```
In[1]:=
```

```
Print[];
Print[" The data for the paper "];
Print[" Structure and energetics of carbon, hexagonal boron nitride, "];
Print[" and carbon/hexagonal boron nitride single-layer and bilayer nanoscrolls "];
Print[" / A.I. Siahlo, N.A. Poklonski, A.V. Lebedev, I.V. Lebedeva, A.M. Popov, S.A. Vy
Print[" // Phys. Rev. Materials. - 2018. - V. 2, № 3. - P. 036001 (9 pp.). [DOI: 10.1103/F
Print[" -----"];
Print[" I. All Input Parameters and Constants-----"];
Print[" I.1.The dimensions"];
AA = 0.1 \text{ nm}; m = 10^9 \text{ nm}; meV = eV/1000;
Print[" I.2. The Input Geometry Parameters"];
NumberOfLayers1 = 1; NumberOfLayers2 = 2;
NumberOfLayersp = NumberOfLayers2;
Print[" Number of the layers in carbon nanoscroll NumberOfLayers=",
 NumberOfLayersp];
L15nm = 15 nm; L1p = L15nm;
Print[" The length of a carbon nanoribbon L1=", L1p/nm, "nm"];
w1nm = 1. nm; wp = w1nm;
Print[" The carbon nanoribbon width w=", wp/nm, "nm"];
RIn1nm = 1.1 nm;
RIn2nm = 2.047 nm;
RIn1p = RIn2nm;
Print[" The inner radius of the nanoscroll RIn1=", RIn1p/nm, "nm"];
Print[" I.3. The Input Energy Constants"];
Print[" eps - the interlayer interaction energy per one atom of"];
Print[" the nanoscroll:"];
eps35 = 35.0 meV/atom; epsp = eps35;
Print[" eps=", epsp/(eV/atom), "eV/atom"];
Print[" C - the bending elastic constant:"];
C201 = 2.01 \text{ eV AA}^2/\text{atom};
CBN1328 = 1.328 \text{ eV } AA^2/atom;
CCp = C201;
CBNp = CBN1328;
CBNp = CCp;
Print[" CCelast=", CCp/(eV AA^2/atom), "eV AA^2/atom"];
Print[" CCBNelast=", CBNp/(eV AA^2/atom), "eV AA^2/atom"];
Print[" I.4.The Input Geometry constants----"];
Print[" The interatomic distance aCC and the interlayer distance h"];
aCC142AA = 1.42 AA; aCCp = aCC142AA;
h335nm = 0.3354 nm; hp = h335nm;
Print[" aCC=",aCCp/nm,"nm, h=", hp/nm, "nm"];
Print[" dPhi12 - The difference of the inner angles of the spirales"];
Print[" of the Layers"];
dPhi12eq0 = 0.0 Pi;
dPhi12eqPi = 1.0 Pi;
dPhi12LowLeq0 = 0.0 Pi;
dPhi12HighLeqPi = Pi;
dPhi12p = 0.0 Pi;
dPhi120 = 0.0 Pi;
dPhi12Pi03 = 0.3 Pi;
dPhi12Pi05 = 0.5 Pi;
dPhi12Pi07 = 0.7 Pi;
dPhi12Pi=Pi;
dPhi12HighLp = Pi;
Print[" dPhi12=", dPhi12p/(2 Pi), "(2Pi), for the high L dPhi12HighL=",
 dPhi12HighLp/(2 Pi), "(2Pi)"];
Print[" I.5.The parameters for the visualisation"];
RIn1MinMonoScroll = hp/5;
RIn1MinBiScroll = hp/5;
```

```
RIn1MaxMonoScroll = 4 nm;
RIn1MaxBiScroll = 8 nm;
PlotRangeMonoScroll = {-4eV/atom, 12eV/atom};
PlotRangeBiScroll = {-10eV/atom, 30eV/atom};
ShowSpirales = True;
ShowThePlot = True;
Print[" I.6. The parameters of the output file"];
NanoscrollNamep=StringJoin["Nanoscroll", ToString[NumberOfLayersp], "L", ToString[Llp/nm],
Print[" NanoscrollName=", NanoscrollNamep];
CarbonNanoscrollEnergyVsRInFileName=StringJoin[NanoscrollNamep,".txt"];
Print[CarbonNanoscrollEnergyVsRInFileName];
Print[" (The output of the data to a file Is Not Performed)"];
npRIn1=1000;
Print[" The number of the output points = ",npRIn1];
Print[" I.7. The Input Numerical Constants used in the programm"];
Print[" The Indexes used for the work with EVdW[...] function"];
iEVdW = 1; iEVdW1Un1 = 2; iEVdW1Ov1 = 3; iEVdW1Un2 = 4; iEVdW1Ov2 = 5;
5; iEVdW2Un1 = 6; iEVdW2Ov1 = 7;
Print[" -----End Of The Input-----"];
Print[" II. The derivated parameters and the functions required"];
Print[" II.1. The derivated parameters"];
fSa[aCC_] := aCC^2 3 Sqrt[3]/4; fSa[aCCp]; Sap = fSa[aCCp];
Print[" The cell area Sa=", fSa[aCC], "=", Sap/nm^2, "nm^2"];
Print[" II.2. The required functions----"];
Print[" II.2.1. The function"];
Print[" fSpiraleLen[NumberOfLayers,PhiIn, PhiOut, h]"];
Print[" defines the Length of a Spirale with the inner agle PhiIn and
the outer angle PhiOut"];
fSpiraleLen[NumberOfLayersv_,PhiInv_, PhiOutv_, hv_] :=
 UnitStep[PhiOutv -
    PhiInv] (1/(4 Pi) hv NumberOfLayersv (-PhiInv Sqrt[1 + PhiInv^2] +
       PhiOutv Sqrt[1 + PhiOutv^2] - ArcSinh[PhiInv] +
      ArcSinh[PhiOutv]));
Print[" II.2.2. The function fElast[PhiIn, PhiOut] is required to
calculate an elastic energy "];
fElast[PhiInv ,
  PhiOutv ] := (Sqrt[PhiInv^2 + 1]/PhiInv -
