### **Batch Normalization**

In [1]: | ## Import and setups

In this notebook, you will implement the batch normalization layers of a neural network to increase its performance. Please review the details of batch normalization from the lecture notes.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc\_net, nndl.layers, and nndl.layer\_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.fc net import *
        from nndl.layers import *
        from cs231n.data utils import get CIFAR10 data
        from cs231n.gradient_check import eval_numerical_gradient, eval_numerical_grad
        ient_array
        from cs231n.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipyt
        hon
        %load ext autoreload
        %autoreload 2
        def rel error(x, y):
             """ returns relative error """
            return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
In [2]:
        # Load the (preprocessed) CIFAR10 data.
        data = get CIFAR10 data()
        for k in data.keys():
            print('{}: {} '.format(k, data[k].shape))
        X_train: (49000, 3, 32, 32)
        y train: (49000,)
        X val: (1000, 3, 32, 32)
        y val: (1000,)
        X_test: (1000, 3, 32, 32)
        y test: (1000,)
```

### **Batchnorm forward pass**

Implement the training time batchnorm forward pass, batchnorm\_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [3]: # Check the training-time forward pass by checking means and variances
        # of features both before and after batch normalization
        # Simulate the forward pass for a two-layer network
        N, D1, D2, D3 = 200, 50, 60, 3
        X = np.random.randn(N, D1)
        W1 = np.random.randn(D1, D2)
        W2 = np.random.randn(D2, D3)
        a = np.maximum(0, X.dot(W1)).dot(W2)
        print('Before batch normalization:')
        print(' means: ', a.mean(axis=0))
        print(' stds: ', a.std(axis=0))
        # Means should be close to zero and stds close to one
        print('After batch normalization (gamma=1, beta=0)')
        a_norm, _ = batchnorm_forward(a, np.ones(D3), np.zeros(D3), {'mode': 'train'})
        print(' mean: ', a_norm.mean(axis=0))
        print(' std: ', a_norm.std(axis=0))
        # Now means should be close to beta and stds close to gamma
        gamma = np.asarray([1.0, 2.0, 3.0])
        beta = np.asarray([11.0, 12.0, 13.0])
        a_norm, _ = batchnorm_forward(a, gamma, beta, {'mode': 'train'})
        print('After batch normalization (nontrivial gamma, beta)')
        print(' means: ', a_norm.mean(axis=0))
        print(' stds: ', a_norm.std(axis=0))
        Before batch normalization:
          means: [ 14.49830898 -1.37373884 -43.13935238]
          stds: [35.33485743 27.08321613 33.11813014]
        After batch normalization (gamma=1, beta=0)
          mean: [-2.12052598e-16 -4.99600361e-18 -6.91668944e-16]
          std: [1.
                            0.99999999 1.
        After batch normalization (nontrivial gamma, beta)
          means: [11. 12. 13.]
                             1.99999999 2.999999991
          stds: [1.
```

Implement the testing time batchnorm forward pass, batchnorm\_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [14]: # Check the test-time forward pass by running the training-time
         # forward pass many times to warm up the running averages, and then
         # checking the means and variances of activations after a test-time
         # forward pass.
         N, D1, D2, D3 = 200, 50, 60, 3
         W1 = np.random.randn(D1, D2)
         W2 = np.random.randn(D2, D3)
         bn_param = {'mode': 'train'}
         gamma = np.ones(D3)
         beta = np.zeros(D3)
         for t in np.arange(50):
             X = np.random.randn(N, D1)
             a = np.maximum(0, X.dot(W1)).dot(W2)
             batchnorm_forward(a, gamma, beta, bn_param)
         bn param['mode'] = 'test'
         X = np.random.randn(N, D1)
         a = np.maximum(0, X.dot(W1)).dot(W2)
         a norm, = batchnorm forward(a, gamma, beta, bn param)
         # Means should be close to zero and stds close to one, but will be
         # noisier than training-time forward passes.
         print('After batch normalization (test-time):')
         print(' means: ', a_norm.mean(axis=0))
                  stds: ', a_norm.std(axis=0))
         After batch normalization (test-time):
           means: [-0.07889814 0.00551766 0.12740709]
           stds: [1.01883564 0.91502566 1.02751596]
```

## **Batchnorm backward pass**

Implement the backward pass for the batchnorm layer, batchnorm\_backward in nndl/layers.py . Check your implementation by running the following cell.

```
In [15]: # Gradient check batchnorm backward pass
         N, D = 4, 5
         x = 5 * np.random.randn(N, D) + 12
         gamma = np.random.randn(D)
         beta = np.random.randn(D)
         dout = np.random.randn(N, D)
         bn param = {'mode': 'train'}
         fx = lambda x: batchnorm_forward(x, gamma, beta, bn_param)[0]
         fg = lambda a: batchnorm forward(x, gamma, beta, bn param)[0]
         fb = lambda b: batchnorm_forward(x, gamma, beta, bn_param)[0]
         dx num = eval numerical gradient array(fx, x, dout)
         da num = eval numerical gradient array(fg, gamma, dout)
         db_num = eval_numerical_gradient_array(fb, beta, dout)
         _, cache = batchnorm_forward(x, gamma, beta, bn_param)
         dx, dgamma, dbeta = batchnorm_backward(dout, cache)
         print('dx error: ', rel error(dx num, dx))
         print('dgamma error: ', rel_error(da_num, dgamma))
         print('dbeta error: ', rel_error(db_num, dbeta))
```

dx error: 3.809742869855928e-09
dgamma error: 8.336383976364184e-12
dbeta error: 3.689529723400366e-12

# Implement a fully connected neural network with batchnorm layers

Modify the FullyConnectedNet() class in nndl/fc\_net.py to incorporate batchnorm layers. You will need to modify the class in the following areas:

- (1) The gammas and betas need to be initialized to 1's and 0's respectively in init .
- (2) The batchnorm\_forward layer needs to be inserted between each affine and relu layer (except in the output layer) in a forward pass computation in loss. You may find it helpful to write an affine batchnorm relu() layer in nndl/layer utils.py although this is not necessary.
- (3) The batchnorm backward layer has to be appropriately inserted when calculating gradients.

After you have done the appropriate modifications, check your implementation by running the following cell.

Note, while the relative error for W3 should be small, as we backprop gradients more, you may find the relative error increases. Our relative error for W1 is on the order of 1e-4.

```
In [14]: N, D, H1, H2, C = 2, 15, 20, 30, 10
         X = np.random.randn(N, D)
         y = np.random.randint(C, size=(N,))
         for reg in [0, 3.14]:
             print('Running check with reg = ', reg)
             model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
                                        reg=reg, weight_scale=5e-2, dtype=np.float64,
                                        use batchnorm=True)
             loss, grads = model.loss(X, y)
             print('Initial loss: ', loss)
             for name in sorted(grads):
                 f = lambda _: model.loss(X, y)[0]
                 grad_num = eval_numerical_gradient(f, model.params[name], verbose=Fals
         e, h=1e-5)
                 print('{} relative error: {}'.format(name, rel error(grad num, grads[n
         ame])))
             if reg == 0: print('\n')
         Running check with reg = 0
         Initial loss: 2.0695995151858475
         W1 relative error: 3.4978149667794715e-05
         W2 relative error: 6.354165854386234e-06
         W3 relative error: 5.673183795002378e-10
         b1 relative error: 6.772360450213455e-07
         b2 relative error: 4.85722573273506e-08
         b3 relative error: 1.2727389829316949e-10
         beta1 relative error: 1.9229561631622186e-07
         beta2 relative error: 1.9961434488023226e-08
         gamma1 relative error: 1.7488820096966392e-07
         gamma2 relative error: 8.073429866940405e-08
         Running check with reg = 3.14
         Initial loss: 5.903495149039081
         W1 relative error: 3.8733381531170215e-06
         W2 relative error: 4.966000040150471e-07
         W3 relative error: 8.346628581999191e-10
         b1 relative error: 1.1926223897340549e-09
         b2 relative error: 7.077671781985373e-08
         b3 relative error: 2.3687034436225695e-10
         beta1 relative error: 1.9034358853460448e-06
         beta2 relative error: 5.79097362786806e-08
         gamma1 relative error: 1.6912616076735815e-06
         gamma2 relative error: 5.2455565616045825e-08
```

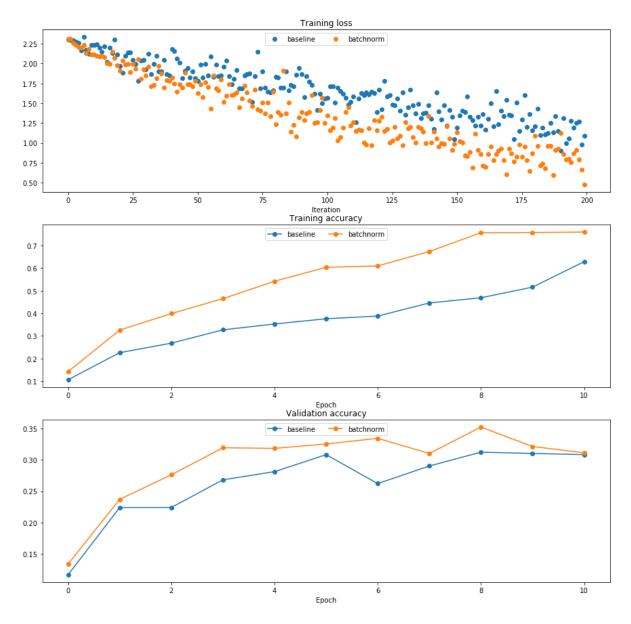
# Training a deep fully connected network with batch normalization.

To see if batchnorm helps, let's train a deep neural network with and without batch normalization.

