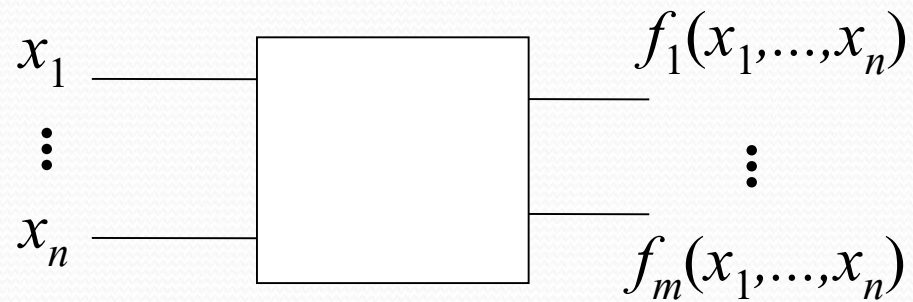
- Desenați circuitele operațiilor logice „și”, „sau”, „not” folosind doar poartă „**nor**” / „nand”





# Circuit combinațional

- Un circuit logic cu  $m$  ieșiri se numește *circuit combinațional*.

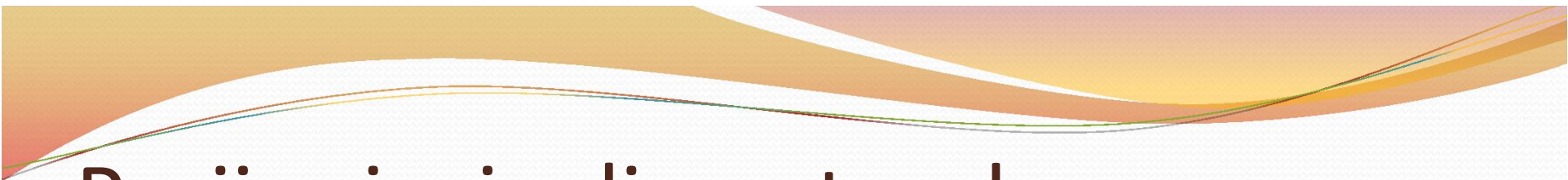




# Circuite logice combinaționale ∈ Hard-ul calculatorului

- decodorul
- circuitul comparator
- circuitul sumator
  
- detectorul de paritate
- ”shift”
- ...





# Pașii principali pentru desenarea circuitelor

1. identificarea intrărilor (variabilelor) / ieșirilor (funcțiilor)
2. construirea tabeli de valori asociate
3. obținerea expresiilor funcțiilor
4. simplificarea funcțiilor
5. desenarea circuitului

# Decodorul

1.

- intrare: 4 cifre binare -  $x_1, x_2, x_3, x_4$
- ieșire:  $f_i(x_1, x_2, x_3, x_4) = 1$  pentru  $x_1x_2x_3x_4_{(2)} = i_{(10)}$ ,  $i = \overline{0, 9}$



# Decodorul (2)

2.

3.

