

Pravdepodobnosť a štatistika – vzorce

$$P(A) = \sum_i P(H_i)P(A|H_i), \quad P(H_k|A) = \frac{P(H_k)P(A|H_k)}{\sum_i P(H_i)P(A|H_i)}$$

$$X \sim A(p), \quad H = \{0, 1\}, \quad f(0) = 1-p, f(1) = p, \quad E(X) = p, \quad \text{var}(X) = p(1-p)$$

$$X \sim R\{x_1, x_2, \dots, x_n\}, \quad f(x_i) = 1/n, \quad E(X) = \sum_i x_i / n, \quad \text{var}(X) = \sum_i (x_i - E(X))^2 / n$$

$$X \sim Bi(n, p), \quad f(k) = C(n, k)p^k(1-p)^{n-k}, k = 0, 1, \dots, n, \quad E(X) = np, \quad \text{var}(X) = np(1-p)$$

$$X \sim Po(\lambda), \quad f(k) = \lambda^k e^{-\lambda} / k! \quad k = 0, 1, \dots, \quad E(X) = \lambda, \quad \text{var}(X) = \lambda$$

$$X \sim G(p), \quad f(k) = (1-p)^k p \quad k = 0, 1, \dots, \quad E(X) = \frac{1-p}{p}, \quad \text{var}(X) = \frac{1-p}{p^2}$$

$$X \sim R(a, b), \quad f(x) = \frac{1}{b-a} \quad x \in (a, b), \quad E(X) = \frac{a+b}{2}, \quad \text{var}(X) = \frac{(b-a)^2}{12}$$

$$X \sim Exp(\lambda), \quad f(x) = \lambda e^{-\lambda x} \quad x > 0, \quad E(X) = \frac{1}{\lambda}, \quad \text{var}(X) = \frac{1}{\lambda^2}$$

$$X \sim N(\mu, \sigma^2), \quad f(x) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right), \quad E(X) = \mu, \quad \text{var}(X) = \sigma^2$$

$$g(y) = f(h^{-1}(y)) \left| \frac{dh^{-1}(y)}{dy} \right|, \text{ pre } y \in K, \text{ kde } K = \{h(x) : f(x) > 0\}$$

$$P((X, Y) \in [a, b] \times [c, d]) = F(b, d) - F(a, d) - F(b, c) + F(a, c)$$

$$E(X) = \sum_{x \in H} xf(x) \quad \text{resp.} \quad E(X) = \int_{-\infty}^{\infty} xf(x)dx$$

$$\text{var}(X) = \sum_{x \in H} (x - E(X))^2 f(x) \quad \text{resp.} \quad \text{var}(X) = \int_{-\infty}^{\infty} (x - E(X))^2 f(x) dx$$

$$\text{var}(X) = E((X - E(X))^2), \quad \sigma_X = \sqrt{\text{var}(X)}$$

$$E(h(X)) = \sum_{x \in H} h(x) f(x) \quad \text{resp.} \quad E(h(X)) = \int_{-\infty}^{\infty} h(x) f(x) dx$$

$$E(h(X, Y)) = \sum_{x \in H} \sum_{y \in K} h(x, y) f(x, y) \quad \text{resp.} \quad E(h(X, Y)) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} h(x, y) f(x, y) dx dy$$

$$\mu'_k = E(X^k), \quad \text{resp.} \quad \mu_k = E((X - E(X))^k)$$

$$\text{cov}(X, Y) = \sum_{x \in H} \sum_{y \in K} (x - E(X))(y - E(Y)) f(x, y), \quad \text{resp.}$$

$$\text{cov}(X, Y) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} (x - E(X))(y - E(Y)) f(x, y) dx dy$$

$$\rho(X, Y) = \frac{\text{cov}(X, Y)}{\sqrt{\text{var}(X) \text{var}(Y)}}$$

$$Y_n = \frac{\sum_{i=1}^n X_i - mn}{b\sqrt{n}} \quad \text{má asymptoticky normálne rozdelenie } N(0, 1)$$

$$M'_k = \frac{1}{n} \sum_{i=1}^n X_i^k \quad \text{resp.} \quad M_k = \frac{1}{n} \sum_{i=1}^n (X_i - \bar{X})^k \quad S^2 = \frac{1}{n-1} \sum_{i=1}^n (X_i - \bar{X})^2$$