```
In [15]: # Try training a very deep net with batchnorm
         hidden dims = [100, 100, 100, 100, 100]
         num train = 1000
         small_data = {
              'X_train': data['X_train'][:num_train],
              'y_train': data['y_train'][:num_train],
             'X_val': data['X_val'],
              'y_val': data['y_val'],
         }
         weight_scale = 2e-2
         bn_model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batch
         norm=True)
         model = FullyConnectedNet(hidden dims, weight scale=weight scale, use batchnor
         m=False)
         bn_solver = Solver(bn_model, small_data,
                          num_epochs=10, batch_size=50,
                          update rule='adam',
                          optim config={
                            'learning_rate': 1e-3,
                          verbose=True, print every=200)
         bn_solver.train()
         solver = Solver(model, small data,
                          num_epochs=10, batch_size=50,
                          update rule='adam',
                          optim config={
                            'learning_rate': 1e-3,
                          verbose=True, print every=200)
         solver.train()
```

```
(Iteration 1 / 200) loss: 2.311105
(Epoch 0 / 10) train acc: 0.142000; val_acc: 0.134000
(Epoch 1 / 10) train acc: 0.326000; val acc: 0.237000
(Epoch 2 / 10) train acc: 0.399000; val acc: 0.276000
(Epoch 3 / 10) train acc: 0.465000; val acc: 0.319000
(Epoch 4 / 10) train acc: 0.542000; val_acc: 0.318000
(Epoch 5 / 10) train acc: 0.604000; val acc: 0.325000
(Epoch 6 / 10) train acc: 0.610000; val acc: 0.334000
(Epoch 7 / 10) train acc: 0.674000; val_acc: 0.310000
(Epoch 8 / 10) train acc: 0.757000; val acc: 0.352000
(Epoch 9 / 10) train acc: 0.758000; val acc: 0.321000
(Epoch 10 / 10) train acc: 0.760000; val acc: 0.311000
(Iteration 1 / 200) loss: 2.302117
(Epoch 0 / 10) train acc: 0.106000; val_acc: 0.117000
(Epoch 1 / 10) train acc: 0.226000; val acc: 0.224000
(Epoch 2 / 10) train acc: 0.268000; val acc: 0.224000
(Epoch 3 / 10) train acc: 0.327000; val acc: 0.268000
(Epoch 4 / 10) train acc: 0.353000; val acc: 0.281000
(Epoch 5 / 10) train acc: 0.376000; val acc: 0.308000
(Epoch 6 / 10) train acc: 0.388000; val acc: 0.262000
(Epoch 7 / 10) train acc: 0.446000; val_acc: 0.290000
(Epoch 8 / 10) train acc: 0.469000; val acc: 0.312000
(Epoch 9 / 10) train acc: 0.516000; val acc: 0.310000
(Epoch 10 / 10) train acc: 0.629000; val_acc: 0.308000
```

```
In [16]: fig, axes = plt.subplots(3, 1)
         ax = axes[0]
         ax.set title('Training loss')
         ax.set_xlabel('Iteration')
         ax = axes[1]
         ax.set_title('Training accuracy')
         ax.set_xlabel('Epoch')
         ax = axes[2]
         ax.set_title('Validation accuracy')
         ax.set_xlabel('Epoch')
         ax = axes[0]
         ax.plot(solver.loss_history, 'o', label='baseline')
         ax.plot(bn_solver.loss_history, 'o', label='batchnorm')
         ax = axes[1]
         ax.plot(solver.train_acc_history, '-o', label='baseline')
         ax.plot(bn_solver.train_acc_history, '-o', label='batchnorm')
         ax = axes[2]
         ax.plot(solver.val_acc_history, '-o', label='baseline')
         ax.plot(bn_solver.val_acc_history, '-o', label='batchnorm')
         for i in [1, 2, 3]:
             ax = axes[i - 1]
             ax.legend(loc='upper center', ncol=4)
         plt.gcf().set_size_inches(15, 15)
         plt.show()
```



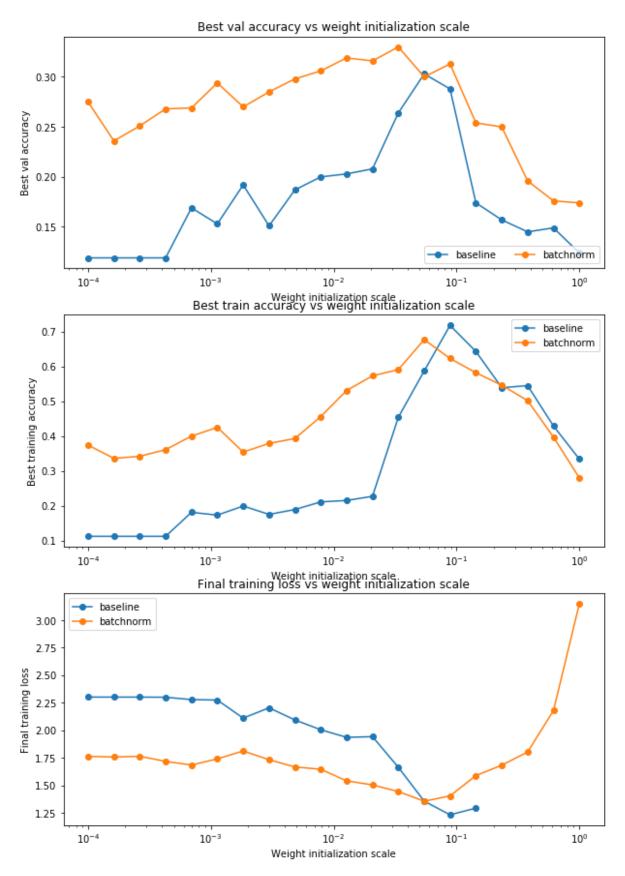
## **Batchnorm and initialization**

The following cells run an experiment where for a deep network, the initialization is varied. We do training for when batchnorm layers are and are not included.

```
In [17]: # Try training a very deep net with batchnorm
         hidden dims = [50, 50, 50, 50, 50, 50, 50]
         num train = 1000
         small data = {
              'X_train': data['X_train'][:num_train],
              'y_train': data['y_train'][:num_train],
             'X val': data['X val'],
              'y_val': data['y_val'],
         }
         bn_solvers = {}
         solvers = {}
         weight scales = np.logspace(-4, 0, num=20)
         for i, weight scale in enumerate(weight scales):
             print('Running weight scale {} / {}'.format(i + 1, len(weight_scales)))
             bn model = FullyConnectedNet(hidden dims, weight scale=weight scale, use b
         atchnorm=True)
             model = FullyConnectedNet(hidden dims, weight scale=weight scale, use batc
         hnorm=False)
             bn_solver = Solver(bn_model, small_data,
                              num epochs=10, batch size=50,
                              update_rule='adam',
                              optim config={
                                'learning rate': 1e-3,
                              },
                              verbose=False, print_every=200)
             bn solver.train()
             bn_solvers[weight_scale] = bn_solver
             solver = Solver(model, small_data,
                              num epochs=10, batch size=50,
                              update_rule='adam',
                              optim_config={
                                'learning_rate': 1e-3,
                              },
                              verbose=False, print every=200)
             solver.train()
             solvers[weight scale] = solver
```

```
Running weight scale 1 / 20
Running weight scale 2 / 20
Running weight scale 3 / 20
Running weight scale 4 / 20
Running weight scale 5 / 20
Running weight scale 6 / 20
Running weight scale 7 / 20
Running weight scale 8 / 20
Running weight scale 9 / 20
Running weight scale 10 / 20
Running weight scale 11 / 20
Running weight scale 12 / 20
Running weight scale 13 / 20
Running weight scale 14 / 20
Running weight scale 15 / 20
Running weight scale 16 / 20
C:\Users\Showb\Desktop\Books\ECE C147\HW4-code\nndl\layers.py:419: RuntimeWar
ning: divide by zero encountered in log
  loss = -np.sum(np.log(probs[np.arange(N), y])) / N
Running weight scale 17 / 20
Running weight scale 18 / 20
Running weight scale 19 / 20
Running weight scale 20 / 20
```

```
In [18]: # Plot results of weight scale experiment
         best train accs, bn best train accs = [], []
         best val accs, bn best val accs = [], []
         final train loss, bn final train loss = [], []
         for ws in weight scales:
             best train accs.append(max(solvers[ws].train acc history))
             bn best train accs.append(max(bn solvers[ws].train acc history))
             best_val_accs.append(max(solvers[ws].val acc history))
             bn best val accs.append(max(bn solvers[ws].val acc history))
             final train loss.append(np.mean(solvers[ws].loss history[-100:]))
             bn final train loss.append(np.mean(bn solvers[ws].loss history[-100:]))
         plt.subplot(3, 1, 1)
         plt.title('Best val accuracy vs weight initialization scale')
         plt.xlabel('Weight initialization scale')
         plt.ylabel('Best val accuracy')
         plt.semilogx(weight scales, best val accs, '-o', label='baseline')
         plt.semilogx(weight scales, bn best val accs, '-o', label='batchnorm')
         plt.legend(ncol=2, loc='lower right')
         plt.subplot(3, 1, 2)
         plt.title('Best train accuracy vs weight initialization scale')
         plt.xlabel('Weight initialization scale')
         plt.ylabel('Best training accuracy')
         plt.semilogx(weight_scales, best_train_accs, '-o', label='baseline')
         plt.semilogx(weight scales, bn best train accs, '-o', label='batchnorm')
         plt.legend()
         plt.subplot(3, 1, 3)
         plt.title('Final training loss vs weight initialization scale')
         plt.xlabel('Weight initialization scale')
         plt.ylabel('Final training loss')
         plt.semilogx(weight_scales, final_train_loss, '-o', label='baseline')
         plt.semilogx(weight scales, bn final train loss, '-o', label='batchnorm')
         plt.legend()
         plt.gcf().set size inches(10, 15)
         plt.show()
```



## **Question:**

In the cell below, summarize the findings of this experiment, and WHY these results make sense.

#### **Answer:**

We can note that the batchnorm outperforms the baseline at all three figures of merit: specifically, best validation accuracy, best training accuracy, and final training loss. Since batchnorm normalizes the outputs of each layers, this makes the network more robust to initialization and saturation. Total accuracy decays after 10^-1 since the weights become too large.

The baseline is heavily dependent on weight initializations. If the weights are originally initialized to be small, then the activations will decay throughout later layers. Whereas if weights are initialized to be large, then these activations will instead increase exponentially throughout later layers. Hence, this is why the baseline curve tends to act erraticaly.

We can also observe that the baseline validation accuracy performs best somewhere in the wegith range from 10^-2 to 10^-1, whereas the batchnorm validation accjuracy exhibits better accuracy over a larger weight range. The training accuracy curves additionally exhibit the same behavior as the validation accuracy curves mentioned above.

Lastly, we can observe that the batchnorm exhibits lower loss at all weight scales.

In [1]: | ## Import and setups

## **Dropout**

In this notebook, you will implement dropout. Then we will ask you to train a network with batchnorm and dropout, and acheive over 55% accuracy on CIFAR-10.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc\_net, nndl.layers, and nndl.layer\_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.fc net import *
        from nndl.layers import *
        from cs231n.data utils import get CIFAR10 data
        from cs231n.gradient_check import eval_numerical_gradient, eval_numerical_grad
        ient_array
        from cs231n.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipyt
        hon
        %load ext autoreload
        %autoreload 2
        def rel error(x, y):
             """ returns relative error """
            return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
In [2]:
        # Load the (preprocessed) CIFAR10 data.
        data = get CIFAR10 data()
        for k in data.keys():
            print('{}: {} '.format(k, data[k].shape))
        X_train: (49000, 3, 32, 32)
        y train: (49000,)
        X val: (1000, 3, 32, 32)
        y val: (1000,)
        X_test: (1000, 3, 32, 32)
        y_test: (1000,)
```

