

(Debug) In[1]:=

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Print[];
Print[" The data for the paper "]
Print[" Structure and energetics of carbon, hexagonal boron nitride, "];
Print[" and carbon/hexagonal boron nitride single-layer and bilayer nanoscrolls "];
Print[" / A.I. Siahlo, N.A. Poklonski, A.V. Lebedev, I.V. Lebedeva, A.M. Popov, S.A. Vyrk
Print[" // Phys. Rev. Materials.- 2018.- V. 2, № 3.- P. 036001 (9 pp.). [DOI: 10.1103/Phy
Print[" -----"];
Print[" I. All Input Parameters and Constants-----"];
Print[" I.1.The dimensions"];
eV=1;atom=1;nm=1;
AA = 0.1 nm; m = 10^9 nm; meV = eV/1000;
Print[" I.2. The Input Geometry Parameters"];
NumberOfLayers1 = 1; NumberOfLayers2 = 2;
NumberOfLayersp = NumberOfLayers1;
Print[" Number of the layers in carbon nanoscroll NumberOfLayers=",
      NumberOfLayersp];
L15nm = 15 nm; L1p = L15nm;
Print[" The length of a carbon nanoribbon L1=", L1p/nm, "nm"];
w1nm = 1 nm; wp = w1nm; width = w1nm;
Print[" The carbon nanoribbon width w=", wp/nm, "nm"];
RIn1nm = 1.1 nm;
RIn2nm = 2.047 nm;
RIn1p = RIn2nm;
Print[" The inner radius of the nanoscroll RIn1=", RIn1p/nm, "nm"];
Print[" I.3. The Input Energy Constants"];
Print[" eps - the interlayer interaction energy per one atom of"];
Print[" the nanoscroll:"];
eps35 = 35.0 meV/atom; epsp = eps35;
Print[" eps=", epsp/(eV/atom), "eV/atom"];
Print[" C - the bending elastic constant:"];
C201 = 2.01 eV AA^2/atom;
CBN1328 = 1.328 eV AA^2/atom;
CCp = C201;
CBNp = CBN1328;
CBNp = CCp;
Print[" CCelast=", CCp/(eV AA^2/atom), "eV AA^2/atom"];
Print[" CCBNelast=", CBNp/(eV AA^2/atom), "eV AA^2/atom"];
Print[" I.4.The Input Geometry constants-----"];
Print[" The interatomic distance aCC and the interlayer distance h"];
aCC142AA = 1.42 AA; aCCp = aCC142AA;
h335nm = 0.3354 nm; hp = h335nm;
Print[" aCC=",aCCp/nm,"nm, h=", hp/nm, "nm"];
Print[" dPhil2 - The difference of the inner angles of the spirales"];
Print[" of the Layers"];
dPhil2eq0 = 0.0 Pi;
dPhil2eqPi = 1.0 Pi;
dPhil2LowLeq0 = 0.0 Pi;
dPhil2HighLeqPi = Pi;
dPhil2p = 0.0 Pi;
dPhil20 = 0.0 Pi;
dPhil2Pi03 = 0.3 Pi;
dPhil2Pi05 = 0.5 Pi;
dPhil2Pi07 = 0.7 Pi;
dPhil2Pi=Pi;
dPhil2HighLp = Pi;
Print[" dPhil2=", dPhil2p/(2 Pi), "(2Pi),for the high L dPhil2HighL=",
      dPhil2HighLp/(2 Pi), "(2Pi)"];
Print[" I.5.The parameters for the visualisation"];
RIn1MinMonoScroll = hp/5;
RIn1MinBiScroll = hp/5;
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RInlMaxMonoScroll = 4 nm;
RInlMaxBiScroll = 8 nm;
PlotRangeMonoScroll = {-4eV/atom, 12eV/atom};
PlotRangeBiScroll = {-10eV/atom, 30eV/atom};
ShowSpirales = True;
ShowThePlot = True;
Print[" I.6. The parameters of the output file"];
NanoscrollName=StringJoin["Nanoscroll",ToString[NumberOfLayersp],"L",ToString[Llp/nm],"n"];
Print[" NanoscrollName=",NanoscrollName];
CarbonNanoscrollEnergyVsRInFileName=StringJoin[NanoscrollName,".txt"];
Print[CarbonNanoscrollEnergyVsRInFileName];
Print[" (The output of the data to a file Is Not Performed)"];
npRInl=1000;
Print[" The number of the output points = ",npRInl];
Print[" I.7. The Input Numerical Constants used in the programm"];
Print[" The Indexes used for the work with EVdW[...] function"];
iEVdW = 1; iEVdW1Unl = 2; iEVdW1Ov1 = 3; iEVdW1Un2 = 4; iEVdW1Ov2 = 5;
5; iEVdW2Unl = 6; iEVdW2Ov1 = 7;
Print[" -----End Of The Input-----"];
Print[" II. The derivated parameters and the functions required"];
Print[" II.1. The derivated parameters"];
fSa[aCC_] := aCC^2 3 Sqrt[3]/4; fSa[aCCp]; Sap = fSa[aCCp];
Print[" The cell area Sa=", fSa[aCC], "=", Sap/nm^2, "nm^2"];
Print[" II.2. The required functions-----"];
Print[" II.2.1. The function"];
Print[" fSpiraleLen[NumberOfLayers,PhiIn, PhiOut, h]"];
Print[" defines the Length of a Spirale with the inner aple PhiIn and
the outer angle PhiOut"];
fSpiraleLen[NumberOfLayersv_,PhiInv_, PhiOutv_, hv_] :=
UnitStep[PhiOutv -
PhiInv] (1/(4 Pi) hv NumberOfLayersv (-PhiInv Sqrt[1 + PhiInv^2] +
PhiOutv Sqrt[1 + PhiOutv^2] - ArcSinh[PhiInv] +
ArcSinh[PhiOutv]));
Print[" II.2.2. The function fElast[PhiIn,PhiOut] is required to
calculate an elastic energy "];
fElast[PhiInv_,
PhiOutv_] := (Sqrt[PhiInv^2 + 1]/PhiInv -
Sqrt[PhiOutv^2 + 1]/PhiOutv - ArcSinh[PhiInv] + ArcSinh[PhiOutv]);
Print[" fElast[PhiIn,PhiOut]=", fElast[PhiIn, PhiOut]];
Print[" II.2.3. The function fPhiOutvsPhiInLh[NumberOfLayers,PhiIn,L,h] is a
good approximation"];
Print[" to obtain the value of PhiOut for the defined PhiIn,L,h "];
fPhiOutvsPhiInLh[NumberOfLayersv_,PhiInv_, Lv_, hv_] :=
Sqrt[4 Pi Lv/(NumberOfLayersv hv) + PhiInv^2];
Print[" fPhiOutvsPhiInLh[NumberOfLayers,PhiIn, L, h]=",
fPhiOutvsPhiInLh[NumberOfLayers,PhiIn, L, h]];
Print[" and the inverse function fPhiInvsPhiOutLh[NumberOfLayers,PhiOut, L, h]:"];
fPhiInvsPhiOutLh[NumberOfLayersv_,PhiOutv_, Lv_, hv_] :=
Sqrt[PhiOutv^2-4 Pi Lv/(NumberOfLayersv hv)];
Print[" fPhiInvsPhiOutLh[NumberOfLayers,PhiOut,L,h]=",
fPhiInvsPhiOutLh[NumberOfLayers,PhiOut, L, h]];
Print[" III. Begin of Calculation "];
Print[" III.1. The inner and the outer angles of the spirales"];
Print[" PhiInl=RInl 2 Pi/(NumberOfLayers h),
PhiOutl=fPhiOutvsPhiInLh[NumberOfLayers,,PhiInl,L1,h]."];
Print[" For RInl=", RInlp/nm, "nm,h=", hp/nm, "nm,NumberOfLayers=",
NumberOfLayersp, ""];
fPhiInl[NumberOfLayersv_, RInlv_, hv_] := RInlv 2 Pi/(NumberOfLayersv hv);
PhiInlp = fPhiInl[NumberOfLayersp, RInlp, hp];
fPhiOutl[NumberOfLayersv_, Llv_, RInlv_, hv_] :=
fPhiOutvsPhiInLh[NumberOfLayersv,fPhiInl[NumberOfLayersv, RInlv, hv], Llv, hv];

