

# Card Trick

I am learning magic tricks to impress my girlfriend Alice. My latest trick is a probabilistic one, i.e. it does work in most cases, but not in every case. To perform the trick, I first shuffle a set of many playing cards and put them all in one line with faces up on the table. Then Alice secretly selects one of the first ten cards (i.e. she chooses  $x_0$ , a secret number between 1 and 10 inclusive) and skips cards repeatedly as follows: after having selected a card at position  $x_i$  with a number  $c(x_i)$  on its face, she will select the card at position  $x_{i+1} = x_i + c(x_i)$ . Jack (J), Queen (Q), and King (K) count as 10, Ace (A) counts as 11. You may assume that there are at least ten cards on the table.

Alice stops this procedure as soon as there is no card at position  $x_i + c(x_i)$ . I then perform the same procedure from a randomly selected starting position that may be different from the position selected by Alice. It turns out that often, I end up at the same position. Alice is very impressed by this trick.

However, I am more interested in the underlying math. Given my randomly selected starting position and the card faces of every selected card (including my final one), can you compute the probability that Alice chose a starting position ending up on the same final card? You may assume that her starting position is randomly chosen with uniform probability (between 1 and 10 inclusive).

I forgot to note the cards that I skipped, so these cards are unknown. You may assume that the card face of every single of the unknown cards is independent of the other card faces and random with uniform probability out of the possible card faces (i.e. 2-10, J, Q, K, and A).

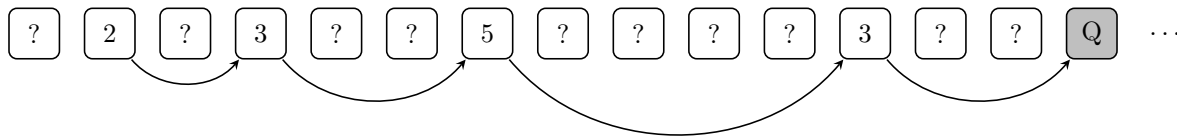


Figure 1: Illustration of first sample input: my starting position is 2, so I start selecting that card. Then I keep skipping cards depending on the card's face. This process iterates until there are not enough cards to skip (in this sample: Q). The final Q card is followed by 0 to 9 unknown cards, since Q counts as 10.

## Input

The first line of the input contains an integer  $t$ .  $t$  test cases follow, each of them separated by a blank line.

Each test case consists of:

- A line containing two integers  $n$  and  $m$  where  $n$  is the number of selected cards and  $m$  is the 1-based position of my first selected card.
- A line with  $n$  tokens that specify the  $n$  selected card faces (in order, including the final card). Each card face is given either as an integer  $x$  ( $2 \leq x \leq 10$ ) or as a single character (J, Q, K, or A as specified above).

## Output

For each test case, print a line containing “Case # $i$ :  $y$ ” where  $i$  is its number, starting at 1, and  $y$  is the probability that Alice chooses a starting position that leads to the same final card.

Your output should have an absolute error of at most  $10^{-7}$ . Each line of the output should end with a line break.

## Constraints

- $1 \leq t \leq 30$
- $1 \leq n \leq 100$
- $1 \leq m \leq 10$

**Sample Input 1**

```
7
5 2
2 3 5 3 Q

1 1
A

1 2
A

1 10
A

6 1
2 2 2 2 2 2

7 1
2 2 2 2 2 2 2

3 10
10 J K
```

**Sample Output 1**

```
Case #1: 0.4871377757023326
Case #2: 0.1
Case #3: 0.1
Case #4: 0.1748923357025314
Case #5: 0.5830713210321767
Case #6: 0.627922961111575
Case #7: 0.33465658276032717
```