### **Dropout forward pass**

Implement the training and test time dropout forward pass, dropout\_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [3]: x = np.random.randn(500, 500) + 10

for p in [0.3, 0.6, 0.75]:
    out, _ = dropout_forward(x, {'mode': 'train', 'p': p})
    out_test, _ = dropout_forward(x, {'mode': 'test', 'p': p})

    print('Running tests with p = ', p)
    print('Mean of input: ', x.mean())
    print('Mean of train-time output: ', out.mean())
    print('Mean of test-time output: ', out_test.mean())
    print('Fraction of train-time output set to zero: ', (out == 0).mean())
    print('Fraction of test-time output set to zero: ', (out_test == 0).mean())
```

```
Running tests with p = 0.3
Mean of input: 9.998607064493596
Mean of train-time output: 7.006490469881562
Mean of test-time output: 9.998607064493596
Fraction of train-time output set to zero: 0.299232
Fraction of test-time output set to zero: 0.0
Running tests with p = 0.6
Mean of input: 9.998607064493596
Mean of train-time output: 4.024759190346156
Mean of test-time output: 9.998607064493596
Fraction of train-time output set to zero: 0.59746
Fraction of test-time output set to zero: 0.0
Running tests with p = 0.75
Mean of input: 9.998607064493596
Mean of train-time output: 2.512504526277114
Mean of test-time output: 9.998607064493596
Fraction of train-time output set to zero:
Fraction of test-time output set to zero: 0.0
```

### **Dropout backward pass**

Implement the backward pass, dropout\_backward, in nndl/layers.py. After that, test your gradients by running the following cell:

dx relative error: 1.8928952047377214e-11

# Implement a fully connected neural network with dropout layers

Modify the FullyConnectedNet() class in nndl/fc\_net.py to incorporate dropout. A dropout layer should be incorporated after every ReLU layer. Concretely, there shouldn't be a dropout at the output layer since there is no ReLU at the output layer. You will need to modify the class in the following areas:

- (1) In the forward pass, you will need to incorporate a dropout layer after every relu layer.
- (2) In the backward pass, you will need to incorporate a dropout backward pass layer.

Check your implementation by running the following code. Our W1 gradient relative error is on the order of 1e-6 (the largest of all the relative errors).

```
In [5]: N, D, H1, H2, C = 2, 15, 20, 30, 10
        X = np.random.randn(N, D)
        y = np.random.randint(C, size=(N,))
        for dropout in [0.5, 0.75, 1.0]:
            print('Running check with dropout = ', dropout)
            model = FullyConnectedNet([H1, H2], input dim=D, num classes=C,
                                       weight scale=5e-2, dtype=np.float64,
                                       dropout=dropout, seed=123)
            loss, grads = model.loss(X, y)
            print('Initial loss: ', loss)
            for name in sorted(grads):
                f = lambda : model.loss(X, y)[0]
                grad_num = eval_numerical_gradient(f, model.params[name], verbose=Fals
        e, h=1e-5)
                print('{} relative error: {}'.format(name, rel error(grad num, grads[n
        ame])))
            print('\n')
        Running check with dropout = 0.5
        Initial loss: 2.3052017574074988
        W1 relative error: 8.424304166650062e-07
        W2 relative error: 3.639927148829238e-07
        W3 relative error: 8.059827996258932e-08
        b1 relative error: 1.792820732695455e-08
        b2 relative error: 1.7028480139083283e-09
        b3 relative error: 9.885993030503735e-11
        Running check with dropout = 0.75
        Initial loss: 2.3025570024040185
        W1 relative error: 6.393720367005828e-07
        W2 relative error: 9.586432697009482e-09
        W3 relative error: 2.7054675498916053e-08
        b1 relative error: 6.023301232972825e-09
        b2 relative error: 6.159225257232955e-10
        b3 relative error: 1.3510593625504552e-10
        Running check with dropout = 1.0
        Initial loss: 2.3053332250963194
        W1 relative error: 1.2744095365229032e-06
        W2 relative error: 4.678743300473988e-07
        W3 relative error: 4.331673892536035e-08
        b1 relative error: 4.0853539035931665e-08
        b2 relative error: 1.951342257912746e-09
        b3 relative error: 9.387142701440351e-11
```

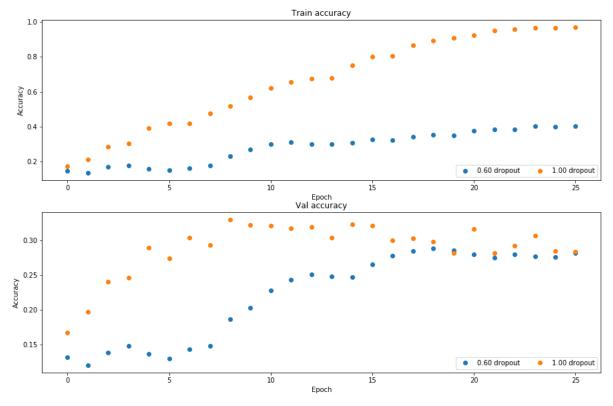
# Dropout as a regularizer

In class, we claimed that dropout acts as a regularizer by effectively bagging. To check this, we will train two small networks, one with dropout and one without dropout.

```
In [6]: # Train two identical nets, one with dropout and one without
        num_train = 500
        small_data = {
            'X_train': data['X_train'][:num_train],
             'y_train': data['y_train'][:num_train],
             'X_val': data['X_val'],
             'y_val': data['y_val'],
        }
        solvers = \{\}
        dropout_choices = [0.6, 1.0]
        for dropout in dropout_choices:
            model = FullyConnectedNet([100, 100, 100], dropout=dropout)
            solver = Solver(model, small_data,
                             num_epochs=25, batch_size=100,
                             update_rule='adam',
                             optim_config={
                               'learning rate': 5e-4,
                             verbose=True, print_every=100)
            solver.train()
            solvers[dropout] = solver
```

```
(Iteration 1 / 125) loss: 2.302534
(Epoch 0 / 25) train acc: 0.146000; val_acc: 0.131000
(Epoch 1 / 25) train acc: 0.134000; val acc: 0.120000
(Epoch 2 / 25) train acc: 0.168000; val acc: 0.138000
(Epoch 3 / 25) train acc: 0.176000; val acc: 0.148000
(Epoch 4 / 25) train acc: 0.156000; val acc: 0.136000
(Epoch 5 / 25) train acc: 0.150000; val acc: 0.130000
(Epoch 6 / 25) train acc: 0.160000; val acc: 0.143000
(Epoch 7 / 25) train acc: 0.176000; val_acc: 0.148000
(Epoch 8 / 25) train acc: 0.232000; val acc: 0.186000
(Epoch 9 / 25) train acc: 0.270000; val acc: 0.203000
(Epoch 10 / 25) train acc: 0.298000; val_acc: 0.228000
(Epoch 11 / 25) train acc: 0.310000; val acc: 0.243000
(Epoch 12 / 25) train acc: 0.298000; val acc: 0.251000
(Epoch 13 / 25) train acc: 0.300000; val acc: 0.248000
(Epoch 14 / 25) train acc: 0.306000; val_acc: 0.247000
(Epoch 15 / 25) train acc: 0.326000; val acc: 0.265000
(Epoch 16 / 25) train acc: 0.322000; val acc: 0.278000
(Epoch 17 / 25) train acc: 0.340000; val acc: 0.285000
(Epoch 18 / 25) train acc: 0.352000; val acc: 0.288000
(Epoch 19 / 25) train acc: 0.350000; val_acc: 0.286000
(Epoch 20 / 25) train acc: 0.376000; val acc: 0.280000
(Iteration 101 / 125) loss: 1.859258
(Epoch 21 / 25) train acc: 0.384000; val acc: 0.275000
(Epoch 22 / 25) train acc: 0.384000; val_acc: 0.280000
(Epoch 23 / 25) train acc: 0.404000; val acc: 0.277000
(Epoch 24 / 25) train acc: 0.400000; val acc: 0.276000
(Epoch 25 / 25) train acc: 0.404000; val acc: 0.282000
(Iteration 1 / 125) loss: 2.300607
(Epoch 0 / 25) train acc: 0.172000; val acc: 0.167000
(Epoch 1 / 25) train acc: 0.210000; val_acc: 0.197000
(Epoch 2 / 25) train acc: 0.284000; val acc: 0.240000
(Epoch 3 / 25) train acc: 0.302000; val acc: 0.246000
(Epoch 4 / 25) train acc: 0.392000; val acc: 0.289000
(Epoch 5 / 25) train acc: 0.420000; val acc: 0.274000
(Epoch 6 / 25) train acc: 0.420000; val acc: 0.304000
(Epoch 7 / 25) train acc: 0.474000; val_acc: 0.293000
(Epoch 8 / 25) train acc: 0.516000; val acc: 0.330000
(Epoch 9 / 25) train acc: 0.566000; val acc: 0.322000
(Epoch 10 / 25) train acc: 0.620000; val acc: 0.321000
(Epoch 11 / 25) train acc: 0.656000; val_acc: 0.317000
(Epoch 12 / 25) train acc: 0.676000; val acc: 0.319000
(Epoch 13 / 25) train acc: 0.680000; val_acc: 0.304000
(Epoch 14 / 25) train acc: 0.752000; val_acc: 0.323000
(Epoch 15 / 25) train acc: 0.802000; val_acc: 0.321000
(Epoch 16 / 25) train acc: 0.804000; val acc: 0.300000
(Epoch 17 / 25) train acc: 0.868000; val_acc: 0.303000
(Epoch 18 / 25) train acc: 0.894000; val acc: 0.298000
(Epoch 19 / 25) train acc: 0.910000; val_acc: 0.282000
(Epoch 20 / 25) train acc: 0.926000; val_acc: 0.316000
(Iteration 101 / 125) loss: 0.245816
(Epoch 21 / 25) train acc: 0.950000; val acc: 0.282000
(Epoch 22 / 25) train acc: 0.958000; val acc: 0.292000
(Epoch 23 / 25) train acc: 0.966000; val acc: 0.307000
(Epoch 24 / 25) train acc: 0.966000; val_acc: 0.285000
(Epoch 25 / 25) train acc: 0.970000; val acc: 0.284000
```

