'Pricing under Rough Volatilty Models' Lab Report

Group 2

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Abstract

In the present paper we investigate the roughness of the Russian stock market in the context of the rough stochastic volatility model. We obtain the estimation of the Hurst parameter for the major Russian corporations. In the end we form the conclusion that the rough volatility model is a working model for the Russian stock market and formulate the future research horizon.

0.1 Introduction

The first revolutionary model of Mathematical Finance was introduced by F. Black and M. Sholes in 1973's article [BS73], and a similar model introduced in 1976 by F. Black in [Bla76] (the only fundamental difference was the use of the forward prices instead of spot prices, which is proven to be useful for some markets). Later there were created some local volatility models (like Dupire's LVM), and first stochastic volatility models (Heston SVM), but they still were not a perfect fit for pricing, even when first LSVMs were introduced.

Fractional Brownian motions were first employed in volatility modelling by F. Comte and E. Renault [CR98]. Their model (called FSV) used a fractional Brownian motion with Hurst parameter H > 0.5 to model volatility as a long-memory process i.e. one where autocorrelation decays slowly, which was a widely accepted stylized fact. They thus introduced the class of fractional stochastic volatility models.

In 2014, J. Gatheral, T. Jaisson, and M. Rosenbaum showed in [GJR18] that for major American indices Hurst parameter estimations have the order of 1e-1 (i.e. H<0.5, therefore, there is no long-memory in the FSV-based models), and called the corresponding model (FSV + H<0.5) a rough fractional stochastic volatility model (RFSV) to emphasise that the volatility is indeed rough.

However, their approach requires the use of a model, therefore, it is not perfect still. In 2022, R. Cont and P. Das [CD22] proposed a method of estimating the roughness of an asset without the need of a model, which can be used to find statistical evidence that volatility is rough even without RFSV.

In the present paper I show that the Hurst parameters of the major Russia-originated assets (stocks and depositary reciepts of Russian corporations) are less than 0.5 under RFSV, i.e. Comte and Renault's basic FSV model is not working well for the Russian stock markets, therefore, RFSV should be used instead.

Chapter 1

Rough Fractional Stochastic Volatilty Model Estimation

1.1 Realized volatility

Consider a stochastic volatility model

$$dS_t = \mu_t S_t dt + \sigma_t S_t dW_t, \tag{1.1.1}$$

where S_t is an asset price process, and σ_t is a stochastic volatility process representing a so-called *spot* volatility. Spot volatility, in fact, is not observable in the market, therefore, we should estimate it somehow.

Definition 1.1.1. The realized variance of a price process S over time interval $[t, t + \delta]$ sampled along the time partition π^n is defined as

$$RVar_{t,t+\delta}(\pi^n) = \sum_{\pi^n \cap [t,t+\delta]} \left(\log S_{t_{i+1}^n} - \log S_{t_i^n} \right)^2$$
 (1.1.2)

and realized volatility is defined as

$$RV_{t,t+\delta}(\pi^n) = \sqrt{\sum_{\pi^n \cap [t,t+\delta]} \left(\log S_{t_{i+1}^n} - \log S_{t_i^n}\right)^2}$$
 (1.1.3)

Definition 1.1.2. Let S satisfy (1.1.1). Then the integrated variance is defined as

$$IVar_t = \int_0^t \sigma_s^2 ds \tag{1.1.4}$$

It has been shown many times (e.g. [BS02]) and mentioned in [CD22] that the realized variance converges in probability to the integrated variance as sampling frequency increases for all assets satisfying the equation (1.2.1) (i.e. stochastic volatility models).

Proposition 1.1.1. As time partition scale of π^n tends to 0, $RV_{t,t+\delta}(\pi^n) \approx \sqrt{\delta}\sigma_t$, i.e. $RV_{t,t+\delta}/\sqrt{\delta}\sigma_t$ could be considered as a consistent estimator of the spot volatility.

Definition 1.1.3. The fractional Brownian motion $(W_t^H)_{t \in \mathbb{R}_+}$ with Hurst parameter $H \in (0,1)$ is a Gaussian process with the following properties:

- 1. $W_0^H = 0$,
- 2. $\mathbb{E}\left[W_t^H\right] \equiv 0$,
- 3. $\mathbb{E}\left[W_s^H W_t^H\right] = \frac{1}{2} \left(t^{2H} + s^{2H} |t s|^{2H}\right)$

Definition 1.1.4. A stationary fOU process X_t is defined as the stationary solution of the stochastic differential equation

$$dX_t = \nu dW_t^H - \alpha (X_t - m)dt, \tag{1.1.5}$$

where $m \in \mathbb{R}$ and ν and α are positive parameters, see [CKM03].

1.1.1 What is a long-memory process?

Definition 1.1.5. A process X_t is said to have a long memory, if

$$\sum_{k=0}^{\infty} Cov \left[X_1, X_k - X_{k-1} \right] = +\infty.$$
 (1.1.6)

In particular, the fractional Brownian motion with $H > \frac{1}{2}$ is a long-memory process. Long-memory of the stochastic volatility process in stochastic volatility models framework used to be a widely-accepted stylized fact [BCD98; CR98; CR96; DGE93].

1.2 Model description

In [GJR18] the authors considered the following model, as did I. Let there be a riskless asset $B_t \equiv 1$, and a risky asset, whose price S_t is defined by the following equations:

$$dS_t = \alpha S_t dt + \sigma_t S_t dW_t, \tag{1.2.1}$$

$$d\log \sigma_t = \alpha (m - \log \sigma_t) dt + \nu dW_t^H, \tag{1.2.2}$$

The risky asset is being traded in the market in numeraire prices (in our case, $B_t = 1$ RUB for stocks and GBP for depositary reciepts).

Definition 1.2.1. A model (1.2.1) – (1.2.2) is called a *Fractional Stochastic Volatility Model* (FSV). For a special case H < 0.5 the model is called a *Rough Fractional Stochastic Volatility Model* (RFSV) to emphasise a so-called roughness of the trajectories of the fBm.

In [CKM03] an exact formula for the autocovariance function of the log-volatility in the RFSV model was derived:

$$cov \left[\log \sigma_t, \log \sigma_{t+\Delta} \right] =$$

$$=\frac{H(2H-1)\nu^2}{2\alpha^{2H}}\left(e^{-\alpha\Delta}\Gamma(2H-1)+e^{-\alpha\Delta}\int_0^{\alpha\Delta}\frac{e^u}{u^{2-2H}}du+e^{\alpha\Delta}\int_{\alpha\Delta}^{+\infty}\frac{e^u}{u^{2-2H}}du\right) \quad (1.2.3)$$

Via the explicit formula for the covariance function of the log-volatility in the RFSV model (1.2.3), we can write a closed-form expression for a theoretical $m(q, \Delta)$:

$$m(q, \Delta) = 2 \left(\operatorname{var} \log \sigma_t - \operatorname{cov} \left[\log \sigma_t, \log \sigma_{t+\Delta} \right] \right),^2$$
 (1.2.4)

1.3 Normality Statistical Tests

In the following, x_i denotes a sample of n observations, g_1 and g_2 are the sample skewness and kurtosis, μ_j 's are the j-th sample central moments, and \overline{x} is the sample mean.

1.3.1 D'Agostino's K-squared test

The sample skewness and kurtosis are defined as

$$g_1 = \frac{m_3}{m_2^{3/2}} = \frac{\frac{1}{n} \sum_{i=1}^n (x_i - \overline{x})^3}{\left(\frac{1}{n} \sum_{i=1}^n (x_i - \overline{x})^2\right)^{3/2}},$$
(1.3.1)

$$g_2 = \frac{m_4}{m_2^2} - 3 = \frac{\frac{1}{n} \sum_{i=1}^n (x_i - \overline{x})^4}{\left(\frac{1}{n} \sum_{i=1}^n (x_i - \overline{x})^2\right)^2} - 3.$$
 (1.3.2)

¹Despite the original [CR98] naming (Comte and Renault used a model with long memory of volatility as a stylized fact), we shall call our model FSV for any $H \in (0,1)$

 $^{^{2}}m(q,\Delta) = \mathbb{E}\left[\left(\log \sigma_{t+\Delta} - \log \sigma_{t}\right)^{2}\right]$

Let

$$Z_1(g_1) = \delta \operatorname{asinh}\left(\frac{g_1}{\alpha\sqrt{\mu_2}}\right),$$
 (1.3.3)

where constants α and δ are computed as

$$W^2 = \sqrt{2\gamma_2 + 4} - 1, (1.3.4)$$

$$\delta = 1/\sqrt{\ln W},\tag{1.3.5}$$

$$\alpha^2 = 2/(W^2 - 1),\tag{1.3.6}$$

and

$$Z_2(g_2) = \sqrt{\frac{9A}{2}} \left\{ 1 - \frac{2}{9A} - \left(\frac{1 - 2/A}{1 + \frac{g_2 - \mu_1}{\sqrt{\mu_2}} \sqrt{2/(A - 4)}} \right)^{1/3} \right\}, \tag{1.3.7}$$

where

$$A = 6 + \frac{8}{\gamma_1} \left(\frac{2}{\gamma_1} + \sqrt{1 + 4/\gamma_1^2} \right), \tag{1.3.8}$$

$$\mu_1(g_2) = -\frac{6}{n+1},\tag{1.3.9}$$

$$\mu_2(g_2) = \frac{24n(n-2)(n-3)}{(n+1)^2(n+3)(n+5)},\tag{1.3.10}$$

$$\gamma_1(g_2) \equiv \frac{\mu_3(g_2)}{\mu_2(g_2)^{3/2}} = \frac{6(n^2 - 5n + 2)}{(n+7)(n+9)} \sqrt{\frac{6(n+3)(n+5)}{n(n-2)(n-3)}},$$
(1.3.11)

$$\gamma_2(g_2) \equiv \frac{\mu_4(g_2)}{\mu_2(g_2)^2} - 3 = \frac{36(15n^6 - 36n^5 - 628n^4 + 982n^3 + 5777n^2 - 6402n + 900)}{n(n-3)(n-2)(n+7)(n+9)(n+11)(n+13)}.$$
 (1.3.12)

The analytical expressions for skewness and kurtosis (1.3.11) - (1.3.12) were derived by E. Pearson in [Pea31].

Definition 1.3.1. The *D'Agostino-Pearson* statistic is defined as

$$K^2 = Z_1(g_1)^2 + Z_2(g_2)^2 (1.3.13)$$

Null hypothesis: the sample is normally distributed.

NB. The K^2 statistic is able to detect deviations from both skewness and kurtosis. If the null hypothesis is true, then the test statistic has the χ^2 distribution with 2 degrees of freedom.

1.3.2 Shapiro-Wilk test

Definition 1.3.2. The Shapiro–Wilk test statistic is defined as

$$W = \frac{\left(\sum_{i=1}^{n} a_i x_{(i)}\right)^2}{\sum_{i=1}^{n} (x_i - \overline{x})^2},$$
(1.3.14)

where

$$(a_1, \dots, a_n) = \frac{m^T V^{-1}}{C}, \quad C = ||V^{-1} m|| = (m^T V^{-1} V^{-1} m)^{1/2},$$

and $m = (m_1, ..., m_n)^T$ is a mean of order statistic from a normally distributed sample, V is the covariance matrix of those normal order statistics. Null hypothesis: the sample is normally distributed.

 ${\bf NB.}$ The W statistic has no distinguishable name, and the cutoff values are calculated numerically by Monte-Carlo simulation.

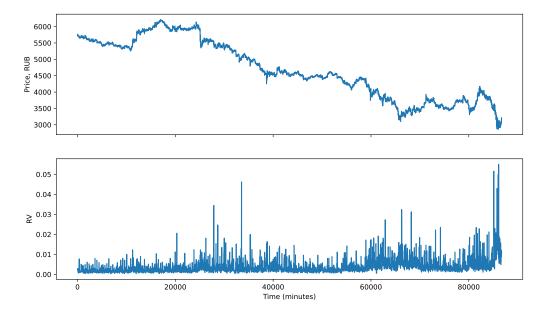


Figure 1.1: YNDX RX Equity. Price and Realized Volatility

1.4 Statistical Analysis

1.4.1 Data Preprocessing and Realized Volatility Estimation

In the present paper we used high-frequency data for two types of assets:

- 1. Stocks: Yandex, Sberbank, Gazprom, VTB, Moscow Exchange, Lukoil, and X5 Group
- 2. Depositary reciepts: Sberbank, Gazprom, VTB, and Lukoil

Some text to be written

Using this approach to estimate the realized volatility we can be sure that our data is correlated in the least way possible.

1.4.2 Hurst Parameter Estimation

Let $m(q, \Delta, \pi^n)$ be a sample q-th absolute moment of $\log RV_{t+\Delta} - \log RV_t$ (under stationarity of increments assumptions):

$$m(q, \Delta, \pi^n) := \frac{1}{n} \sum_{t} |\log RV_{t+\Delta} - \log RV_t|^q,$$
 (1.4.1)

i.e. $m(q, \Delta, \pi^n)$ is an empirical counterpart of $\mathbb{E}[|\log RV_{\Delta} - \log RV_0|^q]$. In my work we used the uniform partition with Δ -minutes increments, so we omit the π^n notation and use $m(q, \Delta)$.

Due to the similarities in the obtained results for all assets, we shall deeply analyze the Hurst parameter estimation only for the Yandex stocks (YNDX RX Equity). Plots for other equities could be found in the appendix, whereas the Hurst parameter estimations for them could be found in the table 1.1. Estimation parameters:

- Realized volatility is estimated by 15 minute disjoint windows
- $\Delta \in [0, 40]$ for ζ_q estimation and other plots

NB. We did not manage to obtain more HF data (only 5 months of 1m-tick data), therefore my estimations are not precise and could not be used for further application.

Asset Type	Ticker	\hat{H}
Stock	YNDX	0.0521766
Stock	SBER	0.1551646
Stock	VTBR	0.0917236
Stock	MOEX	0.0853878
Stock	LKOH	0.0730521
Stock	GAZP	0.1309705
Stock	FIVE	0.0630289
Depositary reciept	OGZD	0.0523981
Depositary reciept	VTBR	0.0370185
Depositary reciept	SBER	0.0578053
Depositary reciept	LKOD	0.0352792

Table 1.1: Hurst parameter estimations for major Russian companies stocks and depositary reciepts

In the figure 1.2 we can see that for q = 0.6, 0.8, and 1.0 the dots are very discrepant for $\log \Delta > 2.0$. However, we get a pretty decent linear fit for q = 0.2 and q = 0.4, therefore, the estimation on these two point would be the best one we can manage to extract. On the other hand, on ζ_q plot we observe a perfect linear fit for all q-s, therefore, H is its slope indeed.

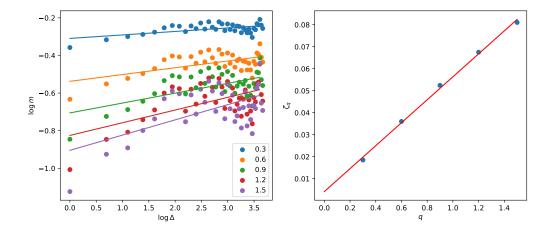


Figure 1.2: YNDX RX Equity. Plots for \hat{H}

We note that the graphs for ζ_q are slightly concave, which correlates with [GJR18] results. They conclude that this effect takes place due to the finite statistical population size.

1.4.3 Smoothing Effect Estimation

Smoothing effect is throroughly discussed in the appendix of [GJR18].

We can clearly see that due to the positive slope of the plot 1.4, the hypothesis about increasing \hat{H} and decreasing $\hat{\alpha}$ as δ increases is to be accepted.