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PhiOutlp = fPhiOutl[NumberOfLayersp, Llp, RInlp, hp];
ROutlp = PhiOutlp / NumberOfLayersp * hp / (2 * Pi);
Print[" PhiInl=", PhiInlp / (2 * Pi), "(2Pi),PhiOutl=", PhiOutlp / (2 * Pi),
      "(2Pi)"];
fPhiIn2[NumberOfLayersv_, RInlv_, hv_, dPhi12v_] :=
  fPhiInl[NumberOfLayersv, RInlv, hv] + dPhi12v;
PhiIn2dPhi120p =
  fPhiIn2[NumberOfLayersp, RInlp, hp, 0];
PhiIn2dPhi12Pip =
  fPhiIn2[NumberOfLayersp, RInlp, hp, Pi];
fPhiOut2[NumberOfLayersv_, Llv_, RInlv_, hv_, dPhi12v_] :=
  fPhiOutvsPhiInLh[NumberOfLayersv, fPhiIn2[NumberOfLayersv, RInlv, hv, dPhi12v], Llv, hv]
PhiOut2dPhi120p =
  fPhiOut2[NumberOfLayersp, Llp, RInlp, hp, 0];
Print[" for dPhi12=0: PhiIn2=", PhiIn2dPhi120p / (2 * Pi), "(2Pi),PhiOut2=", PhiOut2dPhi120p /
      "(2Pi)"];
PhiOut2dPhi12Pip =
  fPhiOut2[NumberOfLayersp, Llp, RInlp, hp, Pi];
Print[" for dPhi12=Pi: PhiIn2=", PhiIn2dPhi12Pip / (2 * Pi), "(2Pi),PhiOut2=", PhiOut2dPhi12Pip /
      "(2Pi)"];
Print[" Plot Spirales of the layers for dPhi12=0 and dPhi12=Pi"];
Spirale1Plot =
  PolarPlot[(Phiv) NumberOfLayersp hp / (2 * Pi) / nm, {Phiv, PhiInlp,
    PhiOutlp},
  PlotRange -> {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm,
    1.1 ROutlp / nm}}, PlotStyle -> {Red, Thin}, Axes -> None];
Spirale2dPhi120Plot =
  If[NumberOfLayersp == 2,
    PolarPlot[(Phiv - Pi) NumberOfLayersp hp / (2 * Pi) / nm, {Phiv,
      PhiIn2dPhi120p + Pi, PhiOut2dPhi120p + Pi},
    PlotRange -> {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm,
      1.1 ROutlp / nm}}, PlotStyle -> {Blue, Thin}, Axes -> None], {}];
Spirale2dPhi12PiPlot =
  If[NumberOfLayersp == 2,
    PolarPlot[(Phiv - Pi) NumberOfLayersp hp / (2 * Pi) / nm, {Phiv,
      PhiIn2dPhi12Pip + Pi, PhiOut2dPhi12Pip + Pi},
    PlotRange -> {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm,
      1.1 ROutlp / nm}}, PlotStyle -> {Blue, Thin}, Axes -> None], {}];
Print[Show[{Spirale1Plot, Spirale2dPhi120Plot}], Show[{Spirale1Plot, Spirale2dPhi12PiPlot}]]
If[NumberOfLayersp == 1,
  Spirale1OverSpirale1Plot =
    If[PhiInlp + 2 * Pi < PhiOutlp,
      PolarPlot[(Phiv) NumberOfLayersp hp / (2 * Pi) / nm, {Phiv, PhiInlp + 2 * Pi,
        PhiOutlp},
      PlotRange -> {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm,
        1.1 ROutlp / nm}}, PlotStyle -> {Red, Thick}, Axes -> None], {}];
  Spirale1UnderSpirale1Plot =
    If[PhiInlp < PhiOutlp - 2 * Pi,
      PolarPlot[(Phiv) NumberOfLayersp hp / (2 * Pi) / nm, {Phiv, PhiInlp,
        PhiOutlp - 2 * Pi},
      PlotRange -> {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm,
        1.1 ROutlp / nm}}, PlotStyle -> {Red, Thick}, Axes -> None], {}];
  Print[" {Spirale,
Spirale1UnderSpirale1},{Spirale1,Spirale1OverSpirale1}"];
  Print[Show[{Spirale1Plot, Spirale1UnderSpirale1Plot}],
    Show[{Spirale1Plot, Spirale1OverSpirale1Plot}]]];
If[NumberOfLayersp == 2,
  Spirale1UnderSpirale2dPhi120Plot =
    If[PhiInlp < PhiOut2dPhi120p - Pi,
      PolarPlot[(Phiv) NumberOfLayersp hp / (2 * Pi) / nm, {Phiv, PhiInlp,
        PhiOut2dPhi120p - Pi}, PlotStyle -> {Red, Thick},

