Homework 5 Optimization, Integration, and Library Upkeep Due Nov 27, 2021

1: The golden-section search and parabolic interpolation

Consider the following function:

$$f(x) = x^4 + 2x^3 + 8x^2 + 5x$$

- (a) Use an analytical and/or graphical method to show the function has a minimum for some value of x in the domain $-2 \le x \le 1$.
- (b) Use the golden-section search with $x_1 = -2$, $x_2 = 1$, tol = 1%. Report the minimum.
- -0.34711191
- (c) Use parabolic interpolation with $x_1 = -2$, $x_2 = -1$, and $x_3 = 1$ for 5 iterations. Report the minimum.
- -0.34725047

2: The composite trapezoid rule

Add the Composite Trapezoid Rule to your library in a new class "Integration". Use it to determine the distance fallen by the free-falling bungee jumper in the first 3 seconds by evaluating the integral of

The second
$$v(t) = c_d tanh$$
 derivative of $v(t)$ r_{gm} $r_{gc_d m} t$ is
$$-2g^{3/2} \qquad t \qquad sech^2 \quad r_{cg m}$$

$$r_{c} \qquad m tanh \quad r_{cg m}$$

$$v''(t) = \qquad t$$

which is used to find the average of the second derivative $_0$ –2 $g^{3/2}$ p

$$\underbrace{\frac{c}{mtanh}}_{tq} \underbrace{\frac{cg}{m}}_{sech} \underbrace{\frac{cg}{tq}}_{m}$$

$$R_{3}$$

$$v''(t) = \underbrace{\frac{cg}{mtanh}}_{3-0} \underbrace{\frac{cg}{tq}}_{m}$$

Apply the recursive composite trapezoid rule to this problem with a tolerance of 0.00001, and the following parameter values: g = 9.81 m/s2, m = 68.1 kg, and $c_d = 0.25$ kg/m. Report

- 1. the distance fallen by the free-falling bungee jumper \rightarrow 41.9480426
- 2. the number of segments needed to reach the tolerance \rightarrow 512

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3: The composite Simpson's 1/3 rule

 R_3

Add the Composite Simpson's 1/3 Rule to your library in the appropriate class. Use it to determine the distance fallen by the free-falling bungee jumper in the first 3 seconds by evaluating the integral of

The fourth
$$v(t) = c_d tanh$$
 derivative of $v(t)$ r_{gm} $r_{gc_d m} t$ is r_{gm} $r_{gc_d m} t$ $r_{gc_d m} t$

which is used to find the average of the fourth derivative

NOTE: The average value for the 4th derivative is a positive value so you will have to change the if statement in your code to if (abs(error)>tol) to for your recursion code to work since $E_a < 0$. You should change this in both methods for your code to be robust.

Apply the recursive composite Simpson's 1/3 rule to this problem with a tolerance of 0.00001, and the following parameter values: g = 9.81 m/s2, m = 68.1 kg, and $c_d = 0.25$ kg/m. Report:

- 1. the distance fallen by the free-falling bungee jumper \rightarrow 41.9480541
- 2. the number of segments needed to reach the tolerance \rightarrow 16

4: Integrating a data set

You've just been handed a set of experimental data to integrate, xData and fxData.

(a) Of the methods we've covered during lecture for integrating sets of data, which method would you choose use to integrate this data set? Why?

Since we are given the premade data files, I would choose the Data Trapezoid function. I could use the Data Simpson function as well but since we have to write the data in a list for that one I would rather use Data Trapezoid. Also, since the data points are NOT equispaced using Data simpsons would give us an inaccurate result.

(b) Apply the method you chose to the set of data provided with this assignment. Report the integral value (sum). 1.91124932

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5: Submit Your Library

By this point in time your library should contain the following routines:

- The Bisection method,
 Bisect(double a, double b, double tol, double (*f)(double x))
- Newton-Raphson method, NewtonRaphson(double a, double tol, double maxit, double (*f)(double x), double (*df)(double x))
- Golden-Section Search Method,
 GoldenSectionSearch(double xu, double xl, double tol, double (*f)(double x))
- Parabolic Interpolation,
 ParabolicInterpolation(double x1, double x2, double x3, double tol, double (*f)(double x))
- The Recursive Trapezoid Rule for functions,
 CompositeTrapezoid(double a, double b, int n, double avgdf2, double tol, double (*f)(double

x))

- Recursive Simpson's 1/3 Rule for functions,
 CompositeSimpsons13(double a, double b, int n, double avgdf4, double tol, double (*f)(double x))
- Simpson's Rules for data,
 DataSimpsons(double data[], double x[], int n)
- Trapezoid Rule for data,
 DataTrapezoid(vector<double> x, vector<double> fx, int n)

Make sure that these routines work by testing them on the functions we covered in class, if they are not working you will not receive full credit for them. You are not required to submit any output for these tests, but we will check them to make sure they are working.

6: Submission Details

Only the functions used for Questions 1 and 3 of this assignment should be defined within your Main.cpp. Within the main function of your Main.cpp, you should be only be calling

- 1. GoldenSectionSearch
- 2. ParabolicInterpolation
- 3. CompositeTrapezoid
- 4. CompositeSimpsons13
- 5. DataSimpsons

with their appropriate parameters and reporting their returned values. Submit your entire SciProgLib folder as a .zip file.