1. Trayectorio más certa de un cono inuntedo de restir x. en coordena cilindrica.

Ton
$$\alpha = \frac{r}{2}$$
 $\Rightarrow \frac{r}{r} = \frac{r}{2} \cos t d$
 $\Rightarrow r = \frac{r}{2} \tan \alpha$
 $\Rightarrow \frac{\partial}{\partial t} \left(\frac{\partial f}{\partial \dot{q}} \right) - \frac{\partial f}{\partial \dot{q}} = 0$
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Reemploganole:

3 (22) - 27 - 27 De lomará el cudrado de la Longitud. 2 = 2 rec(d) 2 -> 2 (2 sec2(a) 2) = 2 rec2(a) 2 2F = 22 ton2d => 2 rec²(x) 2-22 ton² d = 0 2 Sec² d - 2 tom² d = 0 $\frac{2}{2} = \frac{2 \tan^2 \alpha}{\sec^2 \alpha} = \frac{2 \tan^2 \alpha}{1 + \tan^2 \alpha}$ $\frac{d2}{d0} = \frac{2}{1 + \tan^2 d} = \frac{d2}{2} = \frac{6 \text{ am}^2 d}{1 + \tan^2 d} d\theta$ tg'(α) = A => [n 121 = tonid 0 + K 2(6) = Ke [+tg2(a)] 0 d2 = KeAO do 2 = Ke + Kr > función minimor.

donde
$$y(x)$$
 tiene $y(0) = 0$ $y(1) = 1$

The field $y(x)$ tiene $y(0) = 0$ $y(1) = 1$

The field enteries $L(x,y,y) = y^2 + 12xy$

For ever - lagrange tiens:

$$\frac{d}{dx} \left(\frac{\partial L}{\partial y} \right) - \frac{\partial L}{\partial y} = 0$$

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$$\frac{d}{dx$$

y (1) = 1 = 1= y(1) = 1 + C, (1)

=> (c=0)

00 y (x) = x3 Ahora como querenos carcular el valor minimo de la integral. Sustituimes $I = \int_{0}^{2} L((x^{3})^{1})^{2} + 12 \times (x^{3}) dx$ $= \int_{0}^{1} \left[(3x^{2})^{2} + 12x^{4} \right] dx$ = 5 = 5 = 9 × + 12 × 3 d × $= \int_{0}^{1} 21 \times^{7} dx = 21 \times^{5} \int_{0}^{1}$

3. Encontrar la geoderica entre P. (a,o,o), P. (-a,o,M)
sobre la superficie x²+y²-a²=0. X 5+ A 5 = 0 5 = + 5 92 = 915 + 15 90 5 + 935 ds2 = a2de2+d32 ds = /do2 (a2 + (d3/d0)2) = do/a2 + 22 I = / Va2 + 22 do. $\frac{d}{d\theta}\left(\frac{\partial f}{\partial \hat{z}}\right) - \frac{\partial f}{\partial \hat{z}} = 0. \Rightarrow \frac{\partial f}{\partial \hat{z}} = 0$ $\frac{\partial f}{\partial \hat{z}} = \frac{1}{2\sqrt{a^2 + \hat{z}^2}} \cdot 2\hat{z} = \frac{\hat{z}}{\sqrt{a^2 + \hat{z}^2}}$ Como $\frac{\partial}{\partial \Theta} \left[\frac{\vec{z}}{\sqrt{a^2 + \vec{z}^2}} \right] = 0$, entences $\vec{z}/\sqrt{a^2 + \vec{z}^2}$ es etc. $\frac{1}{\sqrt{a^2+2^2}} = C \Rightarrow \frac{1}{2} = \frac$ = ac

$$\frac{7}{1 - \alpha^{2}} = \frac{3}{1 -$$

Solvaión 4

un cuerpo se dega coe desde una assura h y areanser el suero en on trempo T. la ecuación de monmovo y=h-g,t- y=h-1 92t2 y=h-1 92t3 remostrar que un forma correctures aquera me podoce er vavor de minima acción. a) trayectoria 1 y = h-g,t (1) el lagrangiaro de acción pora cooa caso está dado L=T-V= 1 my2 - mgy Para travectoria , se tee ij = -91 por tento s, = 5 2m (-9,)2 - mg (h-9, E) dE 51 = 1 mg2 t - mg (ht - 1 9, 6) (= 1 mg; t+ - mg (ht, - 19 t2)

abolic bien debenos three en cuenter ros conticiones iniciou 5

0= 7(0) = -9, => 9,=0

> 5 = -mght =: 5 = -mgh (b)

por (1) pora y= h = 6

n- 1292 12 (2) > 9 = - 192.26 => L= 1 m (-92+)2 -mg(h-1292+2) => J2 = 5te +2 mg2 +2 - mgh + + mst292 = 1 mg2 t3 - mght + 1 mgg2 t3 6 ÿ (0) = -9 = -92 ° 92 = 9. => S2 = mB2 to (92+9) - mghte = 2 mg2 tg - mghta. y=6 se tiene 0=h-19262 t = 52h 52= 2mg2 (2h)3/2 - mgh (2h)1/2

