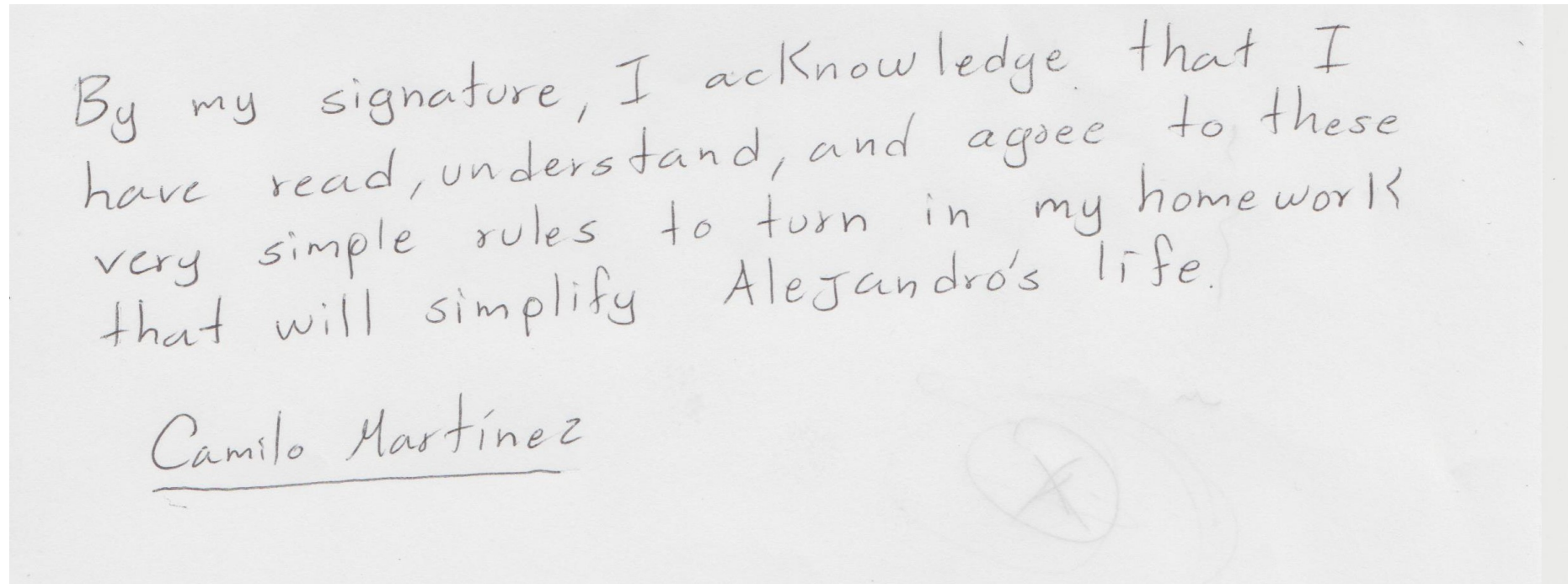


Programming

```
In [57]: from IPython.display import Image  
Image("signature.jpg")
```

Out[57]:



1.

```
In [47]: import numpy as np  
  
def obtain_lucas_numbers_by_an_n(n):  
    L = np.zeros(n)  
    L[0], L[1] = 1, 3  
  
    for i in range(2, n):  
        L[i] = L[i-1] + L[i-2]  
  
    return L
```

2.

Answer:

If we take into account that around 10^8 operations last about 1 second, and that **obtain_lucas_numbers_by_an_n** is $O(n)$, then we could make some approximation that in one hour it can calculate about $3 * 10^{10}$ lucas numbers. That's just taking into account the time, however if it reach the maximum memory before completing the hour it would be less. For the purpose of the point, I built another function that doesn't store the lucas numbers, instead it just return the last lucas number it could calculate along with the index of that number for a given amount of minutes. Also, because of my memory is not so big then I just can store about 10^4 numbers. Those are the ones of the plot I show below.

[Github link of the repository \(https://github.com/Andresmps/Simulation-class\)](https://github.com/Andresmps/Simulation-class)

```
In [55]: n = 10**5  
lucas_numbers = obtain_lucas_numbers_by_an_n(n)
```