1.4.4 Tests for normality of volatility's log-increments

In order to test the normality of the log-increments of the realized volatility, we used the following tests:

- 1. Visual analysis of histograms: KDE vs normal fit vs empirical fit
- 2. Visual analysis of excessed kurtosis plot
- 3. D'Agostino's K Squared normality test
- 4. Shapiro-Wilk normality test

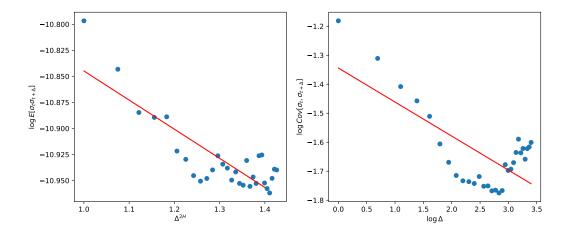


Figure 1.3: YNDX RX Equity. Empirical counterpart of $\log \mathbb{E}\left[\sigma_t \sigma_{t+\Delta}\right]$ as a function of Δ^{2H} (left) and Empirical counterpart of $\log \operatorname{cov}[\sigma_t, \sigma_{t+\Delta}]$ as a function of $\log \Delta$ (right)

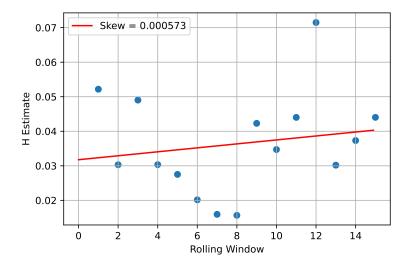


Figure 1.4: YNDX RX Equity. Smoothing Effect

In [GJR18] the authors used **only** the visual analysis of the histograms, which, as we can now say, is not surprising due to the inadequacy of results for other numerical experiments.

Visual analysis of histograms and excessed kurtosis plot

- 1. KDE is the kernel density estimator of the data.
- 2. Normal fit $NF(\Delta)$ is the normal distribution fitted to the data with the same mean and variance.
- 3. Empirical fit $EF(\Delta)$ is the scaled normal distribution:
 - EF(1) is said to be same as the NF(1)
 - $EF(\Delta)$ for $\Delta > 1$ is said to be a scaled NF(1) by the factor of $\Delta^{\hat{H}}$ (by this we test the monofractal scaling property of normal distribution)

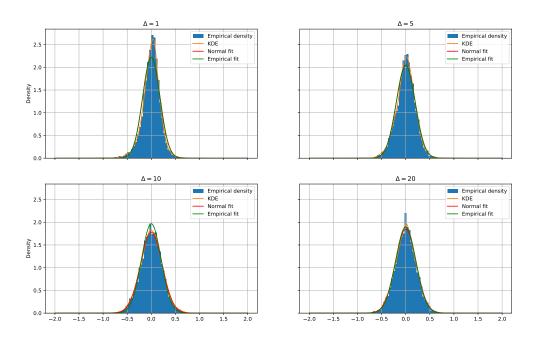


Figure 1.5: YNDX RX Equity. Empirical density of $\log \sigma_{t+\Delta} - \log \sigma_t$ for $\Delta = 1, 5, 10, 20$ days.

Looking at the figure 1.5, we may form a conclusion: KDE and EF are a decent normality approximations for $\Delta=10,20$. For others, we don't get a fancy picture: KDE(1) and KDE(5) have a large kurtosis (they are too 'peaky' for them to be normally distributed). Excessed curtosis plot 1.6 confirms our visual conclusion for KDE and EF plots.

Statistical tests for normality

We fix the confidence level to be $\alpha = 0.05$.

NB. Both of these tests require the data to be independent, but we cannot guarantee this due to the dependence of fBm's increments. We do our best to analyse the population, but these two tests give us weak proof of normality due to possible correlations.

Looking at the tables with the results of Shapiro-Wilk and D'Agostino's K-Squared tests (tables 3.1 - 3.11), we can see that for the majority of lags and for the majority of the considered assets, both tests showed the result "Not normal", i.e. both tests rejected the null hypothesis.

The three possible explanations are:

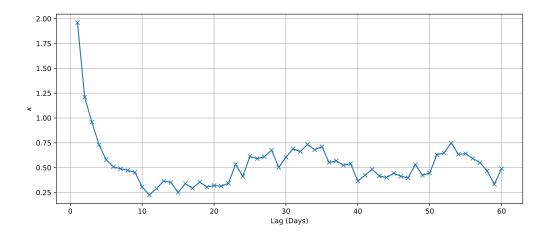


Figure 1.6: YNDX RX Equity. Excessed kurtosis κ as a function of Δ

- 1. The tests are correct and the data is not normally distributed or is correlated strongly.
- 2. The visual analysis of the histograms show that for many lags the KDE plot, the normal fit and the empirical fit are very similar, therefore, the distribution is normal, but the data is correlated strongly. The excessed kurtosis plot shows that the data is distributed very close to the normal distribution for $\Delta > 5$, and at its closest distance for $\Delta \in [10, 22]$.
- 3. We get a population sampling error (not enough data).

Chapter 2

Zumbach Effect Estimation

Chapter 3

Conclusion

3.1 Conclusion

We got aquainted with the fractional stochastic volatility models framework and studied the statistical properties of RFSV. We obtained roughness estimations for major Russian companies stocks and depositary reciepts, and reproduced some effects described in [GJR18].

Reproduced hypotheses:

- 1. The Hurst exponent of the considered assets has the order of 1e-1 and is less than $\frac{1}{2}$.
- 2. The volatility of the considered assets **does not** have a property of long memory under fractional stochastic volatility models.
- 3. Visual analysis and normality tests for the log-increments of volatility shows that for $\Delta \in [10, 25]$ the normality of log-increments hypothesis holds.
- 4. The smoothing effect holds for the estimations of H and α (volatility of volatility under fOU). But **only** for VTBR LI Equity we got a negative slope of the smoothing effect. For other asset we got a nearly perfect linear fit and positive smoothing slopes.

Bibliography

- [Pea31] Egon S. Pearson. "Note on Tests for Normality". In: *Biometrika* 22.3-4 (May 1931), pp. 423–424. ISSN: 0006-3444. DOI: 10.1093/biomet/22.3-4.423.
- [BS73] Fischer Black and Myron Scholes. "The Pricing of Options and Corporate Liabilities". In: Journal of Political Economy 81.3 (1973), pp. 637–657. ISSN: 1537534X. DOI: 10.1086/260062.
- [Bla76] Fischer Black. "The pricing of commodity contracts". In: *Journal of Financial Economics* 3.1-2 (Jan. 1976), pp. 167–179. ISSN: 0304-405X. DOI: 10.1016/0304-405X(76)90024-6.
- [DGE93] Zhuanxin Ding, Clive W.J. Granger, and Robert F. Engle. "A long memory property of stock market returns and a new model". In: *Journal of Empirical Finance* 1 (1 June 1993), pp. 83–106. ISSN: 0927-5398. DOI: 10.1016/0927-5398(93)90006-D.
- [CR96] F. Comte and E. Renault. "Long memory continuous time models". In: *Journal of Econometrics* 73 (1 July 1996), pp. 101–149. ISSN: 0304-4076. DOI: 10.1016/0304-4076 (95) 01735-6.
- [BCD98] F. Jay Breidt, Nuno Crato, and Pedro De Lima. "The detection and estimation of long memory in stochastic volatility". In: *Journal of Econometrics* 83.1-2 (1998), pp. 325–348. ISSN: 03044076. DOI: 10.1016/S0304-4076(97)00072-9.
- [CR98] Fabienne Comte and Eric Renault. "Long memory in continuous-time stochastic volatility models". In: *Mathematical Finance* 8.4 (Oct. 1998), pp. 291–323. ISSN: 1467-9965. DOI: 10.1111/1467-9965.00057.
- [BS02] Ole E Barndorff-Nielsen and Neil Shephard. "Econometric analysis of realized volatility and its use in estimating stochastic volatility models". In: *Journal of the Royal Statistical Society:* Series B (Statistical Methodology) 64.2 (May 2002), pp. 253–280. ISSN: 13697412. DOI: 10. 1111/1467-9868.00336.
- [CKM03] Patrick Cheridito, Hideyuki Kawaguchi, and Makoto Maejima. "Fractional Ornstein-Uhlenbeck Processes". In: *Electronic Journal of Probability* 8(3):14 (2003). DOI: 10.1214/EJP.V8-125.
- [GJR18] Jim Gatheral, Thibault Jaisson, and Mathieu Rosenbaum. "Volatility is rough". In: *Quantitative Finance* 18.6 (2018), pp. 933–949. ISSN: 14697696. DOI: 10.1080/14697688.2017. 1393551. arXiv: 1410.3394.
- [CD22] Rama Cont and Purba Das. "Rough volatility: fact or artefact?" In: (Mar. 2022). DOI: 10. 48550/ARXIV.2203.13820. arXiv: 2203.13820.