```
In [7]:
        # Plot train and validation accuracies of the two models
        train_accs = []
        val accs = []
        for dropout in dropout_choices:
            solver = solvers[dropout]
            train_accs.append(solver.train_acc_history[-1])
            val accs.append(solver.val acc history[-1])
        plt.subplot(3, 1, 1)
        for dropout in dropout choices:
            plt.plot(solvers[dropout].train_acc_history, 'o', label='%.2f dropout' % d
        ropout)
        plt.title('Train accuracy')
        plt.xlabel('Epoch')
        plt.ylabel('Accuracy')
        plt.legend(ncol=2, loc='lower right')
        plt.subplot(3, 1, 2)
        for dropout in dropout choices:
            plt.plot(solvers[dropout].val acc history, 'o', label='%.2f dropout' % dro
        pout)
        plt.title('Val accuracy')
        plt.xlabel('Epoch')
        plt.ylabel('Accuracy')
        plt.legend(ncol=2, loc='lower right')
        plt.gcf().set_size_inches(15, 15)
        plt.show()
```



## Question

Based off the results of this experiment, is dropout performing regularization? Explain your answer.

#### **Answer:**

We observe that dropout has a lower training accuracy but has a larger validation accuracy, which indicates that when using dropout, the network is not simply overfitting to the training data and is generalizing better than the baseline to data it has not seen before (test / validation set). Hence, dropout is performing regularization

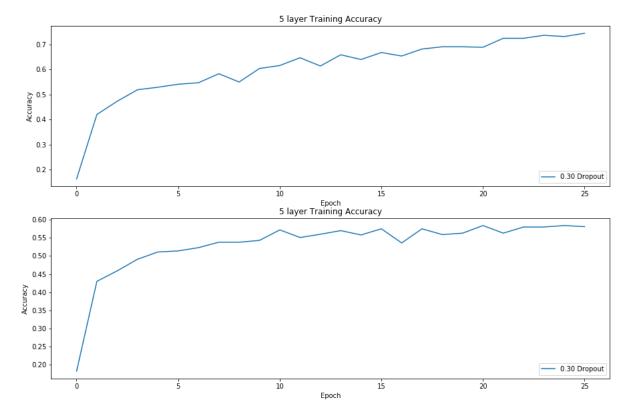
#### Final part of the assignment

Get over 55% validation accuracy on CIFAR-10 by using the layers you have implemented. You will be graded according to the following equation:

min(floor((X - 32%)) / 23%, 1) where if you get 55% or higher validation accuracy, you get full points.

```
In [9]:
       # YOUR CODE HERE:
          Implement a FC-net that achieves at least 55% validation accuracy
          on CIFAR-10.
       dropout choices = [0.3]
       learning rate = 1e-3
       weight scale = 1e-1
       lr decay = 1
       for dropout in dropout choices:
          time start = time.time()
          model = FullyConnectedNet([500, 500, 500, 500], weight_scale = weight
       scale,
                               use batchnorm=True,dropout=dropout)
          solver = Solver(model, data, num_epochs=25, batch_size=200, update_rule='r
       msprop',
                       optim_config={'learning_rate': learning_rate}, lr_decay = 1
       r_decay,
                       verbose=True, print every=10e5)
          solver.train()
          solvers[dropout] = solver
       train accs = []
       val accs = []
       for dropout in dropout choices:
          solver = solvers[dropout]
          train_accs.append(solver.train_acc_history[-1])
          val accs.append(solver.val acc history[-1])
       plt.subplot(3,1,1)
       for dropout in dropout choices:
          plt.plot(solvers[dropout].train acc history, label = '%.2f Dropout' % drop
       out)
       plt.title('5 layer Training Accuracy')
       plt.xlabel('Epoch')
       plt.ylabel('Accuracy')
       plt.legend(ncol = 2, loc = 'lower right')
       plt.subplot(3,1,2)
       for dropout in dropout_choices:
          plt.plot(solvers[dropout].val acc history, label = '%.2f Dropout' % dropou
       t)
       plt.title('5 layer Training Accuracy')
       plt.xlabel('Epoch')
       plt.ylabel('Accuracy')
       plt.legend(ncol = 2, loc = 'lower right')
       plt.gcf().set size inches(15, 15)
       plt.show()
       # END YOUR CODE HERE
```

```
(Iteration 1 / 6125) loss: 2.943690
(Epoch 0 / 25) train acc: 0.162000; val_acc: 0.182000
(Epoch 1 / 25) train acc: 0.420000; val acc: 0.430000
(Epoch 2 / 25) train acc: 0.473000; val acc: 0.459000
(Epoch 3 / 25) train acc: 0.519000; val acc: 0.491000
(Epoch 4 / 25) train acc: 0.529000; val acc: 0.511000
(Epoch 5 / 25) train acc: 0.541000; val acc: 0.514000
(Epoch 6 / 25) train acc: 0.547000; val acc: 0.523000
(Epoch 7 / 25) train acc: 0.583000; val acc: 0.538000
(Epoch 8 / 25) train acc: 0.550000; val acc: 0.538000
(Epoch 9 / 25) train acc: 0.604000; val acc: 0.543000
(Epoch 10 / 25) train acc: 0.616000; val acc: 0.572000
(Epoch 11 / 25) train acc: 0.647000; val acc: 0.551000
(Epoch 12 / 25) train acc: 0.614000; val_acc: 0.560000
(Epoch 13 / 25) train acc: 0.659000; val acc: 0.570000
(Epoch 14 / 25) train acc: 0.640000; val acc: 0.558000
(Epoch 15 / 25) train acc: 0.668000; val acc: 0.575000
(Epoch 16 / 25) train acc: 0.654000; val acc: 0.536000
(Epoch 17 / 25) train acc: 0.682000; val acc: 0.575000
(Epoch 18 / 25) train acc: 0.691000; val acc: 0.559000
(Epoch 19 / 25) train acc: 0.691000; val_acc: 0.563000
(Epoch 20 / 25) train acc: 0.689000; val acc: 0.584000
(Epoch 21 / 25) train acc: 0.725000; val acc: 0.563000
(Epoch 22 / 25) train acc: 0.725000; val acc: 0.580000
(Epoch 23 / 25) train acc: 0.737000; val_acc: 0.580000
(Epoch 24 / 25) train acc: 0.732000; val acc: 0.584000
(Epoch 25 / 25) train acc: 0.745000; val acc: 0.581000
```



```
In [ ]:
```

## Optimization for Fully Connected Networks ¶

In this notebook, we will implement different optimization rules for gradient descent. We have provided starter code; however, you will need to copy and paste your code from your implementation of the modular fully connected nets in HW #3 to build upon this.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc\_net, nndl.layers, and nndl.layer\_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
In [21]:
         ## Import and setups
         import time
         import numpy as np
         import matplotlib.pyplot as plt
         from nndl.fc net import *
         from cs231n.data utils import get CIFAR10 data
         from cs231n.gradient check import eval numerical gradient, eval numerical grad
         ient array
         from cs231n.solver import Solver
         %matplotlib inline
         plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
         plt.rcParams['image.interpolation'] = 'nearest'
         plt.rcParams['image.cmap'] = 'gray'
         # for auto-reloading external modules
         # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipyt
         hon
         %load ext autoreload
         %autoreload 2
         def rel error(x, y):
              """ returns relative error """
             return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

The autoreload extension is already loaded. To reload it, use: %reload\_ext autoreload

```
In [22]: # Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
    for k in data.keys():
        print('{}: {} '.format(k, data[k].shape))

X_train: (49000, 3, 32, 32)
    y_train: (49000,)
    X_val: (1000, 3, 32, 32)
    y_val: (1000,)
    X_test: (1000, 3, 32, 32)
    y test: (1000,)
```

## **Building upon your HW #3 implementation**

Copy and paste the following functions from your HW #3 implementation of a modular FC net:

- affine\_forward in nndl/layers.py
- affine\_backward in nndl/layers.py
- relu\_forward in nndl/layers.py
- relu\_backward in nndl/layers.py
- affine\_relu\_forward in nndl/layer\_utils.py
- affine\_relu\_backward in nndl/layer\_utils.py
- The FullyConnectedNet class in nndl/fc\_net.py

#### Test all functions you copy and pasted

```
In [23]: from nndl.layer tests import *
         affine forward test(); print('\n')
         affine backward test(); print('\n')
         relu forward test(); print('\n')
         relu_backward_test(); print('\n')
         affine relu test(); print('\n')
         fc net test()
         If affine forward function is working, difference should be less than 1e-9:
         difference: 9.769849468192957e-10
         If affine backward is working, error should be less than 1e-9::
         dx error: 9.7001660972913e-10
         dw error: 1.9467331804642562e-10
         db error: 2.401197073619289e-11
         If relu forward function is working, difference should be around 1e-8:
         difference: 4.999999798022158e-08
         If relu_forward function is working, error should be less than 1e-9:
         dx error: 3.275607283548242e-12
         If affine relu forward and affine relu backward are working, error should be
         less than 1e-9::
         dx error: 1.6210368436607981e-10
         dw error: 1.0685547312930863e-09
         db error: 2.03873222614578e-11
         Running check with reg = 0
         Initial loss: 2.298504732662749
         W1 relative error: 3.441720876378726e-07
         W2 relative error: 0.0016453542989429007
         W3 relative error: 1.1332196898657888e-05
         b1 relative error: 2.7032532322688614e-08
         b2 relative error: 9.765722933298838e-08
         b3 relative error: 9.316189665269062e-11
         Running check with reg = 3.14
         Initial loss: 5.768866480591484
         W1 relative error: 2.3215103605328982e-08
         W2 relative error: 1.491477525896267e-08
         W3 relative error: 6.950832483991784e-07
         b1 relative error: 1.664922788940843e-08
         b2 relative error: 1.0978462564862063e-08
```

b3 relative error: 2.3746117107946084e-10

# Training a larger model

In general, proceeding with vanilla stochastic gradient descent to optimize models may be fraught with problems and limitations, as discussed in class. Thus, we implement optimizers that improve on SGD.

#### SGD + momentum

In the following section, implement SGD with momentum. Read the nndl/optim.py API, which is provided by CS231n, and be sure you understand it. After, implement sgd\_momentum in nndl/optim.py. Test your implementation of sgd momentum by running the cell below.