   Sqrt[PhiOutv^2 + 1]/PhiOutv - ArcSinh[PhiInv] + ArcSinh[PhiOutv]);
Print[" fElast[PhiIn, PhiOut] = ", fElast[PhiIn, PhiOut]];
Print[" II.2.3. The function fPhiOutvsPhiInLh[NumberOfLayers,PhiIn,L,h] is a
good approximation"];
Print[" to obtain the value of PhiOut for the defined PhiIn, L, h "];
fPhiOutvsPhiInLh[NumberOfLayersv , PhiInv , Lv , hv ] :=
  Sqrt[4 π Lv/(NumberOfLayersv hv) + PhiInv^2];
Print[" fPhiOutvsPhiInLh[NumberOfLayers,PhiIn,L,h]=",
 fPhiOutvsPhiInLh[NumberOfLayers,PhiIn, L, h]];
Print[" and the inverse function fPhiInvsPhiOutLh[NumberOfLayers, PhiOut, L, h]:"];
fPhiInvsPhiOutLh[NumberOfLayersv , PhiOutv , Lv , hv ] :=
 Sqrt[PhiOutv^2-4 \pi Lv/(NumberOfLayersv hv)];
Print[" fPhiInvsPhiOutLh[NumberOfLayers,PhiOut,L,h]=",
fPhiInvsPhiOutLh[NumberOfLayers,PhiOut, L, h]];
Print[" III. Begin of Calculation "];
Print[" III.1. The inner and the outer angles of the spirales"];
Print[" PhiIn1=RIn1 2 Pi/(NumberOfLayers h),
PhiOut1=fPhiOutvsPhiInLh[NumberOfLayers, PhiIn1, L1, h]."];
Print[" For RIn1=", RIn1p/nm, "nm, h=", hp/nm, "nm, NumberOfLayers=",
 NumberOfLayersp, ":"];
fPhiIn1[NumberOfLayersv_, RIn1v_, hv_] := RIn1v 2 Pi/(NumberOfLayersv hv);
PhiIn1p = fPhiIn1[NumberOfLayersp, RIn1p, hp];
```

```
fPhiOut1[NumberOfLayersv_, L1v_, RIn1v_, hv_] :=
 fPhiOutvsPhiInLh[NumberOfLayersv, fPhiIn1[NumberOfLayersv, RIn1v, hv], L1v, hv];
PhiOut1p = fPhiOut1[NumberOfLayersp, L1p, RIn1p, hp];
ROut1p = PhiOut1p NumberOfLayersp hp/(2 Pi);
Print[" PhiIn1=", PhiIn1p/(2 Pi), "(2Pi), PhiOut1=", PhiOut1p/(2 Pi),
 "(2Pi)"];
fPhiIn2[NumberOfLayersv , RIn1v , hv , dPhi12v ] :=
 fPhiIn1[NumberOfLaversy, RIn1v, hv] + dPhi12v;
PhiIn2dPhi120p =
 fPhiIn2[NumberOfLayersp, RIn1p, hp,0];
PhiIn2dPhi12Pip =
 fPhiIn2[NumberOfLayersp, RIn1p, hp,Pi];
fPhiOut2[NumberOfLayersv_, L1v_, RIn1v_, hv_, dPhi12v ] :=
 fPhiOutvsPhiInLh[NumberOfLayersv, fPhiIn2[NumberOfLayersv, RIn1v, hv, dPhi12v], L1v, h
PhiOut2dPhi120p =
 fPhiOut2[NumberOfLayersp, L1p, RIn1p, hp,0];
Print[" for dPhi12=0: PhiIn2=", PhiIn2dPhi120p/(2 Pi), "(2Pi), PhiOut2=", PhiOut2dPhi120
 "(2Pi)"];
PhiOut2dPhi12Pip =
 fPhiOut2[NumberOfLayersp, L1p, RIn1p, hp,Pi];
Print[" for dPhi12=Pi: PhiIn2=", PhiIn2dPhi12Pip/(2 Pi), "(2Pi), PhiOut2=", PhiOut2dPhi1
 "(2Pi)"];
Print[" Plot Spirales of the layers for dPhi12=0 and dPhi12=Pi"];
Spirale1Plot =
 PolarPlot[(Phiv) NumberOfLayersp hp/(2 Pi)/nm, {Phiv, PhiIn1p,
   PhiOut1p},
   PlotRange -> {{-1.1 ROut1p/nm, 1.1 ROut1p/nm}, {-1.1 ROut1p/nm,
      1.1 ROut1p/nm}}, PlotStyle -> {Red, Thin}, Axes -> None];
Spirale2dPhi120Plot =
 If[NumberOfLayersp == 2,
  PolarPlot[(Phiv - Pi) NumberOfLayersp hp/(2 Pi)/nm, {Phiv,
    PhiIn2dPhi120p + Pi, PhiOut2dPhi120p + Pi},
    PlotRange -> {{-1.1 ROut1p/nm, 1.1 ROut1p/nm}, {-1.1 ROut1p/nm,
       1.1 ROut1p/nm}}, PlotStyle -> {Blue, Thin}, Axes -> None], {}];
Spirale2dPhi12PiPlot =
 If[NumberOfLayersp == 2,
  PolarPlot[(Phiv - Pi) NumberOfLayersp hp/(2 Pi)/nm, {Phiv,
     PhiIn2dPhi12Pip + Pi, PhiOut2dPhi12Pip + Pi},
    PlotRange \rightarrow {{-1.1 ROut1p/nm, 1.1 ROut1p/nm}, {-1.1 ROut1p/nm,
       1.1 ROut1p/nm}}, PlotStyle -> {Blue, Thin}, Axes -> None], {}];
Print[Show[{Spirale1Plot, Spirale2dPhi120Plot}],Show[{Spirale1Plot, Spirale2dPhi12PiPlot}]
If[NumberOfLayersp == 1,
 Spirale1OverSpirale1Plot =
   If(PhiIn1p + 2 Pi < PhiOut1p,</pre>
    PolarPlot[(Phiv) NumberOfLayersp hp/(2 Pi)/nm, {Phiv, PhiIn1p + 2 Pi,
      PhiOut1p},
     PlotRange -> {{-1.1 ROutlp/nm, 1.1 ROutlp/nm}, {-1.1 ROutlp/nm,
        1.1 ROutlp/nm}}, PlotStyle -> {Red, Thick}, Axes -> None], {}];
 Spirale1UnderSpirale1Plot =
  If[PhiIn1p < PhiOut1p - 2 Pi,</pre>
   PolarPlot[(Phiv) NumberOfLayersp hp/(2 Pi)/nm, {Phiv, PhiIn1p,
      PhiOut1p - 2 Pi},
     PlotRange -> {{-1.1 ROut1p/nm, 1.1 ROut1p/nm}, {-1.1 ROut1p/nm,
        1.1 ROut1p/nm}}, PlotStyle -> {Red, Thick}, Axes -> None], {}];
 Print[" {Spirale,
Spirale1UnderSpirale1, {Spirale1, Spirale1OverSpirale1}"];
 Print[Show[{Spirale1Plot, Spirale1UnderSpirale1Plot}],
  Show[{Spirale1Plot, Spirale1OverSpirale1Plot}]];];
If[NumberOfLayersp == 2,
Spirale1UnderSpirale2dPhi120Plot =
```

```
If[PhiIn1p < PhiOut2dPhi120p - Pi,</pre>
   PolarPlot[(Phiv) NumberOfLayersp hp/(2 Pi)/nm, {Phiv, PhiIn1p,
      PhiOut2dPhi120p - Pi}, PlotStyle -> {Red, Thick},
     PlotRange -> {{-1.1 ROut1p/nm, 1.1 ROut1p/nm}, {-1.1 ROut1p/nm,
       1.1 ROut1p/nm}}], {}];
Spirale10verSpirale2dPhi120Plot =
  If[PhiIn1p + Pi +
      dPhi120 < PhiOut1p,
    PolarPlot[(Phiv) NumberOfLayersp hp/(2 Pi)/nm, {Phiv,
     PhiIn1p + Pi +
      dPhi120, PhiOut1p},
     PlotStyle -> {Red, Thick},
     PlotRange -> {{-1.1 ROutlp/nm, 1.1 ROutlp/nm}, {-1.1 ROutlp/nm,
        1.1 ROutlp/nm}}], {}];
Spirale2UnderSpirale1dPhi120Plot =
   If[PhiIn2dPhi120p + Pi < PhiOut1p,</pre>
    PolarPlot[(Phiv - Pi) NumberOfLayersp hp/(2 Pi)/nm, {Phiv,
      PhiIn2dPhi120p + Pi, PhiOut1p}, PlotStyle -> {Blue, Thick},
     PlotRange -> {{-1.1 ROut1p/nm, 1.1 ROut1p/nm}, {-1.1 ROut1p/nm,
        1.1 ROut1p/nm}}], {}];
Spirale2OverSpirale1dPhi12OPlot =
   If[2 Pi + PhiIn2dPhi120p -
      dPhi120 <
     PhiOut2dPhi120p + Pi,
    PolarPlot[(Phiv - Pi) NumberOfLayersp hp/(2 Pi)/nm, {Phiv,
      2 Pi + PhiIn2dPhi120p -
      dPhi120,
      PhiOut2dPhi120p + Pi}, PlotStyle -> {Blue, Thick},
     PlotRange -> {{-1.1 ROut1p/nm, 1.1 ROut1p/nm}, {-1.1 ROut1p/nm,
        1.1 ROut1p/nm}}], {}];
Spirale1UnderSpirale2dPhi12PiPlot =
   If[PhiIn1p < PhiOut2dPhi12Pip - Pi,</pre>
    PolarPlot[(Phiv) NumberOfLayersp hp/(2 Pi)/nm, {Phiv, PhiIn1p,
      PhiOut2dPhi12Pip - Pi}, PlotStyle -> {Red, Thick},
     PlotRange -> {{-1.1 ROut1p/nm, 1.1 ROut1p/nm}, {-1.1 ROut1p/nm,
        1.1 ROut1p/nm}}], {}];
Spirale10verSpirale2dPhi12PiPlot =
  If[PhiIn1p + Pi +
      dPhi12Pi < PhiOut1p,
    PolarPlot[(Phiv) NumberOfLayersp hp/(2 Pi)/nm, {Phiv,
     PhiIn1p + Pi +
      dPhi12Pi, PhiOut1p},
    PlotStyle -> {Red, Thick},
     PlotRange -> {{-1.1 ROut1p/nm, 1.1 ROut1p/nm}, {-1.1 ROut1p/nm,
        1.1 ROut1p/nm}}], {}];
Spirale2UnderSpirale1dPhi12PiPlot =
   If(PhiIn2dPhi120p + Pi < PhiOut1p,</pre>
    PolarPlot[(Phiv - Pi) NumberOfLayersp hp/(2 Pi)/nm, {Phiv,
      PhiIn2dPhi12Pip + Pi, PhiOut1p}, PlotStyle -> {Blue, Thick},
     PlotRange -> {{-1.1 ROut1p/nm, 1.1 ROut1p/nm}, {-1.1 ROut1p/nm,
        1.1 ROut1p/nm}}], {}];
Spirale2OverSpirale1dPhi12PiPlot =
   If[2 Pi + PhiIn2dPhi12Pip -
      dPhi12Pi <
     PhiOut2dPhi12Pip + Pi,
    PolarPlot[(Phiv - Pi) NumberOfLayersp hp/(2 Pi)/nm, {Phiv,
      2 Pi + PhiIn2dPhi12Pip -
      dPhi12Pi,
      PhiOut2dPhi12Pip + Pi}, PlotStyle -> {Blue, Thick},
     PlotRange \rightarrow {{-1.1 ROut1p/nm, 1.1 ROut1p/nm}, {-1.1 ROut1p/nm,
```

```
1.1 ROut1p/nm}}], {}];
  Print[" {Spirale1, Spirale2, Spirale1UnderSpirale2, Spirale2UnderSpirale1}, "];
  Print["
            {Spirale1, Spirale2, Spirale10verSpirale2, Spirale20verSpirale1}"];
  Print[" for dPhi12=0: ",Show[Spirale1Plot, Spirale2dPhi120Plot],
  Show[Spirale1Plot, Spirale2dPhi120Plot, Spirale1UnderSpirale2dPhi120Plot,
    Spirale2UnderSpirale1dPhi120Plot],
  Show[Spirale1Plot, Spirale2dPhi120Plot, Spirale1OverSpirale2dPhi120Plot,
    Spirale2OverSpirale1dPhi12OPlot]];
Print[" for dPhi12=Pi: ",Show[Spirale1Plot, Spirale2dPhi12PiPlot],
  Show[Spirale1Plot, Spirale2dPhi12PiPlot, Spirale1UnderSpirale2dPhi12PiPlot,
    Spirale2UnderSpirale1dPhi12PiPlot],
   Show[Spirale1Plot, Spirale2dPhi12PiPlot, Spirale1OverSpirale2dPhi12PiPlot,
    Spirale2OverSpirale1dPhi12PiPlot]];
];
Print[" III.2. The nanoscroll energy calculation"];
Print[" III.2.1. The elastic energy calculation"];
fEelastCC[NumberOfLayersv ,wv ,L1v ,RIn1v ,hv ,aCCv ,CCv ] :=
  Module[{},
  Return[2 Pi CCv wv/(hv fSa[aCCv]) fElast[
       fPhiIn1[NumberOfLayersv, RIn1v, hv],
       fPhiOut1[NumberOfLayersv, L1v, RIn1v, hv]]];];
fEelastCBN[NumberOfLayersv_, wv_,Llv_, RIn1v_, hv_, aCCv_, CBNv_] :=
 Module[{},
  Return[2 Pi CBNv wv/(hv fSa[aCCv]) fElast[
       fPhiIn1[NumberOfLayersv, RIn1v, hv],
       fPhiOut1[NumberOfLayersv, L1v, RIn1v, hv]]];];
EelastCCp = fEelastCC[NumberOfLayersp,wp,L1p, RIn1p, hp, aCCp, CCp];
EelastCBNp = fEelastCBN[NumberOfLayersp,wp,L1p, RIn1p, hp, aCCp, CBNp];
Print[" EelastC=", EelastCCp/(eV/atom), "eV/atom"];
Print[" EelastBN=", EelastCBNp/(eV/atom), "eV/atom"];
Print[" III.2.2. The Van-der-Waals energy calculation"];
fEVdWdPhi12[NumberOfLayersv_,wv_,L1v_, RIn1v_, hv_, aCCv_, epsv_, dPhi12v_] :=Module[
{EVdW,
EVdW1Un1=0 (eV/atom), EVdW1Ov1=0 (eV/atom),
 EVdW1Un2=0 (eV/atom), EVdW1Ov2=0 (eV/atom),
 EVdW2Un1=0 (eV/atom), EVdW2Ov1=0 (eV/atom),
 Spirale1UnderSpirale1Length=0 nm, Spirale1OverSpirale1Length=0 nm,
 Spirale1UnderSpirale2Length=0 nm, Spirale1OverSpirale2Length=0 nm,
 Spirale2UnderSpirale1Length=0 nm, Spirale2OverSpirale1Length=0 nm,
PhiIn1 = fPhiIn1[NumberOfLayersv, RIn1v, hv],
 PhiIn2 = fPhiIn2[NumberOfLayersv, RIn1v, hv, dPhi12v],
 PhiOut1 = fPhiOut1[NumberOfLayersv, L1v, RIn1v, hv],
 PhiOut2 = fPhiOut2[NumberOfLayersv, L1v, RIn1v, hv, dPhi12v]
},
If[NumberOfLayersv== 1,
If[PhiIn1 < PhiOut1 - 2 Pi,Spirale1UnderSpirale1Length=fSpiraleLen[NumberOfLayersv,PhiI
If[PhiIn1 + 2 Pi < PhiOut1, Spirale10verSpirale1Length= fSpiraleLen[NumberOfLayersv, PhiI
EVdW1Un1 = -epsv wv/(2 fSa[aCCv]) Spirale1UnderSpirale1Length;
EVdW1Ov1 = -epsv wv/(2 fSa[aCCv]) Spirale1OverSpirale1Length;
EVdW= (EVdW1Un1 + EVdW1Ov1);
1;
If[NumberOfLayersv== 2,
    If[PhiIn1 < PhiOut2 - Pi,Spirale1UnderSpirale2Length = fSpiraleLen[NumberOfLayersv,</pre>
    If[PhiIn1 + Pi +dPhi12v<PhiOut1,Spirale1OverSpirale2Length = fSpiraleLen[NumberOfLa</pre>
    If[PhiIn1 + dPhi12v < PhiOut1 - Pi,Spirale2UnderSpirale1Length = fSpiraleLen[Number</pre>
    If[PhiIn1 - dPhi12v + Pi < PhiOut2 - dPhi12v,Spirale2OverSpirale1Length=fSpiraleLer
EVdW1Un2 = -epsv wv/(2 fSa[aCCv]) Spirale1UnderSpirale2Length;
     EVdW10v2 = -epsv wv/(2 fSa[aCCv]) Spirale10verSpirale2Length;
     EVdW2Un1 = -epsv wv/(2 fSa[aCCv]) Spirale2UnderSpirale1Length;
```

```
EVdW2Ov1 = -epsv wv/(2 fSa[aCCv]) Spirale2OverSpirale1Length;
     EVdW= (EVdW1Un2+EVdW1Ov2+EVdW2Un1+EVdW2Ov1);
1;
Return[{EVdW, EVdW1Un1, EVdW1Ov1, EVdW1Un2, EVdW1Ov2, EVdW2Un1,EVdW2Ov1}];
EVdWdPhi12eq0allp =
fEVdWdPhi12[NumberOfLayers2, wp, L1p, RIn1p, hp, aCCp, epsp, dPhi12eq0];
EVdWvardPhi12allp =
 fEVdWdPhi12[NumberOfLayersp,wp,L1p, RIn1p, hp, aCCp, epsp, dPhi12p];
Print[" for dPhi12=",dPhi12p/Pi,"Pi EVdWvardPhi12allp[[iEVdW]]=",
 EVdWvardPhi12allp[[iEVdW]]/(eV/atom), "eV/atom"];
If[NumberOfLayersp == 1,
 Print[" EVdWvardPhi12allp[[iEVdW1Un1]]=",
  EVdWvardPhi12allp[[iEVdW1Un1]]/(eV/atom), "eV/atom"];
  Print[" EVdWvardPhi12allp[[iEVdW10v1]]=",
  EVdWvardPhi12allp[[iEVdW1Ov1]]/(eV/atom), "eV/atom"];];
If[NumberOfLayersp == 2,
EVdWdPhi12eq0allp =
   fEVdWdPhi12[NumberOfLayersp,wp,L1p,RIn1p, hp, aCCp, epsp, dPhi12eq0];
  Print[" For dPhi12=", dPhi12eq0/Pi, "Pi:"];
 Print[" EVdWvardPhi12allp[[iEVdW]]=",
  EVdWdPhi12eq0allp[[iEVdW]]/(eV/atom), "eV/atom"];
  Print[" EVdWvardPhi12allp[[iEVdW1Un2]]=",
  EVdWdPhi12eq0allp[[iEVdW1Un2]]/(eV/atom), "eV/atom"];
 Print[" EVdWvardPhi12allp[[iEVdW10v2]]=",
  EVdWdPhi12eq0allp[[iEVdW1Ov2]]/(eV/atom), "eV/atom"];
 Print[" EVdWvardPhi12allp[[iEVdW2Un1]]=",
  EVdWdPhi12eq0allp[[iEVdW2Un1]]/(eV/atom), "eV/atom"];
 Print[" EVdWvardPhi12allp[[iEVdW20v2]]=",
  EVdWdPhi12eq0allp[[iEVdW2Ov1]]/(eV/atom), "eV/atom"];
 EVdWdPhi12eqPiallp =
  fEVdWdPhi12[NumberOfLayersp,wp,L1p,RIn1p, hp, aCCp, epsp, dPhi12eqPi];
  Print[" For dPhi12=", dPhi12eqPi/Pi, "Pi:"];
  Print[" EVdWvatdPhi12allp[[iEVdW]]=",
  EVdWdPhi12eqPiallp[[iEVdW]]/(eV/atom), "eV/atom"];
  Print[" EVdWvatdPhi12allp[[iEVdW1Un2]]=",
  EVdWdPhi12eqPiallp[[iEVdW1Un2]]/(eV/atom), "eV/atom"];
 Print[" EVdWvatdPhi12allp[[iEVdW10v2]]=",
  EVdWdPhi12eqPiallp[[iEVdW1Ov2]]/(eV/atom), "eV/atom"];
 Print[" EVdWvatdPhi12allp[[iEVdW2Un1]]=",
  EVdWdPhi12eqPiallp[[iEVdW2Un1]]/(eV/atom), "eV/atom"];
 Print[" EVdWvatdPhi12allp[[iEVdW2Ov2]]=",
  EVdWdPhi12eqPiallp[[iEVdW2Ov1]]/(eV/atom), "eV/atom"];
 EVdWEVdWdPhi12eq0p = EVdWdPhi12eq0allp[[iEVdW]];
 Print[" EVdWdPhi12eg0allp=", EVdWdPhi12eg0allp/(eV/atom),
  "eV/atom"];
 EVdWEVdWdPhi12eqPip = EVdWvardPhi12allp[[iEVdW]];
  Print[" EVdWEVdWdPhi12eqPip=", EVdWEVdWdPhi12eqPip/(eV/atom),
   "eV/atom"];];
Print[" III.3. The energy of flat places "];
fEnergyFlatPlates[NumberOfLayersv_, wv_,L1v_, aCCv_,epsv_]:=If[NumberOfLayersv==2,-epsv
EnergyFlatPlatesp = fEnergyFlatPlates[NumberOfLayersp,wp,L1p, aCCp, epsp];
Print[" EnergyFlatPlates=-eps width/Sa L1(NumberOfLayers-1) =",
 EnergyFlatPlatesp/(eV/atom), "eV/atom"];
Print[" III.4. The total energy of the nanoscroll"];
fScrollEnergydPhi[NumberOfLayersv_, wv_,Llv_, RIn1v_, hv_, aCCv_, epsv_, CCv_,CBNv_, dF
Module[{ScrollEnergyv, EVdWv, EVdWt, iL1,EVdWnoDimv},
 EVdWv = fEVdWdPhi12[NumberOfLayersv,wv,Llv, RIn1v, hv, aCCv, epsv,dPhi12v][[1]];
EVdWnoDimv=EVdWv/.{eV->1,atom->1,nm->1};
  If[NumberOfLayersv == 1,
```

```
If [EVdWnoDimv==0,ScrollEnergyv=fEelastCC [NumberOfLayersv,wv,L1v, RIn1v, hv, aCCv,
                     ScrollEnergyv=EVdWv +fEelastCC[NumberOfLayersv,wv,Llv, RIn1v, hv, aCCv, CCv];]
         1;
    If[NumberOfLayersv == 2,
If[EVdWnoDimv==0,
                  ScrollEnergyv =fEelastCC[NumberOfLayersv,wv,Llv, RIn1v, hv, aCCv, CCv] +
                   fEelastCBN[NumberOfLayersv,wv,L1v, RIn1v, hv, aCCv, CCv],
                  ScrollEnergyv=EVdWv+fEelastCC[NumberOfLayersv,wv,Llv, RIn1v, hv, aCCv, CCv] +
                   fEelastCBN[NumberOfLayersv,wv,Llv, RIn1v, hv, aCCv, CCv];];
    1;
    Return[ScrollEnergyv];
1:
fScrollEnergy[NumberOfLayersv_,wv_,Llv_, RInlv_, hv_, aCCv_, epsv_, CCv_,CBNv_] :=
 Module[{ScrollEnergyv, EVdWv, EVdWt, iL1,
ScrollEnergydPhieqOv, ScrollEnergydPhieqPiv,
dPhi12eq0=0, dPhi12eqPi=Pi},
ScrollEnergydPhieqOv=fScrollEnergydPhi NumberOfLayersv, wv, Llv, RInlv, hv, aCCv, epsv, C
    CBNv, dPhi12ea01;
  ScrollEnergydPhieqPiv=fScrollEnergydPhi[NumberOfLayersv,wv,Llv, RIn1v, hv, aCCv, epsv,
   CBNv, dPhi12eqPi];
      ScrollEnergyv=Min[ScrollEnergydPhieq0v/.\{eV->1,atom->1,nm->1\},ScrollEnergydPhieqPiv/atom->1,nm->1\},ScrollEnergydPhieqPiv/atom->1,nm->1\},ScrollEnergydPhieqPiv/atom->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,nm->1,
    Return[ScrollEnergyv];]
Print[" III.5. Determine the inner angles mismatch for the bi-layer nanoscroll
                for the high nanoribbon Length"];
ScrollEnergydPhi12Pip0p =
   fScrollEnergydPhi[NumberOfLayersp,wp,Llp, RInlp, hp, aCCp, epsp, CCp, CBNp,0];
ScrollEnergydPhi12PipPip =
    fScrollEnergydPhi[NumberOfLayersp,wp,L1p, RIn1p, hp, aCCp, epsp, CCp, CBNp,Pi];
Print[" For L1=", L1p/nm, "nm,RIn=", RIn1p/nm, "nm,h=", hp/nm, "nm and dPhi12=0:"];
Print[" ScrollEnergy=", ScrollEnergydPhi12Pip0p/(eV/atom), "eV/atom"];
Print[" For L1=", L1p/nm, "nm,RIn=", RIn1p/nm, "nm,h=", hp/nm, "nm and dPhi12=Pi:"];
Print[" ScrollEnergy=", ScrollEnergydPhi12Pip/(eV/atom), "eV/atom"];
Print[" IV.The potential energy of the scroll"];
Print[" as a function of the inner radius RIn"];
PlotRangep =
    Switch[NumberOfLayersp, 1, PlotRangeMonoScroll, 2, PlotRangeBiScroll];
RIn1Minp =
   Switch [NumberOfLayersp, 1, RIn1MinMonoScroll, 2, RIn1MinBiScroll];
RIn1Maxp =
    Switch[NumberOfLayersp, 1, RIn1MaxMonoScroll, 2, RIn1MaxBiScroll];
    Switch[NumberOfLayersp, 1, PlotRangeMonoScroll, 2, PlotRangeBiScroll];
RIn1Maxp =
    Switch[NumberOfLayersp, 1, RIn1MaxMonoScroll, 2, RIn1MaxBiScroll];
tL1 = Switch[NumberOfLayersp, 1, {7 nm, 10 nm, 12.5 nm, 15 nm},
      2, {15 nm, 20 nm, 25 nm, 30 nm}];
Print[" NumberOfLayers=", NumberOfLayersp];
Print[" eps=", epsp/(eV/atom),"eV/atom, C=", CCp/(eV nm^2/atom),"(eV nm^2/atom)",
    "(eV nm^2/atom),aCC=", aCCp/nm,"nm,h=", hp/nm, "nm"];
Print[" Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1=", L1p/nm,
     "nm (NumberOfLayers=", NumberOfLayersp, ",w=", wp/nm,"nm"];
PlotScrollEnergyVsRIn1 = Plot[(fScrollEnergy[NumberOfLayersp,wp,L1p,RIn1nmv nm,hp, aCCr
                  CCp, CBNp] -
                {\tt fEnergyFlatPlates[NumberOfLayersp,wp,L1p, aCCp, epsp])/(eV/Memory)} = {\tt fEnergyFlatPlates[NumberOfLayersp,wp,L1p, aCCp, epsp]} = {\tt fEnergyFlatPlates[NumberOfLayersp,wp,L1p, epsp]} = {\tt fEnergyFlatPlates
                   atom), {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange -> PlotRangep/(eV/atom)];
Print[PlotScrollEnergyVsRIn1];
Print[" Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1=", tL1/nm,
    "nm (NumberOfLayers=", NumberOfLayersp, ",w=", wp/nm, "nm)"];
PlotScrollEnergyVsRIn1L1th =
    Plot[(fScrollEnergy[NumberOfLayersp,wp,tL1[[1]], RIn1nmv nm,hp, aCCp, epsp,
```

```
CCp, CBNp] -
             fEnergyFlatPlates[NumberOfLayersp,wp,tL1[[1]], aCCp, epsp])/(eV/
              atom), {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange -> PlotRangep/(eV/atom)];
PlotScrollEnergyVsRIn1L2th =
   Plot[(fScrollEnergy[NumberOfLayersp,wp,tL1[[2]], RIn1nmv nm,hp, aCCp, epsp,
              CCp, CBNp] -
             fEnergyFlatPlates[NumberOfLayersp,wp,tL1[[2]], aCCp, epsp])/(eV/
              atom), {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange -> PlotRangep/(eV/atom)];
PlotScrollEnergyVsRIn1L3th =
   Plot[(fScrollEnergy[NumberOfLayersp,wp,tL1[[3]], RIn1nmv nm,hp, aCCp, epsp,
              CCp, CBNp] -
             fEnergyFlatPlates[NumberOfLayersp,wp,tL1[[3]],aCCp, epsp])/(eV/
              atom), {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange -> PlotRangep/(eV/atom)];
PlotScrollEnergyVsRIn1L4th =
   Plot[(fScrollEnergy[NumberOfLayersp,wp,tL1[[4]], RIn1nmv nm,hp, aCCp, epsp,
              CCp, CBNp] -
             fEnergyFlatPlates[NumberOfLayersp,wp,tL1[[4]], aCCp, epsp])/(eV/
              atom), {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange -> PlotRangep/(eV/atom)];
Print[Show[{PlotScrollEnergyVsRIn1L1th, PlotScrollEnergyVsRIn1L2th,
       PlotScrollEnergyVsRIn1L3th, PlotScrollEnergyVsRIn1L4th}]];
Print[" Export the plot data to the files"];
tRIn1Regular=Table[RIn1Minp+(RIn1Maxp-RIn1Minp) iiRIn/(npRIn1),{iiRIn,1,npRIn1}];
tScrollEnergy=tRIn1Regular;
tScrollEnergymEnergyFlatPlates=tRIn1Regular;
tPlotEvsRin=Table[{},{ii,1,Length[tL1]}];
AllPlotsEVsRin={};L1ptmp=L1p;
For[iiL1=1,iiL1<=Length[tL1],iiL1++,</pre>
L1p=tL1[[iiL1]];
NanoscrollNamep=StringJoin["Nanoscroll", ToString[NumberOfLayersp], "L", ToString[Llp/nm],
Print[" NanoscrollName=", NanoscrollNamep];
ScrollEnergyMEnergyFlatPlatesFileName=ToFileName[NotebookDirectory[],StringJoin["EvsRir
Print[" ScrollEnergyMEnergyFlatPlatesFileName=",ScrollEnergyMEnergyFlatPlatesFileName];
EnergyFlatPlatesp=fEnergyFlatPlates[NumberOfLayersp,wp,L1p, aCCp, epsp];
For[iiRIn1=1,iiRIn1<=npRIn1,iiRIn1++,</pre>
RIn1i=tRIn1Regular[[iiRIn1]];
tScrollEnergy[[iiRIn1]]=fScrollEnergy[NumberOfLayersp,wp,L1p, RIn1i, hp, aCCp, epsp,
              CCp, CBNp];
tScrollEnergymEnergyFlatPlates[[iiRIn1]]=tScrollEnergy[[iiRIn1]]-EnergyFlatPlatesp;
tPlotEvsRin[[iiL1]]=ListPlot[Transpose[{tRIn1Regular/nm,tScrollEnergymEnergyFlatPlates/
"Print[tPlotEvsRin[[iiL1]]];";
AllPlotsEVsRin=Join[{AllPlotsEVsRin,tPlotEvsRin[[iiL1]]}];
CarbonNanoscrollEnergyVsRInFileName=StringJoin[NanoscrollNamep,"dat"];
Export[ScrollEnergyMEnergyFlatPlatesFileName, Transpose[{tRIn1Regular/nm,tScrollEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymEnergymE
1;
Print[" Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1=", tL1/nm,
   "nm (NumberOfLayers=", NumberOfLayersp, ",w=", wp/nm, "nm)"];
Print[Show[AllPlotsEVsRin]];L1p=L1ptmp;
```

```
The data for the paper
Structure and energetics of carbon, hexagonal boron nitride,
and carbon/hexagonal boron nitride single-layer and bilayer nanoscrolls
/ A.I. Siahlo, N.A. Poklonski, A.V. Lebedev, I.V.
Lebedeva, A.M. Popov, S.A. Vyrko, A.A. Knizhnik, Yu.E. Lozovik
// Phys. Rev. Materials. - 2018. - V. 2, Nº 3. -
P. 036001 (9 pp.). [DOI: 10.1103/PhysRevMaterials.2.036001]
I. All Input Parameters and Constants-----
I.1. The dimensions
I.2. The Input Geometry Parameters
Number of the layers in carbon nanoscroll NumberOfLayers=2
The length of a carbon nanoribbon L1=15\,\mathrm{nm}
The carbon nanoribbon width w=1.nm
The inner radius of the nanoscroll RIn1=2.047nm \,
I.3. The Input Energy Constants
eps - the interlayer interaction energy per one atom of
the nanoscroll:
eps=0.035eV/atom
C - the bending elastic constant:
CCelast=2.01eV AA^2/atom
CCBNelast=2.01eV AA^2/atom
I.4. The Input Geometry constants-----
The interatomic distance aCC and the interlayer distance h
aCC=0.142nm, h=0.3354nm
dPhi12 - The difference of the inner angles of the spirales
 of the Layers
```

