

The Large Volatility and the Slow Recovery of the Job-Finding Rate

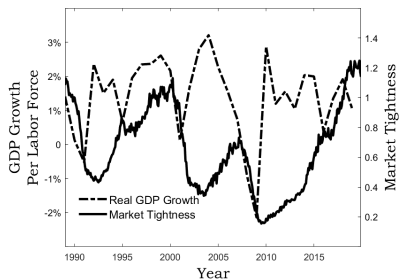
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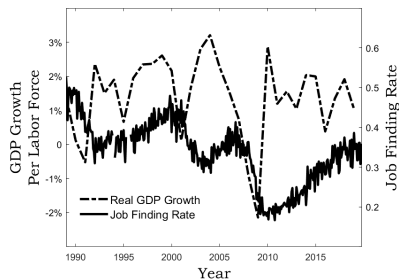
Motivation

- ▶ The job-finding rate exhibits large volatility and slow recovery
 - ▶ Contradict textbook search-and-matching model:
 - ▶ Volatility: Shimer puzzle
 - ▶ Convergence: Know little
- ▶ Important to understand the slow recovery
 - ▶ Guide for empirical work
 - ▶ Policy to accelerate recovery

The Large Drop and Slow Recovery



(a) Labor Market Tightness



(b) Job-Finding Rate

Figure: Aggregate Shock, Market Tightness, and Job-Finding Rate

What I Do

- ▶ The goal of the paper is two-fold:
 1. Derive analytic expression for job-finding rate volatility and convergence
 - ▶ In a class of efficient search-and-matching model a la Kehoe et al. 2020
 - ▶ Nest the textbook search-and-matching model

Results: The Job-Finding Rate Convergence

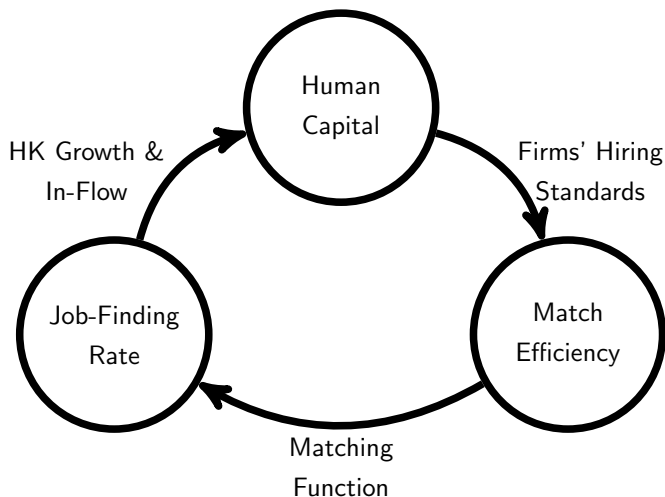
- ▶ Convergence is fast in the perfect foresight equilibrium
 - ▶ Half life is 3 month under standard parameterization
- ▶ Rational expectation equilibrium:
 - ▶ Transmission almost entirely through the aggregate shock
 - ▶ The job-finding rate co-moves with the shock

What I Do Cont.

2. Extend the model to generate slow convergence

- ▶ Two types of workers with human capital:
 - ▶ No-Depreciation (ND)
 - ▶ Fast-Depreciation (FD)
- Endogenous unemployment pool composition
- ▶ Match quality shock and firms' hiring standards
 - Endogenous match efficiency which depends on human capital
- ▶ Complementarity between human capital and match efficiency
 - Multiple equilibria

Model Intuition



Results: Dynamics

- ▶ Dynamics depend on shock size
 - ▶ Small shock: recover to initial steady state
 - ▶ Large shock:
 - ▶ ND workers: Recover
 - ▶ FD workers: Diverge to “corner equilibrium”
→ Lower match efficiency and job-finding rate
- ▶ The relation between match efficiency and the unemployment pool
 - ▶ More low match efficiency worker → Low aggregate match efficiency
E.g. Barnichon et al. 2015
 - ▶ Negative match efficiency shock → Low match efficiency worker

Results: Recovery

- ▶ To recover from the corner equilibrium
 - ▶ Positive aggregate shock
 - ▶ Human capital shock
- ▶ Timing of policy intervention is important:
 - ▶ Small early intervention is sufficient
 - ▶ Late intervention more difficult because human capital too low

Literature

- ▶ Search-and-matching model: Kehoe et al. 2020
- ▶ Match efficiency: Barnichon et al. 2005
- ▶ Firms' hiring standards: Sedláček 2014
- ▶ Human capital loss during unemployment: Ortego-Marti 2017abc

Overview

1. Introduction
2. The Economy
3. Equilibrium
4. Characterizing the Job-Finding Rate Elasticity
5. A Model with Two Types of Workers
6. Quantitative Analysis