Appendix A. Results for Additional Assets

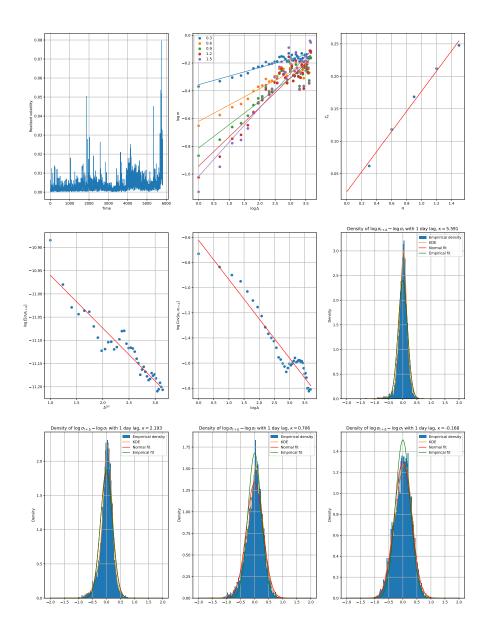


Figure 3.1: SBER RX Equity

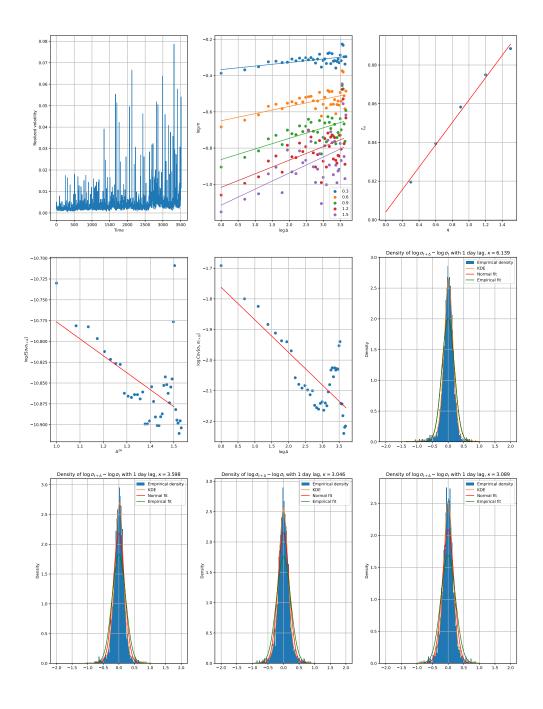


Figure 3.2: SBER LI Equity

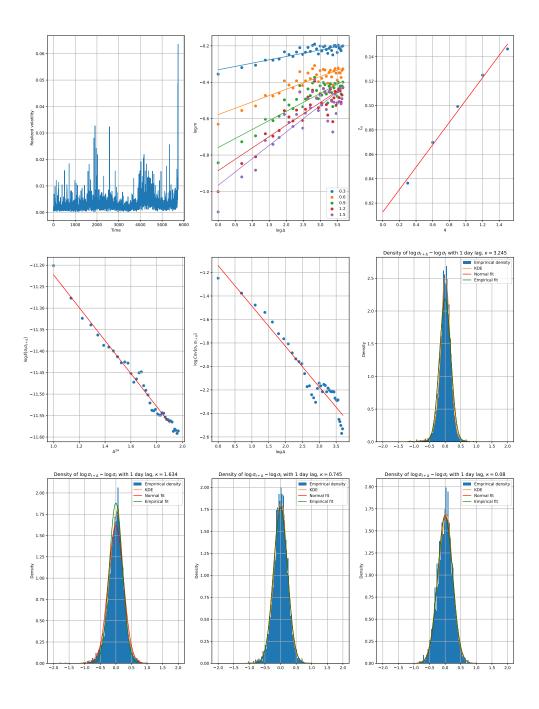


Figure 3.3: VTBR RX Equity

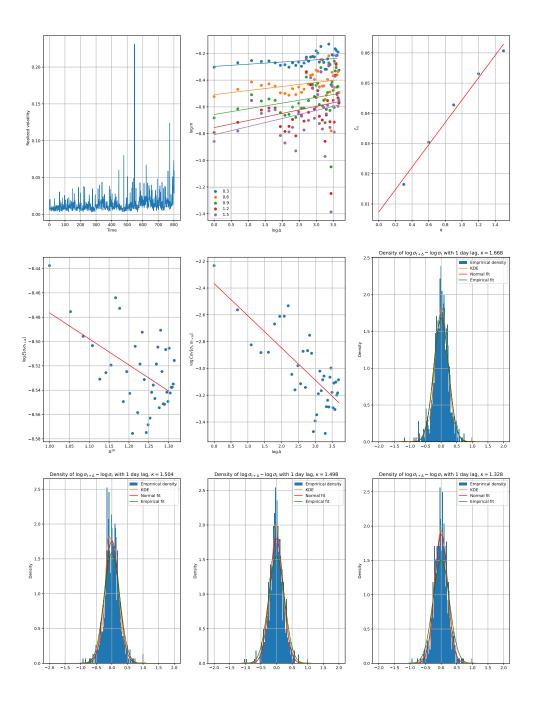


Figure 3.4: VTBR LI Equity

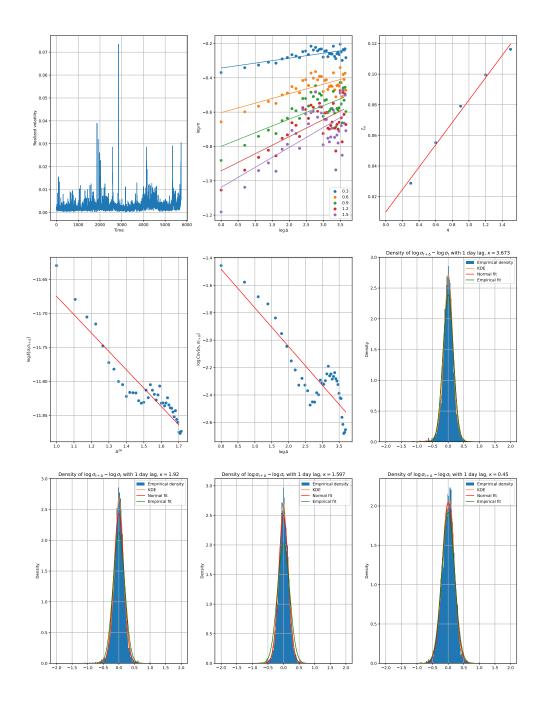


Figure 3.5: LKOH RX Equity

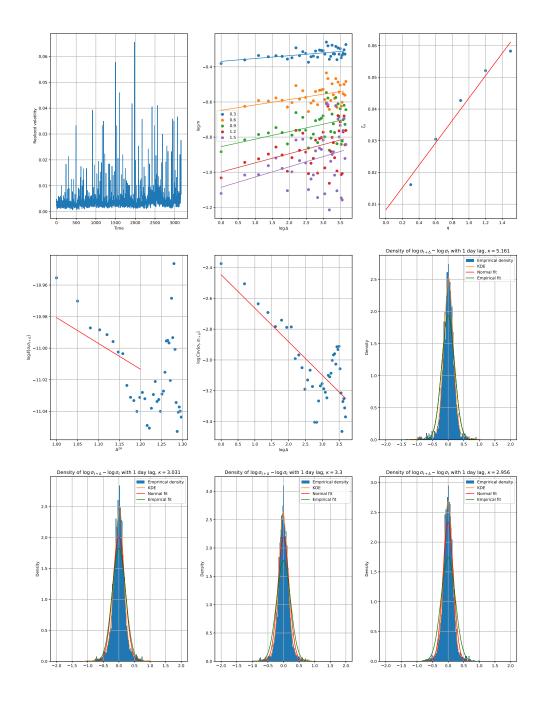


Figure 3.6: LKOD LI Equity

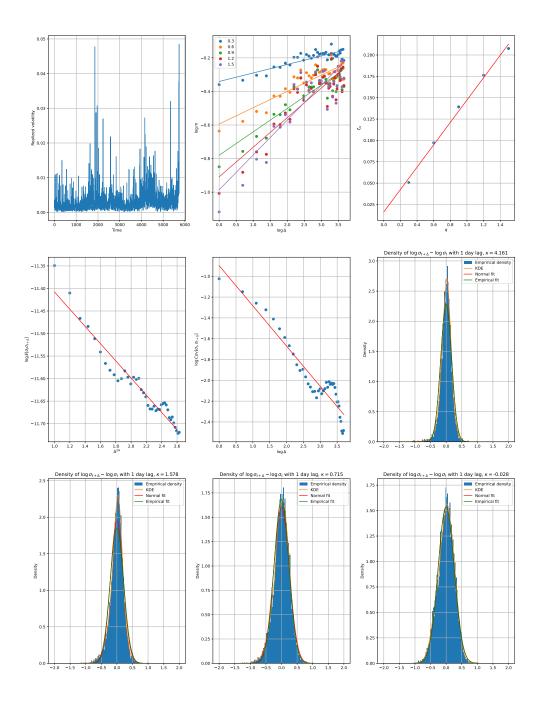


Figure 3.7: GAZP RX Equity

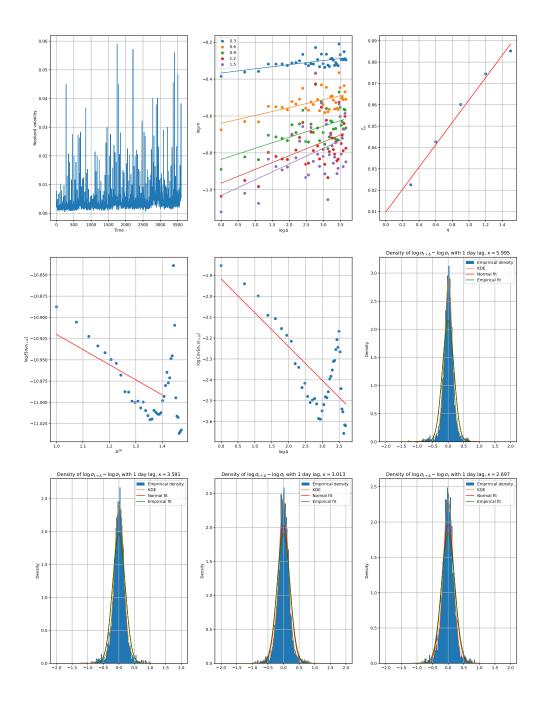


Figure 3.8: OGZD LI Equity

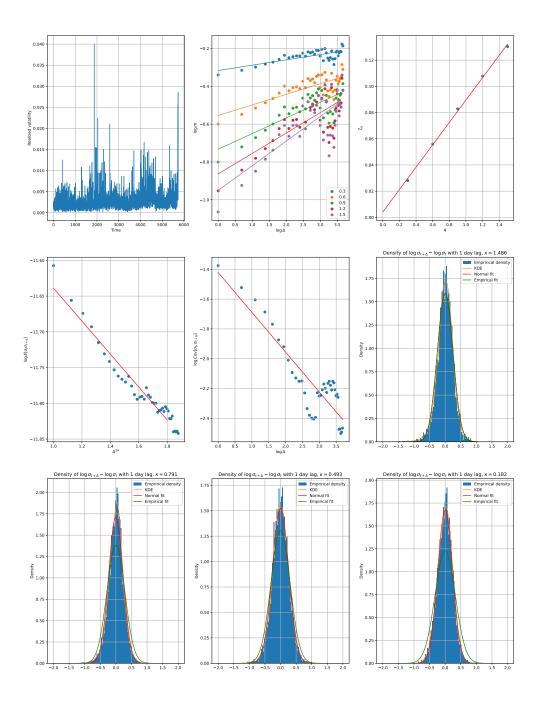


Figure 3.9: MOEX RX Equity

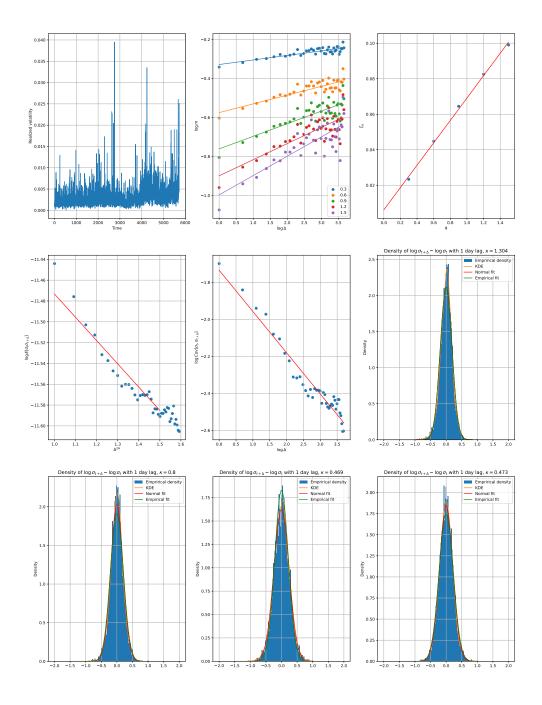


Figure 3.10: FIVE RX Equity

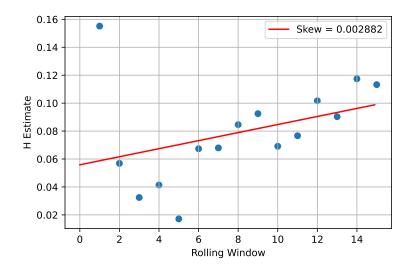


Figure 3.11: SBER RX Equity Smoothing Effect

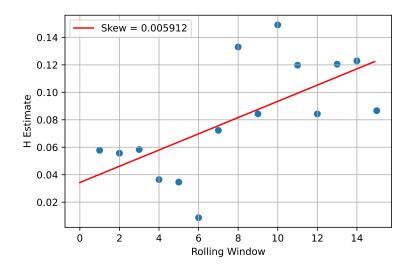


Figure 3.12: SBER LI Equity Smoothing Effect

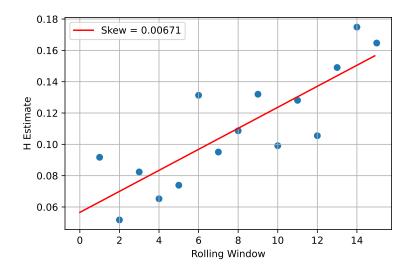


Figure 3.13: VTBR RX Equity Smoothing Effect

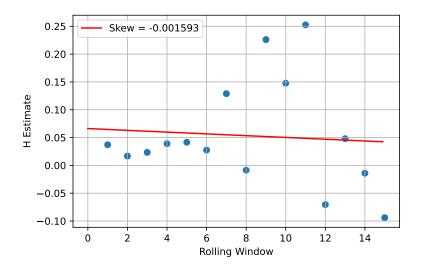


Figure 3.14: VTBR LI Equity Smoothing Effect

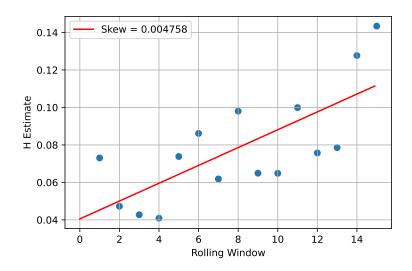


Figure 3.15: LKOH RX Equity Smoothing Effect

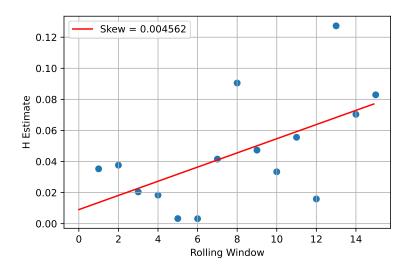


Figure 3.16: LKOD LI Equity Smoothing Effect

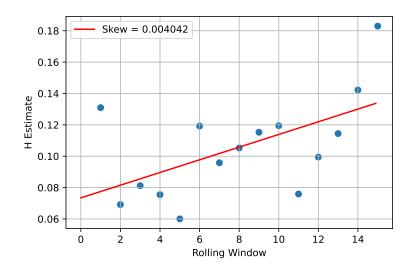


Figure 3.17: GAZP RX Equity Smoothing Effect

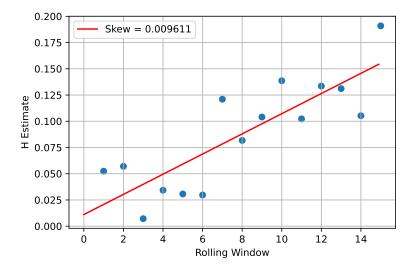


Figure 3.18: OGZD LI Equity Smoothing Effect

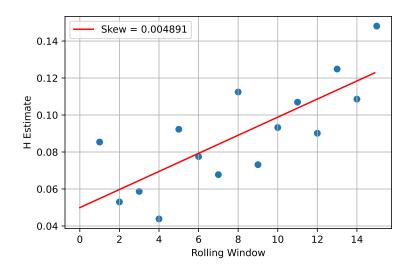


Figure 3.19: MOEX RX Equity Smoothing Effect

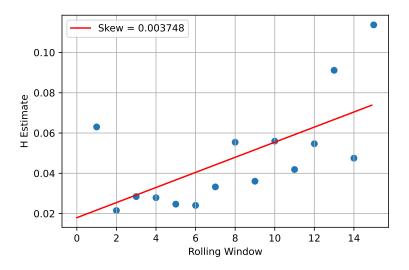


Figure 3.20: FIVE RX Equity Smoothing Effect

1 9.78331E-01 8.521E-29 4.21946E-02 2.374E-92 Not normal 2 9.57221E-01 1.527E-22 2.44650E-02 1.012E-53 Not normal 3 9.91074E-01 1.227E-18 1.66138E-02 8.358E-37 Not normal 4 9.93357E-01 8.959E-16 1.15158E-02 9.587E-26 Not normal 4 9.93357E-01 8.959E-16 1.15158E-02 9.587E-26 Not normal 6 9.97077E-01 3.510E-09 4.01998E-01 8.468E-14 Not normal 7 9.9688E-01 2.150E-09 4.0179ZE-01 2.090E-11 Not normal 8 9.97603E-01 6.943E-08 4.51977E-01 1.333E-10 Not normal 9 9.9784TE-01 3.123E-07 3.43590E-01 3.460E-08 Not normal 1 9.99302E-01 2.198E-02 1.02615E-01 5.91ZE-03 Not normal 1 9.99302E-01 2.198E-02 1.02615E-01 5.91ZE-03 Not normal 1 9.99302E-01 2.198E-02 1.02615E-01 5.91ZE-03 Not normal 1 9.98302E-01 3.325E-04 Not normal 1 9.98302E-01 3.325E-04 1.98332E-01 4.9952E-03 Not normal 1 9.98302E-01 3.325E-04 1.98332E-01 7.46E-06 2.30911E-01 7.445E-07 Not normal 1 9.98578E-01 3.407E-03 1.24075E-01 2.022E-03 Not normal 1 9.98578E-01 3.407E-03 1.24075E-01 2.022E-03 Not normal 1 9.98578E-01 3.347E-03 1.24075E-01 2.022E-03 Not normal 1 9.98578E-01 3.347E-04 1.7385E-01 1.538E-04 Not normal 1 9.98578E-01 3.036E-06 2.25733E-01 1.251E-05 Not normal 1 9.98578E-01 3.036E-06 2.25733E-01 1.251E-05 Not normal 1 9.98578E-01 3.035E-06 1.332E-04 1.332E-01 1.332E-01 1.302E-01 1.3	Δ	Shapiro-Wilk (stat)	Shapiro-Wilk (p-value)	K^2 (stat)	K^2 (p-value)	Conclusion
9,87221E-01	1		- (- /	, ,	(- /	
3 9.91074F-01				·		
4 9.93537E-01 8.950E-16 1.15158E-02 9.857E-26 Not normal 5 9.95637E-01 3.781E-12 7.34235E+01 1.138E-16 Not normal 7 9.96985E-01 2.150E-09 4.91772E-01 2.096E-11 Not normal 7 9.96985E-01 2.150E-09 4.91772E-01 2.096E-11 Not normal 8 9.97603E-01 3.123E-07 3.43590E+01 1.533E-10 Not normal 9 9.97847E-01 3.123E-07 3.43590E+01 3.469E-98 Not normal 11 9.99302E-01 2.198E-02 1.02615E+01 5.912E-03 Not normal 12 9.98813E-01 2.198E-02 1.02615E+01 5.912E-03 Not normal 13 9.98313E-01 3.290E-04 1.98238E-10 4.959E-05 Not normal 14 9.98520E-01 3.258E-05 2.51641E-01 5.912E-03 Not normal 14 9.98520E-01 3.258E-05 2.51641E-10 3.433E-06 Not normal 15 9.9992E-01 3.407E-03 1.24075E+01 2.022E-03 Not normal 16 9.98578E-01 3.407E-03 1.24075E+01 2.022E-03 Not normal 17 9.98762E-01 2.138E-04 1.7388E+01 1.675E-04 Not normal 18 9.98528E-01 2.138E-04 1.7388E+01 1.675E-04 Not normal 19 9.9884E-01 8.096E-06 2.25738E+01 1.254E-05 Not normal 19 9.9884E-01 4.177E-04 1.91251E+01 7.031E-05 Not normal 19 9.98878TE-01 2.632E-04 2.03521E+01 3.807E-05 Not normal 22 9.98509E-01 3.033E-05 2.39327E+01 6.355E-06 Not normal 23 9.99638E-01 3.035E-05 2.39327E+01 6.355E-06 Not normal 24 9.98072E-01 1.391E-06 3.02773E+01 2.633E-07 Not normal 25 9.99638E-01 3.875E-10 6.1347E+01 4.849E-14 Not normal 26 9.99638E-01 3.875E-10 6.1347E+01 4.849E-14 Not normal 27 9.96638E-01 3.875E-10 6.1347E+01 4.849E-14 Not normal 28 9.99638E-01 3.875E-10 6.1347E+01 4.849E-14 Not normal 39 9.9668E-01 3.875E-10 6.1347E+01 4.849E-14 Not normal 39 9.9668E-01 3.285E-07 4.04066F-10 1.682E-09 Not normal 39 9.9668E-01 3.285E-07 3.4066E-10 3.092E-17 Not normal 39 9.96690E-01 3.285E-06 3.032E-01 3.392E-07 Not normal 39 9.96900E-01 3.285E-06 3.03			I .			
5						
6 9.97077F-01 3.510F-09 4.91772E-01 2.096E-11 Not normal 8 9.97603F-01 6.943E-08 4.91772E-01 1.533E-10 Not normal 9 9.97847F-01 3.123E-07 3.43590E-101 3.460F-08 Not normal 10 9.99302E-01 3.123E-07 3.43590E-101 3.450F-08 Not normal 11 9.99302E-01 2.198E-02 1.02615E+01 5.912E-03 Not normal 12 9.98813E-01 3.220E-04 1.98233E-01 7.9658E-01 7.9658E-01 7.9658E-01 7.945E-07 Not normal 13 9.98531E-01 3.220E-04 1.98233E-01 7.945E-07 Not normal 14 9.98520F-01 3.258E-05 2.51641E-101 7.945E-07 Not normal 15 9.9962E-01 3.258E-05 2.51641E-101 3.433F-06 Not normal 16 9.98578E-01 3.258E-05 2.20390E+01 1.638E-05 Not normal 17 9.98762E-01 3.00F-03 1.24075E+01 2.022E-03 Not normal 17 9.98762E-01 5.054E-05 2.20390E+01 1.638E-05 Not normal 18 9.98328E-01 8.030E-06 2.25738E-01 1.254E-05 Not normal 19 9.9884E-01 4.177E-04 1.91251E-01 7.031E-05 Not normal 19 9.9884E-01 4.077E-04 1.91251E-01 7.031E-05 Not normal 19 9.98532E-01 8.030E-06 2.25738E-01 1.254E-05 Not normal 19 9.98532E-01 3.033E-05 2.33327E-01 2.633E-04 Not normal 19 9.9854E-01 4.177E-04 1.91251E-01 7.031E-05 Not normal 19 9.9853E-01 3.033E-05 2.33327E-01 2.633E-06 Not normal 19 9.9853E-01 3.033E-05 2.33327E-01 2.263E-04 2.03521E+01 3.807E-05 Not normal 19 9.9853E-01 3.033E-05 2.33327E-01 2.875E-13 Not normal 22 9.9850E-01 3.033E-05 2.33327E-01 2.263E-07 Not normal 22 9.9850E-01 3.033E-05 2.33327E-01 3.807E-05 Not normal 22 9.9850E-01 3.35E-06 Not normal 24 9.98072E-01 1.331E-06 3.02773E-01 2.2875E-13 Not normal 24 9.98072E-01 1.331E-06 3.02773E-01 2.2875E-13 Not normal 32 9.9563E-01 3.3875E-10 6.13147E+01 4.849E-14 Not normal 27 9.9650E-01 1.33E-07 4.4066E-01 1.63E-09 Not normal 32 9.9563E-01 3.385E-01 6.6325E-01 3.39E-14 Not normal 32 9.9563E-01 1.45E-11 6.6425E-01 4.385E-15 Not normal 32 9.9563E-01 1.35E-01 6.6325E-01 3.332E-01 1.45E-11 6.6425E-01 7.59E-01 1.50E-01 1.99E-12 Not normal 34 9.9586B-01 1.55E-01 3.55E-01 3.39E-14 Not normal 34 9.9586B-01 1.55E-01 3.55E-01 3.39E-14 Not normal 39 9.9590E-01 1.53E-01 5.765E-01 1.50E-01 1.99E-12 Not normal 49 9.9579E-01 1.53E-01 5						
7 9.96985E-01 2.150E-09 4.91772E-101 2.906E-11 Not normal 8 9.97637E-01 6.943E-08 4.51977E+01 1.533E-10 Not normal 10 9.9819E-01 7.683E-04 1.79663E-01 5.912E-03 Not normal 11 9.99302E-01 2.198E-02 1.02615E-101 5.912E-03 Not normal 12 9.98813E-01 3.220E-04 1.98233E-101 5.912E-03 Not normal 13 9.98513E-01 3.250E-05 2.51641E-101 3.33E-06 Not normal 14 9.98520E-01 3.260E-05 2.51641E-101 3.33E-06 Not normal 15 9.99578E-01 3.407E-03 1.24075E-101 1.638E-05 Not normal 16 9.99578E-01 5.564E-05 2.20300E-101 1.638E-05 Not normal 17 9.98762E-01 2.138E-04 1.73885E-101 1.554E-05 Not normal 18 9.9878E-01 4.177E-04 1.9125E-101 7.031E-05 Not normal 20 9.9839E-01 4.67						