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PlotRange -> {{-1.1 ROutlp/nm, 1.1 ROutlp/nm}, {-1.1 ROutlp/nm,
1.1 ROutlp/nm}}, {}];
Spirale1OverSpirale2dPhil120Plot =
If[PhiInlp + Pi +
dPhil120 < PhiOutlp,
PolarPlot[(Phiv) NumberOfLayersp hp/(2 Pi)/nm, {Phiv,
PhiInlp + Pi +
dPhil120, PhiOutlp},
PlotStyle -> {Red, Thick},
PlotRange -> {{-1.1 ROutlp/nm, 1.1 ROutlp/nm}, {-1.1 ROutlp/nm,
1.1 ROutlp/nm}}, {}];
Spirale2UnderSpirale1dPhil120Plot =
If[PhiIn2dPhil120p + Pi < PhiOutlp,
PolarPlot[(Phiv - Pi) NumberOfLayersp hp/(2 Pi)/nm, {Phiv,
PhiIn2dPhil120p + Pi, PhiOutlp}, PlotStyle -> {Blue, Thick},
PlotRange -> {{-1.1 ROutlp/nm, 1.1 ROutlp/nm}, {-1.1 ROutlp/nm,
1.1 ROutlp/nm}}, {}];
Spirale2OverSpirale1dPhil120Plot =
If[2 Pi + PhiIn2dPhil120p -
dPhil120 <
PhiOut2dPhil120p + Pi,
PolarPlot[(Phiv - Pi) NumberOfLayersp hp/(2 Pi)/nm, {Phiv,
2 Pi + PhiIn2dPhil120p -
dPhil120,
PhiOut2dPhil120p + Pi}, PlotStyle -> {Blue, Thick},
PlotRange -> {{-1.1 ROutlp/nm, 1.1 ROutlp/nm}, {-1.1 ROutlp/nm,
1.1 ROutlp/nm}}, {}];
Spirale1UnderSpirale2dPhil12PiPlot =
If[PhiInlp < PhiOut2dPhil12Pip - Pi,
PolarPlot[(Phiv) NumberOfLayersp hp/(2 Pi)/nm, {Phiv, PhiInlp,
PhiOut2dPhil12Pip - Pi}, PlotStyle -> {Red, Thick},
PlotRange -> {{-1.1 ROutlp/nm, 1.1 ROutlp/nm}, {-1.1 ROutlp/nm,
1.1 ROutlp/nm}}, {}];
Spirale1OverSpirale2dPhil12PiPlot =
If[PhiInlp + Pi +
dPhil12Pi < PhiOutlp,
PolarPlot[(Phiv) NumberOfLayersp hp/(2 Pi)/nm, {Phiv,
PhiInlp + Pi +
dPhil12Pi, PhiOutlp},
PlotStyle -> {Red, Thick},
PlotRange -> {{-1.1 ROutlp/nm, 1.1 ROutlp/nm}, {-1.1 ROutlp/nm,
1.1 ROutlp/nm}}, {}];
Spirale2UnderSpirale1dPhil12PiPlot =
If[PhiIn2dPhil120p + Pi < PhiOutlp,
PolarPlot[(Phiv - Pi) NumberOfLayersp hp/(2 Pi)/nm, {Phiv,
PhiIn2dPhil12Pip + Pi, PhiOutlp}, PlotStyle -> {Blue, Thick},
PlotRange -> {{-1.1 ROutlp/nm, 1.1 ROutlp/nm}, {-1.1 ROutlp/nm,
1.1 ROutlp/nm}}, {}];
Spirale2OverSpirale1dPhil12PiPlot =
If[2 Pi + PhiIn2dPhil12Pip -
dPhil12Pi <
PhiOut2dPhil12Pip + Pi,
PolarPlot[(Phiv - Pi) NumberOfLayersp hp/(2 Pi)/nm, {Phiv,
2 Pi + PhiIn2dPhil12Pip -
dPhil12Pi,
PhiOut2dPhil12Pip + Pi}, PlotStyle -> {Blue, Thick},
PlotRange -> {{-1.1 ROutlp/nm, 1.1 ROutlp/nm}, {-1.1 ROutlp/nm,
1.1 ROutlp/nm}}, {}];

Print[" {Spirale1,Spirale2,Spirale1UnderSpirale2,Spirale2UnderSpirale1},"];
Print[" {Spirale1,Spirale2,Spirale1OverSpirale2,Spirale2OverSpirale1}"];

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Print[" for dPhi12=0: ",Show[Spirale1Plot, Spirale2dPhi120Plot],
Show[Spirale1Plot, Spirale2dPhi120Plot, Spirale1UnderSpirale2dPhi120Plot,
Spirale2UnderSpirale1dPhi120Plot],
Show[Spirale1Plot, Spirale2dPhi120Plot, Spirale1OverSpirale2dPhi120Plot,
Spirale2OverSpirale1dPhi120Plot]];
Print[" for dPhi12=Pi: ",Show[Spirale1Plot, Spirale2dPhi12PiPlot],
Show[Spirale1Plot, Spirale2dPhi12PiPlot, Spirale1UnderSpirale2dPhi12PiPlot,
Spirale2UnderSpirale1dPhi12PiPlot],
Show[Spirale1Plot, Spirale2dPhi12PiPlot, Spirale1OverSpirale2dPhi12PiPlot,
Spirale2OverSpirale1dPhi12PiPlot]];
];
Print[" III.2. The nanoscroll energy calculation"];
Print[" III.2.1. The elastic energy calculation"];
fElastCC[NumberOfLayersv_, Llv_, RInlv_, hv_, aCCv_, CCv_] :=
Module[{},
Return[2 Pi CCv width/(hv fSa[aCCv]) fElast[
fPhiIn1[NumberOfLayersv, RInlv, hv],
fPhiOut1[NumberOfLayersv, Llv, RInlv, hv]]]];
fElastCBN[NumberOfLayersv_, Llv_, RInlv_, hv_, aCCv_, CBNv_] :=
Module[{},
Return[2 Pi CBNv width/(hv fSa[aCCv]) fElast[
fPhiIn1[NumberOfLayersv, RInlv, hv],
fPhiOut1[NumberOfLayersv, Llv, RInlv, hv]]]];
EelastCCp = fElastCC[NumberOfLayersp, Llp, RInlp, hp, aCCp, CCp];
EelastCBNp = fElastCBN[NumberOfLayersp, Llp, RInlp, hp, aCCp, CBNp];
Print[" EelastC=", EelastCCp/(eV/atom), "eV/atom"];
Print[" EelastBN=", EelastCBNp/(eV/atom), "eV/atom"];
Print[" III.2.2. The Van-der-Waals energy calculation"];
fEvdWdPhi12[NumberOfLayersv_, Llv_, RInlv_, hv_, aCCv_, epsv_, dPhi12v_] :=
Module[{EvdW, PhiIn1, PhiIn2, PhiOut1, PhiOut2,
EvdW1Un1=0 (eV/atom), EVdW1Ov1=0 (eV/atom),
EvdW1Un2=0 (eV/atom), EVdW1Ov2=0 (eV/atom),
EvdW2Un1=0 (eV/atom), EVdW2Ov1=0 (eV/atom),
Spirale1UnderSpirale1Length=0 nm, Spirale1OverSpirale1Length=0 nm,
Spirale1UnderSpirale2Length=0 nm, Spirale1OverSpirale2Length=0 nm,
Spirale2UnderSpirale1Length=0 nm, Spirale2OverSpirale1Length=0 nm},
PhiIn1 = fPhiIn1[NumberOfLayersv, RInlv, hv];
PhiIn2 =
fPhiIn2[NumberOfLayersv, RInlv, hv, dPhi12v];
PhiOut1 = fPhiOut1[NumberOfLayersv, Llv, RInlv, hv];
PhiOut2 =
fPhiOut2[NumberOfLayersv, Llv, RInlv, hv, dPhi12v];
EvdW =
Switch[NumberOfLayersv, 1,
Spirale1UnderSpirale1Length =
If[PhiIn1 < PhiOut1 - 2 Pi,
fSpiraleLen[NumberOfLayersv, PhiIn1, PhiOut1 - 2 Pi, hv], 0 nm];
Spirale1OverSpirale1Length =
If[PhiIn1 + 2 Pi < PhiOut1,
fSpiraleLen[NumberOfLayersv, PhiIn1 + 2 Pi, PhiOut1, hv], 0 nm];
EvdW1Un1 = -epsv width/(2 fSa[aCCv]) Spirale1UnderSpirale1Length;
EvdW1Ov1 = -epsv width/(2 fSa[aCCv]) Spirale1OverSpirale1Length;
(EvdW1Un1 + EVdW1Ov1), 2,
Spirale1UnderSpirale2Length =
If[PhiIn1 < PhiOut2 - Pi,
fSpiraleLen[NumberOfLayersv, PhiIn1, PhiOut2 - Pi, hv], 0 nm];
Spirale1OverSpirale2Length =
If[PhiIn1 + Pi + dPhi12v < PhiOut1,
fSpiraleLen[NumberOfLayersv,
PhiIn1 + Pi + dPhi12v,
PhiOut1, hv], 0 nm];

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Spirale2UnderSpirale1Length =
  If[PhiIn1 + dPhi12v <
    PhiOut1 - Pi,
    fSpiraleLen[NumberOfLayersv,
      PhiIn1 + dPhi12v,
      PhiOut1 - Pi,hv], 0 nm];
Spirale2OverSpirale1Length =
  If[PhiIn1 - dPhi12v + Pi <
    PhiOut2 - dPhi12v,
    fSpiraleLen[NumberOfLayersv,
      PhiIn1 -dPhi12v+ Pi,
      PhiOut2 - dPhi12v,
      hv], 0 nm];
EvdW1Un2 = -epsv wdh/(2 fSa[aCCv]) Spirale1UnderSpirale2Length;
EvdW1Ov2 = -epsv wdh/(2 fSa[aCCv]) Spirale1OverSpirale2Length;
EvdW2Un1 = -epsv wdh/(2 fSa[aCCv]) Spirale2UnderSpirale1Length;
EvdW2Ov1 = -epsv wdh/(2 fSa[aCCv]) Spirale2OverSpirale1Length;
"EVdW=(EvdW1Un2+EvdW1Ov2+EvdW2Un1+EvdW2Ov1)";
(EvdW1Un2 + EvdW1Ov2 + EvdW2Un1 + EvdW2Ov1)];
Return[{EVdW, EvdW1Un1, EvdW1Ov1, EvdW1Un2, EvdW1Ov2, EvdW2Un1,
  EvdW2Ov1}];];
EvdWwardPhi12allp =
  fEvdWdPhi12[NumberOfLayersp, Llp, RInlp, hp, aCCp, epsp, dPhi12p];
Print[" for dPhi12=",dPhi12p/Pi,"Pi EvdWwardPhi12allp[[iEvdW]]=",
  EvdWwardPhi12allp[[iEvdW]]/(eV/atom), "eV/atom"];
If[NumberOfLayersp == 1,
  Print[" EvdWwardPhi12allp[[iEvdW1Un1]]=",
    EvdWwardPhi12allp[[iEvdW1Un1]]/(eV/atom), "eV/atom"];
  Print[" EvdWwardPhi12allp[[iEvdW1Ov1]]=",
    EvdWwardPhi12allp[[iEvdW1Ov1]]/(eV/atom), "eV/atom"];];
If[NumberOfLayersp == 2,
  EvdWdPhi12eq0allp =
    fEvdWdPhi12[NumberOfLayersp, Llp, RInlp, hp, aCCp, epsp, dPhi12eq0];
  Print[" For dPhi12=", dPhi12eq0/Pi, "Pi:"];
  Print[" EvdWwardPhi12allp[[iEvdW]]=",
    EvdWdPhi12eq0allp[[iEvdW]]/(eV/atom), "eV/atom"];
  Print[" EvdWwardPhi12allp[[iEvdW1Un2]]=",
    EvdWdPhi12eq0allp[[iEvdW1Un2]]/(eV/atom), "eV/atom"];
  Print[" EvdWwardPhi12allp[[iEvdW1Ov2]]=",
    EvdWdPhi12eq0allp[[iEvdW1Ov2]]/(eV/atom), "eV/atom"];
  Print[" EvdWwardPhi12allp[[iEvdW2Un1]]=",
    EvdWdPhi12eq0allp[[iEvdW2Un1]]/(eV/atom), "eV/atom"];
  Print[" EvdWwardPhi12allp[[iEvdW2Ov2]]=",
    EvdWdPhi12eq0allp[[iEvdW2Ov1]]/(eV/atom), "eV/atom"];
  EvdWdPhi12eqPiallp =
    fEvdWdPhi12[NumberOfLayersp, Llp, RInlp, hp, aCCp, epsp, dPhi12eqPi];
  Print[" For dPhi12=", dPhi12eqPi/Pi, "Pi:"];
  Print[" EvdWwardPhi12allp[[iEvdW]]=",
    EvdWdPhi12eqPiallp[[iEvdW]]/(eV/atom), "eV/atom"];
  Print[" EvdWwardPhi12allp[[iEvdW1Un2]]=",
    EvdWdPhi12eqPiallp[[iEvdW1Un2]]/(eV/atom), "eV/atom"];
  Print[" EvdWwardPhi12allp[[iEvdW1Ov2]]=",
    EvdWdPhi12eqPiallp[[iEvdW1Ov2]]/(eV/atom), "eV/atom"];
  Print[" EvdWwardPhi12allp[[iEvdW2Un1]]=",
    EvdWdPhi12eqPiallp[[iEvdW2Un1]]/(eV/atom), "eV/atom"];
  Print[" EvdWwardPhi12allp[[iEvdW2Ov2]]=",
    EvdWdPhi12eqPiallp[[iEvdW2Ov1]]/(eV/atom), "eV/atom"];
  EvdWEvdWdPhi12eq0p = EvdWdPhi12eq0allp[[iEvdW]];
  Print[" EvdWdPhi12eq0allp=", EvdWdPhi12eq0allp/(eV/atom),
    "eV/atom"];
  EvdWEvdWdPhi12eqPip = EvdWwardPhi12allp[[iEvdW]];

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Print[" EVdWEVdWdPhil2eqPip=", EVdWEVdWdPhil2eqPip/(eV/atom),
      "eV/atom"];];
Print[" III.3. The energy of flat places "];
fEnergyFlatPlates[NumberOfLayersv_, Llv_, aCCv_,
  epsv_] := If[NumberOfLayersv == 2, -epsv width/fSa[aCCv] Llv, 0 eV/atom];
EnergyFlatPlatesp = fEnergyFlatPlates[NumberOfLayersp, Llp, aCCp, epsp];
Print[" EnergyFlatPlates=-eps width/Sa L1(NumberOfLayers-1) =",
      EnergyFlatPlatesp/(eV/atom), "eV/atom"];

Print[" III.4. The total energy of the nanoscroll"];
fScrollEnergydPhi[NumberOfLayersv_, Llv_, RInlv_, hv_, aCCv_, epsv_, CCv_,
  CBNv_, dPhil2v_] :=
Module[{ScrollEnergyv, EVdWv, EVdWt, iLl},
  EVdWv = fEVdWdPhil2[NumberOfLayersv, Llv, RInlv, hv, aCCv, epsv,
    dPhil2v][[1]];
  If[NumberOfLayersv == 1,
    ScrollEnergyv =
      EVdWv + fEelastCC[NumberOfLayersv, Llv, RInlv, hv, aCCv, CCv]];
  If[NumberOfLayersv == 2,
    ScrollEnergyv =
      EVdWv + fEelastCC[NumberOfLayersv, Llv, RInlv, hv, aCCv, CCv] +
      fEelastCBN[NumberOfLayersv, Llv, RInlv, hv, aCCv, CCv]];
  Return[ScrollEnergyv];];
fScrollEnergy[NumberOfLayersv_, Llv_, RInlv_, hv_, aCCv_, epsv_, CCv_,
  CBNv_] :=
Module[{ScrollEnergyv, EVdWv, EVdWt, iLl,
  ScrollEnergydPhieq0v, ScrollEnergydPhieqPiv,
  dPhil2eq0=0, dPhil2eqPi=Pi},
  ScrollEnergydPhieq0v = fScrollEnergydPhi[NumberOfLayersv, Llv, RInlv, hv, aCCv, epsv, CCv,
    CBNv, dPhil2eq0];
  ScrollEnergydPhieqPiv = fScrollEnergydPhi[NumberOfLayersv, Llv, RInlv, hv, aCCv, epsv, CCv,
    CBNv, dPhil2eqPi];
  ScrollEnergyv = Min[ScrollEnergydPhieq0v/(eV/atom), ScrollEnergydPhieqPiv/(eV/atom)] (eV/atc
  Return[ScrollEnergyv];]

Print[" III.5. Determine the inner angles mismatch for the bi-layer nanoscroll
      for the high nanoribbon Length"];
ScrollEnergydPhil2Pip0p =
  fScrollEnergydPhi[NumberOfLayersp, Llp, RInlp, hp, aCCp, epsp, CCp, CBNp, 0];
ScrollEnergydPhil2PipPi =
  fScrollEnergydPhi[NumberOfLayersp, Llp, RInlp, hp, aCCp, epsp, CCp, CBNp, Pi];
Print[" For L1=", Llp/nm, "nm, RIn=", RInlp/nm, "nm, h=", hp/nm, "nm and dPhil2=0:"];
Print[" ScrollEnergy=", ScrollEnergydPhil2Pip0p/(eV/atom), "eV/atom"];
Print[" For L1=", Llp/nm, "nm, RIn=", RInlp/nm, "nm, h=", hp/nm, "nm and dPhil2=Pi:"];
Print[" ScrollEnergy=", ScrollEnergydPhil2Pip/(eV/atom), "eV/atom"];