The Economy

A Class of Efficient Search-and-Matching Model

- ▶ Directed search with human capital z : Continuous time Kehoe et al. 2020
- ▶ Human capital growth depending on labor force status

$$\frac{dz_{j,t}}{z_{j,t}} = g_j dt, \quad j = e, u$$

- ▶ Job-finding rate λ_{wt} , vacancy-filling rate λ_{vt}
- ▶ Labor market exit rates ϕ_e and ϕ_u
- ▶ Separation rate δ
- ▶ Labor market entry ζ
- ▶ Aggregate shock

$$\frac{dA_t}{A_t} = g_a dt + \sigma_a dW_{a,t}$$

Consumption

- ▶ Consumption:

$$C_t = A_t \int z e_t(z) dz + b A_t \int z u_t(z) dz - \kappa A_t \int z v_t(z) dz$$

- ▶ Measures

- ▶ Employment $e_t(z)$
- ▶ Unemployment $u_t(z)$
- ▶ Vacancy $v_t(z)$

- ▶ Production:

- ▶ Employed $A_t z$
- ▶ Unemployed $b A_t z$

- ▶ Vacancy posting cost $\kappa A_t z$

Preference

- ▶ A family maximizes expected discounted utility

$$\mathbb{E}_0 \left[\int_0^\infty e^{-\beta t} \frac{(C_t - X_t)^{1-\alpha}}{1-\alpha} dt \right]$$

where X_t is exogenous habit

- ▶ Stochastic discount factor:

$$Q_t = e^{-\beta t} (C_t - X_t)^{-\alpha}$$

- ▶ Define the surplus consumption ratio $S_t = (C_t - X_t)/C_t$

$$Q_t = e^{-\beta t} (S_t C_t)^{-\alpha}$$

- ▶ Directly specify the log surplus consumption ratio $s_t = \log(S_t)$

$$ds_t = (1 - \rho_s)(s - s_t)dt + \sigma_a \lambda_a(s_t) dW_{a,t}$$

The Competitive Search Equilibrium

Submarket and Worker's Value Function

- ▶ Submarket indexed by $(z, W_t(z))$

- ▶ $W_t(z)$ chosen by the firms

- ▶ Matching technology:

$$m(u_t, v_t) = B u_t^\eta v_t^{1-\eta}$$

- ▶ Let $M_t(z)$ be post-match value for a worker

$$(\delta + \phi_e)M_t(z) = \delta U_t(z) + \mathbb{E}_t \left[dM_t(z_t) + M_t(z) \frac{dQ_t}{Q_t} \right]$$

where $U_t(z)$ is the value of unemployment

$$\begin{aligned} (\lambda_{wt}(z) + \phi_u)U_t(z) = & bA_t z + \lambda_{wt}(z)(M_t(z) + W_t(z)) \\ & + \mathbb{E}_t \left[dU_t(z_t) + U_t(z) \frac{dQ_t}{Q_t} \right] \end{aligned}$$

Firm's Value Function

- ▶ Let $Y_t(z)$ be the revenue of a firm in submarket z

$$(\delta + \phi_e)Y_t(z) = A_t z + \mathbb{E}_t \left[dY_t(z_t) + Y_t(z) \frac{dQ_t}{Q_t} \right]$$

- ▶ In the symmetric equilibrium, the optimal choice of $W_t(z)$ is

$$\eta[Y_t(z) - W_t(z)] = (1 - \eta)[W_t(z) + M_t(z) - U_t(z)]$$

- ▶ This is equivalent to the Nash bargaining condition
- ▶ Free entry condition:

$$\kappa A_t z = \lambda_{vt}(\theta_t(z))[Y_t(z) - W_t(z)]$$

Equilibrium

- ▶ The value functions are linear in z :

$$Y_t(z) = Y_t z, \quad W_t(z) = W_t z, \quad M_t(z) = M_t z, \quad U_t(z) = U_t z$$

- ▶ Define
 - ▶ $\mu_{et} = Y_t + M_t$ the total value of a match
 - ▶ $\mu_{ut} = U_t$ the joint outside option

Dynamic System

- ▶ The economy is characterized by the following six equations

- ▶ $r_{ft} = -\mathbb{E}_t\left(\frac{dQ_t}{Q_t}\right)$ the risk-free rate
- ▶ $Z_{et} = \int z e_t(z) dz$, $Z_{ut} = \int z u_t(z) dz$ aggregate human capital
- ▶ The system has the same structure as a RBC model

Dynamic System

- ▶ The economy is characterized by the following six equations

$$\left[(\delta + \phi_e - g_e) - \mathbb{E}_t \left(\frac{dQ_t}{Q_t} \right) \right] \mu_{et} = A_t + \delta \mu_{ut} + \mathbb{E}_t(d\mu_{et})$$
$$\left[(\eta \lambda_{wt} + \phi_u - g_u) - \mathbb{E}_t \left(\frac{dQ_t}{Q_t} \right) \right] \mu_{ut} = bA_t + \eta \lambda_{wt} \mu_{et} + \mathbb{E}_t(d\mu_{ut})$$

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- ▶ $r_{ft} = -\mathbb{E}_t \left(\frac{dQ_t}{Q_t} \right)$ the risk-free rate
- ▶ $Z_{et} = \int z e_t(z) dz$, $Z_{ut} = \int z u_t(z) dz$ aggregate human capital
- ▶ The system has the same structure as a RBC model

The Job-Finding Rate and the Value Functions

- ▶ The free-entry condition relates the job-finding rate to the value functions

$$\log(\lambda_{wt}) = \chi + \left(\frac{1 - \eta}{\eta} \right) \log \left(\frac{\mu_{et} - \mu_{ut}}{A_t} \right)$$

- ▶ $\frac{\mu_{et} - \mu_{ut}}{A_t}$ is the benefit of opening a vacancy

- ▶ The elasticity is large iff $\frac{\mu_{et} - \mu_{ut}}{A_t}$ responds to the shock

$$\mathbb{E}_t \begin{bmatrix} d\mu_{et} \\ d\mu_{ut} \end{bmatrix} = \left(\underbrace{\begin{bmatrix} \delta + \phi_e - g_e & -\delta \\ -\eta\lambda_{wt} & \eta\lambda_{wt} + \phi_u - g_u \end{bmatrix}}_{B_1: \text{ search model}} + \underbrace{\begin{bmatrix} -\mathbb{E}_t \left(\frac{dQ_t}{Q_t} \right) & 0 \\ 0 & -\mathbb{E}_t \left(\frac{dQ_t}{Q_t} \right) \end{bmatrix}}_{B_2: \text{ preference}} \right) \begin{bmatrix} \mu_{et} \\ \mu_{ut} \end{bmatrix} + \begin{bmatrix} -A_t \\ -bA_t \end{bmatrix}$$

Characterizing the Job-Finding Rate Elasticity and Convergence

The Risk-Free Rate

Lemma

The risk-free rate to a first order approximation in the log surplus consumption ratio s_t is

$$r_{ft} = -\mathbb{E}_t \left(\frac{dQ_t}{Q_t} \right) \approx -[a_Q + b_Q(s_t - s)]$$

where

$$a_Q = -\beta - \alpha g_a + \frac{1}{2} \alpha \sigma_a^2 \left(\frac{\alpha}{S^2} + 1 \right) \text{ and } b_Q = \alpha(1 - \rho_s) - \frac{\alpha \sigma_a^2 (\alpha + S - 1)}{S^2}$$

► With CRRA preference $Q_t = e^{-\beta t} C_t^{-\alpha}$, $b_Q = 0$

$$r_{ft} = -\beta - \alpha g_a$$

► If no growth in productivity $g_a = 0$

$$r_{ft} = -\beta$$

Characterizing the Job-Finding Rate Elasticity

Proposition

The elasticity of the job-finding rate with respect to the log surplus consumption ratio s_t near $s_t = s$ is

$$\frac{\partial \log(\lambda_{wt})}{\partial s_t} = \underbrace{\frac{b_Q e^{\Theta_1}}{1 - \rho_s}}_{\text{Preference}} \underbrace{\left[\frac{c_h}{-(\gamma_h + a_Q + \Theta_2)} + \frac{c_l}{-(\gamma_l + a_Q + \Theta_2)} \right]}_{\text{Search Model}} \bar{\mu}^{-1}$$

where $\gamma_h < \gamma_l < 0$ are two eigenvalue of the matrix B_1 , c_l and c_h are weights of the eigenvalues, and $\bar{\mu}$ is the long-run average match surplus without shocks.

- ▶ The job-finding rate elasticity can be decomposed into

$$\text{Preference} \times \left(\text{Short-Run Benefit} \right. \\ \left. + \text{Long-Run Benefit} \right)$$

Potential Source of Large Elasticity: Search Model

- ▶ The search model part can be decomposed into

$$\text{Short-run Benefit} + \text{Long-run Benefit}$$

- ▶ The benefits reflect the expected discount value of vacancy creation
- ▶ The Short-run benefit is always small:
 - ▶ Discount by job-finding, which is around 0.46 per month
- ▶ In the textbook search-and-matching model, long-run benefit = 0
 - ▶ Long-run discount rate is the same across employment status
= labor market exit rate
- ▶ Conclusion: small job-finding rate elasticity in the textbook model

Potential Source of Large Elasticity: Search Model

- ▶ Large job-finding elasticity needs differential long-run discount
 - ▶ Human capital growth
 - ▶ Labor market exit rate

Corollary

Differential human capital growth rates or labor market exit rates can lead to positive long-run benefits and hence large job-finding rate elasticity

Parameter Values and the Job-Finding Elasticity

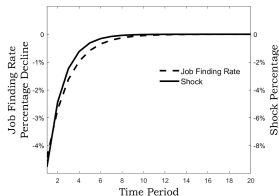
- ▶ The job-finding rate elasticity depends on human capital growth rates
- ▶ Cannot generate large elasticity if HK depreciates fast during unemployment
 - ▶ Empirically: 20% workers with wage growth $< -20\%$
→ Job-finding rate 10% more volatile
 - ▶ Numerically: Job-finding rate elasticity halved

Corollary

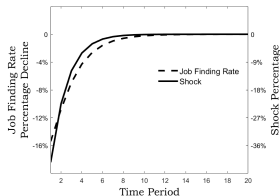
The model cannot generate large job-finding rate elasticity if the human capital depreciation is large during unemployment.

Job-Finding Rate Convergence

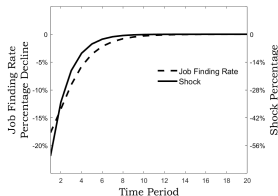
- ▶ I derive the half-life in the perfect foresight equilibrium
 - ▶ Constant human capital
 - ▶ Job-finding rate near the steady-state value
- ▶ Conclusion: Half-life around 3 months
- ▶ This implies that the job-finding rate co-moves with the aggregate shock
 - ▶ If there is no other state variables
- ▶ Numerically study importance of other state variables (human capitals)



(a) Small Shock



(b) Medium Shock



(c) Large Shock

Figure: Convergence of Job-Finding Rate

Job-Finding Rate Elasticity and Convergence: Summarize

- ▶ Model: two mismatch with the data:
 - ▶ Job-finding rate elasticity small if human capital depreciates fast
 - ▶ Job-finding rate co-moves with the aggregate shock

A Model with Two Types of Workers

Model Extension

I make two addition to the model:

1. Two types of workers

- ▶ ND workers: no human capital depreciation during unemployment
- ▶ FD workers: fast human capital depreciation
- ▶ Rubinstein et al. (2006): 20% of workers have 22% wage loss per annum

2. Endogenous match efficiency [more](#)

- ▶ Driven by firms' hiring standards + match quality shock: Sedláček 2014
- ▶ Firms' hiring standards depend on human capital:
Quintini (2011), Pollmann-Schult (2005)

Model Extension

- ▶ Two types of workers n, f
 - ▶ Submarkets are defined by (n, z) and (f, z)
 - ▶ Job-finding rate is

$$\lambda_{j,wt}(z) = \bar{m}_{j,t}(z)\theta_{j,t}^{1-\eta}, \quad j \in \{n, f\}$$

- ▶ Match efficiency:

$$\bar{m}_{j,t}(z) = B_{j,t}\mathbb{P}(q_j z \geq p_j), \quad q_j \sim N(a_{j,q}, \sigma_{j,q}), \quad j \in \{n, f\}$$

- ▶ p_j is firms' hiring standards
 - ▶ q_j is match quality shock
 - ▶ Only part of the matches will be formed
 - ▶ $B_{j,t}$ could vary with the aggregate shock
- ▶ Match efficiency is endogenous
 - ▶ Depends on workers' human capital
 - ▶ Time varying with the aggregate shock

Value Function and Aggregation

- ▶ All the value functions are the same except for the expected revenue:

$$(\delta + \phi_e)Y_{j,t}(z) = A_t q_j z + \mathbb{E}_t \left[dY_{j,t}(z_t) + Y_{j,t}(z) \frac{dQ_t}{Q_t} \right], \quad j \in \{n, f\}$$

- ▶ Aggregate consumption is

$$\begin{aligned} C_t = & n_t \left(A_t \int \chi_n(z) z e_{nt}(z) dz + b A_t \int z u_{nt}(z) dz - \kappa A_t \int z v_{nt}(z) dz \right) \\ & + f_t \left(A_t \int \chi_f(z) z e_{ft}(z) dz + b A_t \int z u_{ft}(z) dz - \kappa A_t \int z v_{ft}(z) dz \right) \end{aligned}$$

where $\chi_j(z) \equiv \mathbb{E}(q_j | q_j z \geq p_j)$: expected match quality

- ▶ The model cannot aggregate linearly
 - ▶ Aggregate consumption depends on the distribution
 - ▶ Matching function depends on the distribution

Aggregation Cont.

- ▶ Simplification:

Match efficiency depends only on aggregates:

$$\bar{M}_{j,t} = B_{j,t} \mathbb{P}[q_j(Z_{j,et} - Z_{j,ut}) \geq p_j] \in [\underline{B}_j, \bar{B}_j], \quad q_j \sim N(a_{j,q}, \sigma_{j,q}), \quad j \in \{n, f\}$$

- ▶ Linear solution exists as before

- ▶ Consistent with firms' hiring standards

- ▶ Numerically equivalent to the disaggregate version if log-linearizing the model

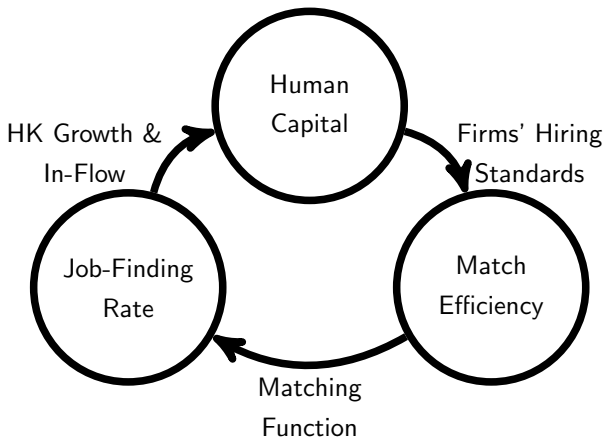
- ▶ Captures two features:

1. Pro-cyclical match efficiency: $\mathbb{P}[q_j(Z_{j,et} - Z_{j,ut}) \geq p_j]$ increasing in $Z_{j,et}$
2. Counter-cyclical match quality:

- ▶ $\chi_{j,t} = \mathbb{E}[q_j | q_j(Z_{j,et} - Z_{j,ut}) \geq p_j]$ decreasing in $Z_{j,et}$
 - ▶ Firms accept better match to compensate lower human capital *on average*

Complementarity and Multiple Equilibria

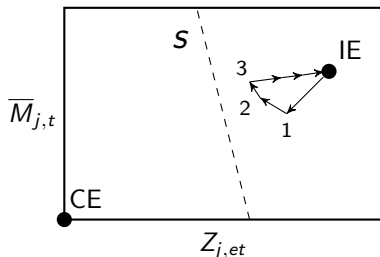
- ▶ Complementarity between the match efficiency and human capital:



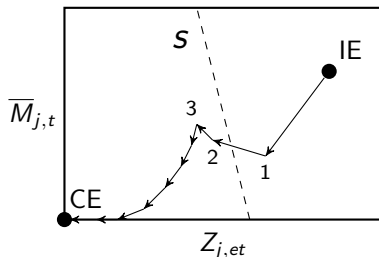
- ▶ The complementarity results in multiple equilibria
 - ▶ Could stuck in an equilibrium with low match efficiency and job-finding rate

Interaction with Aggregate Shock

- ▶ I illustrate the dynamics when interacting with the aggregate shock
- ▶ Denote the interior equilibrium IE and the corner equilibrium CE
- ▶ Assume the aggregate shock lasts for three period
- ▶ Dynamics differ with shock sizes



(a) Small Shock



(b) Large Shock

Figure: The Model Dynamics

Quantitative Analysis

Match Efficiency Functional Form

- ▶ The match efficiency is

$$\overline{M}_{j,t} = B_{j,t} \mathbb{P}[q_j(Z_{j,et} - Z_{j,ut}) \geq p_j] \in [\underline{B}_j, \overline{B}_j], \quad q_j \sim N(a_{j,q}, \sigma_{j,q}), \quad j \in \{n, f\}$$

- ▶ I assume the functional form of $B_{j,t}$

$$B_{j,t} = B_j(\mu_{j,et} - \mu_{j,ut}), \quad j \in \{n, f\}$$

→ affected by the aggregate shock via match surplus

- ▶ State variables: $s_t, Z_{j,et}, Z_{j,ut}$
- ▶ I approximate the match efficiency using global Chebyshev polynomial

Model Calibration: Calibrated Parameters

Table: Parameterization

Panel A: Parameters		Panel B: Moments		
<i>Endogenously Chosen</i>		<i>Targeted</i>	Data	Model
g_a , mean productivity growth (%p.a.)	2.22	Mean productivity growth (%p.a.)	2.22	2.22
σ_a , s.d. productivity growth (%p.a.)	1.84	S.d. productivity growth (%p.a.)	1.84	1.84
B_n , match efficiency, ND workers	0.545	Mean job-finding rate, ND workers	0.46	0.46
B_f , match efficiency, FD workers	0.355	Mean job-finding rate, FD workers	0.31	0.31
κ , hiring cost	0.975	Mean unemployment rate	5.9	5.9
β , time preference factor	0.001	Mean risk-free rate (%p.a.)	0.92	0.92
S , mean of state S_t	0.057	S.d. risk-free rate (%p.a.)	2.31	2.31
α , inverse EIS	5	Maximum Sharpe ratio (p.a.)	0.45	0.45
$\sigma_{q,n}$, match quality variance, ND workers	0.35	S.d. job-finding rate, ND workers	6.66	6.63
$\sigma_{q,f}$, match quality variance, FD workers	0.48	S.d. job-finding rate, FD workers	8.10	8.10

Model Calibration: Assigned Parameters

Table: Parameterization

Panel A: Parameters		Panel B: Moments		
<i>Assigned</i>		<i>Results</i>	Data	Model
b , home production parameter	0.6	Autocorr job-finding rate	0.94	0.98
δ , separation rate	0.028	S.d. unemployment rate	0.75	0.77
η , matching function elasticity	0.5	Autocorr unemployment rate	0.97	0.98
$\phi_{n,f}$, labor market exit rate	0.0028	Corr unemployment, job-finding rate	-0.96	-0.98
ρ_s , persistence of state	0.9944			
$g_{n,e}, g_{f,e}$, employed HK growth (%p.a.)	3.5			
$g_{f,u}$, unemployed HK growth (%p.a.)	-22			

Aggregate Job-Finding Rate

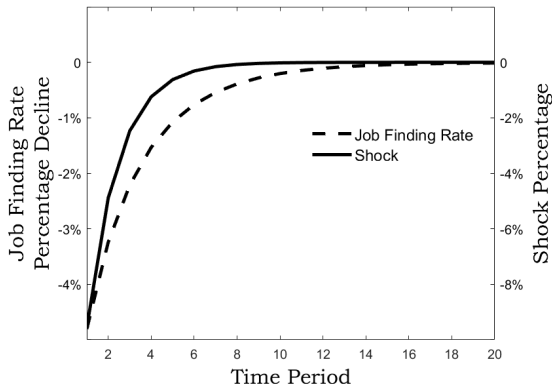
- ▶ The aggregate job-finding rate is

$$\lambda_{wt} = \frac{\xi_t}{1 + \xi_t} \lambda_{f,wt} + \frac{1}{1 + \xi_t} \lambda_{n,wt}, \quad \xi_t = \frac{u_{f,t}}{u_{n,t}}$$

