

$$3) X(t) = \sum a_n \cos(n\omega_0 t) + b_n \sin(n\omega_0 t)$$

$$X'(t) = \sum a_n \frac{d}{dt} \{ \cos(n\omega_0 t) \} + b_n \frac{d}{dt} \sin(n\omega_0 t)$$

$$X'(t) = \sum a_n (-\sin(n\omega_0 t) n\omega_0) + b_n \cos(n\omega_0 t) n\omega_0$$

$$X''(t) = \sum a_n \cos(n\omega_0 t) (-n\omega_0)^2 + b_n \sin(n\omega_0 t) (-n\omega_0)^2$$

$$= \sum (-a_n n^2 \omega_0^2) \cos(n\omega_0 t) + (-b_n n^2 \omega_0^2) \sin(n\omega_0 t)$$

$$\hat{a}_n = \frac{2}{T} \int x''(t) \cos(n\omega_0 t) dt$$

$$-a_n n^2 \omega_0^2 = \hat{a}_n = \frac{2}{(t_i - t_f) n^2 \omega_0^2} \int x''(t) \cos(n\omega_0 t) dt$$

$$b_n = \frac{2}{(t_i - t_f) n^2 \omega_0^2} \int x''(t) \sin(n\omega_0 t) dt$$