

1. Write the equation of tangent line to function:

$$y(x) = 5 \cdot \sin(e^{2x} + \frac{\pi}{2}) \quad \text{at } x_0 = \frac{1}{2}$$

Tangent line equation is:

$$f(x) = y(x_0) + y'(x_0)(x - x_0)$$

$$1. y(x_0) = 5 \cdot \sin(e^{2 \cdot \frac{1}{2}} + \frac{\pi}{2}) = \left| \sin(\alpha + \frac{\pi}{2}) = \cos \alpha \right| = 5 \cdot \cos(e)$$

$$2. y'(x) = 5 \cdot \cos(e^{2x} + \frac{\pi}{2}) \cdot e^{2x} \cdot 2 = 10 \cdot e^{2x} \cdot \cos(e^{2x} + \frac{\pi}{2}) = \\ = \left| \cos(\alpha + \frac{\pi}{2}) = -\sin(\alpha) \right| = -10 \cdot e^{2x} \sin(e^{2x})$$

$$y'(x_0) = -10 \cdot e^{2 \cdot \frac{1}{2}} \cdot \sin(e^{2 \cdot \frac{1}{2}}) = -10 \cdot e \cdot \sin(e)$$

$$3. f(x) = 5 \cdot \cos(e) + (-10 \cdot e \cdot \sin(e)) \left(x - \frac{1}{2}\right) = 5 \cdot \cos(e) + 5 \cdot e \cdot \sin(e) - 10x e \sin(e)$$

Answer:  $5 \cdot \cos(e) + 5 \cdot e \cdot \sin(e) - 10 \cdot x \cdot e \cdot \sin(e)$ .