8 9.97603E-01 6.943E-08 4.51977E-01 1.533E-10 Not normal 9 9.97847E-01 3.123E-07 3.43590E-01 3.460E-08 Not normal 10 9.98919E-01 7.683E-04 1.79663E-01 1.255E-04 Not normal 11 9.99302E-01 2.198E-02 1.02615E-01 5.912E-03 Not normal 12 9.98313E-01 3.220E-04 1.98236E-01 4.950E-05 Not normal 13 9.98313E-01 7.146E-06 2.80911E-01 7.945E-07 Not normal 14 9.98520E-01 3.258E-05 2.51641E+01 3.333E-06 Not normal 15 9.9902E-01 3.407E-03 1.24075E+01 2.022E-03 Not normal 16 9.98578E-01 3.258E-05 2.51641E+01 3.333E-06 Not normal 16 9.98578E-01 5.054E-05 2.20300E-01 1.638E-05 Not normal 17 9.98762E-01 2.138E-04 1.73885E-01 1.565E-05 Not normal 18 9.98328E-01 8.030E-06 2.25733E-01 1.254E-05 Not normal 19 9.98844E-01 4.177E-04 1.91251E-01 7.031E-05 Not normal 19 9.9884E-01 8.695E-04 1.94969E-01 5.538E-05 Not normal 21 9.98787E-01 2.632E-04 2.03521E-01 3.807E-05 Not normal 22 9.98509E-01 3.033E-05 2.39327E-01 3.807E-05 Not normal 24 9.98509E-01 3.033E-05 2.39327E-01 1.561E-0 Not normal 24 9.98072E-01 1.391E-06 3.02773E-01 2.663E-07 Not normal 24 9.98072E-01 1.391E-06 3.02773E-01 2.663E-07 Not normal 25 9.96689E-01 3.875E-10 6.13147E-01 4.549E-11 Not normal 27 9.996502E-01 1.398E-08 4.51613E-01 4.549E-11 Not normal 28 9.99639E-01 3.875E-10 6.13147E-01 4.549E-11 Not normal 29 9.97702E-01 1.328E-09 4.04066E-01 1.682E-09 Not normal 29 9.97702E-01 1.328E-07 4.04066E-01 1.682E-09 Not normal 30 9.98864E-01 1.220E-09 5.6312E-01 5.914E-13 Not normal 30 9.9984E-01 1.144E-11 6.24651E-01 2.272E-14 Not normal 31 9.9648E-01 1.156E-11 6.6322E-01 5.914E-13 Not normal 31 9.9648E-01 1.156E-01 1.56E-01 1.33E-07 4.04066E-01 1.682E-09 Not normal 31 9.9648E-01 1.55E-01 6.58779E-01 2.272E-14 Not normal 39 9.9980E-01 1.144E-11 6.24651E-01 2.204E-14 Not normal 39 9.9980E-01 1.144E-11 6.24651E-01 2.204E-14 Not normal 39 9.9980E-01 1.144E-11 6.930E-15 Not normal 39 9.9980E-01 1.144E-11 6.930E-16 Not normal 39 9.9980E-01 1.144E-11 6.24651E-01 2.204E-14 Not normal 39 9.9980E-01 1.144E-11 6.930E-16 Not normal 39 9.9980E-01 1.144E-11 6.930E-16 Not normal 39 9.9	1		I .			
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11 9.99302E-01 2.198E-02 1.02615F+01 5.912E-03 Not normal 12 9.9813F-01 3.220E-04 1.9823B+01 4.959E-05 Not normal 13 9.98313E-01 7.146E-06 2.80911E+01 7.945E-07 Not normal 14 9.98520E-01 3.258E-05 2.51611E+01 3.433E-06 Not normal 15 9.99092E-01 3.407E-03 1.24075E+01 2.022E-03 Not normal 16 9.98578E-01 5.054E-05 2.20390E+01 1.638E-05 Not normal 17 9.98762E-01 2.138E-04 1.73885E+01 1.254E-05 Not normal 18 9.98328E-01 8.030E-06 2.25733E+01 1.254E-05 Not normal 19 9.9884E-01 4.177E-04 1.91251E+01 7.031E-05 Not normal 19 9.9884E-01 4.177E-04 1.91251E+01 7.031E-05 Not normal 19 9.98878E-01 8.695E-04 1.94969E+01 3.807E-05 Not normal 20 9.98932E-01 8.695E-04 1.94969E+01 3.807E-05 Not normal 21 9.9878TE-01 2.632E-04 2.03521E+101 3.807E-05 Not normal 22 9.98509E-01 3.033E-05 2.39327E+01 6.355E-06 Not normal 23 9.97368E-01 1.828E-08 4.51613E+01 1.561E-10 Not normal 24 9.98072E-01 1.391E-06 3.02773E+01 2.663E-07 Not normal 25 9.96688E-01 4.922E-10 5.77549E+01 2.875E-13 Not normal 25 9.96688E-01 4.922E-10 5.77549E+01 2.875E-13 Not normal 28 9.95934E-01 1.38E-07 4.0466E+01 4.881E-15 Not normal 29 9.97702E-01 1.328E-07 4.0466E+01 4.682E-09 Not normal 29 9.97702E-01 1.328E-07 4.0466E+01 4.682E-09 Not normal 31 9.96448E-01 1.250E-09 5.63125E+01 3.398E-14 Not normal 39 9.98861E-01 1.249E-10 5.74359E+01 4.952E-15 Not normal 39 9.9886E-01 1.249E-10 5.74359E+01 4.952E-15 Not normal 39 9.9860E-01 1.145E-11 6.24651E+01 2.728E-11 Not normal 39 9.99600E-01 1.328E-07 4.0466E+01 2.280E-14 Not normal 39 9.99600E-01 1.438E-10 5.74359E+01 3.092E-17 Not normal 39 9.99600E-01 1.438E-01 5.74359E+01 3.092E-17 Not normal 39 9.99600E-01 1.438E-01 5.74359E+01 3.092E-11 Not normal 39 9.99600E-01 1.438	10					
13	11			1.02615E+01	5.912E-03	
14	12	9.98813E-01	3.220E-04	1.98233E+01	4.959E-05	Not normal
15	13	9.98313E-01	7.146E-06	2.80911E+01	7.945E-07	Not normal
16	14	9.98520E-01	3.258E-05	2.51641E+01	3.433E-06	Not normal
17	15	9.99092E-01	3.407E-03	1.24075E+01	2.022E-03	Not normal
18	16	9.98578E-01	5.054E-05	2.20390E + 01	1.638E-05	Not normal
18	17	9.98762E-01	2.138E-04	1.73885E+01	1.675E-04	Not normal
20 9.98932E-01 8.695E-04 1.94969E+01 5.838E-05 Not normal 21 9.98787E-01 2.632E-04 2.03521E+01 3.807E-05 Not normal 22 9.98509E-01 3.033E-05 2.39327E+01 6.355E-06 Not normal 23 9.97368E-01 1.828E-08 4.51613E+01 1.561E-10 Not normal 24 9.98072E-01 1.391E-06 3.02773E+01 2.663E-07 Not normal 25 9.96688E-01 4.922E-10 5.77549E+01 2.875E-13 Not normal 26 9.96639E-01 3.875E-10 6.13147E+01 4.849E-14 Not normal 27 9.96502E-01 1.986E-10 6.18355E+01 3.738E-14 Not normal 28 9.95934E-01 1.454E-11 6.61228E+01 4.381E-15 Not normal 30 9.9686E-01 1.220E-09 5.63125E+01 5.914E-13 Not normal 30 9.96864E-01 1.220E-09 5.63125E+01 5.914E-13 Not normal 31 9.96448E-01 1.557E-10 6.58779E+01 4.952E-15 Not normal 32 9.95876E-01 1.144E-11 6.24651E+01 2.728E-14 Not normal 33 9.95495E-01 2.278E-12 7.60255E+01 3.099E-17 Not normal 34 9.95883E-01 1.185E-11 6.93021E+01 8.938E-16 Not normal 35 9.95461E-01 1.994E-12 7.52112E+01 4.657E-17 Not normal 37 9.95461E-01 1.994E-12 6.24106E+01 2.804E-14 Not normal 37 9.96425E-01 1.413E-10 5.74359E+01 3.372E-13 Not normal 38 9.97254E-01 1.001E-08 4.73976E+01 3.372E-13 Not normal 39 9.96900E-01 1.506E-09 5.13868E+01 5.102E-11 Not normal 40 9.98060E-01 1.332E-06 2.81409E+01 7.750E-07 Not normal 41 9.97998E-01 8.867E-07 3.33027E+01 5.867E-08 Not normal 42 9.97776E-01 2.150E-07 4.06532E+01 1.437E-09 Not normal 44 9.98152E-01 2.478E-06 3.04860E+01 2.399E-07 Not normal 44 9.98152E-01 2.478E-06 3.04860E+01 2.399E-07 Not normal 44 9.98152E-01 2.350E-06 3.04860E+01 3.815E-07 Not normal 45 9.98049E-01 7.383E-06 3.04860E+01 3.815E-07 Not normal 46 9.9847E-01 2.150E-05 2.85055E+01 4.451E-07 Not normal 47 9.9847E-01 2.07E-07 4.48911E+01 1.787E-10 Not normal 49 9.98279E-01	18	9.98328E-01	8.030E-06	2.25733E+01	1.254E-05	
20 9.98932E-01 8.695E-04 1.94969E+01 5.838E-05 Not normal 21 9.98787E-01 2.632E-04 2.03521E+01 3.807E-05 Not normal 22 9.98509E-01 3.033E-05 2.39327E+01 6.355E-06 Not normal 23 9.97368E-01 1.828E-08 4.51613E+01 1.561E-10 Not normal 24 9.98072E-01 1.391E-06 3.02773E+01 2.663E-07 Not normal 25 9.96688E-01 4.922E-10 5.77549E+01 2.875E-13 Not normal 26 9.96639E-01 3.875E-10 6.13147E+01 4.849E-14 Not normal 27 9.96502E-01 1.986E-10 6.18355E+01 3.738E-14 Not normal 28 9.995934E-01 1.454E-11 6.61228E+01 4.381E-15 Not normal 30 9.96864E-01 1.220E-09 5.63125E+01 5.94E-13 Not normal 31 9.96488E-01 1.220E-09 5.63125E+01 5.94E-13 Not normal 32 9.95876E-01 1.144E-11 6.24651E+01 2.728E-14 Not normal 32 9.95876E-01 1.144E-11 6.24651E+01 2.728E-14 Not normal 34 9.95883E-01 1.185E-11 6.93021E+01 8.938E-16 Not normal 35 9.95461E-01 1.994E-12 7.60255E+01 3.372E-13 Not normal 37 9.96425E-01 1.413E-10 5.74359E+01 3.372E-13 Not normal 38 9.97254E-01 1.4016-08 4.73976E+01 5.102E-11 Not normal 39 9.96900E-01 1.332E-06 2.81409E+01 5.102E-11 Not normal 40 9.98060E-01 1.332E-06 2.81409E+01 5.102E-11 Not normal 41 9.97998E-01 2.478E-06 3.04860E+01 2.399E-07 Not normal 42 9.97776E-01 2.150E-07 4.06532E+01 1.437E-09 Not normal 44 9.98752E-01 2.150E-07 4.06532E+01 3.872E-09 Not normal 44 9.98752E-01 2.150E-07 3.31453E+01 5.168E-09 Not normal 44 9.98752E-01 2.150E-07 3.31453E+01 3.872E-0 Not normal 45 9.98049E-01 7.383E-06 3.81656E+01 5.158E-09 Not normal 46 9.9847E-01 2.150E-05 2.85055E+01 4.787E-09 Not normal 47 9.9847E-01 2.150E-05 2.85055E+01 4.787E-09 Not normal 48 9.97762E-01 2.32E-06 3.81656E+01 5.158E-09 Not normal 50 9.98048E-01 2.007E-07 4.48911E+01 1.787E-10 Not normal 51 9.99077E-01	19	9.98844E-01	4.177E-04	1.91251E+01	7.031E-05	Not normal
22 9.98509E-01 3.033E-05 2.39327E+01 6.355E-06 Not normal 23 9.97368E-01 1.828E-08 4.51613E+01 1.561E-10 Not normal 24 9.98072E-01 1.391E-06 3.02773E+01 2.663E-07 Not normal 25 9.96688E-01 4.922E-10 5.77549E+01 2.875E-13 Not normal 26 9.96630E-01 3.875E-10 6.13147E+01 4.849E-14 Not normal 27 9.96502E-01 1.986E-10 6.18355E+01 3.738E-14 Not normal 28 9.95934E-01 1.454E-11 6.61228E+01 4.381E-15 Not normal 29 9.97702E-01 1.328E-07 4.04066E+01 1.682E-09 Not normal 30 9.96864E-01 1.220E-09 5.63125E+01 5.914E-13 Not normal 31 9.96448E-01 1.557E-10 6.58779E+01 4.952E-15 Not normal 32 9.95876E-01 1.144E-11 6.24651E+01 2.728E-14 Not normal 34 9.95883E-01 1.185	20	9.98932E-01	8.695E-04	1.94969E+01	5.838E-05	Not normal
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58 9.97703E-01 1.422E-07 29 4.31248E+01 4.321E-10 Not normal	56	9.96486E-01	2.004E-10	6.74246E + 01	2.285E-15	Not normal
	57	9.96904E-01	1.613E-09	6.18092E + 01	3.787E-14	Not normal
59 9.98550E-01 4.415E-05 2.18348E+01 1.814E-05 Not normal	58	9.97703E-01	1.422E-07 29	4.31248E+01	4.321E-10	Not normal
	59	9.98550E-01	4.415E-05	2.18348E+01	1.814E-05	Not normal