```
In [24]: | from nndl.optim import sgd_momentum
        N, D = 4, 5
        w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
        dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
        v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
        config = {'learning_rate': 1e-3, 'velocity': v}
        next_w, _ = sgd_momentum(w, dw, config=config)
        expected next w = np.asarray([
            [0.47454737, 0.54133684, 0.60812632, 0.67491579, 0.74170526],
            [ 0.80849474, 0.87528421, 0.94207368, 1.00886316, 1.07565263],
            [ 1.14244211, 1.20923158, 1.27602105, 1.34281053, 1.4096
                                                                       11)
        expected velocity = np.asarray([
                      0.55475789, 0.56891579, 0.58307368, 0.59723158],
            [ 0.5406,
            [ 0.61138947, 0.62554737, 0.63970526, 0.65386316, 0.66802105],
            [ 0.68217895, 0.69633684, 0.71049474, 0.72465263, 0.73881053],
            [ 0.75296842, 0.76712632, 0.78128421, 0.79544211, 0.8096
                                                                       11)
        print('next w error: {}'.format(rel error(next w, expected next w)))
        print('velocity error: {}'.format(rel error(expected velocity, config['velocit
        y'])))
```

next\_w error: 8.882347033505819e-09 velocity error: 4.269287743278663e-09

### **SGD + Nesterov momentum**

Implement sgd\_nesterov\_momentum in ndl/optim.py .

```
In [25]: from nndl.optim import sgd nesterov momentum
         N, D = 4, 5
         w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
         dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
         v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
         config = {'learning rate': 1e-3, 'velocity': v}
         next w, = sgd nesterov momentum(w, dw, config=config)
         expected next w = np.asarray([
             [0.08714, 0.15246105, 0.21778211, 0.28310316, 0.34842421],
             [0.41374526, 0.47906632, 0.54438737, 0.60970842, 0.67502947],
             [0.74035053, 0.80567158, 0.87099263, 0.93631368, 1.00163474],
             [1.06695579, 1.13227684, 1.19759789, 1.26291895, 1.32824]])
         expected_velocity = np.asarray([
             [ 0.5406,
                       0.55475789, 0.56891579, 0.58307368, 0.59723158],
             [ 0.61138947, 0.62554737, 0.63970526, 0.65386316, 0.66802105],
             [0.68217895, 0.69633684, 0.71049474, 0.72465263, 0.73881053],
             [ 0.75296842, 0.76712632, 0.78128421, 0.79544211, 0.8096
                                                                           11)
         print('next_w error: {}'.format(rel_error(next_w, expected_next_w)))
         print('velocity error: {}'.format(rel error(expected velocity, config['velocit
         y'])))
```

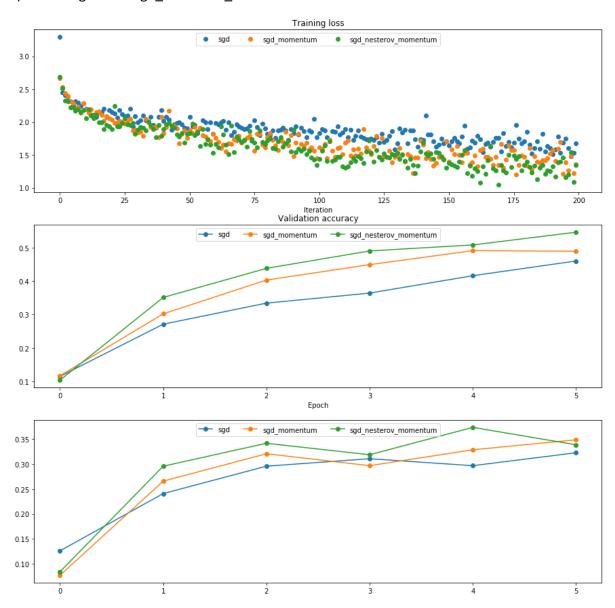
next\_w error: 1.0875186845081027e-08 velocity error: 4.269287743278663e-09

# Evaluating SGD, SGD+Momentum, and SGD+NesterovMomentum

Run the following cell to train a 6 layer FC net with SGD, SGD+momentum, and SGD+Nesterov momentum. You should see that SGD+momentum achieves a better loss than SGD, and that SGD+Nesterov momentum achieves a slightly better loss (and training accuracy) than SGD+momentum.

```
In [26]:
         num train = 4000
         small data = {
             'X_train': data['X_train'][:num_train],
              'y_train': data['y_train'][:num_train],
              'X_val': data['X_val'],
              'y_val': data['y_val'],
         }
         solvers = {}
         for update_rule in ['sgd', 'sgd_momentum', 'sgd_nesterov_momentum']:
             print('Optimizing with {}'.format(update_rule))
             model = FullyConnectedNet([100, 100, 100, 100], weight_scale=5e-2)
             solver = Solver(model, small data,
                              num_epochs=5, batch_size=100,
                              update rule=update rule,
                              optim config={
                                'learning_rate': 1e-2,
                              },
                              verbose=False)
             solvers[update_rule] = solver
             solver.train()
             print
         fig, axes = plt.subplots(3, 1)
         ax = axes[0]
         ax.set title('Training loss')
         ax.set xlabel('Iteration')
         ax = axes[1]
         ax.set title('Training accuracy')
         ax.set xlabel('Epoch')
         ax = axes[1]
         ax.set title('Validation accuracy')
         ax.set_xlabel('Epoch')
         for update rule, solver in solvers.items():
             ax = axes[0]
             ax.plot(solver.loss_history, 'o', label=update_rule)
             ax = axes[1]
             ax.plot(solver.train acc history, '-o', label=update rule)
             ax = axes[2]
             ax.plot(solver.val_acc_history, '-o', label=update_rule)
         for i in [1, 2, 3]:
             ax = axes[i - 1]
             ax.legend(loc='upper center', ncol=4)
         plt.gcf().set_size_inches(15, 15)
         plt.show()
```

Optimizing with sgd Optimizing with sgd\_momentum Optimizing with sgd\_nesterov\_momentum



# **RMSProp**

Now we go to techniques that adapt the gradient. Implement <code>rmsprop</code> in <code>nndl/optim.py</code> . Test your implementation by running the cell below.

```
In [27]: from nndl.optim import rmsprop
         N, D = 4, 5
         w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
         dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
         a = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
         config = {'learning rate': 1e-2, 'a': a}
         next_w, _ = rmsprop(w, dw, config=config)
         expected next w = np.asarray([
           [-0.39223849, -0.34037513, -0.28849239, -0.23659121, -0.18467247],
           [-0.132737, -0.08078555, -0.02881884, 0.02316247, 0.07515774],
           [ 0.12716641, 0.17918792, 0.23122175, 0.28326742, 0.33532447],
           [ 0.38739248, 0.43947102, 0.49155973, 0.54365823, 0.59576619]])
         expected_cache = np.asarray([
           0.5976,
                     0.6126277, 0.6277108, 0.64284931, 0.65804321],
           [ 0.67329252, 0.68859723, 0.70395734, 0.71937285, 0.73484377],
           [ 0.75037008, 0.7659518, 0.78158892, 0.79728144, 0.81302936],
           [ 0.82883269, 0.84469141, 0.86060554, 0.87657507, 0.8926
         print('next_w error: {}'.format(rel_error(expected_next_w, next_w)))
         print('cache error: {}'.format(rel error(expected cache, config['a'])))
```

next\_w error: 9.502645229894295e-08 cache error: 2.6477955807156126e-09

## **Adaptive moments**

Now, implement adam in nndl/optim.py . Test your implementation by running the cell below.

```
In [28]: # Test Adam implementation; you should see errors around 1e-7 or less
        from nndl.optim import adam
        N, D = 4, 5
        w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
        dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
        v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
        a = np.linspace(0.7, 0.5, num=N*D).reshape(N, D)
        config = {'learning_rate': 1e-2, 'v': v, 'a': a, 't': 5}
        next_w, _ = adam(w, dw, config=config)
        expected next w = np.asarray([
          [-0.40094747, -0.34836187, -0.29577703, -0.24319299, -0.19060977],
          [-0.1380274, -0.08544591, -0.03286534, 0.01971428, 0.0722929],
          [ 0.1248705, 0.17744702, 0.23002243, 0.28259667, 0.33516969],
          [ 0.38774145, 0.44031188, 0.49288093, 0.54544852, 0.59801459]])
        expected_a = np.asarray([
          [ 0.64683452, 0.63628604, 0.6257431, 0.61520571, 0.60467385,],
          [ 0.59414753, 0.58362676, 0.57311152, 0.56260183, 0.55209767,],
          [ 0.54159906, 0.53110598, 0.52061845, 0.51013645, 0.49966, ]])
        expected v = np.asarray([
                  0.49947368, 0.51894737, 0.53842105, 0.55789474],
          0.48,
          [ 0.57736842, 0.59684211, 0.61631579, 0.63578947,
                                                            0.65526316],
          [ 0.67473684, 0.69421053, 0.71368421, 0.73315789, 0.75263158],
          [ 0.77210526, 0.79157895, 0.81105263, 0.83052632, 0.85
                                                                      11)
        print('next w error: {}'.format(rel error(expected next w, next w)))
        print('a error: {}'.format(rel error(expected a, config['a'])))
        print('v error: {}'.format(rel_error(expected_v, config['v'])))
```

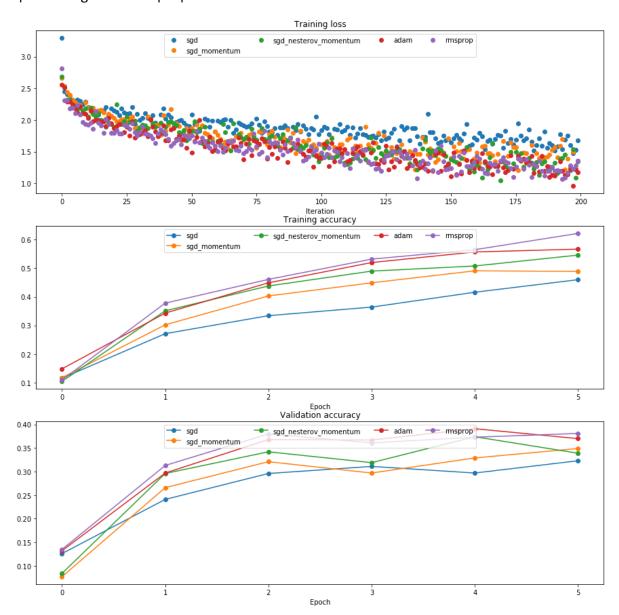
next\_w error: 1.1395691798535431e-07 a error: 4.208314038113071e-09 v error: 4.214963193114416e-09

# Comparing SGD, SGD+NesterovMomentum, RMSProp, and Adam

The following code will compare optimization with SGD, Momentum, Nesterov Momentum, RMSProp and Adam. In our code, we find that RMSProp, Adam, and SGD + Nesterov Momentum achieve approximately the same training error after a few training epochs.