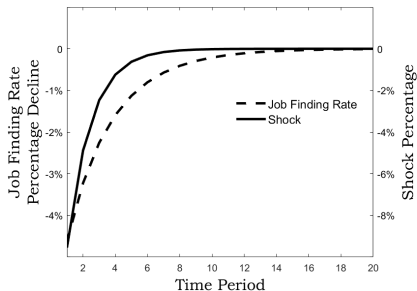
- ▶ Depends on the unemployment composition
 - ▶ If more FD workers in the unemployment pool
→ Job-finding rate behaves like FD workers'

Convergence of the Job-Finding Rate

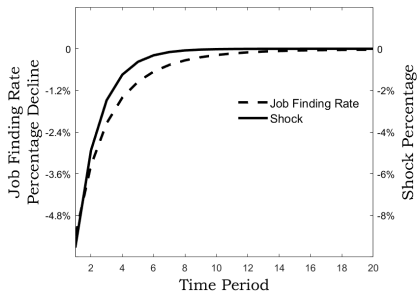
- ▶ I study the convergence of the aggregate job-finding rate
 - ▶ Vary size of the shock
 - ▶ Fix half-life of the shock to be 2 months
 - Shock is 5% of the initial value in 6 months
- ▶ Small shock: 5% decline in the job-finding rate



Convergence: Small Shock



(a) ND Worker



(b) FD Worker

Figure: Convergence of Job-Finding Rate: Small Shock

Convergence: Medium Shock

- ▶ Increase the size of the shock so that the job-finding rate decline by 15%
- ▶ Job-finding rate: large decline and slow recovery
- ▶ Human capital decline leads to lower match efficiency and job-finding rate

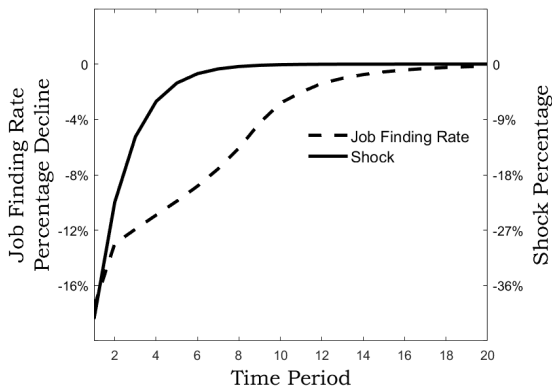
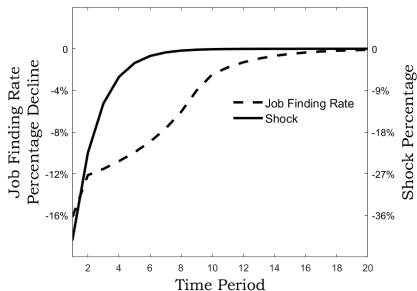
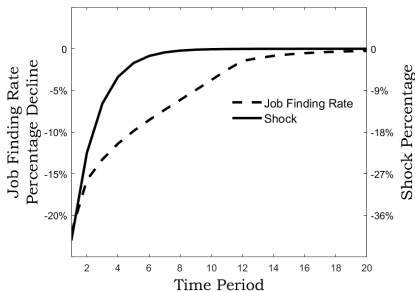


Figure: Aggregate

Convergence: Medium Shock Cont.



(a) ND Worker



(b) FD Worker

Figure: Convergence of Job-Finding Rate: Medium Shock

Convergence: Large Shock

- ▶ Increase the size of the shock so that the job-finding rate decline by 25%
- ▶ Job-finding rate diverges to the corner equilibrium

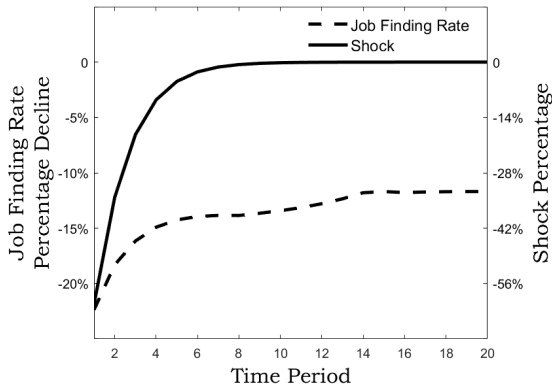
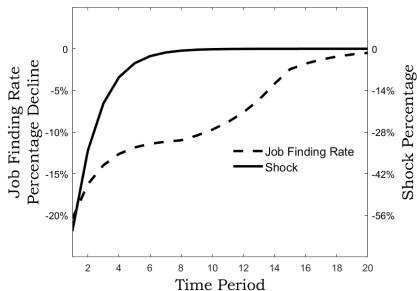
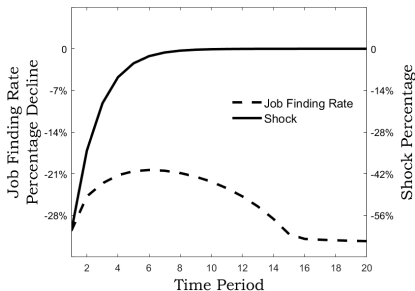


Figure: Aggregate

Convergence: Large Shock Cont.




