

Metodo simplex

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1. $2x + y \leq 5$

Max $4x + 6y = z$

| | x | y | s1 | R |
|----|----|---|----|---|
| S1 | 2 | 1 | 1 | 5 |
| Z | -4 | 0 | 0 | 0 |

variable y sale ingresa sale variable s1

$s1 \rightarrow y$

| | x | y | s1 | R |
|---|---|---|----|----|
| y | 2 | 1 | 1 | 5 |
| Z | 0 | 0 | 6 | 30 |

La solución más optima es $z=30, x=0, y=5, s1=0$

2. Min $8x - 16y = P$
 $x + 3y \geq 11$

Fase 0

| | x | y | s1 | A1 | R |
|----|---|---|----|----|----|
| A1 | 1 | 3 | -1 | 1 | 11 |
| P | 1 | 3 | -1 | 0 | 11 |

Fase 1

| | x | y | s1 | A1 | R |
|---|-----|---|------|-----|------|
| y | 1/3 | 1 | -1/3 | 1/3 | 11/3 |
| P | 0 | 0 | 0 | -1 | 0 |

Fase 2

| | x | y | s1 | R |
|---|------|---|-------|-------|
| y | 1/3 | 1 | -1/3 | 11/3 |
| P | -8/3 | 0 | -16/3 | 176/3 |

solución factible

$P = 176/3$

$x=0, y=11/3, s1=0$

3. Max $P = 10x + 6y$

$2x + y \geq 3$

$2y - 1 \geq 0$

$x \geq y$

| | x | y | s1 | s2 | s3 | A1 | A2 | R |
|----|----|---|----|----|----|----|----|---|
| A1 | 2 | 1 | -1 | 0 | 0 | 1 | 0 | 3 |
| A2 | 0 | 2 | 0 | -1 | 0 | 0 | 1 | 1 |
| S3 | -1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 |
| P | 2 | 3 | -1 | -1 | 0 | 0 | 0 | 4 |

Iteración 1.

| | x | y | S ₁ | S ₂ | S ₃ | A ₁ | A ₂ | R |
|----------------|----|---|----------------|----------------|----------------|----------------|----------------|---|
| A ₁ | 3 | 0 | -1 | 0 | -1 | 1 | 0 | 3 |
| A ₂ | 2 | 0 | 0 | -1 | -2 | 0 | 1 | 1 |
| y | -1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 |
| P | 5 | 0 | -1 | -1 | 3 | 0 | 0 | 4 |

Iteración 2

| | x | y | S ₁ | S ₂ | S ₃ | A ₁ | A ₂ | R |
|----------------|---|---|----------------|----------------|----------------|----------------|----------------|-----|
| A ₁ | 0 | 0 | -1 | 3/2 | 2 | 1 | -3/2 | 3/2 |
| x | 1 | 0 | 0 | -1/2 | -1 | 0 | -1/2 | 1/2 |
| y | 0 | 1 | 0 | -1/2 | 0 | 0 | 1/2 | 1/2 |
| P | 0 | 0 | -1 | 3/2 | 2 | 0 | -5/2 | 3/2 |

| | x | y | S ₁ | S ₂ | S ₃ | A ₁ | A ₂ | R |
|----------------|---|---|----------------|----------------|----------------|----------------|----------------|-----|
| S ₃ | 0 | 0 | -1/2 | 3/4 | 1 | 1/2 | -3/4 | 3/4 |
| x | 1 | 0 | -1/2 | 1/4 | 0 | 1/2 | -1/4 | 5/4 |
| y | 0 | 1 | 0 | -1/2 | 0 | 0 | 1/2 | 1/2 |
| z | 0 | 0 | 0 | 0 | 0 | -1 | -1 | 0 |

Segunda fase:

| | x | y | S ₁ | S ₂ | S ₃ | R |
|----------------|---|---|----------------|----------------|----------------|------|
| S ₃ | 0 | 0 | -1/2 | 3/4 | 1 | 3/4 |
| x | 1 | 0 | -1/2 | 1/4 | 0 | 5/4 |
| y | 0 | 1 | 0 | -1/2 | 0 | 1/2 |
| z | 0 | 0 | -5 | -3/2 | 0 | 33/2 |

La solución al problema es limitada debido a que si debería entrar pero no hay alguna variable pueda ser sustituida

4. $\text{Max } 24x + 32y = z$

$2x + 3y \leq 60$

$x \geq 0$

$y \geq 0$

| | x | y | S ₁ | R |
|----------------|-----|-----|----------------|----|
| S ₁ | 2 | 3 | 1 | 60 |
| z | -24 | -32 | 0 | 0 |

| Iteración 1 | x | y | S ₁ | R |
|-------------|------|---|----------------|-----|
| y | 2/3 | 1 | 1/3 | 20 |
| z | -8/3 | 0 | 32/3 | 640 |

| Iteración 2 | x | y | S ₁ | R |
|-------------|---|-----|----------------|-----|
| x | 1 | 3/2 | 1/2 | 30 |
| z | 0 | 4 | 12 | 720 |

La solución óptima es $z = 720$,
 $x = 30$, $y = 0$, $S_1 = 0$

$$\text{Max } Z = 2x - 4y$$

$$2x - 4y \leq -4$$

$$x_1, x_2 \geq 0$$

$$-2x_1 + 4y - 1s_1 + 1A_1 = 4$$

Primera fase

| | x | y | s ₁ | A ₁ | R |
|----------------|----|---|----------------|----------------|---|
| A ₁ | -2 | 4 | -1 | 1 | 4 |
| Z | -2 | 4 | -1 | 0 | 4 |

Iteración 1

| | x | y | s ₁ | A ₁ | R |
|---|------|---|----------------|----------------|---|
| y | -1/2 | 1 | -1/4 | 1/4 | 1 |
| Z | 0 | 0 | 0 | -1 | 0 |

Segunda fase

| | x | y | s ₁ | R |
|---|------|---|----------------|----|
| y | -1/2 | 1 | -1/4 | 1 |
| Z | 0 | 0 | 1 | -4 |

La solución óptima es
 $Z = -4$, $x = 0$, $y = 1$, $s_1 = 0$