```
In [29]: learning rates = {'rmsprop': 2e-4, 'adam': 1e-3}
         for update_rule in ['adam', 'rmsprop']:
             print('Optimizing with {}'.format(update rule))
             model = FullyConnectedNet([100, 100, 100, 100], weight scale=5e-2)
             solver = Solver(model, small data,
                              num epochs=5, batch size=100,
                              update rule=update rule,
                              optim_config={
                                'learning rate': learning rates[update rule]
                              },
                              verbose=False)
             solvers[update rule] = solver
             solver.train()
             print
         fig, axes = plt.subplots(3, 1)
         ax = axes[0]
         ax.set title('Training loss')
         ax.set_xlabel('Iteration')
         ax = axes[1]
         ax.set_title('Training accuracy')
         ax.set xlabel('Epoch')
         ax = axes[2]
         ax.set title('Validation accuracy')
         ax.set xlabel('Epoch')
         for update_rule, solver in solvers.items():
             ax = axes[0]
             ax.plot(solver.loss_history, 'o', label=update_rule)
             ax = axes[1]
             ax.plot(solver.train_acc_history, '-o', label=update_rule)
             ax = axes[2]
             ax.plot(solver.val_acc_history, '-o', label=update_rule)
         for i in [1, 2, 3]:
             ax = axes[i - 1]
             ax.legend(loc='upper center', ncol=4)
         plt.gcf().set size inches(15, 15)
         plt.show()
```

Optimizing with adam
Optimizing with rmsprop



## **Easier optimization**

In the following cell, we'll train a 4 layer neural network having 500 units in each hidden layer with the different optimizers, and find that it is far easier to get up to 50+% performance on CIFAR-10. After we implement batchnorm and dropout, we'll ask you to get 55+% on CIFAR-10.

```
In [30]:
         optimizer = 'adam'
         best_model = None
         layer dims = [500, 500, 500]
         weight_scale = 0.01
         learning_rate = 1e-3
         lr_decay = 0.9
         model = FullyConnectedNet(layer_dims, weight_scale=weight_scale,
                                    use_batchnorm=True)
         solver = Solver(model, data,
                          num_epochs=10, batch_size=100,
                          update_rule=optimizer,
                          optim_config={
                            'learning_rate': learning_rate,
                          lr_decay=lr_decay,
                          verbose=True, print_every=50)
         solver.train()
```

```
(Iteration 1 / 4900) loss: 2.303543
(Epoch 0 / 10) train acc: 0.223000; val_acc: 0.236000
(Iteration 51 / 4900) loss: 1.616151
(Iteration 101 / 4900) loss: 1.560856
(Iteration 151 / 4900) loss: 1.675130
(Iteration 201 / 4900) loss: 1.504756
(Iteration 251 / 4900) loss: 1.548248
(Iteration 301 / 4900) loss: 1.743961
(Iteration 351 / 4900) loss: 1.635753
(Iteration 401 / 4900) loss: 1.272982
(Iteration 451 / 4900) loss: 1.365792
(Epoch 1 / 10) train acc: 0.446000; val acc: 0.447000
(Iteration 501 / 4900) loss: 1.270328
(Iteration 551 / 4900) loss: 1.338089
(Iteration 601 / 4900) loss: 1.376788
(Iteration 651 / 4900) loss: 1.412572
(Iteration 701 / 4900) loss: 1.294532
(Iteration 751 / 4900) loss: 1.470213
(Iteration 801 / 4900) loss: 1.307858
(Iteration 851 / 4900) loss: 1.083214
(Iteration 901 / 4900) loss: 1.363130
(Iteration 951 / 4900) loss: 1.364597
(Epoch 2 / 10) train acc: 0.539000; val acc: 0.501000
(Iteration 1001 / 4900) loss: 1.207127
(Iteration 1051 / 4900) loss: 1.059530
(Iteration 1101 / 4900) loss: 1.372460
(Iteration 1151 / 4900) loss: 1.206474
(Iteration 1201 / 4900) loss: 1.160314
(Iteration 1251 / 4900) loss: 1.068041
(Iteration 1301 / 4900) loss: 1.189605
(Iteration 1351 / 4900) loss: 1.108745
(Iteration 1401 / 4900) loss: 1.064507
(Iteration 1451 / 4900) loss: 0.972385
(Epoch 3 / 10) train acc: 0.589000; val acc: 0.535000
(Iteration 1501 / 4900) loss: 1.018779
(Iteration 1551 / 4900) loss: 1.099075
(Iteration 1601 / 4900) loss: 1.036061
(Iteration 1651 / 4900) loss: 1.044130
(Iteration 1701 / 4900) loss: 1.105588
(Iteration 1751 / 4900) loss: 1.028885
(Iteration 1801 / 4900) loss: 1.376958
(Iteration 1851 / 4900) loss: 1.024990
(Iteration 1901 / 4900) loss: 1.124237
(Iteration 1951 / 4900) loss: 1.072946
(Epoch 4 / 10) train acc: 0.664000; val acc: 0.555000
(Iteration 2001 / 4900) loss: 1.002824
(Iteration 2051 / 4900) loss: 1.139111
(Iteration 2101 / 4900) loss: 1.245468
(Iteration 2151 / 4900) loss: 0.956545
(Iteration 2201 / 4900) loss: 1.080563
(Iteration 2251 / 4900) loss: 1.364691
(Iteration 2301 / 4900) loss: 1.046358
(Iteration 2351 / 4900) loss: 1.001033
(Iteration 2401 / 4900) loss: 1.006896
(Epoch 5 / 10) train acc: 0.679000; val acc: 0.554000
(Iteration 2451 / 4900) loss: 0.971773
(Iteration 2501 / 4900) loss: 0.982336
```

```
(Iteration 2551 / 4900) loss: 1.043616
(Iteration 2601 / 4900) loss: 0.835508
(Iteration 2651 / 4900) loss: 0.905280
(Iteration 2701 / 4900) loss: 0.917310
(Iteration 2751 / 4900) loss: 1.089185
(Iteration 2801 / 4900) loss: 0.723714
(Iteration 2851 / 4900) loss: 1.046396
(Iteration 2901 / 4900) loss: 0.984314
(Epoch 6 / 10) train acc: 0.689000; val acc: 0.548000
(Iteration 2951 / 4900) loss: 0.965833
(Iteration 3001 / 4900) loss: 0.778126
(Iteration 3051 / 4900) loss: 0.722649
(Iteration 3101 / 4900) loss: 0.780464
(Iteration 3151 / 4900) loss: 0.969116
(Iteration 3201 / 4900) loss: 1.015220
(Iteration 3251 / 4900) loss: 0.839203
(Iteration 3301 / 4900) loss: 0.909355
(Iteration 3351 / 4900) loss: 0.809903
(Iteration 3401 / 4900) loss: 0.688846
(Epoch 7 / 10) train acc: 0.747000; val acc: 0.558000
(Iteration 3451 / 4900) loss: 0.664208
(Iteration 3501 / 4900) loss: 0.821839
(Iteration 3551 / 4900) loss: 0.700366
(Iteration 3601 / 4900) loss: 0.897436
(Iteration 3651 / 4900) loss: 0.594077
(Iteration 3701 / 4900) loss: 0.678255
(Iteration 3751 / 4900) loss: 0.846518
(Iteration 3801 / 4900) loss: 0.943544
(Iteration 3851 / 4900) loss: 0.751994
(Iteration 3901 / 4900) loss: 0.581836
(Epoch 8 / 10) train acc: 0.758000; val_acc: 0.530000
(Iteration 3951 / 4900) loss: 0.730017
(Iteration 4001 / 4900) loss: 0.512517
(Iteration 4051 / 4900) loss: 0.591482
(Iteration 4101 / 4900) loss: 0.631400
(Iteration 4151 / 4900) loss: 0.437395
(Iteration 4201 / 4900) loss: 0.485689
(Iteration 4251 / 4900) loss: 0.683630
(Iteration 4301 / 4900) loss: 0.600873
(Iteration 4351 / 4900) loss: 0.561936
(Iteration 4401 / 4900) loss: 0.630310
(Epoch 9 / 10) train acc: 0.792000; val acc: 0.564000
(Iteration 4451 / 4900) loss: 0.726963
(Iteration 4501 / 4900) loss: 0.617750
(Iteration 4551 / 4900) loss: 0.750790
(Iteration 4601 / 4900) loss: 0.616022
(Iteration 4651 / 4900) loss: 0.654611
(Iteration 4701 / 4900) loss: 0.681487
(Iteration 4751 / 4900) loss: 0.593138
(Iteration 4801 / 4900) loss: 0.577364
(Iteration 4851 / 4900) loss: 0.631781
(Epoch 10 / 10) train acc: 0.821000; val acc: 0.549000
```

```
import numpy as np
import pdb
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use in the
ECE 239AS class at UCLA. This includes the descriptions of what code to
implement as well as some slight potential changes in variable names to be
consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
permission to use this code. To see the original version, please visit
cs231n.stanford.edu.
def affine_forward(x, w, b):
   Computes the forward pass for an affine (fully-connected) layer.
   The input x has shape (N, d_1, \ldots, d_k) and contains a minibatch of N
   examples, where each example x[i] has shape (d_1, \ldots, d_k). We will
   reshape each input into a vector of dimension D = d_1 * ... * d_k, and
   then transform it to an output vector of dimension M.
   Inputs:
   - x: A numpy array containing input data, of shape (N, d 1, ..., d k)
   - w: A numpy array of weights, of shape (D, M)
   - b: A numpy array of biases, of shape (M,)
   Returns a tuple of:
   - out: output, of shape (N, M)
   - cache: (x, w, b)
   out = None
   # YOUR CODE HERE:
      Calculate the output of the forward pass. Notice the dimensions
      of w are D x M, which is the transpose of what we did in earlier
      assignments.
   x reshape = x.reshape(x.shape[0], -1)
   out = np.dot(x_reshape, w) + b
   # END YOUR CODE HERE
   cache = (x, w, b)
   return out, cache
def affine_backward(dout, cache):
   Computes the backward pass for an affine layer.
   Inputs:
   - dout: Upstream derivative, of shape (N, M)
   - cache: Tuple of:
     - x: A numpy array containing input data, of shape (N, d_1, \ldots, d_k)
     - w: A numpy array of weights, of shape (D, M)
     - b: A numpy array of biases, of shape (M,)
   Returns a tuple of:
   - dx: Gradient with respect to x, of shape (N, d1, ..., d_k)
```

