

$$2) f_s = 5 \text{ kHz} \quad X(t) = 3 \cos(1000\pi t) + 5 \sin(3000\pi t) + 10 \cos(11000\pi t)$$

$$T = 1/f_s = \frac{1}{5000}$$

$$\omega_1 = 1000\pi \text{ ( )}; T_1 = 2\pi/\omega_1 = \frac{2\pi}{1000\pi} = \frac{1}{500}$$

$$\omega_2 = 3000\pi; T_2 = 2\pi/\omega_2 = \frac{2\pi}{3000\pi} = \frac{1}{1500}$$

$$\omega_3 = 11000\pi; T_3 = 2\pi/\omega_3 = \frac{2\pi}{11000\pi} = \frac{1}{5500}$$

$$\frac{\omega_1}{\omega_2} = \frac{\frac{1}{500}}{\frac{1}{1500}} = \frac{1500}{500} \in \mathbb{Q}$$

$$\frac{\omega_1}{\omega_3} = \frac{5500}{500} \in \mathbb{Q} \quad \frac{\omega_2}{\omega_3} = \frac{1500}{5500} \in \mathbb{Q}$$

$$f_1 = 1/T_1 = \frac{1}{500} = 500 \text{ Hz} \quad f_2 = 1500 \text{ Hz}$$

$$f_3 = 5500 \text{ Hz}$$

$$f_s \geq 2 \max(f_1, f_2, f_3) \quad f_s \geq 2 \cdot 5500$$

$$\boxed{f_s \geq 11000 \text{ Hz}} \quad \text{aliasing}$$



$$T = Y T_1 = l T_2 = m T_3 = M (M(T_1, T_2, T_3))$$

$$T = Y \frac{1}{500} = l \frac{1}{1500} = m \frac{1}{5500}$$

$$5500 T = Y \frac{5500}{500} = l \frac{5500}{1500} = m 1$$

$$5500 T = Y 11 = 0 11/3 = m 1$$

$$16500 T = Y 33 = 11 = m 3$$

$$MCM(33, 11, 3) = 33 \quad Y=1 \quad m=11 \quad l=3$$

$$16500 T = 33$$

$$T = 33 / 16500 = 1/500 (s)$$