Table 3.1: Normality tests for YNDX RX Equity

Δ	Shapiro-Wilk (stat)	Shapiro-Wilk (p-value)	K^2 (stat)	K^2 (p-value)	Conclusion
1	9.86685E-01	7.644E-04	1.98534E+01	4.885E-05	Not normal
2	9.95955E-01	3.727E-01	3.55025E-01	8.374E-01	Normal
3	9.86980E-01	9.517E-04	9.61101E+00	8.185E-03	Not normal
4	9.90975E-01	1.301E-02	8.45942E+00	1.456E-02	Not normal
5	9.84146E-01	1.834E-04	1.36903E+01	1.065E-03	Not normal
6	9.92491E-01	3.778E-02	8.49787E+00	1.428E-02	Not normal
7	9.96396E-01	4.906E-01	4.66954E-01	7.918E-01	Normal
8	9.91954E-01	2.676E-02	7.31329E+00	2.582E-02	Not normal
9	9.96991E-01	6.615E-01	1.12020E+00	5.712E-01	Normal
10	9.90804E-01	1.261E-02	8.82026E+00	1.215E-02	Not normal
11	9.91761E-01	2.436E-02	2.62911E+00	2.686E-01	Normal
12	9.91065E-01	1.545E-02	7.01541E+00	2.997E-02	Not normal
13	9.94625E-01	1.728E-01	3.80813E+00	1.490E-01	Normal
14	9.96472E-01	5.255E-01	2.86382E+00	2.389E-01	Normal
15	9.95223E-01	2.573E-01	3.25673E+00	1.963E-01	Normal
16	9.84067E-01	2.221E-04	1.18809E+01	2.631E-03	Not normal
17	9.93024E-01	6.157E-02	6.53451E+00	3.811E-02	Normal
18	9.93439E-01	8.224E-02	4.07708E+00	1.302E-01	Normal
19	9.80720E-01	3.933E-05	2.19041E+01	1.752E-05	Not normal
20	9.87062E-01	1.376E-03	1.08698E+01	4.362E-03	Not normal
21	9.93908E-01	1.156E-01	3.20334E+00	2.016E-01	Normal
22	9.97348E-01	7.839E-01	2.29193E-01	8.917E-01	Normal
23	9.97145E-01	7.309E-01	3.81776E-01	8.262E-01	Normal
24	9.87137E-01	1.552E-03	1.11372E+01	3.816E-03	Not normal
25	9.95266E-01	2.824E-01	1.75112E+00	4.166E-01	Normal
26	9.95593E-01	3.446E-01	1.92367E+00	3.822E-01	Normal
27	9.97643E-01	8.627E-01	1.24791E+00	5.358E-01	Normal
28	9.92456E-01	4.784E-02	5.24644E+00	7.257E-02	Normal
29	9.92096E-01	3.828E-02	5.55830E+00	6.209E-02	Normal
30	9.97080E-01	7.258E-01	1.07999E+00	5.828E-01	Normal
31	9.95658E-01	3.681E-01	2.54691E+00	2.799E-01	Normal
32	9.92602E-01	5.516E-02	4.17454E+00	1.240E-01	Normal
33	9.92369E-01	4.799E-02	5.21403E+00	7.375E-02	Normal
34	9.94686E-01	2.118E-01	3.10393E+00	2.118E-01	Normal
35	9.91953E-01	3.761E-02	3.60564E+00	1.648E-01	Normal
36	9.89736E- 01	9.362E-03	6.53296E + 00	3.814E-02	Not normal
37	9.93021E-01	7.643E-02	6.33168E+00	4.218E-02	Normal
38	9.93998E-01	1.432E-01	5.68401E+00	5.831E-02	Normal
39	9.87762E-01	2.974E-03	1.14586E+01	3.249E-03	Not normal
40	9.92452E-01	5.502E-02	4.87885E+00	8.721E-02	Normal
41	9.95051E-01	2.772E-01	1.96688E+00	3.740E-01	Normal
42	9.95197E-01	3.035E-01	1.93721E+00	3.796E-01	Normal
43	9.90776E-01	1.990E-02	7.25416E+00	2.659E-02	Not normal
44	9.94070E-01	1.581E-01	3.04162E+00	2.185E-01	Normal
45	9.94462E-01	2.020E-01	1.97091E+00	3.733E-01	Normal
46	9.95183E-01	3.091E-01	2.74301E+00	2.537E-01	Normal
47	9.93052E-01	8.683E-02	4.84832E+00	8.855E-02	Normal
48	9.94892E-01	2.659E-01	3.67560E+00	1.592E-01	Normal
49	9.95834E-01	4.456E-01	1.54201E+00	4.625E-01	Normal
50	9.95213E-01	3.227E-01	2.13198E+00	3.444E-01	Normal
51	9.89772E-01	1.214E-02	6.72963E+00	3.457E-02	Not normal
52	9.93507E-01	1.209E-01	4.33200E+00	1.146E-01	Normal
53	9.95736E-01	4.332E-01	1.13034E+00	5.683E-01	Normal
54	9.95964E-01	4.872E-01	8.98775E-01	6.380E-01	Normal
55	9.94962E-01	2.906E-01	2.35505E+00	3.080E-01	Normal
56	9.92687E-01	7.667E-02	3.61105E+00	1.644E-01	Normal
57	9.92730E-01	7.958E-02	3.39186E+00	1.834E-01	Normal
58	9.96720E-01	6.852E-01 30		4.862E-01	Normal
59	9.90870E-01	2.652E-02	3.97314E+00	1.372E-01	Normal

Table 3.2: Normality tests for SBER RX Equity

Δ	Shapiro-Wilk (stat)	Shapiro-Wilk (p-value)	K^2 (stat)	K^2 (p-value)	Conclusion
1	9.65738E-01	7.232E-35	7.35050E+02	2.432E-160	Not normal
$\frac{1}{2}$	9.71389E-01	2.284E-32	6.49920E+02	7.440E-142	Not normal
3	9.79383E-01	4.481E-28	4.23467E+02	1.110E-92	Not normal
4	9.84988E-01	3.171E-24	3.30597E+02	1.628E-72	Not normal
5	9.85583E-01	9.374E-24	3.61521E+02	3.138E-79	Not normal
6	9.89094E-01	1.194E-20	2.07574E+02	8.430E-46	Not normal
7	9.88989E-01	9.445E-21	2.07974E+02 2.15389E+02	1.694E-47	Not normal
8	9.92174E-01	2.928E-17	1.53824E+02	3.960E-34	Not normal
9	9.93036E-01	3.810E-16	1.49945E+02	2.754E-33	Not normal
10	9.94618E-01	7.853E-14	1.16543E+02	4.932E-26	Not normal
11	9.97350E-01	1.758E-08	5.17100E+01	5.906E-12	Not normal
12	9.95967E-01	1.756E-05 1.801E-11	8.29198E+01	9.867E-19	Not normal
13	9.96077E-01	2.950E-11	8.25761E+01	1.172E-18	Not normal
14	9.96054E-01	2.665E-11	7.90164E+01	6.947E-18	Not normal
15	9.90034E-01 9.97548E-01				Not normal
		5.559E-08	4.81896E+01	3.434E-11	
16	9.97226E-01	8.895E-09	5.08659E+01	9.007E-12	Not normal
17	9.98737E-01	1.866E-04	1.92402E+01	6.638E-05	Not normal
18	9.98414E-01	1.600E-05	2.86373E+01	6.046E-07	Not normal
19	9.99264E-01	1.642E-02	7.99361E+00	1.837E-02	Not normal
20	9.98622E-01	7.653E-05	1.74282E+01	1.643E-04	Not normal
21	9.98114E-01	1.984E-06	2.40289E+01	6.056E-06	Not normal
22	9.98424E-01	1.737E-05	1.73494E+01	1.709E-04	Not normal
23	9.99005E-01	1.703E-03	8.00492E+00	1.827E-02	Not normal
24	9.99050E-01	2.512E-03	9.11081E+00	1.051E-02	Not normal
25	9.98603E-01	6.657E-05	1.57325E+01	3.835E-04	Not normal
26	9.98893E-01	6.675E-04	8.89888E+00	1.169E-02	Not normal
27	9.99189E-01	8.530E-03	9.28383E+00	9.639E-03	Not normal
28	9.99264E-01	1.658E-02	5.41437E+00	6.672 E-02	Normal
29	9.99255 E-01	1.523E-02	5.62308E+00	6.011E-02	Normal
30	9.99415E-01	6.361E-02	5.14056E+00	7.651E-02	Normal
31	9.99631E- 01	3.774E-01	2.60396E+00	2.720E-01	Normal
32	9.99790E-01	8.805E-01	6.81491E-01	7.112E-01	Normal
33	9.99692 E-01	5.652E-01	3.60012E+00	1.653E-01	Normal
34	9.99200E-01	9.473E-03	4.29943E+00	1.165E-01	Normal
35	9.99333E-01	3.091E-02	2.46657E+00	2.913E-01	Normal
36	9.98552E-01	4.608E-05	$1.67350E{+}01$	2.323E-04	Not normal
37	9.98926E-01	8.949E-04	7.13522E+00	2.822E-02	Not normal
38	9.98399E-01	1.496E-05	1.43961E + 01	7.481E-04	Not normal
39	9.98416E-01	1.696E-05	2.45176E + 01	4.743E-06	Not normal
40	9.98278E-01	6.341E-06	2.15475E + 01	2.094 E-05	Not normal
41	9.97137E-01	5.840E-09	5.18449E+01	5.521E-12	Not normal
42	9.97576E-01	6.999E-08	4.07611E+01	1.409E-09	Not normal
43	9.98056E-01	1.409E-06	2.66872E + 01	1.603E-06	Not normal
44	9.97798E-01	2.705E-07	3.80213E+01	5.543E-09	Not normal
45	9.95813E-01	1.015E-11	7.62067E + 01	2.831E-17	Not normal
46	9.95736E-01	7.323E-12	8.19944E+01	1.567E-18	Not normal
47	9.95476E-01	2.481E-12	9.05709E+01	2.152E-20	Not normal
48	9.95270E-01	1.079E-12	8.31723E+01	8.697E-19	Not normal
49	9.95130E-01	6.226E-13	8.16565E+01	1.856E-18	Not normal
50	9.95059E-01	4.745E-13	1.05254E+02	1.394E-23	Not normal
51	9.93513E-01	2.006E-15	1.12343E+02	4.028E-25	Not normal
52	9.93973E-01	9.279E-15	1.06167E+02	8.832E-24	Not normal
53	9.93427E-01	1.532E-15	1.17624E+02	2.872E-26	Not normal
54	9.93920E-01	7.801E-15	1.05594E+02	1.176E-23	Not normal
55	9.92566E-01	1.091E-16	1.38829E+02	7.141E-31	Not normal
56	9.91137E-01	2.083E-18	1.73103E+02	2.577E-38	Not normal
57	9.91137E-01 9.92097E-01	2.834E-17	1.75103E+02 1.55193E+02	2.577E-38 1.996E-34	Not normal
58	9.92097E-01 9.90628E-01			7.501E-45	Not normal
59					
59	9.91455E-01	4.888E-18	1.80089E+02	7.837E-40	Not normal

Table 3.3: Normality tests for VTBR RX Equity

Δ	Shapiro-Wilk (stat)	Shapiro-Wilk (p-value)	K^2 (stat)	K^2 (p-value)	Conclusion
1	9.86253E-01	3.280E-23	2.96230E+02	4.727E-65	Not normal
$\frac{1}{2}$	9.87673E-01	5.518E-22	2.53330E+02	9.773E-56	Not normal
3	9.89920E-01	8.135E-20	2.08311E+02	5.833E-46	Not normal
4	9.91729E-01	8.373E-18	1.65629E+02	1.082E-36	Not normal
5	9.94132E-01	1.375E-14	1.14501E+02	1.369E-25	Not normal
6	9.95203E-01	7.309E-13	9.26978E+01	7.429E-21	Not normal
7	9.95254E-01	8.981E-13	9.56711E+01	1.680E-21	Not normal
8	9.95090E-01	4.712E-13	1.09261E+02	1.880E-24	Not normal
9	9.96455E-01	1.692E-10	7.12182E+01	3.429E-16	Not normal
10	9.97602E-01	7.606E-08	4.66476E+01	7.423E-11	Not normal
11	9.97015E-01	2.845E-09	5.45817E+01	1.405E-12	Not normal
12	9.97146E-01	5.737E-09	6.12382E+01	5.038E-14	Not normal
13	9.97251E-01	1.025E-08	5.76060E+01	3.098E-13	Not normal
14	9.97845E-01	3.422E-07	4.35574E+01	3.480E-10	Not normal
15	9.97003E-01	2.699E-09	5.72794E+01	3.647E-13	Not normal
16	9.97793E-01	2.485E-07	4.14855E+01	9.807E-10	Not normal
17	9.97878E-01	4.243E-07	3.81333E+01	5.242E-09	Not normal
18	9.98191E-01	3.337E-06	3.21994E+01	1.019E-07	Not normal
19	9.98892E-01	6.580E-04	1.61855E+01	3.057E-04	Not normal
20	9.98923E-01	8.542E-04	1.01833E+01 1.16782E+01	2.911E-03	Not normal
21	9.98554E-01	4.585E-05	1.98113E+01	4.989E-05	Not normal
22	9.99001E-01	1.655E-03	1.57101E+01	3.878E-04	Not normal
23	9.98733E-01	1.840E-04	1.98965E+01	4.781E-05	Not normal
$\frac{23}{24}$	9.98817E-01	3.600E-04	1.98905E+01 1.92406E+01	6.637E-05	Not normal
25	9.98035E-01	1.186E-06	3.38480E+01	4.467E-08	Not normal
$\frac{25}{26}$	9.98353E-01	1.059E-05	2.56078E+01	2.750E-06	Not normal
27	9.98983E-01	1.435E-03	2.30078E + 01 1.35009E + 01	1.170E-03	Not normal
28	9.99120E-01	4.648E-03	1.53009E+01 1.53126E+01	4.731E-04	Not normal
29	9.98133E-01	2.303E-06	3.41161E+01	3.906E-08	Not normal
30	9.98871E-01	5.665E-04	1.91141E+01	7.070E-05	Not normal
31	9.98862E-01	5.234E-04	2.15337E+01	2.109E-05	Not normal
32	9.99436E-01	7.651E-02	9.07413E+00	1.070E-02	Normal
33	9.99371E-01	4.320E-02	1.00014E+01	6.733E-03	Not normal
34	9.99260E-01	1.615E-02	1.26737E+01	1.770E-03	Not normal
35	9.99227E-01	1.199E-02	7.20330E+00	2.728E-02	Not normal
36	9.98581E-01	5.747E-05	2.84615E+01	6.602E-07	Not normal
37	9.97641E-01	1.025E-07	$\frac{2.64619E+01}{4.68187E+01}$	6.815E-11	Not normal
38	9.96837E-01	1.209E-09	6.58118E+01	5.119E-15	Not normal
39	9.98318E-01	8.449E-06	2.93353E+01	4.265E-07	Not normal
40	9.97480E-01	4.005E-08	5.20385E+01	5.012E-12	Not normal
41	9.98181E-01	3.278E-06	3.50333E+01	2.470E-08	Not normal
42	9.98010E-01	1.050E-06	3.76342E+01	6.727E-09	Not normal
43	9.98705E-01	1.522E-04	2.39758E+01	6.219E-06	Not normal
44	9.98891E-01	6.788E-04	2.05627E+01	3.427E-05	Not normal
45	9.97689E-01	1.401E-07	2.03027E+01 4.19281E+01	7.860E-10	Not normal
46	9.98266E-01	5.947E-06	$\frac{4.19281E+01}{3.34811E+01}$	5.366E-08	Not normal
47	9.98035E-01	1.243E-06	3.95202E+01	2.620E-09	Not normal
48	9.97928E-01	6.234E-07	3.93202E+01 3.81473E+01	5.205E-09	Not normal
49	9.98907E-01	7.801E-04	1.76200E+01	1.492E-04	Not normal
50	9.98907E-01 9.97873E-01	4.424E-07	3.74600E+01	7.340E-09	Not normal
51	9.98151E-01	2.733E-06	3.36607E+01	4.905E-08	Not normal
52	9.97664E-01	2.735E-00 1.221E-07	4.45885E+01	4.905E-08 2.078E-10	Not normal
53					Not normal Not normal
54	9.97972E-01	8.384E-07	4.12269E+01	1.116E-09	
55	9.98835E-01	4.359E-04	2.00120E+01	4.513E-05	Not normal
	9.97866E-01	4.264E-07	4.09711E+01	1.268E-09	Not normal
56	9.97252E-01	1.145E-08	5.88577E+01	1.657E-13	Not normal
57	9.97594E-01	8.122E-08	4.41337E+01	2.609E-10	Not normal
58	9.95888E-01	1.476E-11 32		5.627E-20	Not normal
59	9.96174E-01	5.293E-11	7.54012E+01	4.235E-17	Not normal