```
- dw: Gradient with respect to w, of shape (D, M)
   - db: Gradient with respect to b, of shape (M,)
  x, w, b = cache
  dx, dw, db = None, None, None
  # YOUR CODE HERE:
     Calculate the gradients for the backward pass.
  # Notice:
     dout is N x M
     dx should be N x d1 x ... x dk; it relates to dout through multiplication with w, which is D x M
     dw should be D \times M; it relates to dout through multiplication with \times, which is N \times D after reshaping
     db should be M; it is just the sum over dout examples
  x_reshape = x.reshape(x.shape[0], -1)
  db = np.sum(dout, axis=0)
  dw = np.dot(x reshape.T, dout)
  dx = np.dot(dout, w.T).reshape(x.shape)
  # ============================ #
  # END YOUR CODE HERE
  return dx, dw, db
def relu forward(x):
  Computes the forward pass for a layer of rectified linear units (ReLUs).
  Input:
   - x: Inputs, of any shape
  Returns a tuple of:
  - out: Output, of the same shape as x
  # YOUR CODE HERE:
     Implement the ReLU forward pass.
  relu = lambda x: x * (x > 0)
  out = relu(x)
  # END YOUR CODE HERE
  cache = x
  return out, cache
def relu_backward(dout, cache):
  Computes the backward pass for a layer of rectified linear units (ReLUs).
  Input:
   - dout: Upstream derivatives, of any shape
   - cache: Input x, of same shape as dout
  Returns:
   - dx: Gradient with respect to x
```

```
x = cache
   # YOUR CODE HERE:
      Implement the ReLU backward pass
   dx = dout * (x > 0)
   # END YOUR CODE HERE
   return dx
def batchnorm forward(x, gamma, beta, bn param):
   Forward pass for batch normalization.
   During training the sample mean and (uncorrected) sample variance are
   computed from minibatch statistics and used to normalize the incoming data.
   During training we also keep an exponentially decaying running mean of the mean
   and variance of each feature, and these averages are used to normalize data
   at test-time.
   At each timestep we update the running averages for mean and variance using
   an exponential decay based on the momentum parameter:
   running_mean = momentum * running_mean + (1 - momentum) * sample_mean
   running_var = momentum * running_var + (1 - momentum) * sample_var
   Note that the batch normalization paper suggests a different test-time
   behavior: they compute sample mean and variance for each feature using a
   large number of training images rather than using a running average. For
   this implementation we have chosen to use running averages instead since
   they do not require an additional estimation step; the torch7 implementation
   of batch normalization also uses running averages.
   Input:
   - x: Data of shape (N, D)
   - gamma: Scale parameter of shape (D,)
   - beta: Shift paremeter of shape (D,)
   - bn_param: Dictionary with the following keys:
     - mode: 'train' or 'test'; required
     - eps: Constant for numeric stability
     - momentum: Constant for running mean / variance.
     - running_mean: Array of shape (D,) giving running mean of features
     - running_var Array of shape (D,) giving running variance of features
   Returns a tuple of:
   - out: of shape (N, D)
   - cache: A tuple of values needed in the backward pass
   mode = bn param['mode']
   eps = bn_param.get('eps', 1e-5)
   momentum = bn_param.get('momentum', 0.9)
   N, D = x.shape
   running mean = bn param.get('running mean', np.zeros(D, dtype=x.dtype))
   running_var = bn_param.get('running_var', np.zeros(D, dtype=x.dtype))
   out, cache = None, None
   if mode == 'train':
```

```
# ----- #
      # YOUR CODE HERE:
        A few steps here:
          (1) Calculate the running mean and variance of the minibatch.
          (2) Normalize the activations with the running mean and variance.
      #
          (3) Scale and shift the normalized activations. Store this
             as the variable 'out'
          (4) Store any variables you may need for the backward pass in
      #
             the 'cache' variable.
      mean_sample = np.mean(x, axis=0)
      var_sample = np.var(x, axis=0)
      running mean = momentum * running mean + (1 - momentum) * mean sample
      running_var = momentum * running_var + (1 - momentum) * var_sample
      xhat = (x - mean_sample) / np.sqrt(var_sample + eps)
      out = gamma * xhat + beta
      cache = (x, xhat, mean_sample, var_sample, gamma, beta, eps)
      # END YOUR CODE HERE
      elif mode == 'test':
      # YOUR CODE HERE:
      # Calculate the testing time normalized activation. Normalize using
        the running mean and variance, and then scale and shift appropriately.
      # Store the output as 'out'.
      outhat = (x - running_mean) / np.sqrt(running_var + eps)
      out = outhat * gamma + beta
      # END YOUR CODE HERE
      else:
      raise ValueError('Invalid forward batchnorm mode "%s"' % mode)
   # Store the updated running means back into bn param
   bn param['running mean'] = running mean
   bn_param['running_var'] = running var
   return out, cache
def batchnorm_backward(dout, cache):
   Backward pass for batch normalization.
   For this implementation, you should write out a computation graph for
   batch normalization on paper and propagate gradients backward through
   intermediate nodes.
   Inputs:
   - dout: Upstream derivatives, of shape (N, D)
   - cache: Variable of intermediates from batchnorm forward.
   Returns a tuple of:
   - dx: Gradient with respect to inputs x, of shape (N, D)
   - dgamma: Gradient with respect to scale parameter gamma, of shape (D,)
   - dbeta: Gradient with respect to shift parameter beta, of shape (D,)
```

```
dx, dgamma, dbeta = None, None, None
   # YOUR CODE HERE:
     Implement the batchnorm backward pass, calculating dx, dgamma, and dbeta.
   N, D = dout.shape
   x, xhat, sample_mean, var_sample, gamma, _, eps = cache
   dgamma = np.sum(dout * xhat, axis=0)
   dbeta = np.sum(dout, axis=0)
   dxhat = gamma * dout
   var sample eps = 1/np.sqrt(var sample + eps)
   dx = var_sample_eps * (1/N) * gamma * (dout * N - dbeta - (xhat * dgamma))
   # END YOUR CODE HERE
   return dx, dgamma, dbeta
def dropout_forward(x, dropout_param):
   Performs the forward pass for (inverted) dropout.
   Inputs:
   - x: Input data, of any shape
   - dropout_param: A dictionary with the following keys:
    - p: Dropout parameter. We keep each neuron output with probability p.
    - mode: 'test' or 'train'. If the mode is train, then perform dropout;
      if the mode is test, then just return the input.
    - seed: Seed for the random number generator. Passing seed makes this
      function deterministic, which is needed for gradient checking but not in
      real networks.
   Outputs:
   - out: Array of the same shape as x.
   - cache: A tuple (dropout_param, mask). In training mode, mask is the dropout
    mask that was used to multiply the input; in test mode, mask is None.
   p, mode = dropout_param['p'], dropout_param['mode']
   if 'seed' in dropout param:
      np.random.seed(dropout_param['seed'])
   mask = None
   out = None
   if mode == 'train':
      # ----- #
      # YOUR CODE HERE:
         Implement the inverted dropout forward pass during training time.
         Store the masked and scaled activations in out, and store the
         dropout mask as the variable mask.
      # ------ #
      mask = np.random.uniform(low=0, high=1, size = x.shape) > p
      out = x * mask
      # ----- #
      # FND YOUR CODE HERE
      # ============================ #
```

```
elif mode == 'test':
    # ------ #
    # YOUR CODE HERE:
       Implement the inverted dropout forward pass during test time.
    out = x
    # END YOUR CODE HERE
    cache = (dropout param, mask)
  out = out.astype(x.dtype, copy=False)
  return out, cache
def dropout backward(dout, cache):
  Perform the backward pass for (inverted) dropout.
  Inputs:
  - dout: Upstream derivatives, of any shape
  - cache: (dropout_param, mask) from dropout_forward.
  dropout_param, mask = cache
  mode = dropout param['mode']
  dx = None
  if mode == 'train':
    # YOUR CODE HERE:
      Implement the inverted dropout backward pass during training time.
    dx = dout * mask
    # END YOUR CODE HERE
    # ------ #
  elif mode == 'test':
    # ------ #
    # YOUR CODE HERE:
      Implement the inverted dropout backward pass during test time.
    dx = dout
    # ----- #
    # END YOUR CODE HERE
    return dx
def svm_loss(x, y):
  Computes the loss and gradient using for multiclass SVM classification.
  Inputs:
  - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
   for the ith input.
  - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
   \theta \leftarrow y[i] \leftarrow C
```

```
Returns a tuple of:
    - loss: Scalar giving the loss
    - dx: Gradient of the loss with respect to x
   N = x.shape[0]
    correct_class_scores = x[np.arange(N), y]
    margins = np.maximum(0, x - correct_class_scores[:, np.newaxis] + 1.0)
   margins[np.arange(N), y] = 0
    loss = np.sum(margins) / N
    num pos = np.sum(margins > 0, axis=1)
    dx = np.zeros_like(x)
    dx[margins > 0] = 1
    dx[np.arange(N), y] -= num pos
    dx /= N
    return loss, dx
def softmax_loss(x, y):
    Computes the loss and gradient for softmax classification.
    Inputs:
    - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
     for the ith input.
    - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
     0 <= y[i] < C
    Returns a tuple of:
    - loss: Scalar giving the loss
    - dx: Gradient of the loss with respect to x
    probs = np.exp(x - np.max(x, axis=1, keepdims=True))
    probs /= np.sum(probs, axis=1, keepdims=True)
    N = x.shape[0]
    loss = -np.sum(np.log(probs[np.arange(N), y])) / N
    dx = probs.copy()
    dx[np.arange(N), y] -= 1
    dx /= N
    return loss, dx
def affine batchnorm relu forward(x, w, b, gamma, beta, bn param):
 Convenience layer that performs an affine transform, batch normalization,
 and ReLU.
 Inputs:
  - x: Array of shape (N, D1); input to the affine layer
  - w, b: Arrays of shape (D2, D2) and (D2,) giving the weight and bias for
    the affine transform.
  - gamma, beta: Arrays of shape (D2,) and (D2,) giving scale and shift
   parameters for batch normalization.
  - bn_param: Dictionary of parameters for batch normalization.
  Returns:
  - out: Output from ReLU, of shape (N, D2)
  - cache: Object to give to the backward pass.
 a, fc cache = affine forward(x, w, b)
 a_bn, bn_cache = batchnorm_forward(a, gamma, beta, bn_param)
 out, relu cache = relu forward(a bn)
 cache = (fc_cache, bn_cache, relu_cache)
 return out, cache
def affine batchnorm relu backward(dout, cache):
```

Backward pass for the affine-batchnorm-relu convenience layer.