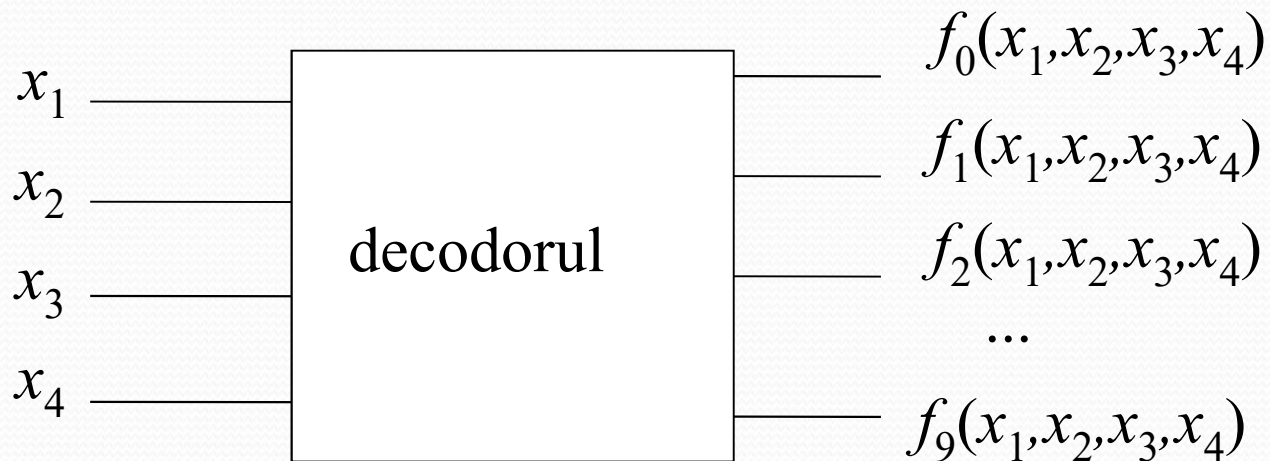
$x_1$	$x_2$	$x_3$	$x_4$	$f_0$	$f_1$	$f_2$	$f_3$	$f_4$	$f_5$	$f_6$	$f_7$	$f_8$	$f_9$	FCD (cu un singur element)
0	0	0	0	1	0	0	0	0	0	0	0	0	0	$f_0(x_1, x_2, x_3, x_4)$
0	0	0	1	0	1	0	0	0	0	0	0	0	0	$f_1(x_1, x_2, x_3, x_4)$
0	0	1	0	0	0	1	0	0	0	0	0	0	0	$f_2(x_1, x_2, x_3, x_4)$
0	0	1	1	0	0	0	1	0	0	0	0	0	0	$f_3(x_1, x_2, x_3, x_4)$
0	1	0	0	0	0	0	0	1	0	0	0	0	0	$f_4(x_1, x_2, x_3, x_4)$
0	1	0	1	0	0	0	0	0	1	0	0	0	0	$f_5(x_1, x_2, x_3, x_4)$
0	1	1	0	0	0	0	0	0	0	1	0	0	0	$f_6(x_1, x_2, x_3, x_4)$
0	1	1	1	0	0	0	0	0	0	0	1	0	0	$f_7(x_1, x_2, x_3, x_4)$
1	0	0	0	0	0	0	0	0	0	0	0	1	0	$f_8(x_1, x_2, x_3, x_4)$
1	0	0	1	0	0	0	0	0	0	0	0	0	1	$f_9(x_1, x_2, x_3, x_4)$
...														

0

# Circuitul decodor – forma generală

4. ...

5. ...





# Circuitul comparator

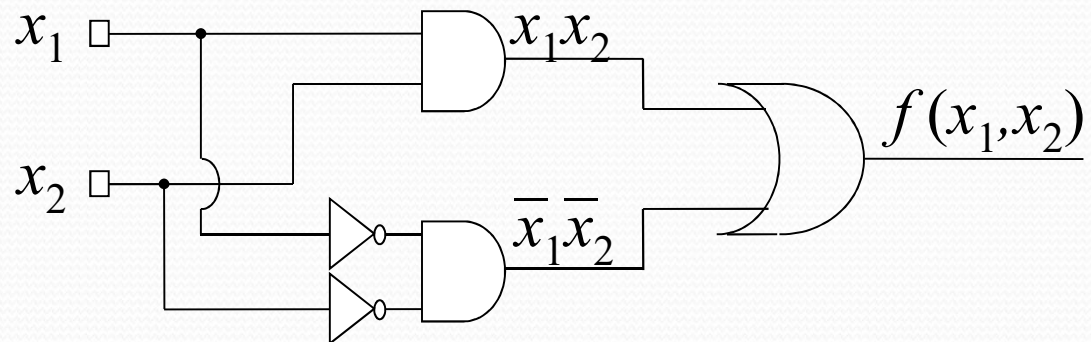
- verifică dacă două cifre binare sunt sau nu identice 1.

2.

$x_1$	$x_2$	$f(x_1, x_2)$
0	0	1
0	1	0
1	0	0
1	1	1

3.  $f(x_1, x_2) = \bar{x}_1 \bar{x}_2 \vee x_1 x_2$  4.

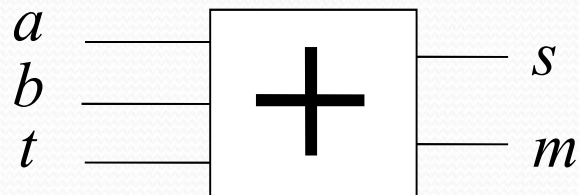
5.



# Sumatorul binar

- calculează suma a două cifre binare:  $a$  și  $b$  de pe aceeași poziție dintr-un număr binar

- 1.
- intrare:  $a$ ,  $b$ , transportul  $t$
  - ieșire:  $s$  ( $= a + b$ ), transportul  $m$



2.