(a) ND Worker



(b) FD Worker

Figure: Convergence of Job-Finding Rate: Large Shock

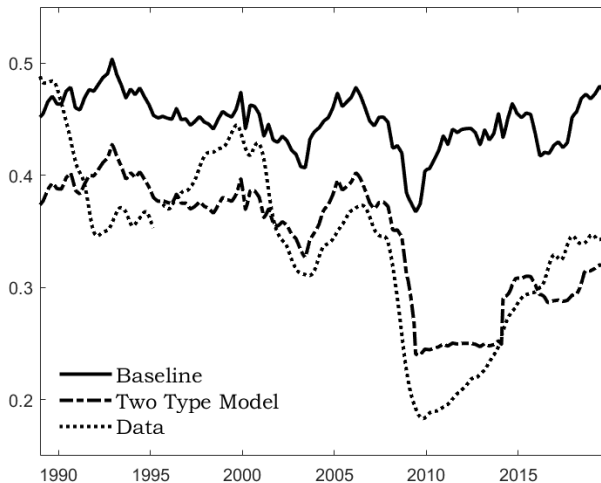
Ergodic Distribution

- ▶ The model features local determinacy
 - ▶ Implication: ergodic distribution 
- ▶ The ND workers are in the corner equilibrium 8% of the time
- ▶ The FD workers 14% of the time
- ▶ Overall average time in recession: 9%
 - ▶ Data from 1989 to 2019: 10%

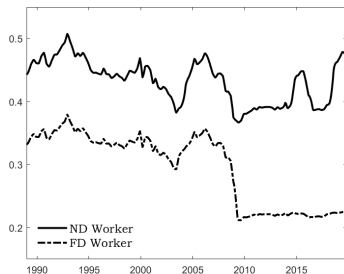
Job-Finding Rate Path

- ▶ I feed in the aggregate productivity shock time series
 - ▶ The baseline model
 - ▶ The two-type model
- ▶ Start the model at the steady state
- ▶ Compare with the empirical job-finding rate path

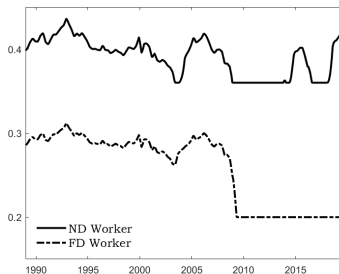
Job-Finding Rate Path Cont.



Job-Finding Rate Path by Workers' Type



(a) Job-Finding Rate



(b) Match Efficiency

Comparison Between the Two Types of Workers

- ▶ The two types of workers behave differently under large shock

1. Initial decline in job-finding rate:

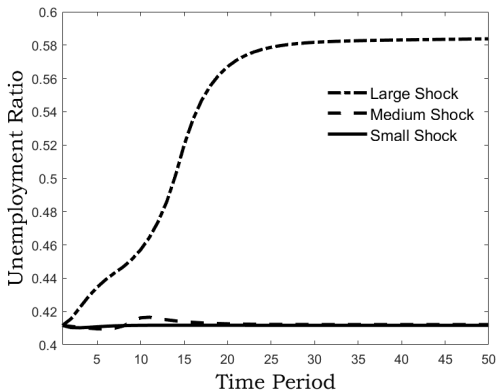
- ▶ Determined by job-finding rate elasticity
- ▶ Larger outflow of employed human capital

2. Human capital depreciation during unemployment

- ▶ Slower inflow of unemployed human capital

Unemployment Pool Composition

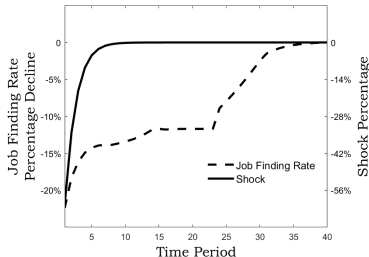
- ▶ The unemployment pool slowly dominated by the FD workers



- ▶ Barnichon et al 2015: long-term unemployment drives low match efficiency
- ▶ My model: low match efficiency could drive long-term unemployment

Recovery From the Corner Equilibrium

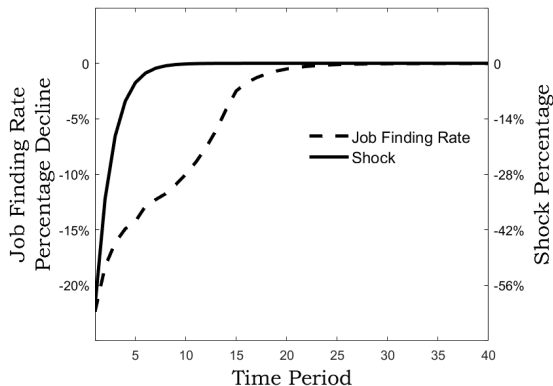
- ▶ Two shocks can recover the economy
 - ▶ Positive aggregate shock
 - ▶ Human capital shock
- ▶ Experiment: 3% human capital increase at month 24



- ▶ Recovery similar to the Great Recession
 - ▶ Human capital captures anything other than aggregate technology
E.g. (search) effort
 - ▶ Consistent with Manovskii et al. 2014
Recovery due to the end of UI extension

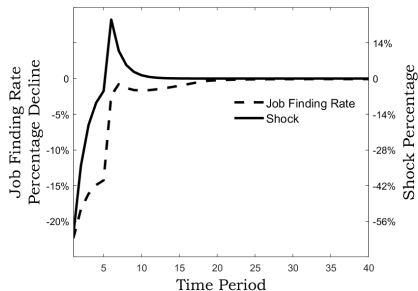
Timing of Policy Intervention

- ▶ Timing of policy intervention is important
 - ▶ Smaller early intervention sufficient
 - ▶ Human capital has not declined by much
- ▶ Comparison: 0.5% human capital shock at month 6

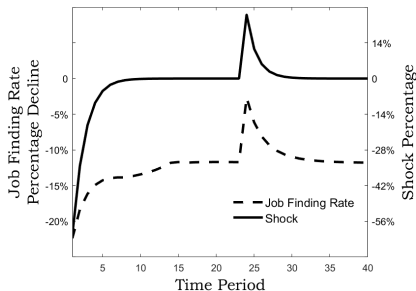


Recovery By Positive Aggregate Shock

- ▶ Positive technology shock can recover the economy
 - ▶ Early intervention more effective
- 25% positive shock in month 6 versus 24



(a) Early Shock



(b) Late Shock

Figure: Recovery by Aggregate Shock

Conclusion

1. Search-and-matching model with constant match efficiency

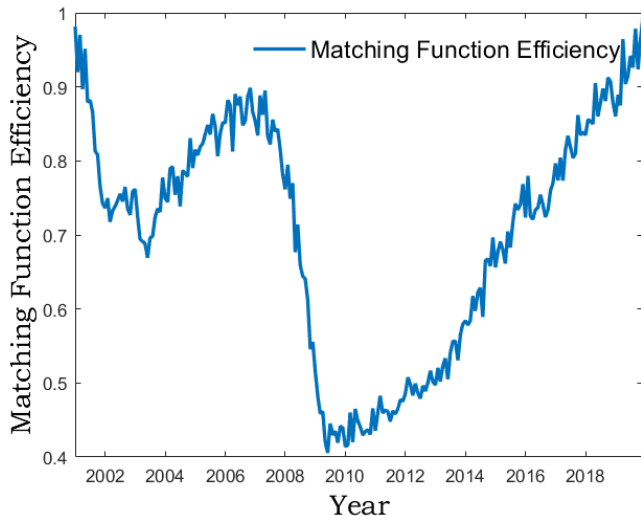
- ▶ Derive job-finding rate elasticity and convergence
- ▶ Elasticity too small if human capital depreciates fast
- ▶ Convergence too fast
- ▶ Transmission depends entirely on the aggregate shock

2. Extension: Two types of workers + firms' hiring standards

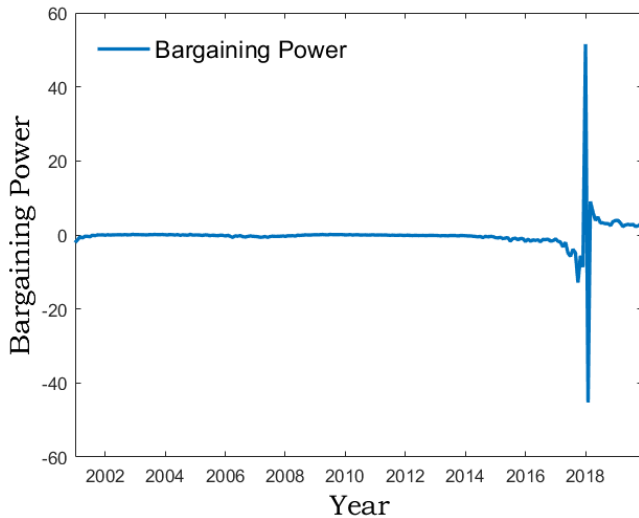
- ▶ Endogenous match efficiency
- ▶ Multiple equilibria
- ▶ Slow recovery due to human capital decline
 - Lower match efficiency and job-finding rate
- ▶ Could stuck in the corner equilibrium
- ▶ Recovery from the corner equilibrium
 - Early intervention important

Appendix

Match Efficiency Variation

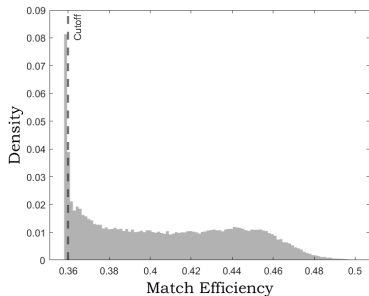


Bargaining Power Variation

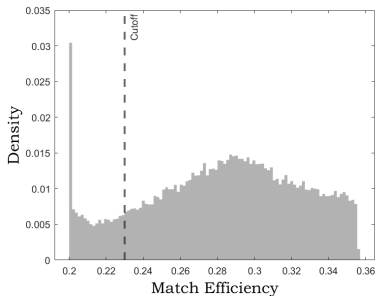


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Ergodic Distribution Cont.



(a) ND Workers



(b) FD Workers

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