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ln[1]:= Print[" Figure3cd(Layers1L15nmRIn1d14.m");
Print[];
Print[" The source of the data of the manuscript"];
Print[" 'Structure and energetics of carbon, ";
Print[" hexagonal boron nitride, and"];
Print[" carbon/hexagonal boron nitride"];
Print[" single-layer and bilayer nanoscrolls' "];
Print[" / A.I. Siahlo, N.A. Poklonski, A.V. Lebedev,"];
Print[" I.V. Lebedeva, A.M. Popov, S.A. Vyrko, "];
Print[" A.A. Knizhnik, Yu.E. Lozovik "];
Print[" // Phys. Rev. Materials.- 2018.- V. 2,"];
Print[" № 3.- P. 036001 (9 pp.)."];
Print[" [DOI: 10.1103/PhysRevMaterials.2.036001] "];
Print[" -----"];

NoL1 = 1; NoL2 = 2;
NoLp = NoL1;
Print[" I.0 The Units (nm, meV, AA)"];
"nm=10^(-9)m;";
nm = 10^(-9) m;
AA = 10^(-10) m;
JJkgms = kg m^2 / s^2;
Cl = Amper s;
"eV=JJ Electronp;";
JJ = eV/Electron;
JJms = (kg m^2) / s^2;
meV = N[eV/1000];
Print["-----"];

Print[" I.1. All Input Parameters and Constants-----"];
Print[" I.1.1. The sampling parameters"]
npRIn1 = 1000;
Print["npRIn1=", npRIn1];
Print[" I.1.2. The Input Geometry Parameters of the system"];
L14d839nm = 14.839 nm;
L12d709nm = 12.709 nm;
L129d678nm = 29.678 nm;
L1p = L129d678nm;
L1p = L14d839nm;

Print[" The carbon nanoribbon length L1=", L1p/nm, "nm"];
Lw11d8nm = 11.8 nm;
Lwp = Lw11d8nm;
Print[" The carbon nanoribbon width Lw=", Lwp/nm, "nm"];
Print["-----"];

Print[" Number of the layers in carbon nanoscroll NoL=", NoLp];
Print[" The length of a carbon nanoribbon L1=", L1p/nm, "nm"];
Lw1nm = 1. nm; Lwp = Lw1nm;
Print[" The carbon nanoribbon width Lw=", Lwp/nm, "nm"];
RIn1d1nm = 1.1 nm;
RIn1d2nm = 1.2 nm;
RIn1d14nm = 1.14 nm;
RIn2nm = 2.047 nm;
RIn2d1nm = 2.1 nm;
RIn2d2nm = 2.2 nm;
RIn2d3nm = 2.3 nm;

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RIn2d4nm = 2.4 nm;
RIn2d5nm = 2.5 nm;
RIn2d6nm = 2.6 nm;
RIn1p = RIn2d5nm;
RIn1p = RIn2d3nm;
RIn1p = RIn2d2nm;
RIn1p = RIn2d1nm;
RIn1p = RIn1d14nm;
Print[" The inner radius of the nanoscroll RIn1=", RIn1p/nm, "nm"];
Print[" I.1.2. The Input Energy Constants"];
Print[" epsVdW - the interlayer interaction energy per one atom of"];
Print[" the nanoscroll:"];
epsVdW35 = 35.0 meV/atom; epsVdWp = epsVdW35;
Print[" epsVdW=", epsVdWp/(eV/atom), "eV/atom"];
Print[" C - the bending elastic constant:"];
C201 = 2.01 eV AA^2/atom;
CBN1328 = 1.328 eV AA^2/atom;
CCp = C201;
CBNp = CBN1328;
CBNp = CCp;
Print[" CCelast=", CCp/(eV AA^2/atom), "eV AA^2/atom"];
Print[" CCBNelast=", CBNp/(eV AA^2/atom), "eV AA^2/atom"];
Print[" I.1.3.The Input Geometry constants-----"];
Print[" The interatomic distance aCC and the interlayer distance h"];
aCC142AA = 1.42 AA; aCCp = aCC142AA;
h335nm = 0.3354 nm; hp = h335nm;
Print["h=", hp/nm, " nm (Interlayer distance)"];
Print[" aCC=", aCCp/nm, "nm, h=", hp/nm, "nm"];
NatomsInCell2 = 2; NatomsInCellp = NatomsInCell2;
Print["NatomsInCell=", NatomsInCellp];

Print[" dPhi12 - The difference of the inner angles of the spirales"];
Print[" of the Layers"];
dPhi12eq0 = 0.0 Pi;
dPhi12eqPi = 1.0 Pi;
dPhi12p = 0.0 Pi;
dPhi12p = 1.0 Pi;
dPhi12p = 0.5 Pi;
Print[" I.4.The parameters for the visualisation"];
RIn1MinMonoScroll = hp/5;
RIn1MinBiScroll = hp/5;
RIn1MaxMonoScroll = 4 nm;
RIn1MaxBiScroll = 8 nm;
PlotRangeMonoScroll = {-4 eV/atom, 12 eV/atom};
PlotRangeBiScroll = {-10 eV/atom, 30 eV/atom};
ShowSpirales = True;
ShowThePlot = True;

Print[" I.5. The parameters of visualization that depend on NoL=", NoLp];
PlotRange = Switch[NoLp, 1, PlotRangeMonoScroll, 2, PlotRangeBiScroll];
RIn1Minp = Switch[NoLp, 1, RIn1MinMonoScroll, 2, RIn1MinBiScroll];
RIn1Maxp = Switch[NoLp, 1, RIn1MaxMonoScroll, 2, RIn1MaxBiScroll];
PlotRange = Switch[NoLp, 1, PlotRangeMonoScroll, 2, PlotRangeBiScroll];
RIn1Maxp = Switch[NoLp, 1, RIn1MaxMonoScroll, 2, RIn1MaxBiScroll];
tL1 = Switch[NoLp, 1, {7. nm, 10. nm, 12.5 nm, 15. nm}, 2, {15. nm, 20. nm, 25. nm, 30. nm}];

Print[" I.6. The parameters of the output file"];

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NanoscrollNamep = StringJoin["Nanoscroll", ToString[NoLp], "L", ToString[Llp/nm], "nm"];
Print[" NanoscrollName=", NanoscrollNamep];
CarbonNanoscrollEnergyVsRInFileName = StringJoin[NanoscrollNamep, ".txt"];
Print[CarbonNanoscrollEnergyVsRInFileName];
Print[" (The output of the data to a file Is Not Performed)"];
npRIn1 = 1000;
Print[" The number of the output points = ", npRIn1];
Print[" I.7. The Input Numerical Constants used in the programm"];
Print[" The Indexes used for the work with EVdW[...] function"];
iEVdW = 1; iEVdW1Un1 = 2; iEVdW1Ov1 = 3; iEVdW1Un2 = 4; iEVdW1Ov2 = 5;
iEVdW2Un1 = 6; iEVdW2Ov1 = 7;
Print[" -----End of the Input-----"];
AA = 0.1 nm; PhiIn :=  $\varphi$ In; PhiOut :=  $\varphi$ Out;
Print["-----"];

Print[" II. The derivated parameters and the functions required"];
Print[" II.1. The derivated parameters"];
fSa[aCC_] := aCC^2 3 Sqrt[3] / 4; fSa[aCCp]; Sap = fSa[aCCp];
Print[" The cell area Sa=", fSa[aCC], "=", Sap/nm^2, "nm^2"];
Print[" II.2. The required functions-----"];
Print[" II.2.1. The function fSpiraleLen[" , NoLp, " $\varphi$ In,  $\varphi$ Out, h] defines"];
Print[
  " the Length of a Spirale with the inner aple  $\varphi$ In and the outer angle  $\varphi$ Out(>= $\varphi$ In):"];
fSpiraleLen[NoLv_, PhiInv_, PhiOutv_, hv_] :=
  (1 / (4 Pi) hv NoLv (-PhiInv Sqrt[1 + PhiInv^2] + PhiOutv Sqrt[1 + PhiOutv^2] -
    ArcSinh[PhiInv] + ArcSinh[PhiOutv]));
Print[" fSpiraleLen[" , NoLp, " $\varphi$ In,  $\varphi$ Out, h]=",
  fSpiraleLen[NoLv, PhiIn, PhiOut, h], "."];
Print[" II.2.2. The function fElast[ $\varphi$ In,  $\rho$ Out] is
  required to calculate an nanoscrolllelastic energy: "];
fElast[PhiInv_, PhiOutv_] := (Sqrt[PhiInv^2 + 1] / PhiInv -
  Sqrt[PhiOutv^2 + 1] / PhiOutv - ArcSinh[PhiInv] + ArcSinh[PhiOutv]);
Print[" fElast[ $\varphi$ In,  $\varphi$ Out] = ", fElast[PhiIn, PhiOut], "."];
Print[" II.2.3. Define the function fPhiOutvsPhiInLh[" , NoLp, " $\varphi$ In, L, h]."];
fPhiOutvsPhiInLh[NoLv_, PhiInv_, Lv_, hv_] := Sqrt[4  $\pi$  Lv / (NoLv hv) + PhiInv^2];
Print[" The function fPhiOutvsPhiInLh[" , NoLp, " $\varphi$ In, L, h]=",
  fPhiOutvsPhiInLh[NoLv, PhiIn, L, h], " is a
  good approximation to obtain the value of  $\varphi$ Out for the defined  $\varphi$ In, L, h."];
fPhiInvsPhiOutLh[NoLv_, PhiOutv_, Lv_, hv_] := Sqrt[PhiOutv^2 - 4 Pi Lv / (NoLv hv)];
Print[" The inverse function fPhiInvsPhiOutLh[" ,
  NoLp, " $\varphi$ Out, L, h]=", fPhiInvsPhiOutLh[NoLv, PhiOut, L, h]];
Print[" could be used in the program applications if ROut
  (instead of RIn) is the input parameter of the system."];

Print[" II.2.4. The functions
  fSpirale1Under(Over)Spirale1Length[NoLv, PhiInlv, PhiOutlv, hv]"];
fSpirale1UnderSpirale1Length[NoLv_, PhiInlv_, PhiOutlv_, hv_] :=
  fSpiraleLen[NoLv, PhiInlv, PhiOutlv - 2 Pi, hv];
fSpirale1OverSpirale1Length[NoLv_, PhiInlv_, PhiOutlv_, hv_] :=
  fSpiraleLen[NoLv, PhiInlv + 2 Pi, PhiOutlv, hv];

fSpirale1UnderSpirale2Length[NoLv_, PhiInlv_, PhiOutlv_, hv_, dPhi12v_] :=
  fSpiraleLen[NoLv, PhiInlv, PhiOutlv - 2 Pi / NoLv, hv];
fSpirale1OverSpirale2Length[NoLv_, PhiInlv_, PhiOutlv_, hv_, dPhi12v_] :=
  fSpiraleLen[NoLv, PhiInlv + 2 Pi / NoLv + dPhi12v, PhiOutlv, hv];
fSpirale2UnderSpirale1Length[NoLv_, PhiInlv_, PhiOutlv_, hv_, dPhi12v_] :=
  fSpiraleLen[NoLv, PhiInlv, PhiOutlv - 2 Pi / NoLv, hv];