dPhi12=0.(2Pi), for the high L dPhi12HighL= $\frac{1}{2}$ (2Pi)

I.5. The parameters for the visualisation

I.6. The parameters of the output file

NanoscrollName=Nanoscroll2L15nm

Nanoscroll2L15nm.txt

(The output of the data to a file Is Not Performed)

The number of the output points = 1000

I.7. The Input Numerical Constants used in the programm

The Indexes used for the work with  ${\tt EVdW[...]}$  function

-----End Of The Input-----

- II. The derivated parameters and the functions required
- II.1. The derivated parameters

The cell area 
$$Sa = \frac{3\sqrt{3} \ aCC^2}{4} = 0.0261938 nm^2$$

- II.2. The required functions-----
- II.2.1. The function

fSpiraleLen[NumberOfLayers, PhiIn, PhiOut, h]

defines the Length of a Spirale with the inner agle PhiIn and the outer angle PhiOut

II.2.2. The function fElast[PhiIn, PhiOut] is required to calculate an elastic energy

$$\texttt{fElast[PhiIn,PhiOut]} = \frac{\sqrt{1 + PhiIn^2}}{PhiIn} - \frac{\sqrt{1 + PhiOut^2}}{PhiOut} - ArcSinh[PhiIn] + ArcSinh[PhiOut]$$

II.2.3. The function fPhiOutvsPhiInLh[NumberOfLayers,PhiIn,L,h] is a good approximation

to obtain the value of PhiOut for the defined PhiIn, L, h

$$\texttt{fPhiOutvsPhiInLh[NumberOfLayers,PhiIn,L,h]} = \sqrt{\frac{4 \text{ L} \pi}{\text{PhiIn}^2 + \frac{4 \text{ L} \pi}{\text{h NumberOfLayers}}}}$$

and the inverse function fPhiInvsPhiOutLh[NumberOfLayers, PhiOut, L, h]:

$$\label{eq:phiouth} fPhiInvsPhiOutLh[NumberOfLayers,PhiOut,L,h] = \sqrt{PhiOut^2 - \frac{4\,L\,\pi}{h\,NumberOfLayers}}$$

III. Begin of Calculation

III.1. The inner and the outer angles of the spirales

PhiIn1=RIn1 2 Pi/(NumberOfLayers h),

PhiOut1=fPhiOutvsPhiInLh[NumberOfLayers,PhiIn1,L1,h].

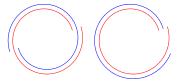
For RIn1=2.047nm, h=0.3354nm, NumberOfLayers=2:

PhiIn1=3.05158(2Pi), PhiOut1=4.05339(2Pi)

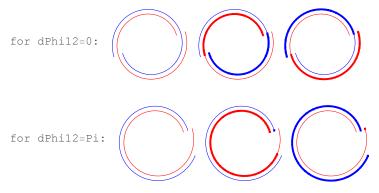
for dPhi12=0: PhiIn2=3.05158(2Pi), PhiOut2=4.05339(2Pi)

for dPhi12=Pi: PhiIn2=3.55158(2Pi), PhiOut2=4.44202(2Pi)

Plot Spirales of the layers for dPhi12=0 and dPhi12=Pi



{Spirale1, Spirale2, Spirale1UnderSpirale2, Spirale2UnderSpirale1}, {Spirale1, Spirale2, Spirale1OverSpirale2, Spirale2OverSpirale1}



III.2. The nanoscroll energy calculation

III.2.1. The elastic energy calculation

EelastC=4.08528eV/atom

EelastBN=4.08528eV/atom

III.2.2. The Van-der-Waals energy calculation

for dPhi12=0.Pi EVdWvardPhi12allp[[iEVdW]]=-20.0994eV/atom

For dPhi12=0.Pi:

EVdWvardPhi12allp[[iEVdW]] = -20.0994eV/atom

EVdWvardPhi12allp[[iEVdW1Un2]]=-4.67195eV/atom

EVdWvardPhi12allp[[iEVdW10v2]]=-5.37776eV/atom

EVdWvardPhi12allp[[iEVdW2Un1]]=-4.67195eV/atom

EVdWvardPhi12allp[[iEVdW2Ov2]]=-5.37776eV/atom

For dPhi12=1.Pi:

EVdWvatdPhi12allp[[iEVdW]]=-17.5926eV/atom

EVdWvatdPhi12allp[[iEVdW1Un2]]=-8.7769eV/atom

EVdWvatdPhi12allp[[iEVdW10v2]]=-0.0206864eV/atom

EVdWvatdPhi12allp[[iEVdW2Un1]]=-0.0181383eV/atom

EVdWvatdPhi12allp[[iEVdW2Ov2]]=-8.7769eV/atom

EVdWEVdWdPhi12eqPip=-20.0994eV/atom

III.3. The energy of flat places

EnergyFlatPlates=-eps width/Sa L1(NumberOfLayers-1) =-20.0429eV/atom

III.4. The total energy of the nanoscroll

III.5. Determine the inner angles mismatch for the bi-layer nanoscroll for the high nanoribbon Length

For L1=15nm, RIn=2.047nm, h=0.3354nm and dPhi12=0:

ScrollEnergy=-11.9289eV/atom

For L1=15nm, RIn=2.047nm, h=0.3354nm and dPhi12=Pi:

atom ScrollEnergydPhi12Pip ScrollEnergy= eV/atom

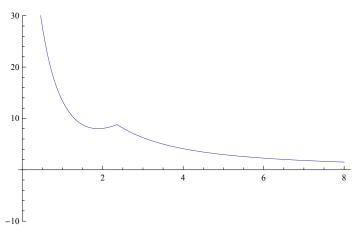
IV. The potential energy of the scroll

as a function of the inner radius RIn

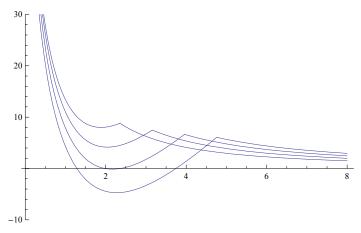
NumberOfLayers=2

eps=0.035eV/atom, C=0.0201(eV nm^2/atom)(eV nm^2/atom),aCC=0.142nm,h=0.3354nm

Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1=15nm (NumberOfLayers=2,w=1.nm



Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1= {15, 20, 25, 30}nm (NumberOfLayers=2, w=1.nm)



Export the plot data to the files

NanoscrollName=Nanoscroll2L15nm

ScrollEnergyMEnergyFlatPlatesFileName=D:\1\EvsRin1Nanoscroll2L15nm.dat

NanoscrollName=Nanoscroll2L2Onm

 ${\tt ScrollEnergyMEnergyFlatPlatesFileName=D:\label{lem:scroll2L20nm.dat} LevsRin1Nanoscroll2L20nm.dat} \\$ 

NanoscrollName=Nanoscroll2L25nm

 ${\tt ScrollEnergyMEnergyFlatPlatesFileName=D:\label{lem:scroll2L25nm.dat} LevsRin1Nanoscroll2L25nm.dat} \\$ 

NanoscrollName=Nanoscroll2L30nm

 $\verb|ScrollEnergyMEnergyFlatPlatesFileName=D: \verb|\label{lenergyMenergyFlatPlatesFileName=D: lenergyMenergyFlatPlatesFileName=D: lenergyMenergyFlatPlatesFileName=D: \verb|\label{lenergyMenergyFlatPlatesFileName=D: lenergyMenergyFlatPlatesFileName=D: lenergyMenergyMenergyFlatPlatesFileName=D: lenergyM$ 

Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1= {15, 20, 25, 30}nm (NumberOfLayers=2,w=1.nm)

