

$$\begin{cases} Qx - A^T \mu = -r_x \\ Ax - y = -r_y \\ Uy + Y\mu = -r_\mu \end{cases}$$

$$(2) \Rightarrow y = Ax + r_y$$

$$(3) \Rightarrow Y\mu = -r_\mu - Uy = -r_\mu - U(Ax + r_y)$$

$$\Rightarrow \mu = -Y^{-1}[r_\mu + U(Ax + r_y)]$$

$$\Rightarrow A^T \mu = -\underbrace{A^T Y^{-1} r_\mu}_{?} - \underbrace{A^T Y^{-1} U Ax}_{\checkmark} - \underbrace{A^T Y^{-1} U r_y}_{\checkmark}$$

$$(1) \Rightarrow Qx = -r_x + A^T \mu$$

$$\Rightarrow Qx + A^T Y^{-1} U Ax = -r_x - \underbrace{A^T Y^{-1} r_\mu}_{\checkmark} - \underbrace{A^T Y^{-1} U r_y}_{\checkmark}$$

$$\Rightarrow \underbrace{(Q + A^T Y^{-1} U A)}_{\checkmark} x = -(r_x + \underbrace{A^T Y^{-1} r_\mu}_{\checkmark} + \underbrace{A^T Y^{-1} U r_y}_{\checkmark})$$