Print[" IV. The potential energy of the scroll"];
Print[" as a function of the inner radius RIn"];
PlotRange =
  Switch[NumberOfLayersp, 1, PlotRangeMonoScroll, 2, PlotRangeBiScroll];
RInlMinp =
  Switch[NumberOfLayersp, 1, RInlMinMonoScroll, 2, RInlMinBiScroll];
RInlMaxp =
  Switch[NumberOfLayersp, 1, RInlMaxMonoScroll, 2, RInlMaxBiScroll];
PlotRange =
  Switch[NumberOfLayersp, 1, PlotRangeMonoScroll, 2, PlotRangeBiScroll];
RInlMaxp =
  Switch[NumberOfLayersp, 1, RInlMaxMonoScroll, 2, RInlMaxBiScroll];
tL1 = Switch[NumberOfLayersp, 1, {7 nm, 10 nm, 12.5 nm, 15 nm},
  2, {15 nm, 20 nm, 25 nm, 30 nm}];
Print[" NumberOfLayers=", NumberOfLayersp];
Print[" eps=", epsp/(eV/atom), "eV/atom, C=", CCp/(eV nm^2/atom),

```

```

    "(eV nm^2/atom),aCC=", aCCp, "nm,h=", hp/nm, "nm");
Print[" Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1=", Llp/nm,
    "nm (NumberOfLayers=", NumberOfLayersp, ",w=", wdth/nm, "nm)"];
PlotScrollEnergyVsRIn1 = Plot[(fScrollEnergy[NumberOfLayersp, Llp, RIn1nmv nm, hp, aCCp,
    CCp, CBNp] -
    fEnergyFlatPlates[NumberOfLayersp, Llp, aCCp, epsp])/(eV/
    atom), {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange -> PlotRange/(eV/atom)];
Print[PlotScrollEnergyVsRIn1];
Print[" Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1=", tL1/nm,
    "nm (NumberOfLayers=", NumberOfLayersp, ",w=", wdth/nm, "nm)"];
PlotScrollEnergyVsRIn1L1th =
    Plot[(fScrollEnergy[NumberOfLayersp, tL1[[1]], RIn1nmv nm, hp, aCCp, epsp,
    CCp, CBNp] -
    fEnergyFlatPlates[NumberOfLayersp, tL1[[1]], aCCp, epsp])/(eV/
    atom), {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange -> PlotRange/(eV/atom)];
PlotScrollEnergyVsRIn1L2th =
    Plot[(fScrollEnergy[NumberOfLayersp, tL1[[2]], RIn1nmv nm, hp, aCCp, epsp,
    CCp, CBNp] -
    fEnergyFlatPlates[NumberOfLayersp, tL1[[2]], aCCp, epsp])/(eV/
    atom), {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange -> PlotRange/(eV/atom)];
PlotScrollEnergyVsRIn1L3th =
    Plot[(fScrollEnergy[NumberOfLayersp, tL1[[3]], RIn1nmv nm, hp, aCCp, epsp,
    CCp, CBNp] -
    fEnergyFlatPlates[NumberOfLayersp, tL1[[3]], aCCp, epsp])/(eV/
    atom), {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange -> PlotRange/(eV/atom)];
PlotScrollEnergyVsRIn1L4th =
    Plot[(fScrollEnergy[NumberOfLayersp, tL1[[4]], RIn1nmv nm, hp, aCCp, epsp,
    CCp, CBNp] -
    fEnergyFlatPlates[NumberOfLayersp, tL1[[4]], aCCp, epsp])/(eV/
    atom), {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange -> PlotRange/(eV/atom)];
Print[Show[{PlotScrollEnergyVsRIn1L1th, PlotScrollEnergyVsRIn1L2th,
    PlotScrollEnergyVsRIn1L3th, PlotScrollEnergyVsRIn1L4th}]];
Clear[eV, atom, nm];

Print[" Export the plot data to the files"];
tRIn1Regular=Table[RIn1Minp+(RIn1Maxp-RIn1Minp) iiRIn/(npRIn1),{iiRIn,1,npRIn1}];
tScrollEnergy=tRIn1Regular;
tScrollEnergyMEnergyFlatPlates=tRIn1Regular;
eV=1;atom=1;nm=1;
tPlotEvsRin=Table[{},{ii,1,Length[tL1]}];
AllPlotsEVsRin={};
For[iiL1=1,iiL1<=Length[tL1],iiL1++,
    Llp=tL1[[iiL1]];
    NanoscrollNamep=StringJoin["Nanoscroll",ToString[NumberOfLayersp],"L",ToString[Llp/nm],"n"];
    Print[" NanoscrollName=",NanoscrollNamep];
    ScrollEnergyMEnergyFlatPlatesFileName=ToFileName[NotebookDirectory[],StringJoin["EvsRin1"
    Print[" ScrollEnergyMEnergyFlatPlatesFileName=",ScrollEnergyMEnergyFlatPlatesFileName];
    EnergyFlatPlatesp=fEnergyFlatPlates[NumberOfLayersp, Llp, aCCp, epsp];
    For[iiRIn1=1,iiRIn1<=npRIn1,iiRIn1++,
        RIn1i=tRIn1Regular[[iiRIn1]];
        tScrollEnergy[[iiRIn1]]=fScrollEnergy[NumberOfLayersp, Llp, RIn1i, hp, aCCp, epsp,
            CCp, CBNp];
        tScrollEnergyMEnergyFlatPlates[[iiRIn1]]=tScrollEnergy[[iiRIn1]]-EnergyFlatPlatesp;
    ];
    tPlotEvsRin[[iiL1]]=ListPlot[Transpose[{tRIn1Regular,tScrollEnergyMEnergyFlatPlates}], Pl
    "Print[tPlotEvsRin[[iiL1]]];";
    AllPlotsEVsRin=Join[{AllPlotsEVsRin,tPlotEvsRin[[iiL1]]}];
    CarbonNanoscrollEnergyVsRinFileName=StringJoin[NanoscrollNamep,"dat"];
    Export[ScrollEnergyMEnergyFlatPlatesFileName,Transpose[{tRIn1Regular,tScrollEnergyMEnergy
    ];
    Print[" Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1=", tL1/nm,

```