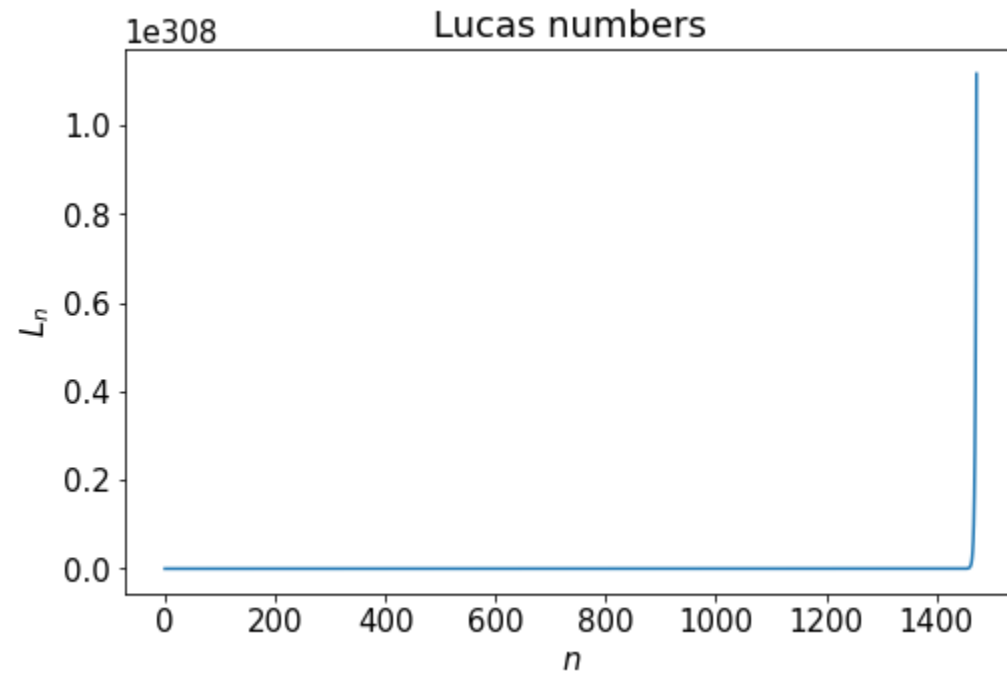
```
C:\Users\camil\anaconda3\lib\site-packages\ipykernel_launcher.py:8: RuntimeWarning: overflow encountered in double_scalars
```

```
In [56]: plt.figure(figsize=(8, 5))
plt.rc('font', size=15)
plt.title('Lucas numbers')
plt.xlabel('$n$')
plt.ylabel('$L_n$')
plt.plot(lucas_numbers)
```

```
Out[56]: [<matplotlib.lines.Line2D at 0x2c4ddd31348>]
```

C:\Users\camil\AppData\Roaming\Python\Python37\site-packages\matplotlib\ticker.py:2234: RuntimeWarning: overflow encountered in multiply

steps = self._extended_steps * scale



```
In [34]: from datetime import datetime
import matplotlib.pyplot as plt

def obtain_lucas_numbers_by_given_minutes(minute):
    try:
        flag = True
        previos_lucas_number_1, previos_lucas_number_2 = [1, 3]
        start_time = get_minutes()
        i = 0

        while flag == True:
            temp = previos_lucas_number_1 + previos_lucas_number_2
            previos_lucas_number_1 = previos_lucas_number_2
            previos_lucas_number_2 = temp
            i += 1
            time = get_minutes()
            if time - start_time >= minute: break

        return previos_lucas_number_1, i+1
    except Exception as e:
        print(f"Error: {e}")
        print(f"Amount of Lucas numbers calculate: {len(L)}")
        return L

def get_minutes():
    time = datetime.now()
    return (time.hour * 60) + time.minute
```

In [35]: %time

```
lucas_numbers = obtain_lucas_numbers_by_given_minutes(1) # Last Lucas number in one minute
lucas_numbers # (Lucas number, index)
```

```
6238429164245303647048033740540027727699674991914538940999643036641643818513290806522906904472664325997380278435814124
7420760346506839150352163354569694397570848633020277367351070836484405434794528287647396986985479032029564485738696979
4216868199784934404380613419093178572619229363598006147775648907028921859850617068440954569185586616474627397417045669
2163122418478632913876219508807595589651988308928167633232649591568792521878429433144347395591932546117540147687842630
9211877697935154314609929043780818864923073568063444152193531182435936392164763241861539363846291713206507665076851852
7981775106817372693525977366210152512776996516948506660945069875542640459037371232877241667977484533139862956845357369
4376058890959135734229258804505176221887528339490303863670304147625206978465177395884561458372414968748374374279746244
4788014660639705506085921706064925385511899528239306014687472759059753846957704313681819384186464163301132101150683051
1311922423119753158617495746763992502416900245139299348182841474153751043894696320130397589893631791093195428477856376
9392235291010498697665541039596511283852997471251190076459101677507341850607654375476757490524719936876594060175570468
7248951669068735088482047868333412549948653254471879934421312933083529818774712058512827845801754348683386300782451173
4045057209868484232025153768394279629816198190490404675759504894447269809875356035533740312384150675286567727156145374
0823181901968511875820813003024018793334922579567886937101071930934446824423405448677585400073621105080909250747338738
2616301692914010537273891519337015973188355402631540487237427196635960687794614217129463389781341999635341102125116402
7113720860968439421664227191700985960321949670355658711793394220301203664460502484088580221141694905483722169091478808
2440992182042145850947406956821801672377898128034691378443148293556409733343195454282379724952643704083259410738164346
0715787094490110553466833815480060880981349643296218944549459648723954242146325778106122586152225333992531101922314303
3949340849762216720012567735012902448794221079375346342612079170281596013821181630357881720045145153901711562387590029
9474790490463331564415697603520954522444045514955866877867364259737304911771057995081813873485446801331565704581767880
```

In []: