UWES R Workshop: Applied Econometrics in R

Andrew Girgis

University of Waterloo

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Discord



Figure 1: Discord QR Code

Overview

By the end of today's Presentation you will(hopefully) have a better understanding of:

- The Data Journey
- Data Visualization
- Regression
- Economic Insights

The Data Journey



Supported by a foundation of stewardship, metadata, standards and quality

Figure 2: The Data Journey¹

¹(Government of Canada 2021)

For today's presentation we will be studying what features can affect a students final grade. First we define our problem.

Objective: To derive what impact important features has on a students final grade.

- Now that we have defined our problem the next step in the data journey is to find and gather our data. For this I will be using a free dataset from the UC Irvine machine learning repository².
- The dataset I will be using is the Student Performance dataset that can be found at archive.ics.uci.edu/dataset/320/student+performance.
- Other sources for free data:
 - Kaggle
 - Statistics Canada
 - US Federal Government Data
 - FRFD Economic Data

Import libraries

Libraries (also known as packages) in R are collections of functions, data sets, and other code that extend the functionality of the base R language. They can be downloaded and installed onto your machine using the install.packages() function, then loaded into your R session using the library() function.

```
# install.packages('readr')
library(readr)
library(plyr)
library(dplyr)
library(ggplot2)
library(tidyverse)
library(GGally)
library(stargazer)
```

Import data

To import data we use the function read_csv() from the readr library.

```
#data_path = '[insert your path here]'
#student df = read csv(data path)
```

- We use the head() function to view the first 6 lines of our data.
- Ensure the data was imported properly.
- Ensure the variables and values make sense.

head(student_df[1:7])

```
## # A tibble 6 x 7
##
     school sex
                     age address famsize Pstatus
                                                     Medu
                                  <chr>
##
     <chr> <chr> <dbl> <chr>
                                           <chr>>
                                                    <dbl>
## 1 GP
                                  GT3
            F
                      18 U
                                           Α
                                                        4
## 2 GP
            F
                      17 U
                                  GT3
            F
   3 GP
                      15 U
                                  LF.3
            F
## 4 GP
                      15 U
                                  GT3
            F
## 5 GP
                      16 U
                                  GT3
## 6 GP
            M
                      16 U
                                  LE3
```

- After viewing the data we must understand the data.
- Some variables may be hard to interpret.
- See this link for full description of data.
- After viewing the descriptions of all the feature variables³ I have choosen to focus on the following variables: absences, higher, activities, studytime, schoolsup, reason, address, sex, age, Pstatus
- For simplicity we will be using the target variable ⁴ G3 for this regression.

³Feature Variables: Variables that will be used as the independents for the regression (predictors for the target variable).

⁴Target Variable: Variable that will be used as our dependent in the regression.

- Summary() is an incredibly useful function!
- Changes its output based on the input. If you input a list(column) the summary function will output basic summary stats. If you input an object(regression) the summary function will output important regression results/statistics.

```
summary(student df["age"])
```

```
##
        age
##
   Min. :15.0
##
  1st Qu.:16.0
   Median:17.0
##
   Mean :16.7
##
##
   3rd Qu.:18.0
   Max. :22.0
##
```

- Table is a great way to get an overview of non-numeric variables.
- Provides a count of the unique values in the dataset.

```
table(student_df[2])
```

```
## sex
     F
##
## 208 187
```

```
table(student df["Mjob"])
```

```
Mjob
   at home
             health
                      other services teacher
##
##
        59
                 34
                         141
                                  103
                                            58
```

Although we wont be using Mjob as a variable in our regression, I would like to show what the table function outputs with a non-binary categorical variable.

- From the UC Irvine Machine Learning Repository we see that this dataset contains no missing values. However we can confirm that this is true.
- Depending where you gather your data you may not know whether there are missing values so it is considered good practice to always inspect and clean your data.

```
# Check for NA values in the entire data
# frame
sum(is.na(student df))
## [1] 0
# Check for NA values in specific columns
# (e.g., age column)
sum(is.na(student df$age))
```

As an example I will input a NA value in the data.

student_df[124, 23] <- NA

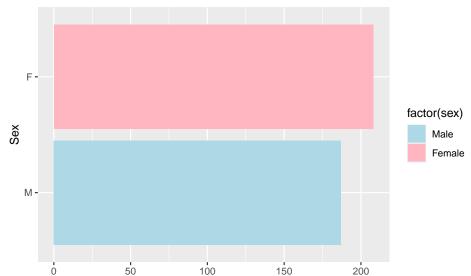
```
# Check for NA values in the entire data
# frame
any(is.na(student_df))
## [1] TRUE
# Find row and column indices with NA values
na locations <- which(is.na(student df), arr.ind = TRUE)
na locations
## row col
```

[1,] 124 23

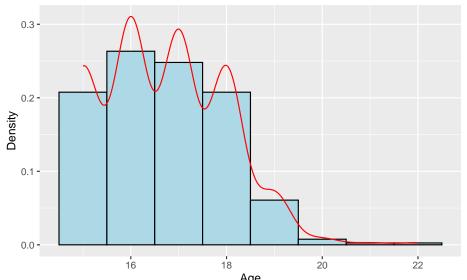
• Finally we will filter our data to hone in on the variables we want to focus on.

```
filtered_df <- student_df %>%
    select(absences, higher, activities, studytime,
        schoolsup, sex, age, G3)
```

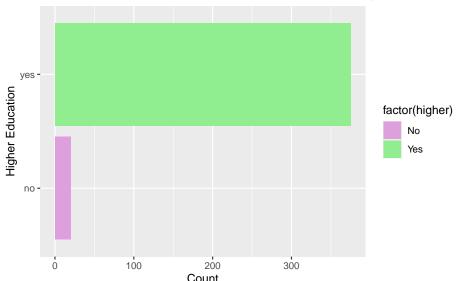




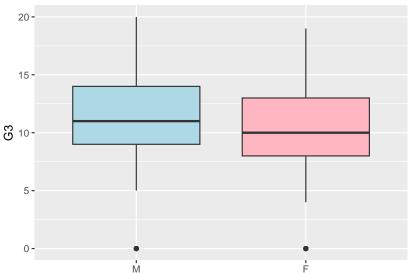
Histogram of Age with density curve



Horizontal Bar Plot of students who want to pursue higher education



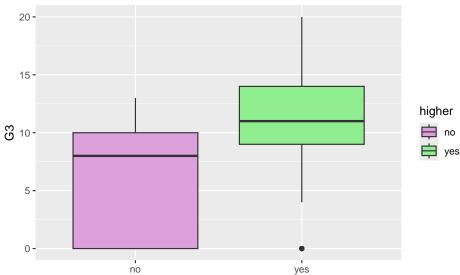
Boxplot of Flnal Average by Sex



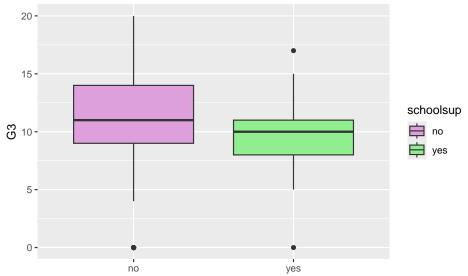
sex



Boxplot of G3 by Higher Education Aspiration



Boxplot of G3 vs wheter a student is getting extra help



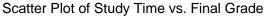
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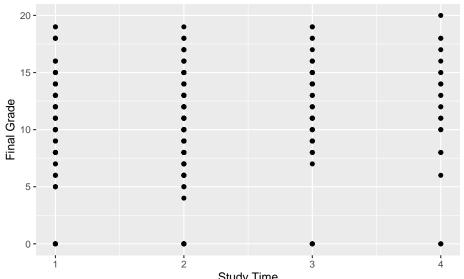
Lets look into this

```
table(filtered_df$schoolsup)
```

```
##
##
    no yes
## 344 51
```

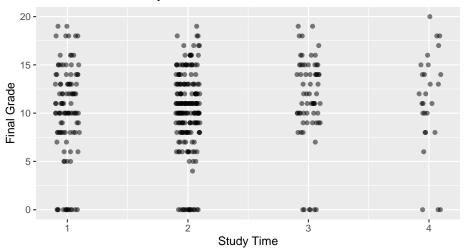
- The lower average can be explained by multiple factors including the smaller sample, the quality in the extra support or the students natural ability.
- An interesting analysis to look into (since we have the data) is to see the affect the extra help had on the difference in average from first year in hs to last.



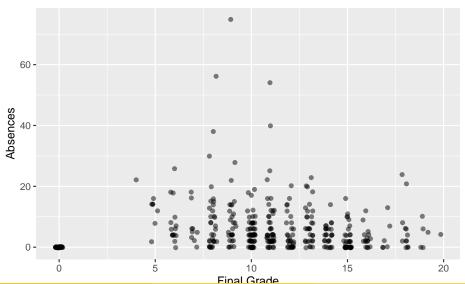


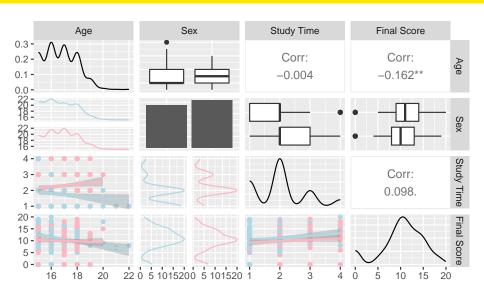
Introducing jitter!

Scatter Plot of Study Time vs. Final Grade



Scatter Plot of Final Grade vs. Absences





- Regression analysis is a way of mathematically identifying which independent variables has an impact on our dependant variable. (Gallo 2022)
- It helps us answer the questions:
 - Which factors(independent variables) matter most?
 - Which can we ignore?
 - How do those factors interact with one another?
 - How certain are we about all these factors?

Simple Linear Regression

Our True Model:

$$y_i = \beta_0 + \beta_1 X_{1i} + \epsilon_i$$

 β_0 : True Intercept

 β_1 : True beta coefficient that quantifies the exact strength and direction of the relationship between each independent variable and the dependent variable.

∈: Error term

Our Estimated Model:

$$\hat{y}_i = \hat{\beta}_0 + \hat{\beta}_1 X_{1i}$$

 $\hat{\beta}_0$: Estimated Intercept

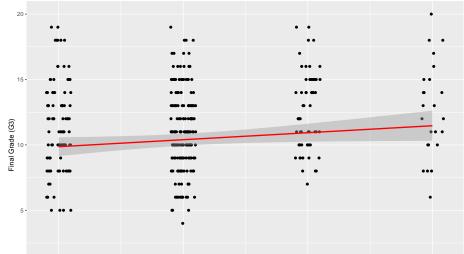
 \hat{eta}_1 : Estimated coefficient that quantifies the strength and direction of the relationship between each independent variable and the dependent variable.

Table 1: Simple Regression Results - Part 1

	Dependent variable:
	G3
studytime	0.534*
	(0.274)
Constant	9.328***
	(0.603)
R^2	0.010
Adjusted R ²	0.007
Residual Std. Error	4.565 (df = 393)
F Statistic	$3.797^* \text{ (df} = 1; 393)$
Note:	*p<0.1; **p<0.05; ***p<0.01

Visually

Scatterplot of Final Grade vs. Study Time



Multiple Linear Regression

Our True Model:

$$y_i = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i} + \beta_3 X_{3i} + \beta_4 X_{4i} + \beta_5 X_{5i} + \beta_6 X_{6i} + \beta_7 X_{7i} + \epsilon_i$$

 β_0 : True Intercept

 β_{1-7} : True beta coefficient that quantifies the exact strength and direction of the relationship between each independent variable and the dependent variable.

 ϵ : Error term

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Our Estimated Model:

$$\hat{y}_i = \hat{\beta}_0 + \hat{\beta}_1 X_{1i} + \hat{\beta}_2 X_{2i} + \hat{\beta}_3 X_{3i} + \hat{\beta}_4 X_{4i} + \hat{\beta}_5 X_{5i} + \hat{\beta}_{6i} X_{6i} + \hat{\beta}_7 X_{7i}$$

 $\hat{\beta}_0$: Estimated Intercept

 $\hat{\beta}_{1-7}$: Estimated coefficient that quantifies the strength and direction of the relationship between each independent variable and the dependent variable.

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This can also be written in matrix notation in a system of equations as follows:

$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \boldsymbol{\varepsilon}$$

where:

$$\mathbf{y} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}, \quad \mathbf{X} = \begin{bmatrix} 1 & X_{11} & X_{12} & X_{13} & X_{14} & X_{15} & X_{16} & X_{17} \\ 1 & X_{21} & X_{22} & X_{23} & X_{24} & X_{25} & X_{26} & X_{27} \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 1 & X_{n1} & X_{n2} & X_{n3} & X_{n4} & X_{n5} & X_{n6} & X_{n7} \end{bmatrix},$$

$$oldsymbol{eta} = egin{bmatrix} eta_0 \ eta_1 \ eta_2 \ eta_3 \ eta_4 \ eta_5 \ eta_6 \ eta_7 \end{bmatrix}, \quad oldsymbol{arepsilon} \quad oldsymbol{arepsilon} = egin{bmatrix} arepsilon_1 \ arepsilon_2 \ arepsilon_2 \ arepsilon_n \end{bmatrix}.$$

Interpretation:

For every one unit increase in X_{ki} our y increases (or decreases, depending on sign) by $\hat{\beta}_k$, on average, while holding other variables constant. where k is the independent variable we are interpreting.

```
filtered_df$sex <- factor(filtered_df$sex, levels = c("M",
    "F"))
filtered df$sex <- as.numeric(filtered df$sex) -
filtered df$sex
# M:0 F:1
# Encode 'higher' variable
filtered_df$higher <- factor(filtered_df$higher,
    levels = c("no", "ves"))
filtered df$higher <- as.numeric(filtered df$higher) -
filtered_df$higher
# 'no': 0, 'yes': 1
```

```
head(filtered_df[1:6])
## # A tibble: 6 x 6
##
    absences higher activities studytime schoolsup
                                                    sex
       <dbl> <dbl>
                         <dbl>
                                  <dbl>
##
                                           <dbl> <dbl>
## 1
           6
          10
```

10

Table 2: Regression Results - Part 1

	Dependent variable:
	G3
absences	0.054*
	(0.028)
higher	3.393***
	(1.057)
activities	-0.348
	(0.452)
studytime	0.712**
	(0.282)

Table 3: Regression Results - Part 2

	Dependent variable:
	G3
schoolsup	-1.622** (0.690)
sex	-1.436*** (0.479)
age	-0.621*** (0.187)
Constant	16.947*** (3.471)

Table 4: Regression Results - Part 3

	Dependent variable:
	G3
Observations	395
R^2	0.099
Adjusted R ²	0.083
Residual Std. Error	4.388 (df = 387)
F Statistic	$6.078^{***} \text{ (df} = 7; 387)$
Note:	*p<0.1; **p<0.05; ***p<0.01

Step 4: Tell the story



Figure 3: Behold the Dragon Scroll

References I

Gallo, Amy. 2022. "A Refresher on Regression Analysis." Harvard Business Review. https://hbr.org/2015/11/a-refresher-on-regression-analysis.

Government of Canada, Statistics Canada, 2021. "Data Journey." Government of Canada, Statistics Canada. https://www.statcan.gc.ca/en/wtc/data-literacy/journey.