```

    "nm (NumberOfLayers=", NumberOfLayersp, ",w=", width/nm, "nm)";
Print[Show[AllPlotsEVsRin]];
Clear[eV, atom, nm];

```

The data for the paper

Structure and energetics of carbon, hexagonal boron nitride,  
and carbon/hexagonal boron nitride single-layer and bilayer nanoscrolls

/ A.I. Siahlo, N.A. Poklonski, A.V. Lebedev, I.V.  
Lebedeva, A.M. Popov, S.A. Vyrko, A.A. Knizhnik, Yu.E. Lozovik  
// Phys. Rev. Materials.— 2018.— V. 2, №  
3.— P. 036001 (9 pp.). [DOI: 10.1103/PhysRevMaterials.2.036001]

-----  
I. All Input Parameters and Constants-----

I.1.The dimensions

I.2. The Input Geometry Parameters

Number of the layers in carbon nanoscroll NumberOfLayers=1

The length of a carbon nanoribbon L1=15nm

The carbon nanoribbon width w=1nm

The inner radius of the nanoscroll RIn1=2.047nm

I.3. The Input Energy Constants

eps - the interlayer interaction energy per one atom of  
the nanoscroll:

eps=0.035eV/atom

C - the bending elastic constant:

CCelast=2.01eV AA<sup>2</sup>/atom

CCBNelast=2.01eV AA<sup>2</sup>/atom

I.4.The Input Geometry constants-----

The interatomic distance aCC and the interlayer distance h

aCC=0.142nm, h=0.3354nm

dPhi12 - The difference of the inner angles of the spirales  
of the Layers

```

dPhi12=0.(2Pi),for the high L dPhi12HighL= $\frac{1}{2}(2Pi)$ 

I.5.The parameters for the visualisation
I.6. The parameters of the output file
NanoscrollName=Nanoscroll1L15nm
Nanoscroll1L15nm.txt

(The output of the data to a file Is Not Performed)
The number of the output points = 1000

I.7. The Input Numerical Constants used in the programm
The Indexes used for the work with EVdW[...] function
-----End Of The Input-----

II. The derivated parameters and the functions required
II.1. The derivated parameters

The cell area Sa= $\frac{3\sqrt{3} aCC^2}{4}=0.0261938nm^2$ 

II.2. The required functions-----
II.2.1. The function
fSpiraleLen[NumberOfLayers,PhiIn, PhiOut, h]

defines the Length of a Spirale with the inner agle PhiIn and
the outer angle PhiOut

II.2.2. The function fElast[PhiIn,PhiOut] is required to
calculate an elastic energy

fElast[PhiIn,PhiOut]= $\frac{\sqrt{1+PhiIn^2}}{PhiIn} - \frac{\sqrt{1+PhiOut^2}}{PhiOut} - ArcSinh[PhiIn] + ArcSinh[PhiOut]$ 

II.2.3. The function fPhiOutvsPhiInLh[NumberOfLayers,PhiIn,L,h] is a
good approximation
to obtain the value of PhiOut for the defined PhiIn,L,h

fPhiOutvsPhiInLh[NumberOfLayers,PhiIn,L,h]= $\sqrt{PhiIn^2 + \frac{4 L \pi}{h NumberOfLayers}}$ 

and the inverse function fPhiInvsPhiOutLh[NumberOfLayers,PhiOut, L, h]:

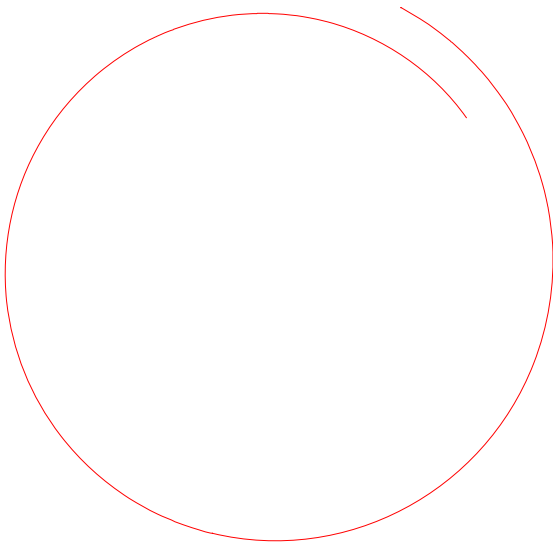
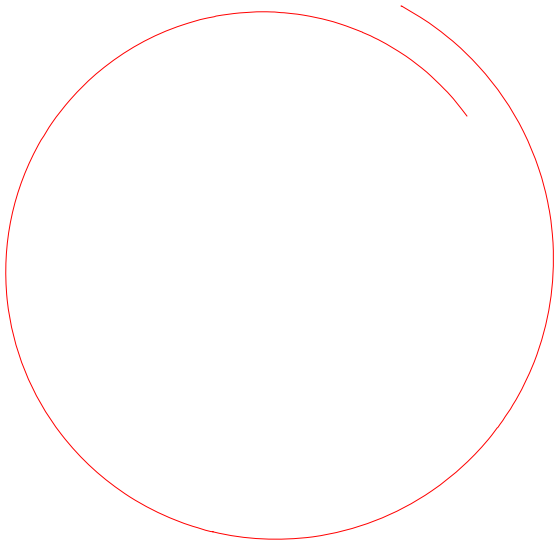
fPhiInvsPhiOutLh[NumberOfLayers,PhiOut,L,h]= $\sqrt{PhiOut^2 - \frac{4 L \pi}{h NumberOfLayers}}$ 

III. Begin of Calculation
III.1. The inner and the outer angles of the spirales
PhiIn1=RIn1 2 Pi/(NumberOfLayers h),
PhiOut1=fPhiOutvsPhiInLh[NumberOfLayers,,PhiIn1,L1,h].
For RIn1=2.047nm,h=0.3354nm,NumberOfLayers=1:
PhiIn1=6.10316(2Pi),PhiOut1=7.17525(2Pi)
for dPhi12=0: PhiIn2=6.10316(2Pi),PhiOut2=7.17525(2Pi)