Table 3.4: Normality tests for MOEX RX Equity

Δ	Shapiro-Wilk (stat)	Shapiro-Wilk (p-value)	K^2 (stat)	K^2 (p-value)	Conclusion
1	9.68911E-01	1.660E-33	7.20790E+02	3.037E-157	Not normal
2	9.71463E-01	2.492E-32	5.90572E+02	5.739E-129	Not normal
3	9.75711E-01	3.532E-30	4.26724E+02	2.178E-93	Not normal
4	9.79322E-01	4.153E-28	4.19047E+02	1.012E-91	Not normal
5	9.84734E-01	2.041E-24	3.13716E+02	7.542E-69	Not normal
6	9.86408E-01	4.474E-23	2.89088E+02	1.680E-63	Not normal
7	9.90080E-01	1.203E-19	2.01964E+02	1.393E-44	Not normal
8	9.91266E-01	2.421E-18	2.06180E+02	1.693E-45	Not normal
9	9.91447E-01	3.940E-18	1.84416E+02	9.009E-41	Not normal
10	9.89510E-01	3.160E-20	2.35492E+02	7.305E-52	Not normal
11	9.94163E-01	1.554E-14	1.24524E+02	9.121E-28	Not normal
12	9.93787E-01	4.326E-15	1.46109E+02	1.875E-32	Not normal
13	9.93911E-01	6.571E-15	1.38988E+02	6.595E-31	Not normal
14	9.93950E-01	7.543E-15	1.46965E + 02	1.222E-32	Not normal
15	9.93708E-01	3.355E-15	1.37426E+02	1.440E-30	Not normal
16	9.95751E-01	7.134E-12	9.03277E+01	2.430E-20	Not normal
17	9.96952E-01	2.065E-09	5.74098E+01	3.417E-13	Not normal
18	9.96794E-01	9.177E-10	6.44851E+01	9.937E-15	Not normal
19	9.97277E-01	1.193E-08	4.13211E+01	1.065E-09	Not normal
20	9.96615E-01	3.774E-10	5.59601E+01	7.054E-13	Not normal
21	9.97329E-01	1.602E-08	3.70555E+01	8.985E-09	Not normal
22	9.97721E-01	1.600E-07	3.96039E+01	2.513E-09	Not normal
23	9.97719E-01	1.591E-07	3.68208E+01	1.010E-08	Not normal
24	9.97401E-01	2.431E-08	3.82352E+01	4.981E-09	Not normal
25	9.96982E-01	2.463E-09	5.46063E+01	1.388E-12	Not normal
26	9.96995E-01	2.649E-09	5.77449E+01	2.890E-13	Not normal
27	9.97392E-01	2.321E-08	4.11806E+01	1.142E-09	Not normal
28	9.97077E-01	4.101E-09	5.16604E+01	6.055E-12	Not normal
29	9.97912E-01	5.382E-07	3.21822E+01	1.027E-07	Not normal
30	9.97734E-01	1.764E-07	$3.65232E{+01}$	1.172E-08	Not normal
31	9.97191E-01	7.662E-09	$4.69101\mathrm{E}{+01}$	6.510E-11	Not normal
32	9.98501E-01	3.134E-05	$2.15089\mathrm{E}{+01}$	2.135E-05	Not normal
33	9.98792E-01	2.966E-04	1.40109E+01	9.069E-04	Not normal
34	9.98960E-01	1.192E-03	1.15583E+01	3.091E-03	Not normal
35	9.98922E-01	8.686E-04	1.34568E+01	1.196E-03	Not normal
36	9.98049E-01	1.331E-06	3.33640E+01	5.690E-08	Not normal
37	9.98014E-01	1.060E-06	3.78066E+01	6.172 E-09	Not normal
38	9.98013E-01	1.054E-06	3.41280E+01	3.883E-08	Not normal
39	9.96742E-01	7.485E-10	$6.64146\mathrm{E}{+01}$	3.787E-15	Not normal
40	9.96384E-01	1.313E-10	6.64622E + 01	3.698E-15	Not normal
41	9.95934E-01	1.702E-11	8.70810E+01	1.232E-19	Not normal
42	9.96809E-01	1.053E-09	6.08614E+01	6.083E-14	Not normal
43	9.96112E-01	3.782E-11	7.46695E+01	6.106E-17	Not normal
44	9.96157E-01	4.657E-11	7.53412E+01	4.364E-17	Not normal
45	9.96278E-01	8.128E-11	7.58787E+01	3.335E-17	Not normal
46	9.95567E-01	3.604E-12	8.10987E+01	2.453E-18	Not normal
47	9.94378E-01	3.751E-14	1.08925E+02	2.224E-24	Not normal
48	9.94402E-01	4.100E-14	1.13494E+02	2.265E-25	Not normal
49	9.94118E-01	1.516E-14	1.08391E+02	2.905E-24	Not normal
50	9.92875E-01	2.717E-16	1.32665E+02	1.557E-29	Not normal
51	9.91462E-01	4.835E-18	1.61506E+02	8.499E-36	Not normal
52	9.90215E-01	2.010E-19	1.83807E+02	1.221E-40	Not normal
53	9.89829E-01	7.999E-20	1.90210E+02	4.971E-42	Not normal
54	9.93211E-01	7.787E-16	1.27503E+02	2.056E-28	Not normal
55	9.88711E-01	6.303E-21	2.58240E+02	8.393E-57	Not normal
56	9.89634E-01	5.118E-20	2.03017E+02	8.231E-45	Not normal
57	9.88348E-01	2.889E-21	2.22824E+02	4.115E-49	Not normal
58	9.89988E-01	1.193E-19 33		3.062E-49	Not normal
59	9.88113E-01	1.764E-21	2.44290E+02	8.975E-54	Not normal

Table 3.5: Normality tests for LKOH RX Equity

Δ	Shapiro-Wilk (stat)	Shapiro-Wilk (p-value)	K^2 (stat)	K^2 (p-value)	Conclusion
1	9.56049E-01	1.783E-38	1.06426E+03	7.904E-232	Not normal
2	9.61786E-01	2.017E-36	8.98275E+02	8.749E-196	Not normal
3	9.67511E-01	4.101E-34	7.02403E+02	2.986E-153	Not normal
4	9.73549E-01	2.647E-31	5.74303E+02	1.958E-125	Not normal
5	9.76946E-01	1.705E-29	4.72138E+02	2.996E-103	Not normal
6	9.81281E-01	7.299E-27	4.06361E+02	5.752E-89	Not normal
7	9.84266E-01	9.098E-25	3.31414E+02	1.082E-72	Not normal
8	9.86635E-01	7.001E-23	2.94586E+02	1.075E-64	Not normal
9	9.89172E-01	1.447E-20	2.45921E+02	3.970E-54	Not normal
10	9.91127E-01	1.692E-18	1.95091E+02	4.331E-43	Not normal
11	9.92274E-01	3.957E-17	1.63712E+02	2.820E-36	Not normal
12	9.92413E-01	5.935E-17	1.49801E+02	2.958E-33	Not normal
13	9.94956E-01	2.831E-13	9.53055E+01	2.017E-21	Not normal
14	9.95707E-01	5.883E-12	7.78854E+01	1.223E-17	Not normal
15	9.96084E-01	3.067E-11	7.48638E+01	5.540E-17	Not normal
16	9.97206E-01	8.010E-09	5.03216E+01	1.183E-11	Not normal
17	9.97038E-01	3.244E-09	4.70147E+01	6.179E-11	Not normal
18	9.97482E-01	3.829E-08	3.87159E + 01	3.917E-09	Not normal
19	9.97719E-01	1.574E-07	3.03331E+01	2.590E-07	Not normal
20	9.97015E-01	2.888E-09	3.89996E+01	3.399E-09	Not normal
21	9.97399E-01	2.382E-08	3.65644E+01	1.149E-08	Not normal
22	9.96733E-01	6.830E-10	4.25579E + 01	5.737E-10	Not normal
23	9.97563E-01	6.210E-08	3.22277E+01	1.004E-07	Not normal
24	9.97895E-01	4.771E-07	2.87768E+01	5.639E-07	Not normal
25	9.97505E-01	4.447E-08	2.47545E+01	4.213E-06	Not normal
26	9.97348E-01	1.804E-08	2.32894E+01	8.765E-06	Not normal
27	9.97913E-01	5.397E-07	2.41669E+01	5.652 E-06	Not normal
28	9.98727E-01	1.754E-04	1.27265E+01	1.724E-03	Not normal
29	9.98934E-01	9.485E-04	1.29167E+01	1.567E-03	Not normal
30	9.98897E-01	6.994E-04	1.15337E+01	3.130E-03	Not normal
31	9.99183E-01	8.091E-03	1.26717E+01	1.772E-03	Not normal
32	9.99203E-01	9.687E-03	1.17127E+01	2.862E-03	Not normal
33	9.99607E-01	3.172E-01	4.10760E+00	1.282E-01	Normal
34	9.99541E-01	1.890E-01	2.43257E+00	2.963E-01	Normal
35	9.99309E-01	2.490E-02	2.24129E+00	3.261E-01	Normal
36	9.99159E-01	6.578E-03	5.40324E+00	6.710E-02	Normal
37	9.98308E-01	7.785E-06	1.57270E+01	3.845E-04 3.907E-05	Not normal
39	9.97952E-01	7.093E-07	$\begin{array}{c} 2.03002\mathrm{E}{+01} \\ 2.57321\mathrm{E}{+01} \end{array}$	2.584E-06	Not normal Not normal
40	9.97223E-01 9.95850E-01	9.310E-09 1.177E-11	$\frac{2.57321E+01}{4.52170E+01}$	2.584E-00 1.518E-10	Not normal
41	9.95429E-01	2.014E-12	6.20961E+01	3.281E-14	Not normal
41	9.95829E-01	2.014E-12 1.081E-11	6.30434E+01	2.043E-14	Not normal
43	9.96428E-01	1.636E-10	5.93910E+01	1.269E-13	Not normal
44	9.95292E-01	1.050E-10 1.168E-12	8.94902E+01	3.694E-20	Not normal
45	9.94243E-01	2.314E-14	1.19861E+02	9.386E-27	Not normal
46	9.94167E-01	1.776E-14	1.18459E+02	1.892E-26	Not normal
47	9.94912E-01	2.678E-13	9.61789E+01	1.303E-21	Not normal
48	9.93552E-01	2.264E-15	1.21170E+02	4.878E-27	Not normal
49	9.94539E-01	6.744E-14	9.76440E+01	6.264E-22	Not normal
50	9.93279E-01	9.481E-16	1.34318E+02	6.811E-30	Not normal
51	9.93509E-01	1.988E-15	1.29407E+02	7.936E-29	Not normal
52	9.92525E-01	9.600E-17	1.41317E+02	2.057E-31	Not normal
53	9.92558E-01	1.062E-16	1.34163E+02	7.361E-30	Not normal
54	9.95571E-01	3.762E-12	8.01582E+01	3.925E-18	Not normal
55	9.94465E-01	5.273E-14	9.58897E + 01	1.506E-21	Not normal
56	9.93733E-01	4.216E-15	1.16978E + 02	3.969E-26	Not normal
57	9.91345E-01	3.624E-18	$1.57010\mathrm{E}{+02}$	8.049E-35	Not normal
58	9.91664E-01	8.604E-18 34	1.35735E+02	3.354E-30	Not normal
59	9.92566E-01	1.112E-16	1.27382E+02	2.185E-28	Not normal