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fSpirale2OverSpirale1Length[NoLv_, PhiInlv_, PhiOutlv_, hv_, dPhi12v_] :=
  fSpiraleLen[NoLv, PhiInlv - dPhi12v + 2 Pi / NoLv, PhiOutlv - dPhi12v, hv];

Print[" These functiona are not required, but could be helpful),"];

If[NoLp == 1, Print["fSpirale1UnderSpirale1Length[1,PhiInlv ,PhiOutlv,hv]="];
  Print[" =fSpiraleLen[NoLv,PhiInlv ,PhiOutlv-2Pi,hv]=",
    fSpiraleLen[NoLv, PhiInlv, PhiOutlv - 2 Pi, hv], ";"];
  Print[" fSpirale1UnderSpirale1Length[NoLp,PhiInlp,PhiOutlp,hp]=
    fSpirale1UnderSpirale1Length[" , NoLp, " , " ,
    PhiInlp / (2 Pi), "(2Pi)", " , PhiOutlp / (2 Pi), "(2Pi)", " , hp / nm, "nm"] ="];
  Print[" =", fSpirale1UnderSpirale1Length[NoLp, PhiInlp, PhiOutlp, hp] / nm, "nm."];
  Print["fSpirale1OverSpirale1Length[1,PhiInlv ,PhiOutlv,hv]="];
  Print[" =fSpiraleLen[NoLv,PhiInlv+2Pi ,PhiOutlv,hv]=",
    fSpiraleLen[NoLv, PhiInlv + 2 Pi, PhiOutlv, hv], ";"];
  Print[" fSpirale1OverSpirale1Length[NoLp,PhiInlp
    ,PhiOutlp,hp]=fSpirale1OverSpirale1Length[" , NoLp, " , " ,
    PhiInlp / (2 Pi), "(2Pi)", " , PhiOutlp / (2 Pi), "(2Pi)", " , hp / nm, "nm"] ="];
  Print[" =", fSpirale1OverSpirale1Length[NoLp, PhiInlp, PhiOutlp, hp] / nm, "nm."];];

If[NoLp == 2, Print[" fSpirale1UnderSpirale2Length[1,PhiInlv ,PhiOutlv,hv,dPhi12v]="];
  Print[" fSpiraleLen[NoLv,PhiInlv ,PhiOutlv -2 Pi/NoLv,hv]=",
    fSpirale1UnderSpirale2Length[1, PhiInlv, PhiOutlv, hv, dPhi12v], ";"];
  Print["fSpirale1UnderSpirale2Length[NoLp,PhiInlp,PhiOutlp,hp,dPhi12p]=
    fSpirale1UnderSpirale2Length[" , NoLp, " , " , PhiInlp / (2 Pi), "(2Pi)",
    PhiOutlp / (2 Pi), "(2Pi)", " , hp / nm, "nm", " , dPhi12p / (2 Pi), "(2Pi)"] ="];
  Print[" =", fSpirale1UnderSpirale2Length[NoLp, PhiInlp, PhiOutlp, hp, dPhi12p] / nm,
    "nm."];
  Print[" fSpirale1OverSpirale2Length[1,PhiInlv ,PhiOutlv,hv,dPhi12v]="];
  Print[" =fSpiraleLen[NoLv,PhiInlv+Pi ,PhiOutlv,hv]=",
    fSpiraleLen[NoLv, PhiInlv + Pi, PhiOutlv, hv], ";"];
  Print["fSpirale1OverSpirale2Length[NoLp,PhiInlp
    ,PhiOutlp,hp]=fSpirale1OverSpirale1Length[" , NoLp, " , " ,
    PhiInlp / (2 Pi), "(2Pi)", " , PhiOutlp / (2 Pi), "(2Pi)", " , hp / nm, "nm"] ="];
  Print[" =", fSpirale1OverSpirale2Length[NoLp, PhiInlp, PhiOutlp, hp, dPhi12p] / nm,
    "nm."];
  Print[""];
  Print[" fSpirale2UnderSpirale1Length[1,PhiInlv ,PhiOutlv,hv]="];
  Print[" fSpiraleLen[NoLv,PhiInlv ,PhiOutlv -2 Pi/NoLv,hv]=",
    fSpirale1UnderSpirale2Length[1, PhiInlv, PhiOutlv, hv, dPhi12v], ";"];
  Print["fSpirale2UnderSpirale1Length[NoLp,PhiInlp,PhiOutlp,hp,dPhi12p]=
    fSpirale2UnderSpirale1Length[" , NoLp, " , " , PhiInlp / (2 Pi), "(2Pi)",
    PhiOutlp / (2 Pi), "(2Pi)", " , hp / nm, "nm", " , dPhi12p / (2 Pi), "(2Pi)"] ="];
  Print[" =", fSpirale1UnderSpirale2Length[NoLp, PhiInlp, PhiOutlp, hp, dPhi12p] / nm,
    "nm."];
  Print[" fSpirale1OverSpirale2Length[1,PhiInlv ,PhiOutlv,hv]="];
  Print[" =fSpiraleLen[NoLv,PhiInlv+Pi ,PhiOutlv,hv]=",
    fSpiraleLen[NoLv, PhiInlv + Pi, PhiOutlv, hv], ";"];
  Print["fSpirale1OverSpirale2Length[NoLp,PhiInlp
    ,PhiOutlp,hp]=fSpirale1OverSpirale2Length[" , NoLp, " , " ,
    PhiInlp / (2 Pi), "(2Pi)", " , PhiOutlp / (2 Pi), "(2Pi)", " , hp / nm, "nm"] ="];
  Print[" =", fSpirale1OverSpirale2Length[NoLp, PhiInlp, PhiOutlp, hp, dPhi12p] / nm,
    "nm."];];

Print[" II.2.4. The function fRIn1Sharp[NoLv,Llv,hv]"]
fRIn1Sharp[NoLv_, Llv_, hv_] := (Llv / (2 Pi) - (NoLv hv / 2));
Print["fRIn1Sharp[NoLv,Llv,hv]=", fRIn1Sharp[NoLv, Llv, hv]];

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Print["is a good approximation to obtain
      the value of the sharp in the dependence ScrollEnergy[RIn]"];
Print["fRIn1Sharp[" , NoLp, " , " , Llp/nm, "nm, " , hp/nm, "nm] = ",
      fRIn1Sharp[NoLp, Llp, hp] / nm, "nm"];
Print["-----"];

Print[" III. Begin of Calculation "];
If[NoLp == 1,
  Print[" III.1. The inner and the outer angle of the spirale of the layer:"]];
If[NoLp == 2, Print[
  " III.1. The inner and the outer angles of the spirales of the layers:"]];
Print["  $\phi_{In1}$ =", RIn1 2 Pi / (NoLp h), " ,  $\phi_{Out1}$ =fPhiOutvsPhiInLh[" , NoLp, " ,  $\phi_{In1}$ , L1, h];"];
fPhiIn1[NoLv_, RInlv_, hv_] := RInlv 2 Pi / (NoLv hv);
PhiIn1p = fPhiIn1[NoLp, RInlp, hp];
fPhiOut1[NoLv_, Llv_, RInlv_, hv_] :=
  fPhiOutvsPhiInLh[NoLv, fPhiIn1[NoLv, RInlv, hv], Llv, hv];
Print[" For RIn1=", RInlp / nm, "nm, h=", hp / nm, "nm:"];
PhiOut1p = fPhiOut1[NoLp, Llp, RInlp, hp];
ROut1p = PhiOut1p NoLp hp / (2 Pi);
Print["  $\phi_{In1}$ =", PhiIn1p / (2 Pi), "(2Pi),  $\phi_{Out1}$ =", PhiOut1p / (2 Pi), "(2Pi)."];
fPhiIn2[NoLv_, RInlv_, hv_, dPhil2v_] := fPhiIn1[NoLv, RInlv, hv] + dPhil2v;
PhiIn2dPhil2p = fPhiIn2[NoLp, RInlp, hp, 0]; (*www orig 2022.10*)
PhiIn2dPhil2p = fPhiIn2[NoLp, RInlp, hp, dPhil2p]; (*for dPhil2p≠0,
checked 2022.10*) PhiIn2dPhil2Pip = fPhiIn2[NoLp, RInlp, hp, Pi];
fPhiOut2[NoLv_, Llv_, RInlv_, hv_, dPhil2v_] :=
  fPhiOutvsPhiInLh[NoLv, fPhiIn2[NoLv, RInlv, hv, dPhil2v], Llv, hv];
PhiOut2dPhil2p = fPhiOut2[NoLp, Llp, RInlp, hp, dPhil2p];
If[NoLp == 2, Print["  $\phi_{In2}$ =", PhiIn2dPhil2p / (2 Pi),
  "(2Pi),  $\phi_{Out2}$ =", PhiOut2dPhil2p / (2 Pi), "(2Pi)"];
PhiOut2dPhil2Pip = fPhiOut2[NoLp, Llp, RInlp, hp, Pi];
Print[" for  $d\phi_{12}=\pi$ :  $\phi_{In2}$ =", PhiIn2dPhil2Pip / (2 Pi),
  "(2Pi),  $\phi_{Out2}$ =", PhiOut2dPhil2Pip / (2 Pi), "(2Pi)"];];
Print["L1=", Llp / nm, "nm, RIn1=", RInlp / nm, "nm"];
If[NoLp == 1, Print[" Plot the Spirale of the layer:"]];
If[NoLp == 2, Print[" Plot Spirales of the layers:"]]; "for  $d\phi_{12}=0$ ";
Spirale1Plot = PolarPlot[(Phiv) NoLp hp / (2 Pi) / nm, {Phiv, PhiIn1p, PhiOut1p},
  PlotRange → {{-1.1 ROut1p / nm, 1.1 ROut1p / nm}, {-1.1 ROut1p / nm, 1.1 ROut1p / nm}},
  PlotStyle → {Red, Thin}, Axes → None];
If[NoLp == 1, Print[Show[Spirale1Plot]]];
Print["Manipulating of Spirale1Plot for the different RIn1 and L:"];
Manipulate[PolarPlot[(Phiv) NoLp hp / (2 Pi) / nm,
  {Phiv, fPhiIn1[NoLp, RInlnmm nm, hp], fPhiOut1[NoLp, Llnmm nm, RInlnmm nm, hp]},
  PlotRange → {{-1.1 ROut1p / nm, 1.1 ROut1p / nm}, {-1.1 ROut1p / nm, 1.1 ROut1p / nm}},
  PlotStyle → {Red, Thin}, Axes → None], {{RInlnmm, RInlp / nm}, RInlMinp / nm, RInlMaxp / nm},
  {{Llnmm, Llp / nm}, 0.5 tL1[[1]] / nm, 1.5 tL1[[Length[tL1]]] / nm}]]
If[NoLp > 1, Print[" Plot the Spirale of the layers:"];
Spirale2Plot =
  PolarPlot[(Phiv - Pi) NoLp hp / (2 Pi) / nm, {Phiv, PhiIn2dPhil2p + Pi, PhiOut2dPhil2p + Pi},
  PlotRange → {{-1.1 ROut1p / nm, 1.1 ROut1p / nm}, {-1.1 ROut1p / nm, 1.1 ROut1p / nm}},
  PlotStyle → {Blue, Thin}, Axes → None];
Spirale2dPhil2PiPlot = PolarPlot[(Phiv - Pi) NoLp hp / (2 Pi) / nm,
  {Phiv, PhiIn2dPhil2p + Pi, PhiOut2dPhil2Pip + Pi},
  PlotRange → {{-1.1 ROut1p / nm, 1.1 ROut1p / nm}, {-1.1 ROut1p / nm, 1.1 ROut1p / nm}},
  PlotStyle → {Blue, Thin}, Axes → None];
Print[Show[{Spirale1Plot, Spirale2Plot}]]];
If[NoLp == 1, Spirale1OverSpirale1Plot = If[PhiIn1p + 2 Pi < PhiOut1p,
  PolarPlot[(Phiv) NoLp hp / (2 Pi) / nm, {Phiv, PhiIn1p + 2 Pi, PhiOut1p},

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PlotRange → {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm, 1.1 ROutlp / nm}},
PlotStyle → {Red, Thick}, Axes → None], {}];
Spirale1UnderSpirale1Plot = If[PhiInlp < PhiOutlp - 2 Pi,
  PolarPlot[(Phiv) NoLp hp / (2 Pi) / nm, {Phiv, PhiInlp, PhiOutlp - 2 Pi},
    PlotRange → {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm, 1.1 ROutlp / nm}},
    PlotStyle → {Red, Thick}, Axes → None], {}];
Print[" {Spirale,Spirale1UnderSpirale1},{Spirale1,Spirale1OverSpirale1}:"];
Print[Show[{Spirale1Plot, Spirale1UnderSpirale1Plot},
  Show[{Spirale1Plot, Spirale1OverSpirale1Plot}]]];
If[NoLp == 2, Spirale1UnderSpirale2dPhi120Plot = If[PhiInlp < PhiOut2dPhi12p - Pi, PolarPlot[
  (Phiv) NoLp hp / (2 Pi) / nm, {Phiv, PhiInlp, PhiOut2dPhi12p - Pi}, PlotStyle → {Red, Thick},
  PlotRange → {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm, 1.1 ROutlp / nm}}], {}];
Spirale1OverSpirale2dPhi120Plot = If[PhiInlp + Pi < PhiOutlp, PolarPlot[(Phiv) NoLp
  hp / (2 Pi) / nm, {Phiv, PhiInlp + Pi + dPhi12p, PhiOutlp}, PlotStyle → {Red, Thick},
  PlotRange → {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm, 1.1 ROutlp / nm}}], {}];
Spirale2UnderSpirale1dPhi120Plot = If[PhiIn2dPhi12p + Pi < PhiOutlp,
  PolarPlot[(Phiv - Pi) NoLp hp / (2 Pi) / nm,
  {Phiv, PhiIn2dPhi12p + Pi, PhiOutlp}, PlotStyle → {Blue, Thick},
  PlotRange → {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm, 1.1 ROutlp / nm}}], {}];
Spirale2OverSpirale1dPhi120Plot = If[2 Pi + PhiIn2dPhi12p - dPhi12p < PhiOut2dPhi12p + Pi,
  PolarPlot[(Phiv - Pi) NoLp hp / (2 Pi) / nm,
  {Phiv, 2 Pi + PhiIn2dPhi12p - dPhi12p, PhiOut2dPhi12p + Pi}, PlotStyle → {Blue, Thick},
  PlotRange → {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm, 1.1 ROutlp / nm}}], {}];
Print["Plot Spirales for dPhi12=Pi (could be NotRequired,
  dPhi12=0 in this program)"];
Spirale1UnderSpirale2dPhi12PiPlot = If[PhiInlp < PhiOut2dPhi12Pi - Pi,
  PolarPlot[(Phiv) NoLp hp / (2 Pi) / nm,
  {Phiv, PhiInlp, PhiOut2dPhi12Pi - Pi}, PlotStyle → {Red, Thick},
  PlotRange → {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm, 1.1 ROutlp / nm}}], {}];
Spirale1OverSpirale2dPhi12PiPlot = If[PhiInlp + Pi + dPhi12p < PhiOutlp,
  PolarPlot[(Phiv) NoLp hp / (2 Pi) / nm,
  {Phiv, PhiInlp + Pi + dPhi12p, PhiOutlp}, PlotStyle → {Red, Thick},
  PlotRange → {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm, 1.1 ROutlp / nm}}], {}];
Spirale2UnderSpirale1dPhi12PiPlot = If[PhiIn2dPhi12p + Pi < PhiOutlp,
  PolarPlot[(Phiv - Pi) NoLp hp / (2 Pi) / nm,
  {Phiv, PhiIn2dPhi12Pi + Pi, PhiOutlp}, PlotStyle → {Blue, Thick},
  PlotRange → {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm, 1.1 ROutlp / nm}}], {}];
Spirale2OverSpirale1dPhi12PiPlot = If[2 Pi + PhiIn2dPhi12Pi - dPhi12p <
  PhiOut2dPhi12Pi + Pi, PolarPlot[(Phiv - Pi) NoLp hp / (2 Pi) / nm, {Phiv,
  2 Pi + PhiIn2dPhi12Pi - dPhi12p, PhiOut2dPhi12Pi + Pi}, PlotStyle → {Blue, Thick},
  PlotRange → {{-1.1 ROutlp / nm, 1.1 ROutlp / nm}, {-1.1 ROutlp / nm, 1.1 ROutlp / nm}}], {}];
Print[" {Spirale1,Spirale2,Spirale1UnderSpirale2,Spirale2UnderSpirale1},"];
Print[" {Spirale1,Spirale2,Spirale1OverSpirale2,Spirale2OverSpirale1}"];
Print[" for dPhi12=0: ", Show[Spirale1Plot, Spirale2Plot,
  Show[Spirale1Plot, Spirale2Plot, Spirale1UnderSpirale2dPhi120Plot,
  Spirale2UnderSpirale1dPhi120Plot], Show[Spirale1Plot, Spirale2Plot,
  Spirale1OverSpirale2dPhi120Plot, Spirale2OverSpirale1dPhi120Plot]]];
Print[" for dPhi12=Pi: ", Show[Spirale1Plot, Spirale2dPhi12PiPlot,
  Show[Spirale1Plot, Spirale2dPhi12PiPlot, Spirale1UnderSpirale2dPhi12PiPlot,
  Spirale2UnderSpirale1dPhi12PiPlot], Show[Spirale1Plot, Spirale2dPhi12PiPlot,
  Spirale1OverSpirale2dPhi12PiPlot, Spirale2OverSpirale1dPhi12PiPlot]]];

Print[" III.2. The nanoscroll energy calculation"];
Print[" III.2.1. The elastic energy calculation"];
fEelastCC[NoLv_, Lwv_, Llv_, RInlv_, hv_, aCCv_, CCv_] :=
Module[{}, Return[2 Pi CCv Lwv / (hv fSa[aCCv])
  fElast[fPhiIn1[NoLv, RInlv, hv], fPhiOut1[NoLv, Llv, RInlv, hv]]];];

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fElastCBN[NoLv_, Lwv_, Llv_, RInlv_, hv_, aCCv_, CBNv_] :=
Module[{}, Return[2 Pi CBNv Lwv / (hv fSa[aCCv])
  fElast[fPhiIn1[NoLv, RInlv, hv], fPhiOut1[NoLv, Llv, RInlv, hv]]];];
ElastCCp = fElastCC[NoLv, Lwv, Llv, RInlv, hv, aCCp, CCp];
ElastCBNp = fElastCBN[NoLv, Lwv, Llv, RInlv, hv, aCCp, CBNp];
Print[" ElastC=", ElastCCp / (eV / atom), "eV/atom"];
If[NoLv == 2, Print[" ElastBN=", ElastCBNp / (eV / atom), "eV/atom"]];
Print[" III.2.2. The Van-der-Waals energy calculation"];
"The definition of the function ";
"'fEvdWLayer1Overlap[NoLv,Lwv,Llv, RInlv, hv, aCCv, epsVdWv]";
"(Note: This function is omitted at calculations";
" but could be helpful at
  calculation of VdW ebergry of monoscroll at debugging";
" for example,";
" fEvdWLayer1Overlap[NoL1,Lwv,15nm, 2nm, hp, aCCp, epsVdWp] ";
" and fEvdWLayersOverlap[NoL2,Lwv,Llv=15nm, 2nm, hp, aCCp, epsVdWp, 0]";
" give the same values";
fEvdWLayer1Overlap[NoLv_, Lwv_, Llv_, RInlv_, hv_, aCCv_, epsVdWv_] :=
Module[{EvdWv, EVdW1Unlv = 0 (eV / atom), EVdW1Ov1v = 0 (eV / atom),
  Spirale1UnderSpirale1Length = 0 nm, Spirale1OverSpirale1Length = 0 nm,
  PhiInlv = fPhiIn1[NoLv, RInlv, hv], PhiOutlv = fPhiOut1[NoLv, Llv, RInlv, hv]},,
  Spirale1OverSpirale1Length = fSpiraleLen[NoLv, PhiInlv + 2 Pi, PhiOutlv, hv];
  Spirale1UnderSpirale1Length = fSpiraleLen[NoLv, PhiInlv, PhiOutlv - 2 Pi, hv];
  "Note: Spirale1OverSpirale1Length>Spirale1UnderSpirale1Length";
  EVdW1Unlv = -epsVdWv Lwv / (2 fSa[aCCv]) Spirale1UnderSpirale1Length;
  EVdW1Ov1v = -epsVdWv Lwv / (2 fSa[aCCv]) Spirale1OverSpirale1Length;
  EVdWv = (EVdW1Unlv + EVdW1Ov1v);
  Return[{EVdWv, EVdW1Unlv, EVdW1Ov1v}];];
"The definition of the function";
"fEvdWLayersOverlap[NoLv_,Lwv_,Llv_, RInlv_, hv_, aCCv_, epsVdWv_, dPhi12v_]";
fEvdWLayersOverlap[NoLv_, Lwv_, Llv_, RInlv_, hv_, aCCv_, epsVdWv_, dPhi12v_] :=
Module[{EvdW, EVdW1Un1 = 0 (eV / atom), EVdW1Ov1 = 0 (eV / atom), EVdW1Un2 = 0 (eV / atom),
  EVdW1Ov2 = 0 (eV / atom), EVdW2Un1 = 0 (eV / atom), EVdW2Ov1 = 0 (eV / atom),
  Spirale1UnderSpirale1Length = 0 nm, Spirale1OverSpirale1Length = 0 nm,
  Spirale1UnderSpirale2Length = 0 nm, Spirale1OverSpirale2Length = 0 nm,
  Spirale2UnderSpirale1Length = 0 nm, Spirale2OverSpirale1Length = 0 nm,
  PhiIn1 = fPhiIn1[NoLv, RInlv, hv], PhiIn2 = fPhiIn2[NoLv, RInlv, hv, dPhi12v], PhiOut1 =
  fPhiOut1[NoLv, Llv, RInlv, hv], PhiOut2 = fPhiOut2[NoLv, Llv, RInlv, hv, dPhi12v],
  ReturnEnergiesv = {1, 2, 3, 4, 5, 6, 7}}, If[NoLv == 1, If[PhiIn1 < PhiOut1 - 2 Pi,
  Spirale1UnderSpirale1Length = fSpiraleLen[NoLv, PhiIn1, PhiOut1 - 2 Pi, hv];];
  If[PhiIn1 + 2 Pi < PhiOut1, Spirale1OverSpirale1Length =
  fSpiraleLen[NoLv, PhiIn1 + 2 Pi, PhiOut1, hv];];
  EVdW1Un1 = -epsVdWv Lwv / (2 fSa[aCCv]) Spirale1UnderSpirale1Length;
  EVdW1Ov1 = -epsVdWv Lwv / (2 fSa[aCCv]) Spirale1OverSpirale1Length;
  EVdW = (EVdW1Un1 + EVdW1Ov1);
  ReturnEnergiesv = {EVdW, EVdW1Un1, EVdW1Ov1};];
If[NoLv == 2, If[PhiIn1 < PhiOut2 - Pi,
  Spirale1UnderSpirale2Length = fSpiraleLen[NoLv, PhiIn1, PhiOut2 - Pi, hv];];
  If[PhiIn1 + Pi + dPhi12v < PhiOut1, Spirale1OverSpirale2Length =
  fSpiraleLen[NoLv, PhiIn1 + Pi + dPhi12v, PhiOut1, hv];];
  If[PhiIn1 + dPhi12v < PhiOut1 - Pi, Spirale2UnderSpirale1Length =
  fSpiraleLen[NoLv, PhiIn1 + dPhi12v, PhiOut1 - Pi, hv];];
  If[PhiIn1 - dPhi12v + Pi < PhiOut2 - dPhi12v, Spirale2OverSpirale1Length =
  fSpiraleLen[NoLv, PhiIn1 - dPhi12v + Pi, PhiOut2 - dPhi12v, hv];];
  EVdW1Un2 = -epsVdWv Lwv / (2 fSa[aCCv]) Spirale1UnderSpirale2Length;
  EVdW1Ov2 = -epsVdWv Lwv / (2 fSa[aCCv]) Spirale1OverSpirale2Length;
  EVdW2Un1 = -epsVdWv Lwv / (2 fSa[aCCv]) Spirale2UnderSpirale1Length;

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    EVdW2Ov1 = -epsVdWv Lwv / (2 fSa[aCCv]) Spirale2OverSpirale1Length;
    EVdW = (EVdW1Un2 + EVdW1Ov2 + EVdW2Un1 + EVdW2Ov1);
    ReturnEnergiesv[[iEVdW]] = EVdW;
    ReturnEnergiesv[[iEVdW1Un2]] = EVdW1Un2;
    ReturnEnergiesv[[iEVdW1Ov2]] = EVdW1Ov2;
    ReturnEnergiesv[[iEVdW2Un1]] = EVdW2Un1;
    ReturnEnergiesv[[iEVdW2Ov1]] = EVdW2Ov1;];
Return[ReturnEnergiesv];];

EVdWdPhil2eq0allp = fEvdWLayersOverlap[NoL2, Lwp, Llp, RInlp, hp, aCCp, epsVdWp, dPhil2eq0];
EVdWvardPhil2allp = fEvdWLayersOverlap[NoLp, Lwp, Llp, RInlp, hp, aCCp, epsVdWp, dPhil2p];
If[NoLp == 1, Print[" EVdWvardPhil2allp[[iEVdW]]=",
    EVdWvardPhil2allp[[iEVdW]] / (eV / atom), "eV/atom"];
Print["( EVdWvardPhil2allp[[iEVdW1Un1]]=",
    EVdWvardPhil2allp[[iEVdW1Un1]] / (eV / atom), "eV/atom"];
Print[" EVdWvardPhil2allp[[iEVdW1Ov1]]=",
    EVdWvardPhil2allp[[iEVdW1Ov1]] / (eV / atom), "eV/atom  )"];];
If[NoLp == 2, Print[" for dPhil2=", dPhil2p / Pi, "Pi EVdWvardPhil2allp[[iEVdW]]=",
    EVdWvardPhil2allp[[iEVdW]] / (eV / atom), "eV/atom"];
Print[" For dPhil2=", dPhil2eq0 / Pi, "Pi:"];
Print[" EVdWvardPhil2allp[[iEVdW]]=",
    EVdWdPhil2eq0allp[[iEVdW]] / (eV / atom), "eV/atom"];
Print[" EVdWvardPhil2allp[[iEVdW1Un2]]=",
    EVdWdPhil2eq0allp[[iEVdW1Un2]] / (eV / atom), "eV/atom"];
Print[" EVdWvardPhil2allp[[iEVdW1Ov2]]=",
    EVdWdPhil2eq0allp[[iEVdW1Ov2]] / (eV / atom), "eV/atom"];
Print[" EVdWvardPhil2allp[[iEVdW2Un1]]=",
    EVdWdPhil2eq0allp[[iEVdW2Un1]] / (eV / atom), "eV/atom"];
Print[" EVdWvardPhil2allp[[iEVdW2Ov2]]=",
    EVdWdPhil2eq0allp[[iEVdW2Ov2]] / (eV / atom), "eV/atom"];
EVdWdPhil2eqPiallp = fEvdWLayersOverlap[NoLp, Lwp, Llp,
    RInlp, hp, aCCp, epsVdWp, dPhil2eqPi];
(**)Print[" For dPhil2=", dPhil2eqPi / Pi, "Pi:"];
Print[" EVdWvatdPhil2allp[[iEVdW]]=",
    EVdWdPhil2eqPiallp[[iEVdW]] / (eV / atom), "eV/atom"];
Print[" EVdWvatdPhil2allp[[iEVdW1Un2]]=",
    EVdWdPhil2eqPiallp[[iEVdW1Un2]] / (eV / atom), "eV/atom"];
Print[" EVdWvatdPhil2allp[[iEVdW1Ov2]]=",
    EVdWdPhil2eqPiallp[[iEVdW1Ov2]] / (eV / atom), "eV/atom"];
Print[" EVdWvatdPhil2allp[[iEVdW2Un1]]=",
    EVdWdPhil2eqPiallp[[iEVdW2Un1]] / (eV / atom), "eV/atom"];
Print[" EVdWvatdPhil2allp[[iEVdW2Ov2]]=",
    EVdWdPhil2eqPiallp[[iEVdW2Ov2]] / (eV / atom), "eV/atom"];
EVdWEvdWdPhil2eq0p = EVdWdPhil2eq0allp[[iEVdW]];
Print[" EVdWdPhil2eq0allp=", EVdWdPhil2eq0allp / (eV / atom), "eV/atom"];
EVdWEvdWdPhil2eqPip = EVdWvardPhil2allp[[iEVdW]];
Print[" EVdWEvdWdPhil2eqPip=", EVdWEvdWdPhil2eqPip / (eV / atom), "eV/atom"];
(**)];

If[NoLp == 2, Print[" III.3. The energy of flat planes "];];
fEnergyFlatPlanes[NoLv_, Lwv_, Llv_, aCCv_, epsVdWv_] :=
    If[NoLv == 2, -epsVdWv Lwv / fSa[aCCv] Llv, 0 eV / atom];
EnergyFlatPlanesp = fEnergyFlatPlanes[NoLp, Lwp, Llp, aCCp, epsVdWp];
If[NoLp == 2, Print[" EnergyFlatPlanes=-eps width/Sa L1(NoL-1) =",
    EnergyFlatPlanesp / (eV / atom), "eV/atom"];];
Print[" III.4. The total energy of the nanoscroll"];
fScrollEnergydPhi[NoLv_, Lwv_, Llv_, RInlv_, hv_, aCCv_, epsVdWv_,
    CCv_, CBNv_, dPhil2v_] := Module[{ScrollEnergyv, EVdWv, EVdWnoDimv},