$t$	$a$	$b$	$s$	$m$
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

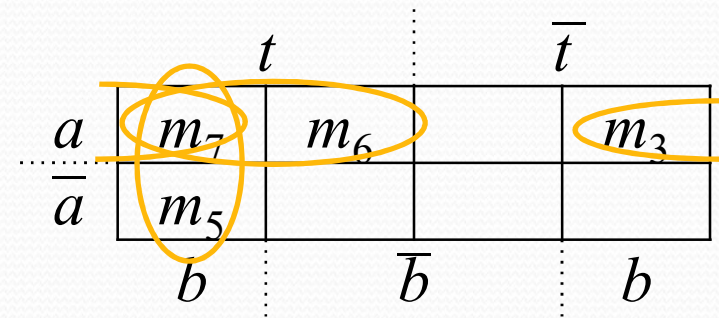
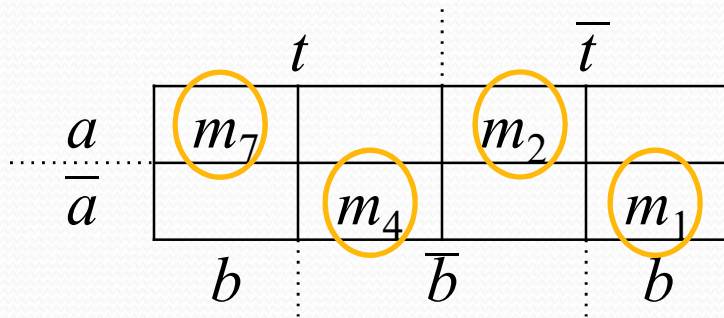
- 3.
- $$s(a,b,t) = \bar{t} \bar{a} b \vee \bar{t} a \bar{b} \vee t \bar{a} \bar{b} \vee t a b$$
- $$m(a,b,t) = \bar{t} a b \vee t \bar{a} b \vee t a \bar{b} \vee t a b$$



## 4.Simplificarea

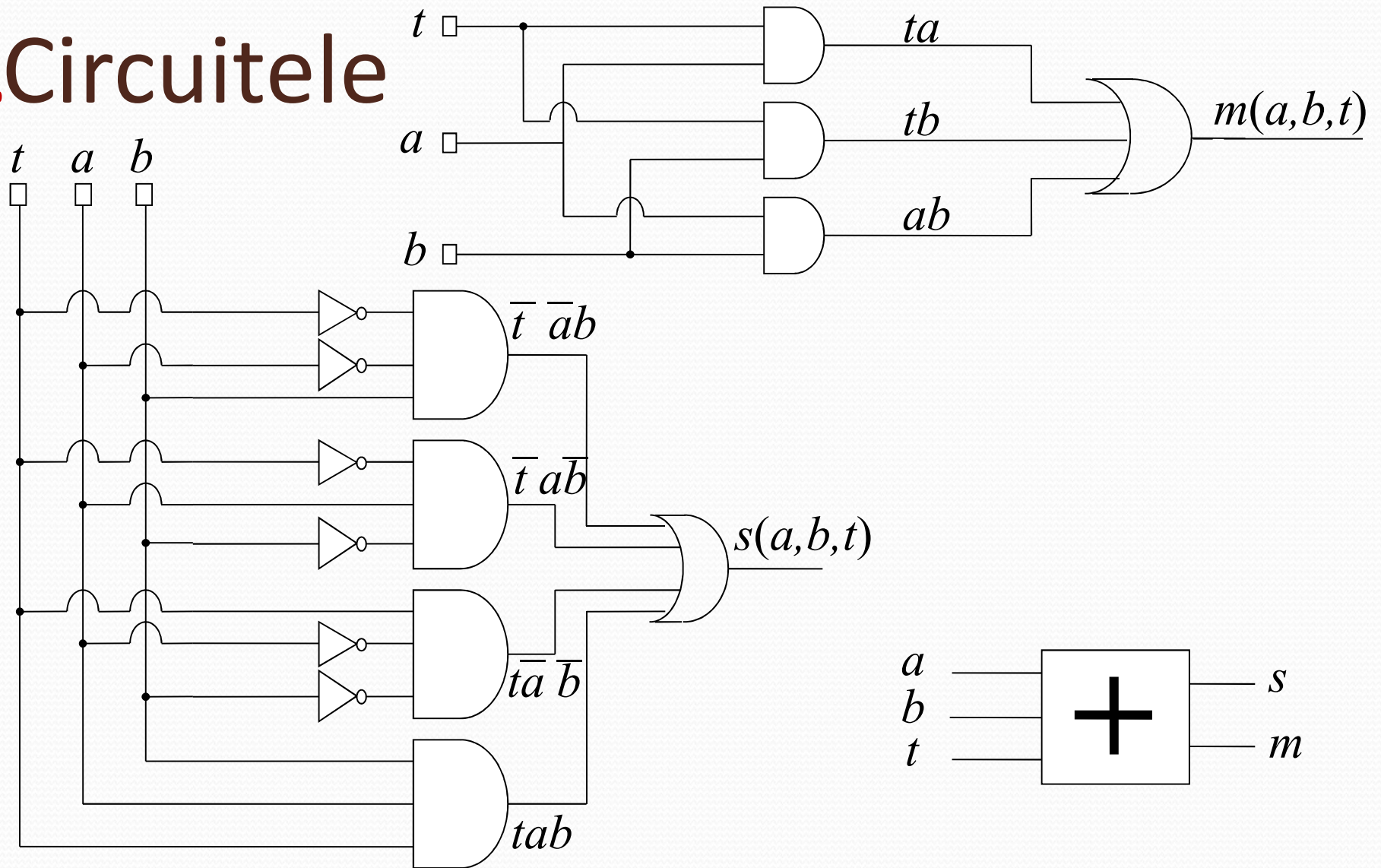
$$m(a,b,t) = \bar{t}ab \vee t\bar{a}b \vee t\bar{a}\bar{b} \vee tab$$

$$s(a,b,t) = \bar{t}\bar{a}b \vee \bar{t}a\bar{b} \vee t\bar{a}\bar{b} \vee tab$$



$$m(a,b,t) = ta \vee tb \vee ab$$

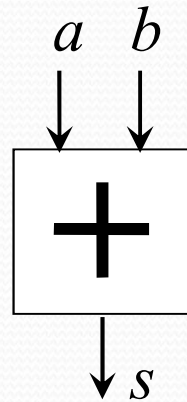
## 5. Circuitele



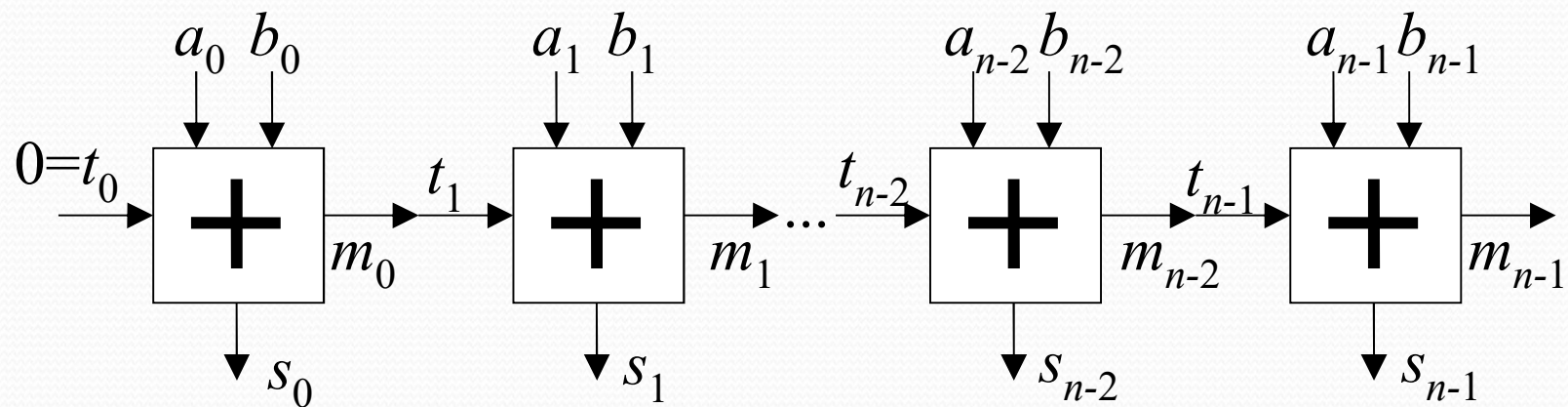


# Sumatorul binar cu $n$ poziții

- $a = a_{n-1} \dots a_0 (2)$  și  $b = b_{n-1} \dots b_0 (2)$
- $s = s_{n-1} \dots s_0 (2)$



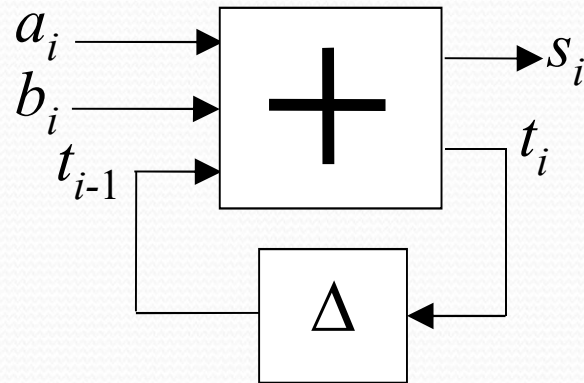
# Compunere de sumatoare simple



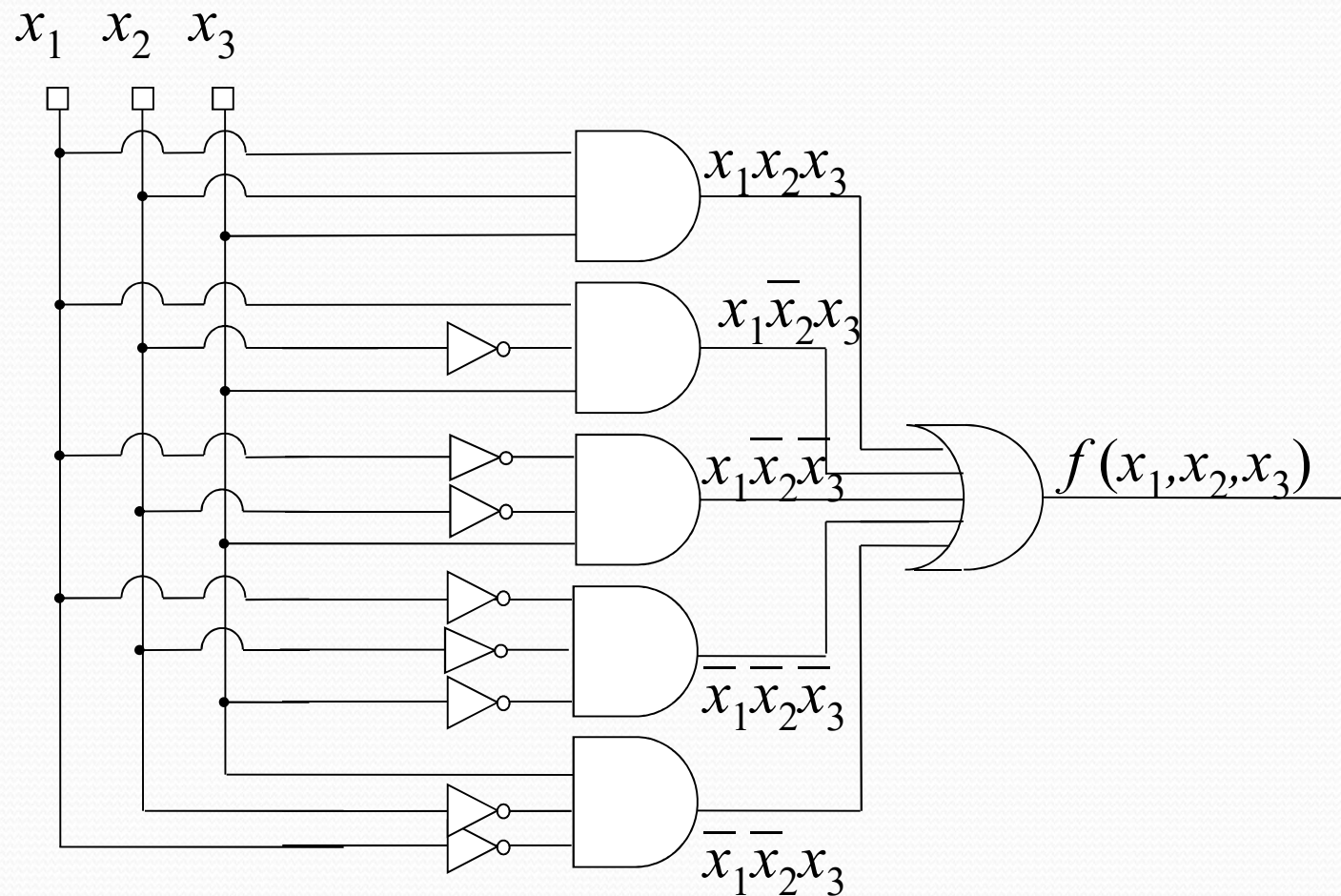


# Circuit cu întârziere

- cifra de transport obținută la un pas se folosește în pasul următor



# Indicații "anti - încălcire"







# Exemplu subiect examen

- Exemple de circuite combinaționale: “circuitul de comparare a 2 cifre binare”, “circuitul de adunare a 2 cifre binare”, “circuitul de adunare binară pe  $n$  biți”, circuitul de decodificare în binar.