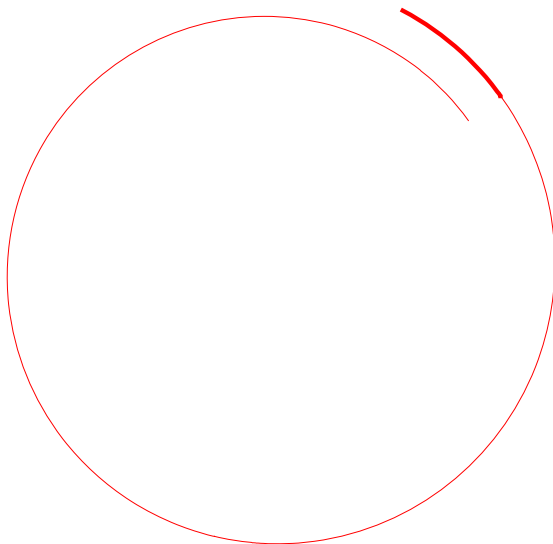
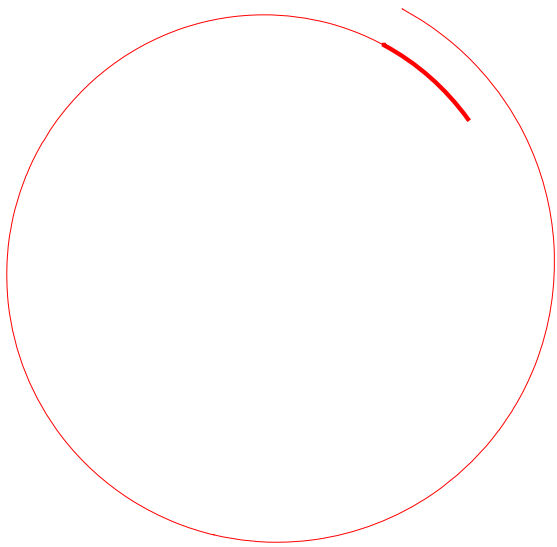
```

```
for dPhi12=Pi: PhiIn2=6.60316(2Pi),PhiOut2=7.60509(2Pi)
```

```
Plot Spirales of the layers for dPhi12=0 and dPhi12=Pi
```



```
{Spirale,  
Spirale1UnderSpirale1},{Spirale1,Spirale1OverSpirale1}
```



III.2. The nanoscroll energy calculation

III.2.1. The elastic energy calculation

$E_{\text{elastC}} = 2.32703 \text{ eV/atom}$

$E_{\text{elastBN}} = 2.32703 \text{ eV/atom}$

III.2.2. The Van-der-Waals energy calculation

for  $d\Phi_{12} = 0$ ,  $E_{\text{VdWvard}\Phi_{12}\text{allp}}[[iE_{\text{VdW}}]] = -1.34816 \text{ eV/atom}$

$E_{\text{VdWvard}\Phi_{12}\text{allp}}[[iE_{\text{VdWlUn1}}]] = -0.623346 \text{ eV/atom}$

$E_{\text{VdWvard}\Phi_{12}\text{allp}}[[iE_{\text{VdWlOv1}}]] = -0.724818 \text{ eV/atom}$

III.3. The energy of flat places

$E_{\text{EnergyFlatPlates}} = -\epsilon_{\text{ps width}} / S_{\text{a L1}} (\text{NumberOfLayers} - 1) = 0 \text{ eV/atom}$

III.4. The total energy of the nanoscroll

III.5. Determine the inner angles mismatch for the bi-layer nanoscroll  
for the high nanoribbon Length

For  $L1=15\text{nm}$ ,  $RIn=2.047\text{nm}$ ,  $h=0.3354\text{nm}$  and  $d\Phi12=0$ :

ScrollEnergy=0.978871eV/atom

For  $L1=15\text{nm}$ ,  $RIn=2.047\text{nm}$ ,  $h=0.3354\text{nm}$  and  $d\Phi12=\pi$ :

ScrollEnergy=ScrollEnergydPhi12PipeV/atom

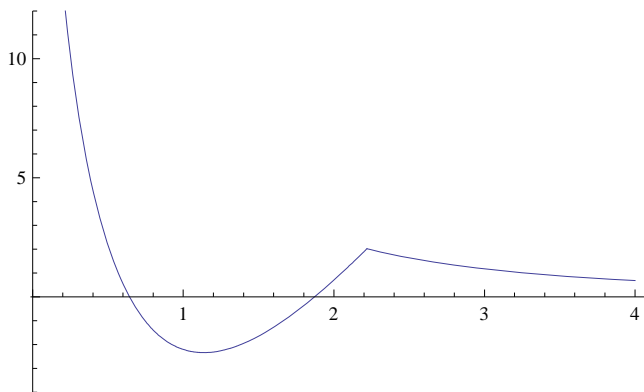
IV. The potential energy of the scroll

as a function of the inner radius  $RIn$

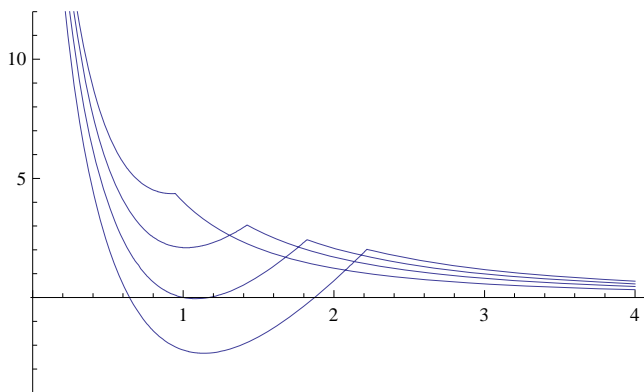
NumberOfLayers=1

$\epsilon=0.035\text{eV/atom}$ ,  $C=0.0201(\text{eV nm}^2/\text{atom})$ ,  $aCC=0.142\text{nm}$ ,  $h=0.3354\text{nm}$

Plot ScrollEnergy[ $RIn1/\text{nm}$ ]/(eV/atom) for  $L1=15\text{nm}$  (NumberOfLayers=1,  $w=1\text{nm}$ )



Plot ScrollEnergy[ $RIn1/\text{nm}$ ]/(eV/atom) for  $L1=\{7, 10, 12.5, 15\}\text{nm}$  (NumberOfLayers=1,  $w=1\text{nm}$ )



Export the plot data to the files

NanoscrollName=Nanoscroll1L7nm

ScrollEnergyMEnergyFlatPlatesFileName=C:\1\EvsRin1Nanoscroll1L7nm.dat

NanoscrollName=Nanoscroll1L10nm

ScrollEnergyMEnergyFlatPlatesFileName=C:\1\EvsRin1Nanoscroll1L10nm.dat

NanoscrollName=Nanoscroll1L12.5nm

ScrollEnergyMEnergyFlatPlatesFileName=C:\1\EvsRin1Nanoscroll1L12.5nm.dat

NanoscrollName=Nanoscroll1L15nm

ScrollEnergyMEnergyFlatPlatesFileName=C:\1\EvsRin1Nanoscroll1L15nm.dat

Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1={7, 10, 12.5, 15}nm (NumberOfLayers=1,w=1nm)