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EvdWv = fEvdWLayersOverlap[NoLv, Lwv, Llv, RInlv, hv, aCCv, epsVdWv, dPhil2v][[1]];
EvdWnoDimv = EVdWv /. {eV → 1, atom → 1, nm → 1};
If[NoLv == 1,
  If[EvdWnoDimv == 0, ScrollEnergyv = fEelastCC[NoLv, Lwv, Llv, RInlv, hv, aCCv, CCv],
    ScrollEnergyv = EVdWv + fEelastCC[NoLv, Lwv, Llv, RInlv, hv, aCCv, CCv];];];
If[NoLv == 2, If[EvdWnoDimv == 0, ScrollEnergyv = fEelastCC[NoLv, Lwv, Llv,
  RInlv, hv, aCCv, CCv] + fEelastCBN[NoLv, Lwv, Llv, RInlv, hv, aCCv, CCv],
  ScrollEnergyv = EVdWv + fEelastCC[NoLv, Lwv, Llv, RInlv, hv, aCCv, CCv] +
    fEelastCBN[NoLv, Lwv, Llv, RInlv, hv, aCCv, CCv];];];
Return[ScrollEnergyv];];

fScrollEnergyVdWandElast[NoLv_, Lwv_, Llv_, RInlv_, hv_, aCCv_, epsVdWv_, CCv_, CBNv_] :=
Module[{ScrollEnergyVdWandElastv, EVdWv},
  (*If[NoLv==1, EVdWv=fEvdWLayer1Overlap[NoLv, Lwv, Llv, RInlv, hv, aCCv, epsVdWv][[1]];
  If[NoLv==2, EVdWv=fEvdWLayersOverlap[NoLv, Lwv, Llv, RInlv, hv, aCCv, epsVdWv][[1]];*)
  EVdWv = fEvdWLayer1Overlap[NoLv, Lwv, Llv, RInlv, hv, aCCv, epsVdWv][[1]];
  If[NoLv == 1, ScrollEnergyVdWandElastv =
    EVdWv + fEelastCC[NoLv, Lwv, Llv, RInlv, hv, aCCv, CCv];];
  If[NoLv == 2, ScrollEnergyVdWandElastv = EVdWv + fEelastCC[NoLv, Lwv, Llv, RInlv,
    hv, aCCv, CCv] + fEelastCC[NoLv, Lwv, Llv, RInlv, hv, aCCv, CBNv];];
  Return[ScrollEnergyVdWandElastv];];

fScrollEnergy[NoLv_, Lwv_, Llv_, RInlv_, hv_, aCCv_, epsVdWv_, CCv_, CBNv_] :=
Module[{ScrollEnergyv = -10^20 eV / atom},
  If[RInlv / m ≤ fRInlSharp[NoLv, Llv, hv] / m, ScrollEnergyv =
    fScrollEnergyVdWandElast[NoLv, Lwv, Llv, RInlv, hv, aCCv, epsVdWv, CCv, CBNv];
  "note: the function fScrollEnergyVdWandElast[1,...] is analytcal";
  "whereas the function fScrollEnergy[....] uses the 'If[...]'- function";];
  If[RInlv / m ≥ fRInlSharp[NoLv, Llv, hv] / m,
    If[NoLv == 1, ScrollEnergyv = fEelastCC[NoLv, Lwv, Llv, RInlv, hv, aCCv, CCv];];
    If[NoLv == 2, ScrollEnergyv = fEelastCC[NoLv, Lwv, Llv, RInlv, hv, aCCv, CCv] +
      fEelastCC[NoLv, Lwv, Llv, RInlv, hv, aCCv, CBNv];];];
  Return[ScrollEnergyv];];

ScrollEnergyyp = fScrollEnergy[NoLv, Lwv, Llv, RInlv, hv, aCCv, epsVdWv, CCv, CBNv];
ScrollEnergy = fScrollEnergy[1, Lwv, Llv, RInlv, hv, aCCv, epsVdWv, CCv, CBNv];
Print["fScrollEnergy[1,Lwv,Llv, RInlv,hv, aCCv, epsVdWv,CCv,CBNv]="];
Print["=fScrollEnergy[1, Lw=", Lwv/nm, "nm, L1=",
  Llv/nm, "nm, RInl=", RInlv/nm, "nm, h=", hv/nm, "nm,"];
Print[" aCC=", aCCv/nm, "nm, epsVdW=", epsVdWv/(eV/atom),
  "eV/atom, CC=", CCv/(eV AA^2/atom), "(eV AA^2/atom)="];
Print[" =", ScrollEnergyyp/(eV/atom), "eV/atom"];

Print[" III.5. Determine the inner angles mismatch for the bi-layer nanoscroll
  for the high nanoribbon Length"];
Print[" For L1=", Llv/nm, "nm,RIn=", RInlv/nm, "nm,h=", hv/nm, "nm and dPhil2=0:"];
Print[" ScrollEnergy=", ScrollEnergyyp/(eV/atom), "eV/atom"];
Print[" For L1=", Llv/nm, "nm,RIn=",
  RInlv/nm, "nm,h=", hv/nm, "nm and dPhil2=Pi:"];
Print[" ScrollEnergy=", ScrollEnergyyp/(eV/atom), "eV/atom"];
Print["-----"];

Print[" IV.The potential energy of the nanoscroll"];
Print[" as a function of the inner radius RIn"];
Print[" NoLv=", NoLv];
Print[" epsVdW=", epsVdWv/(eV/atom), "eV/atom, C=", CCv/(eV nm^2/atom),
  "(eV nm^2/atom)", "(eV nm^2/atom),aCC=", aCCv/nm, "nm,h=", hv/nm, "nm"];

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Print[" Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1=",
      Llp/nm, "nm (NoL=", NoLp, ",Lw=", Lwp/nm, "nm)"];
PlotScrollEnergyVsRIn1 =
  Plot[(fScrollEnergy[NoLp, Lwp, Llp, RIn1nmv nm, hp, aCCp, epsVdWp, CCp, CBNp]) / (eV/atom),
        {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange → PlotRange / (eV/atom)];
Print[PlotScrollEnergyVsRIn1];
Print[" Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1=",
      tL1/nm, "nm (NoL=", NoLp, ",w=", Lwp/nm, "nm)"];
PlotScrollEnergyVsRIn1L1th = Plot[
  (fScrollEnergy[NoLp, Lwp, tL1[[1]], RIn1nmv nm, hp, aCCp, epsVdWp, CCp, CBNp]) / (eV/atom),
  {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange → PlotRange / (eV/atom)];
PlotScrollEnergyVsRIn1L2th = Plot[
  (fScrollEnergy[NoLp, Lwp, tL1[[2]], RIn1nmv nm, hp, aCCp, epsVdWp, CCp, CBNp]) / (eV/atom),
  {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange → PlotRange / (eV/atom)];
PlotScrollEnergyVsRIn1L3th = Plot[
  (fScrollEnergy[NoLp, Lwp, tL1[[3]], RIn1nmv nm, hp, aCCp, epsVdWp, CCp, CBNp]) / (eV/atom),
  {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange → PlotRange / (eV/atom)];
PlotScrollEnergyVsRIn1L4th = Plot[
  (fScrollEnergy[NoLp, Lwp, tL1[[4]], RIn1nmv nm, hp, aCCp, epsVdWp, CCp, CBNp]) / (eV/atom),
  {RIn1nmv, RIn1Minp/nm, RIn1Maxp/nm}, PlotRange → PlotRange / (eV/atom)];
Print[Show[{PlotScrollEnergyVsRIn1L1th, PlotScrollEnergyVsRIn1L2th,
  PlotScrollEnergyVsRIn1L3th, PlotScrollEnergyVsRIn1L4th}]];
Print["The examples of using of 'fScrollEnergy[...]' function:"]
Print["fScrollEnergy[NoLp,Lwp,tL1[[1]],RIn1p,hp, aCCp, epsVdWp,CCp,CBNp]=",
      fScrollEnergy[NoLp, Lwp, tL1[[1]], RIn1p, hp, aCCp, epsVdWp, CCp, CBNp] / (eV/atom),
      " eV/atom"];
Print["fScrollEnergy[NoLp,Lwp,tL1[[1]],1nm,hp, aCCp, epsVdWp,CCp, CBNp]=",
      fScrollEnergy[NoLp, Lwp, tL1[[1]], 1 nm, hp, aCCp, epsVdWp, CCp, CBNp] / (eV/atom),
      " eV/atom"];
Print["fScrollEnergy[NoLp,Lwp,7nm,1nm,hp, aCCp, epsVdWp,CCp, CBNp]=",
      fScrollEnergy[NoLp, Lwp, 7. nm, 1. nm, hp, aCCp, epsVdWp, CCp, CBNp] / (eV/atom),
      " eV/atom"];
Print["fEVdWLayer1Overlap[1,Lwp,7.nm,1.nm,hp,aCCp,epsVdWp][[1]]=",
      fEVdWLayer1Overlap[1, Lwp, 7. nm, 1. nm, hp, aCCp, epsVdWp][[1]] / (eV/atom),
      "eV/atom (right !=0 value, because the layer overlaps)"];
Print["fEVdWLayer1Overlap[1,Lwp,7.nm,1.5nm,hp,aCCp,epsVdWp][[1]]=",
      fEVdWLayer1Overlap[1, Lwp, 7. nm, 2.5 nm, hp, aCCp, epsVdWp][[1]] / (eV/atom),
      "eV/atom !=0, wrong value of the fEVdWLayer1Overlap[...]
      function because the layer does not not overlap"];
Print[];
Print["The analytical expressions of the fEVdWLayer1Overlap[...] function:"];
Print[];
Print["--- fEVdWLayer1Overlap[NoL1,Lwv,Lpv,RInv,hv,aCCv,epsVdWv][[1]]: ---"];
Print[fEVdWLayer1Overlap[NoL1, Lwv, Lpv, RInv, hv, aCCv, epsVdWv][[1]]];
Print[];
Print["--- fEVdWLayer1Overlap[NoL2,Lwv,Lpv,RInv,hv,aCCv,epsVdWv][[1]]: ---"];
Print[fEVdWLayer1Overlap[NoL2, Lwv, Lpv, RInv, hv, aCCv, epsVdWv][[1]]];
Print[];
Print["The Analytical expression of "];
Print["fScrollEnergyVdWandElast[",
      NoLp, ",Lwv,Llv,RInlv,hv,aCCv, epsVdWv, CCv,CBNv]:"];
Print[fScrollEnergyVdWandElast[NoLp, Lwv, Llv, RInlv, hv, aCCv, epsVdWv, CCv, CBNv]];
Print["-----"];

Print["V. Export the data of the plots of the nanoscroll energy"];
Print[" as a function of the inner radius"];
Print["The parameters of the output file"];

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Print["The number of the output points = ", npRIn1];
Print["Export the plot data to the files:"];
tRIn1nmRegular =
  Table[(RIn1Minp + (RIn1Maxp - RIn1Minp) iiRin / (npRIn1)) / nm, {iiRin, 1, npRIn1}];
tScrollEnergy = tRIn1nmRegular;
tScrollEnergyeVatom = tRIn1nmRegular;
tPlotEvsRin = Table[{}, {ii, 1, Length[tL1]}];
AllPlotsEvsRin = {};