73 = -3.93t. >> L= 1 m (-3 93 t2)2 - mg (h- + 93 t3) 53 = 5 (9 mg (h - 4 93 t3)) de = 9 mg3 to - mghto + 1 mg 33to -9= 3(t) =- 6 93t :. 93 = 39 t 0=h-493 to te= (4h) 1/3 =7 93 = (2 3 (4 h) 1/3) 3/2 reamos que se habia concivido: S, = -mgh () con 9, = 0 \$ 1.m 55 - - 20

sin importa h, m & es - x ahora her si h= 10 m g= 9,8 m/2 m= 1 kg 4e tendría que: para la trajectoria 2 como 9,29 $\Rightarrow 5_2 = 2 (1) (4.8)^2 \left(2 (10) \right)^{3/2} - (4)(4.8) \left(\frac{2 \times 10}{4.8} \right)^{1/2}$ 1 52 00-4 6.66. y para la trayectoria 3. $9_3 = (2 - 9_3)^{3/2}$ 9, 22.64. Y to = (4(10) 1/3 & 247. 83 = 9 (1) (2.64)2 (2.49) - (1)(9.8)(10) (2.44) + 1 (9.8) (2.64) (2.43)4 153 2 -14.5.83 ses un extremo de todos que acciones por tanto se compie con ia forma correcta poes 91 crear ex lagrangiaro de res conta libre se

> my + xg = 0 > 5 = -9 regultado =>) \quad = \left - g \cdot + c_1 -> \quad \quad \cdot = -9\cdot^2 + c_1\cdot + c_2 y=h => C2=h y Porce Para i(0) =0 > C,=0 · of y(t) = -9t2 + h que se comobara con el car colo de la acción de la travectoria. or to travectoria 2 genera es extremo de la acción.

Lagrangiano de una función. Let-V 3: L= m° x" + m x²p(x) - f²(x), mol e. lee lenumes de (31) - 31 = 0 (2)(0)(2) 04 07/14 * 21 = m2 4 x3 + mf(x) + m x 2f(n) - 2x - 2f(4) 2x $\frac{21}{2x} = \frac{m^2}{3}x^3 + 2mxf(x)$ * \frac{1}{32} = \frac{m^2}{3} 3 \hat{x}^2 \hat{x} + 2m \hat{x} f(x) + 2m \hat{x} f(x) \hat{x} = \frac{m^2}{3} \hat{x}^2 \hat{x} + 2m \hat{x} f(x) * 31 = mx fcx) - 2fcx) fcx) => mx x x + 2mx f(x) + 2mx f(x) - mx2f(x) + 2f(x) f'(x) = 0 X (m2 x3 + sw t(x)) + swx f(x) - wx, t(x) + s t(x) t, (x) = 0 xm(mx2+2fcx)+f'(x)[2mx2-mx2+2f(x)]=0 Xm = - f'(x) [2mx2-mx2+ 2x(x)] m x² + 2 f(x)

Soloción 6.

denostral que s' L= 1 3ab (9c) 996 (1)

=> qq+ Tq qbqc=0

donde 19 = 1 9 2d (29 6d + 29 cd - 25 6c)

a postris des lagrangearo (1) obermos las ecuaciones de evier lagrange

 $\frac{d}{de}\left(\frac{\partial Z}{\partial \dot{q}^{\alpha}}\right) - \frac{\partial Z}{\partial \dot{q}^{\alpha}} = 0$

7 2 (½ 9 cb (9c) 9 9 9) = 1 9 cb (3 9 9 4 9 9 7)

= 1 9 00 [8 9 + 9 5] = 1 9 0 8 9 + 1 9 0 6 6

= \frac{1}{2} Sab q³ + \frac{1}{2} Sca q⁴ c et on indice libre

- 2 9ab 9 + 2 9 6a 9

usardo la mipotegis Sab = Oba

= 1 9 9 9 4 1 9 9 9 = 9 9 9 9

de (32) = d (9a, q0) = 2 9as qq 1 9as q 6 = 12 3360 96 90 29 4 9 4 9 4 9 4 9 4 9 4 6 = 0 9 ab 9 + 9 c 9 (2 9ab - 1 2 3bc) = 0 me it i pricando amnos judos por izquierda por ga gda gas gb + gc gb gda (23ab - 1,29bc) =0 8 g g + 1 g g g g da (2 2 3 gab - 3 g bc) -0