Table 3.6: Normality tests for GAZP RX Equity

Δ	Shapiro-Wilk (stat)	Shapiro-Wilk (p-value)	K^2 (stat)	K^2 (p-value)	Conclusion
1	9.89149E-01	1.440E-20	2.11558E+02	1.150E-46	Not normal
2	9.92807E-01	1.980E-16	1.25557E+02	5.442E-28	Not normal
3	9.92463E-01	7.149E-17	1.47435E+02	9.660E-33	Not normal
4	9.95311E-01	1.180E-12	8.39926E+01	5.771E-19	Not normal
5	9.95284E-01	1.064E-12	8.65874E+01	1.577E-19	Not normal
6	9.95607E-01	3.998E-12	7.66845E+01	2.229E-17	Not normal
7	9.96999E-01	2.698E-09	6.16007E+01	4.203E-14	Not normal
8	9.95491E-01	2.485E-12	8.42088E+01	5.180E-19	Not normal
9	9.95874E-01	1.259E-11	8.27650E+01	1.066E-18	Not normal
10	9.97820E-01	3.007E-07	3.71969E+01	8.372E-09	Not normal
11	9.96943E-01	2.040E-09	5.36498E+01	2.239E-12	Not normal
12	9.94875E-01	2.207E-13	1.13773E+02	1.970E-25	Not normal
13	9.96081E-01	3.181E-11	7.88351E+01	7.606E-18	Not normal
14	9.97788E-01	2.485E-07	3.97882E+01	2.291E-09	Not normal
15	9.98412E-01	1.635E-05	2.80273E+01	8.202E-07	Not normal
16	9.97516E-01	4.849E-08	4.67270E + 01	7.134E-11	Not normal
17	9.97296E-01	1.386E-08	5.18974E+01	5.378E-12	Not normal
18	9.96388E-01	1.326E-10	6.67637E + 01	3.180E-15	Not normal
19	9.96317E-01	9.543E-11	6.57686E+01	5.230E-15	Not normal
20	9.97940E-01	6.557E-07	3.65087E+01	1.181E-08	Not normal
21	9.95803E-01	9.605E-12	7.94880E+01	5.488E-18	Not normal
22	9.96592E-01	3.566E-10	6.51825E+01	7.011E-15	Not normal
23	9.96155E-01	4.586E-11	7.60146E+01	3.116E-17	Not normal
24	9.95771E-01	8.460E-12	8.05830E + 01	3.174E-18	Not normal
25	9.96496E-01	2.265E-10	5.87647E+01	1.735E-13	Not normal
26	9.96724E-01	6.948E-10	5.75120E+01	3.247E-13	Not normal
27	9.96707E-01	6.378E-10	5.98148E+01	1.027E-13	Not normal
28	9.96399E-01	1.442E-10	7.34665E+01	1.114E-16	Not normal
29	9.94702E-01	1.220E-13	9.69006E + 01	9.085E-22	Not normal
30	9.93983E-01	9.534E-15	1.19606E + 02	1.066E-26	Not normal
31	9.96809E-01	1.077E-09	6.16684E + 01	4.063E-14	Not normal
32	9.96604E-01	3.894E-10	6.34852E + 01	1.638E-14	Not normal
33	9.96763E-01	8.611E-10	6.11305E+01	5.317E-14	Not normal
34	9.96101E-01	3.707E-11	7.31724E+01	1.291E-16	Not normal
35	9.96325E-01	1.039E-10	6.76906E+01	2.001E-15	Not normal
36	9.97920E-01	6.006E-07	3.86586E + 01	4.031E-09	Not normal
37	9.97329E-01	1.753E-08	4.89143E+01	2.390E-11	Not normal
38	9.97673E-01	1.300E-07	4.14242E+01	1.011E-09	Not normal
39	9.97700E-01	1.532E-07	4.00133E+01	2.048E-09	Not normal
40	9.96417E-01	1.619E-10	6.67443E+01	3.211E-15	Not normal
41	9.96531E-01	2.807E-10	6.14349E+01	4.566E-14	Not normal
42	9.97150E-01	6.624E-09	4.48000E+01	1.870E-10	Not normal
43	9.97340E-01	1.893E-08	4.47499E+01	1.917E-10	Not normal
44	9.97456E-01	3.674E-08	4.76599E+01	4.475E-11	Not normal
45	9.96870E-01	1.527E-09	5.75197E+01	3.234E-13	Not normal
46	9.96453E-01	1.953E-10	6.51374E+01	7.171E-15	Not normal
47	9.97887E-01	4.966E-07	4.02643E+01	1.806E-09	Not normal
48	9.97498E-01	4.722E-08	4.53862E+01	1.395E-10	Not normal
49	9.97173E-01	7.634E-09	4.59928E+01	1.030E-10	Not normal
50	9.98349E-01	1.112E-05	2.82064E+01	7.500E-07	Not normal
51	9.97047E-01	3.911E-09	5.65365E+01	5.287E-13	Not normal
52	9.96419E-01	1.691E-10	6.74260E+01	2.284E-15	Not normal
53	9.95953E-01	2.034E-11	7.15530E+01	2.900E-16	Not normal
54	9.96405E-01	1.592E-10	6.26662E+01	2.467E-14	Not normal
55	9.96753E-01	8.668E-10	5.78789E+01	2.702E-13	Not normal
56	9.96377E-01	1.406E-10	6.27691E+01	2.344E-14	Not normal
57	9.96872E-01	1.595E-09	5.58669E+01	7.390E-13	Not normal
58	9.96600E-01	4.104E-10 35		1.499E-14	Not normal
59	9.95737E-01	8.152E-12	7.93532E+01	5.871E-18	Not normal

Table 3.7: Normality tests for FIVE RX Equity

Δ	Shapiro-Wilk (stat)	Shapiro-Wilk (p-value)	K^2 (stat)	K^2 (p-value)	Conclusion
1	9.16093E-01	7.966E-41	7.45140E+02	1.566E-162	Not normal
2	9.44144E-01	6.515E-35	4.41209E+02	1.558E-96	Not normal
3	9.52090E-01	8.336E-33	3.22623E+02	8.774E-71	Not normal
4	9.49936E-01	2.135E-33	3.69807E+02	4.983E-81	Not normal
5	9.53330E-01	1.911E-32	3.32630E+02	5.892E-73	Not normal
6	9.65898E-01	2.221E-28	2.34592E+02	1.146E-51	Not normal
7	9.62768E-01	1.747E-29	2.55825E+02	2.807E-56	Not normal
8	9.59215E-01	1.182E-30	2.73767E+02	3.567E-60	Not normal
9	9.57407E-01	3.231E-31	2.77472E+02	5.595E-61	Not normal
10	9.61492E-01	6.643E-30	2.62974E+02	7.868E-58	Not normal
11	9.57214E-01	2.868E-31	2.80485E+02	1.240E-61	Not normal
12	9.61110E-01	5.047E-30	2.67378E + 02	8.703E-59	Not normal
13	9.56193E-01	1.427E-31	2.87605E+02	3.526E-63	Not normal
14	9.59917E-01	2.092E-30	2.60580E + 02	2.605E-57	Not normal
15	9.61243E-01	5.731E-30	2.62390E+02	1.054E-57	Not normal
16	9.64922E-01	1.070E-28	2.44020E+02	1.027E-53	Not normal
17	9.63944E-01	4.858E-29	2.46135E+02	3.568E-54	Not normal
18	9.63785E-01	4.311E-29	2.47039E+02	2.271E-54	Not normal
19	9.69194E-01	4.432E-27	2.33854E+02	1.657E-51	Not normal
20	9.67114E-01	7.046E-28	2.36390E+02	4.663E-52	Not normal
21	9.66581E-01	4.490E-28	2.33284E+02	2.203E-51	Not normal
22	9.69864E-01	8.399E-27	2.27362E+02	4.257E-50	Not normal
23	9.67283E-01	8.365E-28	2.39343E+02	1.065E-52	Not normal
24	9.71067E-01	2.645E-26	2.06032E+02	1.823E-45	Not normal
25	9.68260E-01	2.009E-27	2.31279E+02	6.005E-51	Not normal
26	9.70900E-01	2.292E-26	2.06869E+02	1.200E-45	Not normal
27	9.73732E-01	3.783E-25	1.98302E+02	8.695E-44	Not normal
28	9.74143E-01	5.830E-25	1.94709E+02	5.242E-43	Not normal
29	9.71793E-01	5.539E-26	2.29552E+02	1.424E-50	Not normal
30	9.72140E-01	7.835E-26	2.14537E+02	2.593E-47	Not normal
31	9.73693E-01	3.750E-25	2.03344E+02	6.990E-45	Not normal
32	9.73670E-01	3.691E-25	2.19927E+02	1.751E-48	Not normal
33	9.77717E-01	3.054E-23	1.93543E+02	9.389E-43	Not normal
34	9.73527E-01	3.239E-25	2.45564E+02	4.749E-54	Not normal
35	9.75398E-01	2.322E-24	2.07112E+02	1.062E-45	Not normal
36	9.73753E-01	4.148E-25	2.09353E+02	3.464 E-46	Not normal
37	9.72966E-01	1.880E-25	2.10007E+02	2.498E-46	Not normal
38	9.71097E-01	3.042E-26	2.15054E+02	2.002E-47	Not normal
39	9.72950E- 01	1.879E-25	2.04092E+02	4.809E-45	Not normal
40	9.73475E-01	3.219E-25	2.04878E + 02	3.246E-45	Not normal
41	9.73955E-01	5.309E-25	1.94008E+02	7.442E-43	Not normal
42	9.68037E-01	1.894E-27	2.22260E+02	5.456E-49	Not normal
43	9.71054E-01	3.040E-26	2.08359E + 02	5.693E-46	Not normal
44	9.71082E-01	3.146E-26	$2.15078\mathrm{E}{+02}$	1.979E-47	Not normal
45	9.68133E-01	2.114E-27	2.10301E+02	2.156E-46	Not normal
46	9.73918E-01	5.313E-25	1.87425E+02	2.000E-41	Not normal
47	9.66248E-01	4.199E-28	$2.36185\mathrm{E}{+02}$	5.164E-52	Not normal
48	9.68876E-01	4.206E-27	2.16760E + 02	8.533E-48	Not normal
49	9.65666E-01	2.616E-28	2.37476E+02	2.709E-52	Not normal
50	9.68382E-01	2.747E-27	2.62969E+02	7.887E-58	Not normal
51	9.67431E-01	1.199E-27	2.45256E+02	5.537E-54	Not normal
52	9.68457E-01	2.986E-27	2.30804E+02	7.613E-51	Not normal
53	9.69424E-01	7.208E-27	2.11612E+02	1.120E-46	Not normal
54	9.71484E-01	5.010E-26	2.04386E+02	4.151E-45	Not normal
55	9.68487E-01	3.145E-27	2.25115E+02	1.309E-49	Not normal
56	9.69498E-01	7.899E-27	2.37076E+02	3.309E-52	Not normal
57	9.69453E-01	7.642E-27	2.11768E+02	1.035E-46	Not normal
58	9.73844E-01		1.94218E+02	6.701E-43	Not normal
59	9.76912E-01	1.477E-23	1.76893E+02	3.874E-39	Not normal

Table 3.8: Normality tests for OGZD LI Equity

Δ	Shapiro-Wilk (stat)	Shapiro-Wilk (p-value)	K^2 (stat)	K^2 (p-value)	Conclusion
1	9.82993E-01	5.006E-08	4.57060E+01	1.189E-10	Not normal
2	9.85074E-01	2.820E-07	3.16814E+01	1.320E-07	Not normal
3	9.85636E-01	4.649E-07	3.80277E+01	5.526E-09	Not normal
4	9.88654E-01	7.649E-06	2.70348E+01	1.347E-06	Not normal
5	9.86365E-01	9.119E-07	3.01748E+01	2.803E-07	Not normal
6	9.82377E-01	3.363E-08	3.88751E+01	3.617E-09	Not normal
7	9.88597E-01	7.538E-06	3.06923E+01	2.164E-07	Not normal
8	9.89462E-01	1.806E-05	2.69168E+01	1.429E-06	Not normal
9	9.91369E-01	1.372E-04	1.80303E+01	1.216E-04	Not normal
10	9.88297E-01	5.881E-06	2.92982E+01	4.345E-07	Not normal
11	9.92087E-01	3.139E-04	1.84233E+01	9.987E-05	Not normal
12	9.90715E-01	6.992E-05	2.12548E+01	2.424E-05	Not normal
13	9.87502E-01	2.893E-06	3.01331E+01	2.862E-07	Not normal
14	9.93198E-01	1.186E-03	1.36409E+01	1.091E-03	Not normal
15	9.93235E-01	1.251E-03	1.44308E+01	7.352E-04	Not normal
16	9.93077E-01	1.047E-03	1.50232E+01	5.467E-04	Not normal
17	9.94136E-01	3.834E-03	$1.55500E{+}01$	4.201E-04	Not normal
18	9.89858E-01	3.079E-05	2.98982E + 01	3.219E-07	Not normal
19	9.81866E-01	2.848E-08	4.67719E + 01	6.976E-11	Not normal
20	9.90493E-01	6.103E-05	2.44317E + 01	4.951E-06	Not normal
21	9.90315E-01	5.131E-05	2.31470E + 01	9.412E-06	Not normal
22	9.92037E-01	3.350E-04	$1.65608E{+}01$	2.534E-04	Not normal
23	9.91606E-01	2.097E-04	2.35676E + 01	7.627E-06	Not normal
24	9.94293E-01	4.954E-03	1.27558E+01	1.699E-03	Not normal
25	9.87393E-01	3.116E-06	3.49143E+01	2.621E-08	Not normal
26	9.94398E-01	5.741E-03	1.29231E+01	1.562E-03	Not normal
27	9.94787E-01	9.431E-03	9.67430E+00	7.930E-03	Not normal
28	9.93294E-01	1.528E-03	1.07536E+01	4.623E-03	Not normal
29	9.92209E-01	4.395E-04	1.71344E+01	1.902E-04	Not normal
30	9.95644E-01	2.878E-02	7.87842E+00	1.946E-02	Not normal
31	9.93164E-01	1.349E-03	1.81142E+01	1.166E-04	Not normal
32	9.96560E-01	9.429E-02	6.62962E+00	3.634E-02	Normal
33	9.91827E-01	3.001E-04	1.83914E+01	1.015E-04	Not normal
34	9.94971E-01	1.258E-02	1.24906E+01	1.940E-03	Not normal
35	9.92499E-01	6.518E-04	1.61940E+01	3.045E-04	Not normal
36	9.92463E-01 9.91986E-01	6.325E-04	$\begin{array}{c} 1.59004 \text{E}{+01} \\ 1.89193 \text{E}{+01} \end{array}$	3.526E-04	Not normal
37	9.93833E-01	3.742E-04 3.199E-03	1.89193E+01 1.40878E+01	7.793E-05 8.727E-04	Not normal Not normal
39	9.92985E-01	1.188E-03	1.49684E+01	5.619E-04	Not normal
40	9.95383E-01 9.95383E-01	2.213E-02	1.49034E + 01 1.17387E + 01	2.825E-03	Not normal
41	9.92732E-01	9.054E-04	1.97880E+01	5.048E-05	Not normal
42	9.94233E-01	5.388E-03	1.97830E + 01 1.27901E + 01	1.670E-03	Not normal
43	9.91526E-01	2.422E-04	1.82732E+01	1.077E-04	Not normal
44	9.95652E-01	3.199E-02	9.87608E+00	7.169E-03	Not normal
45	9.96290E-01	7.197E-02	7.09833E+00	2.875E-02	Normal
46	9.94307E-01	6.106E-03	1.46661E+01	6.536E-04	Not normal
47	9.95911E-01	4.522E-02	8.25592E+00	1.612E-02	Not normal
48	9.93541E-01	2.484E-03	1.15884E+01	3.045E-03	Not normal
49	9.94234E-01	5.736E-03	1.41470E+01	8.473E-04	Not normal
50	9.89833E-01	4.560E-05	2.70051E+01	1.367E-06	Not normal
51	9.94510E-01	8.156E-03	1.14057E + 01	3.336E-03	Not normal
52	9.97626E-01	3.643E-01	4.22345E+00	1.210E-01	Normal
53	9.94407E-01	7.324E-03	1.41504E+01	8.458E-04	Not normal
54	9.96045E-01	5.587E-02	$9.59555E{+00}$	8.248E-03	Normal
55	9.96406E-01	8.809E-02	6.83182E+00	3.285E-02	Normal
56	9.91433E-01	2.555E-04	2.44818E+01	4.829E-06	Not normal
57	9.93013E-01	1.474E-03	$1.35057E{+}01$	1.168E-03	Not normal
58	9.92420E-01	7.644E-04 37		7.822E-06	Not normal
59	9.91035E-01	1.741E-04	1.98998E+01	4.773E-05	Not normal