For[iiL1 = 1, iiL1 ≤ Length[tL1], iiL1++, L1pi = tL1[[iiL1]];
  NanoscrollNamep =
    StringJoin["Nanoscroll", ToString[NoLp], "L", ToString[L1pi / nm], "nm"];
  Print["NanoscrollName=", NanoscrollNamep];
  ScrollEnergyFileName = StringJoin["EvsRIn1", NanoscrollNamep, ".dat"];
  Print["ScrollEnergyFileName=", ScrollEnergyFileName];
  For[iiRIn1 = 1, iiRIn1 ≤ npRIn1, iiRIn1++, RIn1pi = tRIn1nmRegular[[iiRIn1]] nm;
    tScrollEnergy[[iiRIn1]] =
      fScrollEnergy[NoLp, Lwp, L1pi, RIn1pi, hp, aCCp, epsVdWp, CCp, CBNp];
    tScrollEnergyeVatom[[iiRIn1]] = (tScrollEnergy[[iiRIn1]]) / (eV / atom);
  tPlotEvsRin[[iiL1]] = ListPlot[
    Transpose[{tRIn1nmRegular, tScrollEnergyeVatom}], PlotRange → PlotRange / (eV / atom)];
  Print[tPlotEvsRin[[iiL1]]];
  AllPlotsEvsRin = Join[{AllPlotsEvsRin, tPlotEvsRin[[iiL1]]}];
  CarbonNanoscrollEnergyVsRinFileName = StringJoin[NanoscrollNamep, "dat"];
  Export[ToFileName[NotebookDirectory[], ScrollEnergyFileName],
    Transpose[{Insert[tRIn1nmRegular, "RIn1[nm]", 1],
      Insert[tScrollEnergyeVatom, "E[eV/atom]", 1]}]];
  Print["Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1=", tL1 / nm,
    "nm (NoL=", NoLp, ", Lw=", Lwp / nm, "nm)"];
  Print[Show[AllPlotsEvsRin]];

Print[];
Print["Manipulating of the plot of the nanoscroll energy as the functoon"];
Print[" of the nanoscroll inner radius:"];
Print[" "];
Print[" (Manipulate[Plot[fScrollEnergy[... , L1nm, RIn1, hp, ...]], "];
Print["           where L1nm (is L1 in nanometers) "];
Print["           is the manipulated value"];
Print["           )"];
Manipulate[Plot[
  (fScrollEnergy[NoLp, Lwp, L1nm nm, RIn1nmv nm, hp, aCCp, epsVdWp, CCp, CBNp]) / (eV / atom),
  {RIn1nmv, RIn1Minp / nm, RIn1Maxp / nm}, PlotRange → PlotRange / (eV / atom),
  {{L1nm, L1p / nm}, 0.5 tL1[[1]] / nm, 1.5 tL1[[Length[tL1]]] / nm}]

```

Figure3cd(Layers1L15nmRIn1d14.m

The source of the data of the manuscript

'Structure and energetics of carbon,

hexagonal boron nitride, and

carbon/hexagonal boron nitride

single-layer and bilayer nanoscrolls'

/ A.I. Siahlo, N.A. Poklonski, A.V. Lebedev,

I.V. Lebedeva, A.M. Popov, S.A. Vyrko,

A.A. Knizhnik, Yu.E. Lozovik

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№ 3.— P. 036001 (9 pp.).

[DOI: 10.1103/PhysRevMaterials.2.036001]

I.0 The Units (nm, meV, AA)

I.1. All Input Parameters and Constants-----

I.1.1. The sampling parameters

npRIn1=1000

I.1.2. The Input Geometry Parameters of the system

The carbon nanoribbon length L1=14.839nm

The carbon nanoribbon width Lw=11.8nm

Number of the layers in carbon nanoscroll NoL=1

The length of a carbon nanoribbon L1=14.839nm

The carbon nanoribbon width Lw=1.nm

The inner radius of the nanoscroll RIn1=1.14nm

I.1.2. The Input Energy Constants

epsVdW - the interlayer interaction energy per one atom of
the nanoscroll:

epsVdW=0.035eV/atom

C - the bending elastic constant:

CCelast=2.01eV AA²/atom

CCBNelast=2.01eV AA²/atom

I.1.3.The Input Geometry constants-----

The interatomic distance aCC and the interlayer distance h

h=0.3354 nm (Interlayer distance)

aCC=0.142nm, h=0.3354nm

NatomsInCell=2

dPhil2 - The difference of the inner angles of the spirales
of the Layers

I.4.The parameters for the visualisation

I.5. The parameters of visualization that depend on NoL=1

I.6. The parameters of the output file

NanoscrollName=Nanoscroll1L14.839nm

Nanoscroll1L14.839nm.txt

(The output of the data to a file Is Not Performed)

The number of the output points = 1000

I.7. The Input Numerical Constants used in the programm

The Indexes used for the work with EVdW[...] function

-----End of the Input-----

II. The derivated parameters and the functions required

II.1. The derivated parameters

The cell area $Sa = \frac{3\sqrt{3} aCC^2}{4} = 0.0261938nm^2$

II.2. The required functions-----

II.2.1. The function fSpiraleLen[1,φIn, φOut, h] defines

the Length of a Spirale with the inner angle φIn and the outer angle φOut(>=φIn):

$$fSpiraleLen[1, \varphi In, \varphi Out, h] = \frac{h \left(-\varphi In \sqrt{1 + \varphi In^2} + \varphi Out \sqrt{1 + \varphi Out^2} - \text{ArcSinh}[\varphi In] + \text{ArcSinh}[\varphi Out] \right)}{4 \pi}.$$

II.2.2. The function fElast[φIn,ρOut] is required to calculate an nanoscrolllelastic energy:

$$fElast[\varphi In, \varphi Out] = \frac{\sqrt{1 + \varphi In^2}}{\varphi In} - \frac{\sqrt{1 + \varphi Out^2}}{\varphi Out} - \text{ArcSinh}[\varphi In] + \text{ArcSinh}[\varphi Out].$$

II.2.3. Define the function fPhiOutvsPhiInLh[1,φIn,L,h].

The function $fPhiOutvsPhiInLh[1, \varphi In, L, h] = \sqrt{\frac{4 L \pi}{h} + \varphi In^2}$ is a good approximation to obtain the value of φOut for the defined φIn,L,h.

The inverse function $fPhiInvsPhiOutLh[1, \varphi Out, L, h] = \sqrt{-\frac{4 L \pi}{h} + \varphi Out^2}$

could be used in the program applications

if ROut (instead of RIn) is the input parameter of the system.

II.2.4. The functions fSpirale1Under(Over)Spirale1Length[NoLv,PhiInlv ,PhiOutlv,hv]

These functiona are not required, but could be helpful),

fSpirale1UnderSpirale1Length[1,PhiInlv ,PhiOutlv,hv]=

$$= fSpiraleLen[NoLv, \Phi Inlv, \Phi Outlv - 2\pi, hv] = \frac{1}{4 \pi}$$

$$hv NoLv \left(-\Phi Inlv \sqrt{1 + \Phi Inlv^2} + \sqrt{1 + (\Phi Outlv - 2 \pi)^2} (\Phi Outlv - 2 \pi) - \text{ArcSinh}[\Phi Inlv] + \text{ArcSinh}[\Phi Outlv - 2 \pi] \right);$$

fSpirale1UnderSpirale1Length[NoLp,PhiInlp,PhiOutlp,hp]=fSpirale1UnderSpirale1Length[

$$1, \frac{\Phi Inlp}{2 \pi} (2\pi), \frac{\Phi Outlp}{2 \pi} (2\pi), 0.3354nm] =$$

$$=0.0266903 \left(-\text{PhiInlp} \sqrt{1 + \text{PhiInlp}^2} + \sqrt{1 + (\text{PhiOutlp} - 2\pi)^2} (\text{PhiOutlp} - 2\pi) - \text{ArcSinh}[\text{PhiInlp}] + \text{ArcSinh}[\text{PhiOutlp} - 2\pi] \right) \text{nm}.$$

fSpirale1OverSpirale1Length[1,PhiInlv,PhiOutlv,hv]=

$$=\text{fSpiraleLen}[\text{NoLv},\text{PhiInlv}+2\pi,\text{PhiOutlv},\text{hv}]=\frac{1}{4\pi}$$

$$\text{hv NoLv} \left(\text{PhiOutlv} \sqrt{1 + \text{PhiOutlv}^2} + (-\text{PhiInlv} - 2\pi) \sqrt{1 + (\text{PhiInlv} + 2\pi)^2} + \text{ArcSinh}[\text{PhiOutlv}] - \text{ArcSinh}[\text{PhiInlv} + 2\pi] \right);$$

$$\begin{aligned} \text{fSpirale1OverSpirale1Length}[\text{NoLv},\text{PhiInlp},\text{PhiOutlp},\text{hp}] &= \text{fSpirale1OverSpirale1Length}[\\ 1, \frac{\text{PhiInlp}}{2\pi}(2\pi), \frac{\text{PhiOutlp}}{2\pi}(2\pi), 0.3354\text{nm}] &= \\ =0.0266903 \left(\text{PhiOutlp} \sqrt{1 + \text{PhiOutlp}^2} + \right. \\ \left. (-\text{PhiInlp} - 2\pi) \sqrt{1 + (\text{PhiInlp} + 2\pi)^2} + \text{ArcSinh}[\text{PhiOutlp}] - \text{ArcSinh}[\text{PhiInlp} + 2\pi] \right) \text{nm}. \end{aligned}$$

II.2.4. The function fRIn1Sharp[NoLv,Llv,hv]

$$\text{fRIn1Sharp}[\text{NoLv},\text{Llv},\text{hv}] = -\frac{\text{hv NoLv}}{2} + \frac{\text{Llv}}{2\pi}$$

is a good approximation to obtain the value of the sharp in the dependence ScrollEnergy[RIn]

$$\text{fRIn1Sharp}[1, 14.839\text{nm}, 0.3354\text{nm}] = 2.194\text{nm}$$

III. Begin of Calculation

III.1. The inner and the outer angle of the spirale of the layer:

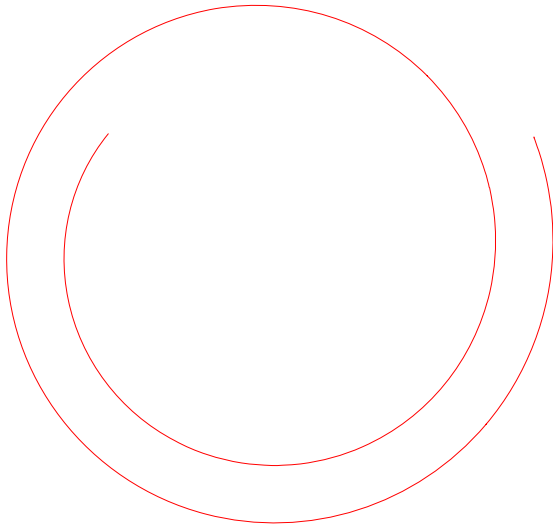
$$\varphi_{\text{Inl}} = \frac{2\pi R_{\text{Inl}}}{h}, \quad \varphi_{\text{Outl}} = \text{fPhiOutvsPhiInLh}[1, \varphi_{\text{Inl}}, L1, h];$$

For RInl=1.14nm, h=0.3354nm:

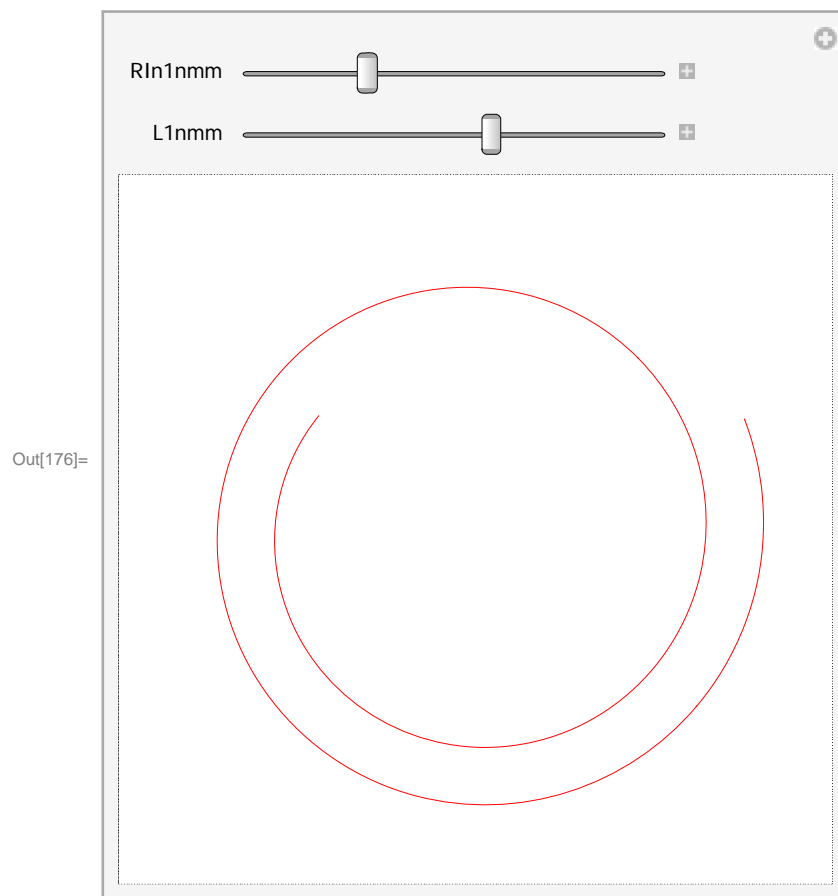
$$\varphi_{\text{Inl}} = 3.39893(2\pi), \quad \varphi_{\text{Outl}} = 5.06316(2\pi).$$

L1=14.839nm, RInl=1.14nm

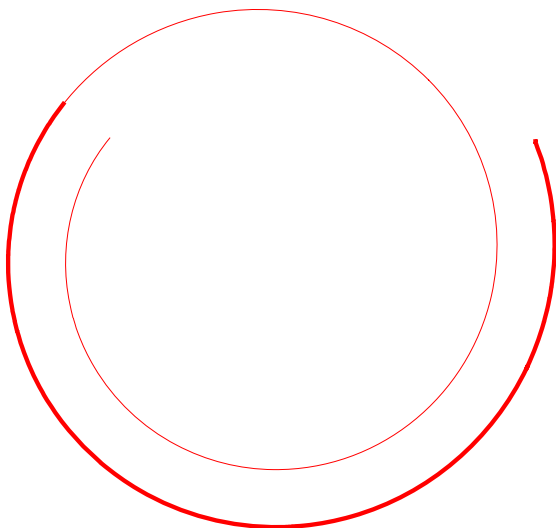
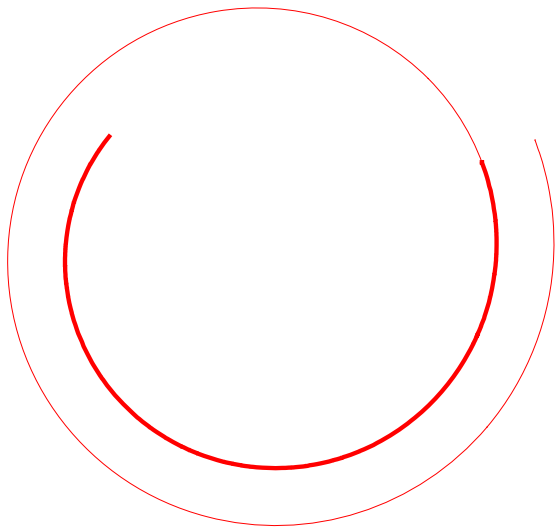
Plot the Spirale of the layer:



Manipulating of Spirale1Plot for the different RIn1 and L:



