

• El sistema masa-resorte y amortiguador se puede modelar a partir de la conservación de fuerzas:

$$F_s(t) + F_f(t) + F_I(t) = F_E(t)$$

Donde:

• $F_s(t)$ (Fuerza del resorte)

$$F_s(t) = K y(t)$$

K = Constante del resorte

$y(t)$ = desplazamiento de la masa

• $F_f(t)$ (Fuerza del amortiguador)

$$F_f(t) = c \frac{dy(t)}{dt}$$

• Fuerza inercial (masa)

$$F_I(t) = m \frac{d^2 y(t)}{dt^2}$$

Por consiguiente

$$m \frac{d^2 y(t)}{dt^2} + c \frac{dy(t)}{dt} + ky(t) = F_E(t) = X(t)$$

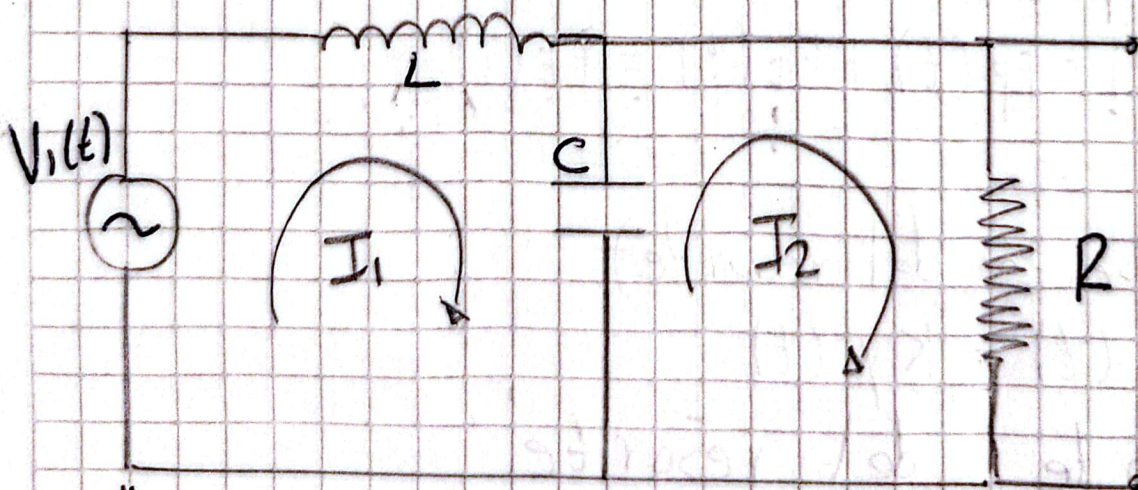
Aplicando transformada de Laplace

$$\mathcal{L}\left\{\frac{d^2 X(t)}{dt^2}\right\} = S^2 X(s)$$

$$m S^2 Y(s) + c S Y(s) + k Y(s) = X(s)$$

$$H(s) = \frac{Y(s)}{X(s)} = \frac{1}{ms^2 + cs + k}$$

Para el circuito



Malla 1

$$V_i(t) = L \frac{d\bar{i}_1(t)}{dt} + \frac{1}{C} \int \bar{i}_1(t) - \bar{i}(t) dt$$

Pasando a Laplace

$$V_i(s) = L s \bar{i}_1(s) + \frac{1}{Cs} (\bar{i}_1(s) - \bar{i}_2(s))$$

Malla 2

$$\phi = \frac{1}{C} \int (\bar{i}_2(t) - \bar{i}_1(t)) dt + R \cdot \bar{i}_2(t)$$

Pasando a Laplace

$$V_{i2}(t) = \frac{1}{Cs} (\bar{i}_2(s) - \bar{i}_1(s)) + R \cdot \bar{i}_2(s)$$

Despejando $\bar{i}_1(t)$

$$\bar{i}_1(s) = \bar{i}_2(s) (1 + CRs)$$

Se reemplaza en la entrada:

$$V_i(t) = L s \bar{i}_2(s) (1 + CRs) + (\bar{i}_2(s) (1 + CRs) - \bar{i}_2(s)) \frac{1}{Cs}$$

$$V_i(t) = L s \bar{i}_2(s) + CR s^2 \bar{i}_2(s) + \bar{i}_2(s) \frac{1}{Cs} + \bar{i}_2(s) R - \bar{i}_2(s) \frac{1}{Cs}$$

$$V_i(s) = \bar{i}_2(s) (CRLs^2 + Ls + R)$$

$$\frac{\bar{i}_2(s)}{V_i(s)} = \frac{1}{CRLs^2 + Ls + R}$$

$$R \bar{i}_2(s) = V_o(s) = \frac{R}{CRLs^2 + Ls + R}$$

$$= H(s) = \frac{V_o(s)}{V_i(s)} = \frac{1}{CLs^2 + \frac{L}{R}s + 1}$$