Table 3.9: Normality tests for VTBR LI Equity

Δ	Shapiro-Wilk (stat)	Shapiro-Wilk (p-value)	K^2 (stat)	K^2 (p-value)	Conclusion
1	9.13318E-01	6.311E-41	7.95465E+02	1.849E-173	Not normal
2	9.37291E-01	3.524E-36	4.62610E+02	3.513E-101	Not normal
3	9.52292E-01	2.084E-32	3.44665E+02	1.435E-75	Not normal
4	9.50895E-01	8.619E-33	3.76979E+02	1.381E-82	Not normal
5	9.54370E-01	8.315E-32	3.15510E+02	3.075E-69	Not normal
6	9.59861E-01	3.971E-30	2.76277E+02	1.017E-60	Not normal
7	9.59492E-01	3.054E-30	2.71379E+02	1.177E-59	Not normal
8	9.57224E-01	6.044E-31	2.98988E+02	1.190E-65	Not normal
9	9.56950E-01	5.032E-31	3.02204E+02	2.383E-66	Not normal
10	9.63086E-01	4.812E-29	2.56106E+02	2.439E-56	Not normal
11	9.59285E-01	2.720E-30	2.76762E+02	7.978E-61	Not normal
12	9.58918E-01	2.100E-30	2.77372E+02	5.880E-61	Not normal
13	9.54142E-01	7.681E-32	2.90227E+02	9.505E-64	Not normal
14	9.55976E-01	2.680E-31	2.89217E+02	1.575E-63	Not normal
15	9.60515E-01	6.992E-30	2.65751E + 02	1.962E-58	Not normal
16	9.57320E-01	6.947E-31	2.73249E+02	4.620E-60	Not normal
17	9.58247E-01	1.354E-30	2.73619E + 02	3.841E-60	Not normal
18	9.58431E-01	1.559E-30	2.66388E+02	1.428E-58	Not normal
19	9.63958E-01	1.041E-28	2.54757E + 02	4.789E-56	Not normal
20	9.62549E-01	3.446E-29	2.59575E + 02	4.305E-57	Not normal
21	9.61678E-01	1.775E-29	2.68759E + 02	4.363E-59	Not normal
22	9.58310E-01	1.481E-30	2.79888E+02	1.672E-61	Not normal
23	9.59798E-01	4.405E-30	2.82275E+02	5.068E-62	Not normal
24	9.58887E-01	2.285E-30	2.68742E + 02	4.399E-59	Not normal
25	9.56327E-01	3.771E-31	2.82561E + 02	4.392E-62	Not normal
26	9.62401E-01	3.238E-29	2.61570E + 02	1.588E-57	Not normal
27	9.62269 E-01	2.949E-29	2.56963E+02	1.589E-56	Not normal
28	9.62077E-01	2.564E-29	2.61847E + 02	1.382E-57	Not normal
29	9.60691E-01	9.019E-30	2.58613E+02	6.964E-57	Not normal
30	9.60910E-01	1.073E-29	2.78557E + 02	3.252E-61	Not normal
31	9.65352E-01	3.587E-28	2.57907E+02	9.913E-57	Not normal
32	9.58076E-01	1.371E-30	2.82094E+02	5.548E-62	Not normal
33	9.68252E-01	4.335E-27	2.51904E+02	1.994E-55	Not normal
34	9.73801E-01	8.420E-25	2.37478E+02	2.705E-52	Not normal
35	9.64556E-01	1.934E-28	2.74991E+02	1.934E-60	Not normal
36	9.67196E-01 9.67553E-01	1.771E-27	2.44979E+02	6.361E-54	Not normal
37	9.65055E-01	2.432E-27 2.982E-28	$\begin{array}{c} 2.45831E{+}02 \\ 2.43595E{+}02 \end{array}$	4.155E-54 1.270E-53	Not normal Not normal
39	9.66544E-01	2.982E-28 1.041E-27	2.43395E+02 2.24342E+02	1.927E-49	Not normal
40	9.64460E-01	1.868E-28	2.37591E+02	2.557E-52	Not normal
41	9.63931E-01	1.231E-28	2.57991E+02 2.55954E+02	2.633E-56	Not normal
42	9.63702E-01	1.231E-28 1.034E-28	2.61902E+02	1.345E-57	Not normal
43	9.62457E-01	3.922E-29	2.49304E+02	7.317E-55	Not normal
44	9.68194E-01	4.515E-27	2.17806E+02	5.058E-48	Not normal
45	9.64438E-01	1.915E-28	2.41953E+02	2.888E-53	Not normal
46	9.68942E-01	8.930E-27	2.23177E+02	3.449E-49	Not normal
47	9.62946E-01	5.945E-29	2.54493E+02	5.464E-56	Not normal
48	9.63642E-01	1.039E-28	2.48004E+02	1.402E-54	Not normal
49	9.63720E-01	1.115E-28	2.56524E+02	1.980E-56	Not normal
50	9.60339E-01	8.358E-30	2.69487E+02	3.031E-59	Not normal
51	9.64539E-01	2.190E-28	2.42080E + 02	2.710E-53	Not normal
52	9.68241E-01	5.034E-27	2.35295E+02	8.058E-52	Not normal
53	9.62265E-01	3.690E-29	2.67887E + 02	6.747E-59	Not normal
54	9.62302E-01	3.830E-29	2.61423E+02	1.709E-57	Not normal
55	9.66365E-01	1.024E-27	$2.35706\mathrm{E}{+02}$	6.563E-52	Not normal
56	9.66954E-01	1.703E-27	2.23357E+02	3.153E-49	Not normal
57	9.63011E-01	6.826E-29	2.40254E+02	6.753E-53	Not normal
58	9.66957E-01	1.737E-27 38		1.985E-53	Not normal
59	9.69328E-01	1.408E-26	2.27468E+02	4.036E-50	Not normal

Table 3.10: Normality tests for SBER LI Equity

Δ	Shapiro-Wilk (stat)	Shapiro-Wilk (p-value)	K^2 (stat)	K^2 (p-value)	Conclusion
1	9.22917E-01	1.578E-37	6.03530E+02	8.814E-132	Not normal
2	9.47011E-01	2.497E-32	3.72757E+02	1.140E-81	Not normal
3	9.55016E-01	3.503E-30	2.73125E+02	4.917E-60	Not normal
4	9.59160E-01	5.979E-29	2.86229E+02	7.017E-63	Not normal
5	9.61506E-01	3.304E-28	2.30324E+02	9.676E-51	Not normal
6	9.60629E-01	1.750E-28	2.54314E+02	5.977E-56	Not normal
7	9.62217E-01	5.725E-28	2.43058E+02	1.662E-53	Not normal
8	9.60513E-01	1.640E-28	2.56242E+02	2.279E-56	Not normal
9	9.61739E-01	4.081E-28	2.31569E+02	5.193E-51	Not normal
10	9.59838E-01	1.027E-28	2.48689E+02	9.953E-55	Not normal
11	9.58708E-01	4.650E-29	2.60906E+02	2.213E-57	Not normal
12	9.54799E-01	3.319E-30	2.62076E + 02	1.233E-57	Not normal
13	9.57787E-01	2.496E-29	2.61489E+02	1.654E-57	Not normal
14	9.60536E-01	1.765E-28	2.44145E+02	9.650E-54	Not normal
15	9.60787E-01	2.140E-28	2.44950E+02	6.452E-54	Not normal
16	9.60725E-01	2.065E-28	2.43798E+02	1.148E-53	Not normal
17	9.59810E-01	1.076E-28	2.47222E+02	2.072 E-54	Not normal
18	9.63692E-01	1.955E-27	2.33689E+02	1.799E-51	Not normal
19	9.65593E-01	8.868E-27	2.24182E+02	2.087E-49	Not normal
20	9.65983E-01	1.228E-26	2.25490E + 02	1.085E-49	Not normal
21	9.61448E-01	3.683E-28	$2.43066\mathrm{E}{+02}$	1.656E-53	Not normal
22	9.69253E-01	1.982E-25	2.13533E+02	4.284E-47	Not normal
23	9.63723E-01	2.099E-27	2.58004E+02	9.444E-57	Not normal
24	9.67500E-01	4.472E-26	2.14095E+02	3.235E-47	Not normal
25	9.64601E-01	4.250E-27	2.29184E+02	1.712E-50	Not normal
26	9.68346E-01	9.348E-26	2.06644E+02	1.342E-45	Not normal
27	9.65983E-01	1.309E-26	2.16035E+02	1.226E-47	Not normal
28	9.71561E-01	1.685E-24	1.88328E+02	1.274E-41	Not normal
29	9.67594E-01	5.064E-26	2.21779E+02	6.939E-49	Not normal
30	9.71936E-01	2.436E-24	1.97484E+02	1.309E-43	Not normal
31	9.72137E-01	2.971E-24	1.95657E + 02	3.262E-43	Not normal
32	9.68553E-01	1.179E-25	2.14293E+02	2.930E-47	Not normal
33	9.72306E-01	3.548E-24	2.15521E+02	1.586E-47	Not normal
34	9.65388E-01	8.634E-27	2.38475E+02	1.644E-52	Not normal
35	9.68796E-01	1.495E-25	2.15422E+02	1.666E-47	Not normal
36	9.71819E-01	2.300E-24	1.96128E+02	2.578E-43	Not normal
37	9.76920E-01 9.74885E-01	3.958E-22 4.682E-23	$\begin{array}{c} 1.70350\mathrm{E}{+02} \\ \hline 1.67726\mathrm{E}{+02} \end{array}$	1.021E-37	Not normal Not normal
39	9.73697E-01	4.062E-23 1.435E-23	1.89028E+02	3.791E-37 8.978E-42	Not normal
40	9.71235E-01	1.455E-25 1.384E-24	1.95857E+02	2.952E-43	Not normal
41	9.68144E-01	9.007E-26	2.02675E+02	9.764E-45	Not normal
42	9.66667E-01	2.631E-26	2.02073E+02 2.23404E+02	3.079E-49	Not normal
43	9.65514E-01	1.038E-26	2.19697E+02	1.965E-48	Not normal
44	9.63365E-01	1.939E-27	2.21510E+02	7.938E-49	Not normal
45	9.69969E-01	4.587E-25	1.92617E+02	1.492E-42	Not normal
46	9.67135E-01	4.024E-26	2.07285E+02	9.742E-46	Not normal
47	9.67062E-01	3.819E-26	2.12947E+02	5.742E-47	Not normal
48	9.67005E-01	3.677E-26	2.16337E+02	1.054E-47	Not normal
49	9.68509E-01	1.323E-25	2.07479E+02	8.842E-46	Not normal
50	9.72337E-01	4.234E-24	1.92021E+02	2.010E-42	Not normal
51	9.72083E-01	3.359E-24	1.92551E+02	1.542E-42	Not normal
52	9.67798E-01	7.412E-26	2.08092E+02	6.507E-46	Not normal
53	9.71112E-01	1.385E-24	1.93688E+02	8.732E-43	Not normal
54	9.69497E-01	3.271E-25	1.91144E+02	3.117E-42	Not normal
55	9.67930E-01	8.517E-26	2.03088E+02	7.941E-45	Not normal
56	9.69218E-01	2.607E-25	$1.95210\mathrm{E}{+02}$	4.080E-43	Not normal
57	9.70037E-01	5.428E-25	2.04058E+02	4.890E-45	Not normal
58	9.77231E-01	6.602E-22 39		6.418E-37	Not normal
59	9.77163E-01	6.181E-22	1.60737E+02	1.248E-35	Not normal

Table 3.11: Normality tests for LKOD LI Equity

Appendix B. Estimation Code.

```
def rlz_vol_est(df: pd.DataFrame,
                count: int,
                rolling_window: int=1) -> np.ndarray:
    log_returns = np.zeros(int(df.shape[0]/rolling_window))
   for i in range(1, log_returns.size):
        log_returns[i] =
                math.log(df["Mean"][i*rolling_window]/
                                    df["Mean"][(i-1)*rolling_window])
   rlz_vol = np.zeros(int(log_returns.size/count))
   for i in range(rlz_vol.size):
        lr_n = np.zeros(count)
        for n in range(count):
            lr_n[n] = log_returns[i*count+n]
        tmp = 0.0
        for j in range(1, lr_n.size):
            tmp += (lr_n[j] - lr_n[j-1])**2
        rlz_vol[i] = math.sqrt(tmp)
   return rlz_vol
def hurst_estimation(name: str,
                     mode: str = 'yf',
                     rolling_window: int = 1,
                     show_pics = True,
                     save_pics = False):
    if mode == 'yf':
        count = days_count
        df = yf.download(name, '2000-01-01', '2019-01-01')
        df["Mean"] = 0.5*(df["Open"]+df["Close"])
    elif mode == 'bb':
        count = minutes_count
        df = pd.read_csv('data_bloomberg/'+name+'.csv', sep="\t")
        df["Mean"] = 0.5*(df["High"]+df["Low"])
   volatility_array = rlz_vol_est(df = df,
                                   count = count,
                                   rolling_window = rolling_window)
                     = np.zeros((2, num_of_q))
   zetaq
    for I in range(0, num_of_q):
        graph_data = np.zeros((2, pD-sD))
                 = step_of_q*(1+I)
        line_start = math.log(sD)
        line_stop = math.log(pD)
        for Delta in range(sD, pD):
            graph_data[0, Delta-sD] = math.log(Delta)
            graph_data[1, Delta-sD] = math.log(m(q, Delta, volatility_array))
                        = np.polyfit(graph_data[0],graph_data[1], 1)
        linear_model
        linear_model_fn = np.poly1d(linear_model)
                        = np.arange(line_start, line_stop, 0.1)
        x_s
```

```
skew_of_linear_model = skew(line_start,
                                    line_stop,
                                    linear_model_fn(line_start),
                                    linear_model_fn(line_stop))
        zetaq[0, I] = q
        zetaq[1, I] = skew_of_linear_model
    linear_model_H
                    = np.polyfit(zetaq[0], zetaq[1], 1)
    linear_model_H_fn = np.poly1d(linear_model_H)
                      = np.arange(0, step_of_q*(num_of_q+1), step_of_q)
    x_s
   H_{est} = skew(0,
                 step_of_q*(num_of_q)+1,
                 linear_model_H_fn(0),
                 linear_model_H_fn(step_of_q*(num_of_q)+1))
    sz = 40
   graph_data = np.zeros((2, sz))
   for Delta in range(1, sz+1):
        graph_data[0, Delta-1] = Delta**(2*H_est)
        graph_data[1, Delta-1] = ACov(volatility_array, Delta)
   linear_model
                   = np.polyfit(graph_data[0],graph_data[1], 1)
   linear_model_fn = np.poly1d(linear_model)
   x_s
                    = np.arange(1, (sz+1)**(2*H_est), 0.1)
   for Delta in range(1, sz+1):
        graph_data[0, Delta-1] = math.log(Delta)
    linear_model
                    = np.polyfit(graph_data[0],graph_data[1], 1)
    linear_model_fn = np.poly1d(linear_model)
                    = np.arange(0, math.log(sz+1), 0.1)
   x_s
   def lag_array(Delta):
        retarr = np.zeros(volatility_array.size - Delta)
        if Delta >= 0:
            for i in range(0, volatility_array.size-Delta):
                retarr[i] = np.log(volatility_array[i+Delta]) -
                                        np.log(volatility_array[i])
            for i in range(0, volatility_array.size-math.abs(Delta)):
                retarr[i] = np.log(volatility_array[i]) -
                                        np.log(volatility_array[i-Delta])
        retarr = retarr/retarr.max()
        return retarr
   return H_est
def f(theta):
    return (1/((2*H+1)*(2*H+2)*theta**2)*((1+theta)**(2*H+2) - 2)
                    -2 * theta**(2*H+2) + (1-theta)**(2*H+2)))
def smoothing_theoretical(delta: float):
   num_of_Deltas = 200
   plot = np.zeros((2, num_of_Deltas))
```

```
Delta = np.arange(1, num_of_Deltas+1, 1)
    plot[0] = np.log(Delta)
    plot[1] = np.log(Delta**(2*H) * f(delta/Delta))
    linear_model
                   = np.polyfit(plot[0],plot[1], 1)
    linear_model_fn = np.poly1d(linear_model)
                    = np.arange(0, 5, 0.1)
    x_s
    print(skew(0, 1, linear_model_fn(0), linear_model_fn(1))*0.5)
    print(skew(0, 1, linear_model_fn(0), linear_model_fn(1))*0.5/H - 1)
def smoothing_empirical(name: str, show_pics: bool=True):
    num_of_wind = 20
    graph_data = np.zeros((2, num_of_wind))
    for i in range(1, num_of_wind+1):
        graph_data[0, i-1] = i
        graph_data[1, i-1] = analyse_volatility(name=name,
                                                mode='bb',
                                                rolling_window=i,
                                                show_pics=False)
    return [np.mean(graph_data[1]),
            np.std(graph_data[1]),
            np.min(graph_data[1])]
```