```
{Spirale, Spirale1UnderSpirale1}, {Spirale1, Spirale1OverSpirale1}:
```



III.2. The nanoscroll energy calculation

III.2.1. The elastic energy calculation

ElastC=5.7333eV/atom

III.2.2. The Van-der-Waals energy calculation

EVdWwardPhi12allp[[iEVdW]]=-7.91941eV/atom

(EVdWwardPhi12allp[[iEVdWlUn1]]=-3.49244eV/atom

EVdWwardPhi12allp[[iEVdWlOv1]]=-4.42696eV/atom)

III.4. The total energy of the nanoscroll

fScrollEnergy[1,Lwp,Llp, RInlp,hp, aCCp, epsVdWp,CCp,CBNp]=

=fScrollEnergy[1, Lw=1.nm, L1=14.839nm, RIn1=1.14nm, h=0.3354nm,


```
aCC=0.142nm, epsVdW=0.035eV/atom, CC=2.01(eV AA^2/atom)=
=-2.18611eV/atom
```

III.5. Determine the inner angles mismatch for the bi-layer nanoscroll
for the high nanoribbon Length

```
For L1=14.839nm,RIn=1.14nm,h=0.3354nm and dPhi12=0:
```

```
ScrollEnergy=-2.18611eV/atom
```

```
For L1=14.839nm,RIn=1.14nm,h=0.3354nm and dPhi12=Pi:
```

```
ScrollEnergy=-2.18611eV/atom
```

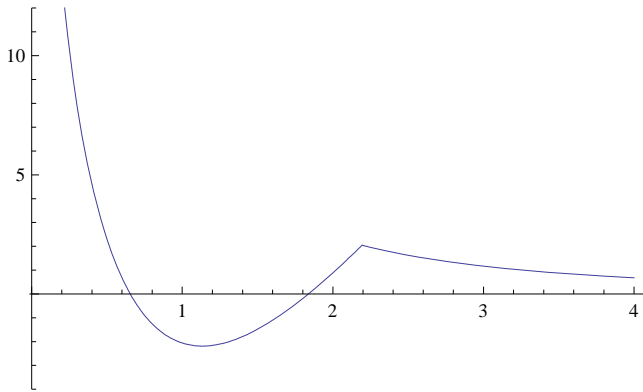
IV.The potential energy of the nanoscroll

as a function of the inner radius RIn

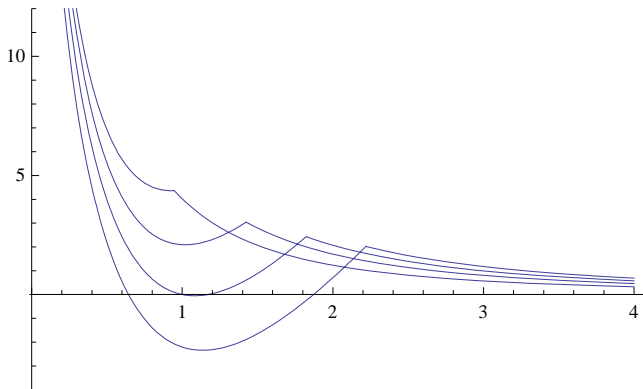
```
NoL=1
```

```
epsVdW=0.035eV/atom, C=0.0201(eV nm^2/atom)(eV nm^2/atom),aCC=0.142nm,h=0.3354nm
```

```
Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1=14.839nm (NoL=1,Lw=1.nm)
```



```
Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1={7., 10., 12.5, 15.}nm (NoL=1,w=1.nm)
```



The examples of using of 'fScrollEnergy[...]' function:

```
fScrollEnergy[NoLp,Lwp,tL1[[1]],RInlp,hp, aCCp, epsVdWp,CCp,CBNp]=3.26809 eV/atom
```

```
fScrollEnergy[NoLp,Lwp,tL1[[1]],1nm,hp, aCCp, epsVdWp,CCp, CBNp]=4.01569 eV/atom
```

```
fScrollEnergy[NoLp,Lwp,7nm,1nm,hp, aCCp, epsVdWp,CCp, CBNp]=4.01569 eV/atom
```

```
fEVdWLayer1Overlap[1,Lwp,7.nm,1.nm,hp,aCCp,epsVdWp][[1]]=
0.39374eV/atom (right !=0 value, because the layer overlaps
```

```
fEVdWLayer1Overlap[1,Lwp,7.nm,1.5nm,hp,aCCp,epsVdWp][[1]]=
12.2479eV/atom !=0, wrong value of the
fEVdWLayer1Overlap[..] function because the layer does not overlap
```

The analytical expressions of the fEVdWLayer1Overlap[..] function:

```
--- fEVdWLayer1Overlap[NoL1,Lwv,Lpv,RInv,hv,aCCv,epsVdWv][[1]]: ---
```

$$\begin{aligned}
& -\frac{1}{6\sqrt{3}aCCv^2\pi}\text{epsVdWv}hvLwv \\
& \left(\sqrt{\frac{4Lpv\pi}{hv} + \frac{4\pi^2RInv^2}{hv^2}} \sqrt{1 + \frac{4Lpv\pi}{hv} + \frac{4\pi^2RInv^2}{hv^2}} + \left(-2\pi - \frac{2\pi RInv}{hv}\right) \sqrt{1 + \left(2\pi + \frac{2\pi RInv}{hv}\right)^2} - \right. \\
& \quad \left. \text{ArcSinh}\left[2\pi + \frac{2\pi RInv}{hv}\right] + \text{ArcSinh}\left[\sqrt{\frac{4Lpv\pi}{hv} + \frac{4\pi^2RInv^2}{hv^2}}\right] \right) - \frac{1}{6\sqrt{3}aCCv^2\pi}\text{epsVdWv}hvLwv \\
& \left(-\frac{2\pi RInv}{hv} \sqrt{1 + \frac{4\pi^2RInv^2}{hv^2}} + \left(-2\pi + \sqrt{\frac{4Lpv\pi}{hv} + \frac{4\pi^2RInv^2}{hv^2}}\right) \sqrt{1 + \left(-2\pi + \sqrt{\frac{4Lpv\pi}{hv} + \frac{4\pi^2RInv^2}{hv^2}}\right)^2} - \right. \\
& \quad \left. \text{ArcSinh}\left[\frac{2\pi RInv}{hv}\right] - \text{ArcSinh}\left[2\pi - \sqrt{\frac{4Lpv\pi}{hv} + \frac{4\pi^2RInv^2}{hv^2}}\right] \right)
\end{aligned}$$

```
--- fEVdWLayer1Overlap[NoL2,Lwv,Lpv,RInv,hv,aCCv,epsVdWv][[1]]: ---
```

$$\begin{aligned}
& -\frac{1}{3\sqrt{3}aCCv^2\pi}\text{epsVdWv}hvLwv \\
& \left(\sqrt{\frac{2Lpv\pi}{hv} + \frac{\pi^2RInv^2}{hv^2}} \sqrt{1 + \frac{2Lpv\pi}{hv} + \frac{\pi^2RInv^2}{hv^2}} + \left(-2\pi - \frac{\pi RInv}{hv}\right) \sqrt{1 + \left(2\pi + \frac{\pi RInv}{hv}\right)^2} - \right. \\
& \quad \left. \text{ArcSinh}\left[2\pi + \frac{\pi RInv}{hv}\right] + \text{ArcSinh}\left[\sqrt{\frac{2Lpv\pi}{hv} + \frac{\pi^2RInv^2}{hv^2}}\right] \right) - \frac{1}{3\sqrt{3}aCCv^2\pi}\text{epsVdWv}hvLwv \\
& \left(-\frac{\pi RInv}{hv} \sqrt{1 + \frac{\pi^2RInv^2}{hv^2}} + \left(-2\pi + \sqrt{\frac{2Lpv\pi}{hv} + \frac{\pi^2RInv^2}{hv^2}}\right) \sqrt{1 + \left(-2\pi + \sqrt{\frac{2Lpv\pi}{hv} + \frac{\pi^2RInv^2}{hv^2}}\right)^2} - \right. \\
& \quad \left. \text{ArcSinh}\left[\frac{\pi RInv}{hv}\right] - \text{ArcSinh}\left[2\pi - \sqrt{\frac{2Lpv\pi}{hv} + \frac{\pi^2RInv^2}{hv^2}}\right] \right)
\end{aligned}$$

The Analytical expression of

fScrollEnergyVdWandElast[1,Lwv,Llv,RInlv,hv,aCCv, epsVdWv, CCv,CBNv]:

$$\begin{aligned}
 & \frac{8 \text{CCv} \text{Lwv} \pi \left(\frac{h v \sqrt{1 + \frac{4 \pi^2 \text{RInlv}^2}{h v^2}}}{2 \pi \text{RInlv}} - \frac{\sqrt{1 + \frac{4 \text{Llv} \pi}{h v} + \frac{4 \pi^2 \text{RInlv}^2}{h v^2}}}{\sqrt{\frac{4 \text{Llv} \pi}{h v} + \frac{4 \pi^2 \text{RInlv}^2}{h v^2}}} - \text{ArcSinh}\left[\frac{2 \pi \text{RInlv}}{h v}\right] + \text{ArcSinh}\left[\sqrt{\frac{4 \text{Llv} \pi}{h v} + \frac{4 \pi^2 \text{RInlv}^2}{h v^2}}\right] \right)}{3 \sqrt{3} \text{aCCv}^2 h v} - \\
 & \frac{1}{6 \sqrt{3} \text{aCCv}^2 \pi} \text{epsVdWv} h v \text{Lwv} \\
 & \left(\sqrt{\frac{4 \text{Llv} \pi}{h v} + \frac{4 \pi^2 \text{RInlv}^2}{h v^2}} \sqrt{1 + \frac{4 \text{Llv} \pi}{h v} + \frac{4 \pi^2 \text{RInlv}^2}{h v^2}} + \left(-2 \pi - \frac{2 \pi \text{RInlv}}{h v} \right) \sqrt{1 + \left(2 \pi + \frac{2 \pi \text{RInlv}}{h v} \right)^2} - \right. \\
 & \left. \text{ArcSinh}\left[2 \pi + \frac{2 \pi \text{RInlv}}{h v}\right] + \text{ArcSinh}\left[\sqrt{\frac{4 \text{Llv} \pi}{h v} + \frac{4 \pi^2 \text{RInlv}^2}{h v^2}}\right] \right) - \frac{1}{6 \sqrt{3} \text{aCCv}^2 \pi} \text{epsVdWv} h v \text{Lwv} \\
 & \left(-\frac{2 \pi \text{RInlv} \sqrt{1 + \frac{4 \pi^2 \text{RInlv}^2}{h v^2}}}{h v} + \left(-2 \pi + \sqrt{\frac{4 \text{Llv} \pi}{h v} + \frac{4 \pi^2 \text{RInlv}^2}{h v^2}} \right) \sqrt{1 + \left(-2 \pi + \sqrt{\frac{4 \text{Llv} \pi}{h v} + \frac{4 \pi^2 \text{RInlv}^2}{h v^2}} \right)^2} - \right. \\
 & \left. \text{ArcSinh}\left[\frac{2 \pi \text{RInlv}}{h v}\right] - \text{ArcSinh}\left[2 \pi - \sqrt{\frac{4 \text{Llv} \pi}{h v} + \frac{4 \pi^2 \text{RInlv}^2}{h v^2}}\right] \right)
 \end{aligned}$$

V. Export the data of the plots of the nanoscroll energy

as a function of the inner radius

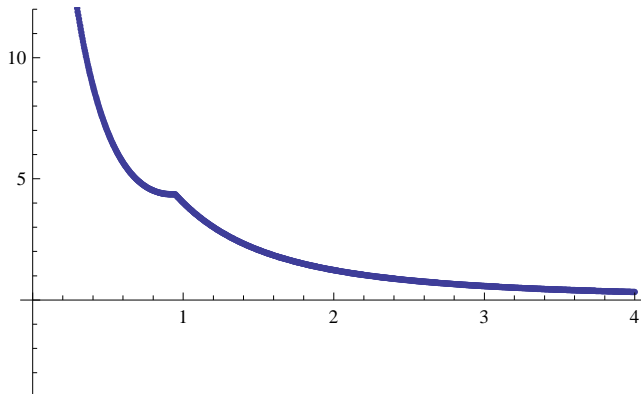
The parameters of the output file

The number of the output points = 1000

Export the plot data to the files:

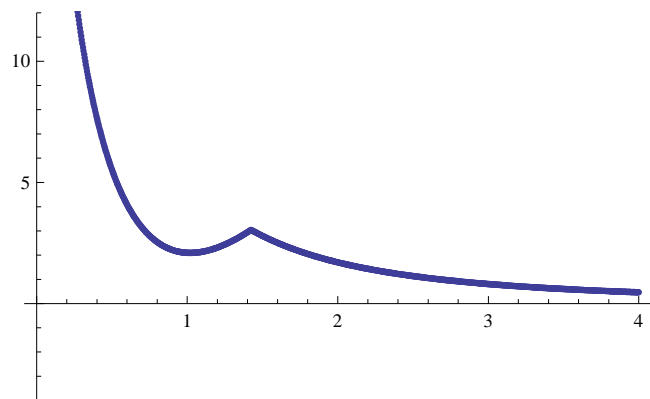
NanoscrollName=Nanoscroll1L7.nm

ScrollEnergyFileName=EvsRIn1Nanoscroll1L7.nm.dat



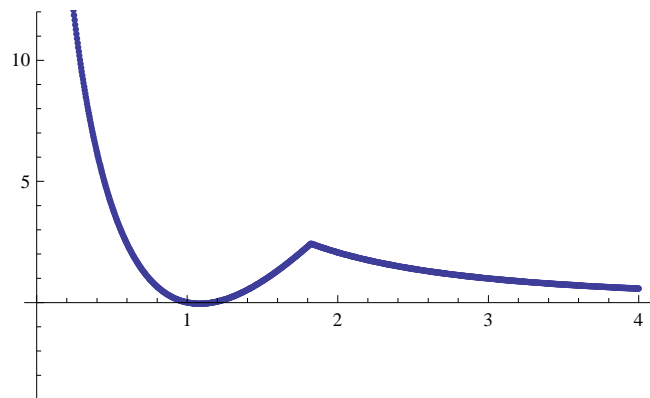
NanoscrollName=Nanoscroll11L10.nm

ScrollEnergyFileName=EvsRIn1Nanoscroll11L10.nm.dat



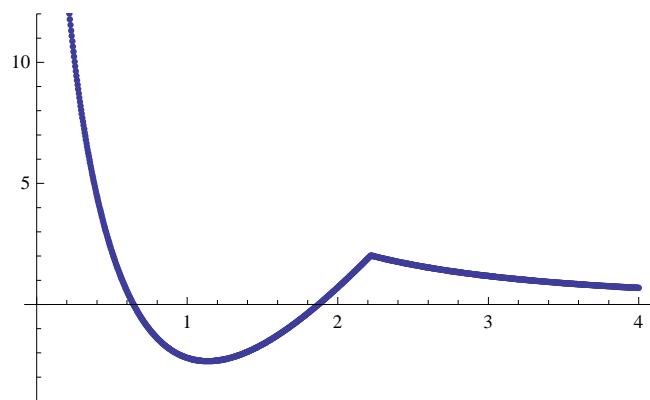
NanoscrollName=Nanoscroll11L12.5nm

ScrollEnergyFileName=EvsRIn1Nanoscroll11L12.5nm.dat

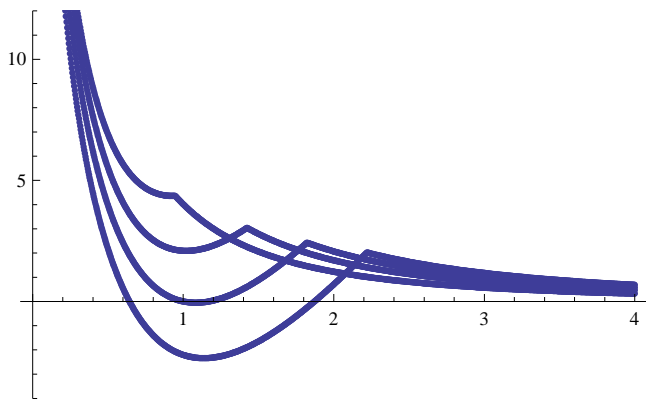


NanoscrollName=Nanoscroll11L15.nm

ScrollEnergyFileName=EvsRIn1Nanoscroll11L15.nm.dat



Plot ScrollEnergy[RIn1/nm]/(eV/atom) for L1={7., 10., 12.5, 15.}nm (NoL=1,Lw=1.nm)



Manipulating of the plot of the nanoscroll energy as the function
of the nanoscroll inner radius:

```
(Manipulate[Plot[fScrollEnergy[... , L1nm, RIn1, hp, ...]],
  where L1nm (is L1 in nanometers)
  is the manipulated value
)
```

Out[278]=