```
fc_cache, bn_cache, relu_cache = cache
da_bn = relu_backward(dout, relu_cache)
da, dgamma, dbeta = batchnorm_backward(da_bn, bn_cache)
dx, dw, db = affine_backward(da, fc_cache)
return dx, dw, db, dgamma, dbeta
```

```
import numpy as np
```

.....

This code was originally written for CS 231n at Stanford University (cs231n.stanford.edu). It has been modified in various areas for use in the ECE 239AS class at UCLA. This includes the descriptions of what code to implement as well as some slight potential changes in variable names to be consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for permission to use this code. To see the original version, please visit cs231n.stanford.edu.

.....

This file implements various first-order update rules that are commonly used for training neural networks. Each update rule accepts current weights and the gradient of the loss with respect to those weights and produces the next set of weights. Each update rule has the same interface:

def update(w, dw, config=None):

## Inputs:

- w: A numpy array giving the current weights.
- dw: A numpy array of the same shape as w giving the gradient of the loss with respect to w.
- config: A dictionary containing hyperparameter values such as learning rate, momentum, etc. If the update rule requires caching values over many iterations, then config will also hold these cached values.

## Returns:

- next\_w: The next point after the update.
- config: The config dictionary to be passed to the next iteration of the update rule.

NOTE: For most update rules, the default learning rate will probably not perform well; however the default values of the other hyperparameters should work well for a variety of different problems.

For efficiency, update rules may perform in-place updates, mutating w and setting next\_w equal to w.

```
def sgd(w, dw, config=None):
    """
    Performs vanilla stochastic gradient descent.

    config format:
        - learning_rate: Scalar learning rate.
        """
    if config is None: config = {}
        config.setdefault('learning_rate', 1e-2)

    w -= config['learning_rate'] * dw
    return w, config

def sgd_momentum(w, dw, config=None):
    """
```

Performs stochastic gradient descent with momentum.

```
config format:
   - Learning rate: Scalar Learning rate.
   - momentum: Scalar between 0 and 1 giving the momentum value.
    Setting momentum = 0 reduces to sqd.
   - velocity: A numpy array of the same shape as w and dw used to store a moving
    average of the gradients.
   if config is None: config = {}
   config.setdefault('learning rate', 1e-2)
   config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
   v = config.get('velocity', np.zeros like(w)) # gets velocity, else sets it to zero.
   # YOUR CODE HERE:
     Implement the momentum update formula. Return the updated weights
     as next w, and the updated velocity as v.
   # ----- #
   alpha = config['momentum']
   epsilon = config['learning rate']
   v = alpha * v - epsilon * dw
   next w = w + v
   # ----------- #
   # END YOUR CODE HERE
   # ----------- #
   config['velocity'] = v
   return next w, config
def sgd_nesterov_momentum(w, dw, config=None):
   Performs stochastic gradient descent with Nesterov momentum.
   config format:
   - Learning rate: Scalar learning rate.
   - momentum: Scalar between 0 and 1 giving the momentum value.
    Setting momentum = 0 reduces to sqd.
   - velocity: A numpy array of the same shape as w and dw used to store a moving
    average of the gradients.
   if config is None: config = {}
   config.setdefault('learning_rate', 1e-2)
   config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
   v = config.get('velocity', np.zeros like(w)) # gets velocity, else sets it to zero.
   # ----------- #
   # YOUR CODE HERE:
     Implement the momentum update formula. Return the updated weights
   # as next_w, and the updated velocity as v.
   # ------ #
   alpha = config['momentum']
   epsilon = config['learning_rate']
   v old = v
   v = alpha * v - epsilon * dw
   next w = w + v + alpha * (v - v old)
   # ----- #
   # END YOUR CODE HERE
   config['velocity'] = v
```

```
return next w, config
def rmsprop(w, dw, config=None):
   Uses the RMSProp update rule, which uses a moving average of squared gradient
   values to set adaptive per-parameter learning rates.
   config format:
   - Learning_rate: Scalar Learning rate.
   - decay rate: Scalar between 0 and 1 giving the decay rate for the squared
     gradient cache.
   - epsilon: Small scalar used for smoothing to avoid dividing by zero.
   - beta: Moving average of second moments of gradients.
   if config is None: config = {}
   config.setdefault('learning_rate', 1e-2)
   config.setdefault('decay rate', 0.99)
   config.setdefault('epsilon', 1e-8)
   config.setdefault('a', np.zeros_like(w))
   next w = None
   # YOUR CODE HERE:
     Implement RMSProp. Store the next value of w as next w. You need
     to also store in config['a'] the moving average of the second
      moment gradients, so they can be used for future gradients. Concretely,
     config['a'] corresponds to "a" in the lecture notes.
   a = config['a']
   learning_rate = config['learning_rate']
   epsilon = config['epsilon']
   beta = 0.99
   a = beta * a + (1 - beta) * dw * dw
   next_w = w - learning_rate * dw / (np.sqrt(a + epsilon))
   config['a'] = a
   # END YOUR CODE HERE
   return next_w, config
def adam(w, dw, config=None):
   Uses the Adam update rule, which incorporates moving averages of both the
   gradient and its square and a bias correction term.
   config format:
   - Learning rate: Scalar Learning rate.
   - beta1: Decay rate for moving average of first moment of gradient.
   - beta2: Decay rate for moving average of second moment of gradient.
   - epsilon: Small scalar used for smoothing to avoid dividing by zero.
   - m: Moving average of gradient.
   - v: Moving average of squared gradient.
   - t: Iteration number.
   if config is None: config = {}
   config.setdefault('learning_rate', 1e-3)
   config.setdefault('beta1', 0.9)
```

```
config.setdefault('beta2', 0.999)
config.setdefault('epsilon', 1e-8)
config.setdefault('v', np.zeros_like(w))
config.setdefault('a', np.zeros like(w))
config.setdefault('t', 0)
next w = None
# ------ #
# YOUR CODE HERE:
  Implement Adam. Store the next value of w as next w. You need
  to also store in config['a'] the moving average of the second
# moment gradients, and in config['v'] the moving average of the
  first moments. Finally, store in config['t'] the increasing time.
# =========== #
learning_rate = config['learning_rate']
beta1 = config['beta1']
beta2 = config['beta2']
epsilon = config['epsilon']
v = config['v']
a = config['a']
t = config['t']
t+=1
v = beta1 * v + (1 - beta1)*dw
a = beta2 * a + (1 - beta2) * dw * dw
v_{tild} = v / (1 - beta1**t)
a_{tild} = a / (1 - beta2**t)
next_w = w - learning_rate * v_tild / (np.sqrt(a_tild) + epsilon)
config['v'] = v
config['a'] = a
config['t'] = t
# END YOUR CODE HERE
```

return next\_w, config

```
import numpy as np
import pdb
from .layers import *
from .layer_utils import *
.....
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use in the
ECE 239AS class at UCLA. This includes the descriptions of what code to
implement as well as some slight potential changes in variable names to be
consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
permission to use this code. To see the original version, please visit
cs231n.stanford.edu.
class TwoLayerNet(object):
 A two-layer fully-connected neural network with ReLU nonlinearity and
 softmax loss that uses a modular layer design. We assume an input dimension
 of D, a hidden dimension of H, and perform classification over C classes.
 The architecure should be affine - relu - affine - softmax.
 Note that this class does not implement gradient descent; instead, it
 will interact with a separate Solver object that is responsible for running
 optimization.
 The learnable parameters of the model are stored in the dictionary
 self.params that maps parameter names to numpy arrays.
 def __init__(self, input_dim=3*32*32, hidden_dims=100, num_classes=10,
             dropout=0, weight_scale=1e-3, reg=0.0):
   Initialize a new network.
   Inputs:
   - input_dim: An integer giving the size of the input
   - hidden_dims: An integer giving the size of the hidden layer
   - num_classes: An integer giving the number of classes to classify
   - dropout: Scalar between 0 and 1 giving dropout strength.
   - weight scale: Scalar giving the standard deviation for random
     initialization of the weights.
   - reg: Scalar giving L2 regularization strength.
   self.params = {}
   self.reg = reg
   Initialize W1, W2, b1, and b2. Store these as self.params['W1'],
      self.params['W2'], self.params['b1'] and self.params['b2']. The
      biases are initialized to zero and the weights are initialized
      so that each parameter has mean 0 and standard deviation weight scale.
      The dimensions of W1 should be (input_dim, hidden_dim) and the
       dimensions of W2 should be (hidden dims, num classes)
   self.params['W2'] = weight_scale * np.random.randn(hidden_dims, num_classes)
   self.params['b2'] = np.zeros(num classes)
   self.params['W1'] = weight scale * np.random.randn(input dim, hidden dims)
   self.params['b1'] = np.zeros(hidden_dims)
   # ------ #
   # END YOUR CODE HERE
```

```
# ------ #
def loss(self, X, y=None):
 Compute loss and gradient for a minibatch of data.
 Innuts:
 - X: Array of input data of shape (N, d_1, ..., d_k)
 - y: Array of labels, of shape (N,). y[i] gives the label for X[i].
 Returns:
 If y is None, then run a test-time forward pass of the model and return:
 - scores: Array of shape (N, C) giving classification scores, where
   scores[i, c] is the classification score for X[i] and class c.
 If y is not None, then run a training-time forward and backward pass and
 return a tuple of:
 - loss: Scalar value giving the loss
 - grads: Dictionary with the same keys as self.params, mapping parameter
   names to gradients of the loss with respect to those parameters.
 scores = None
 # YOUR CODE HERE:
    Implement the forward pass of the two-layer neural network. Store
    the class scores as the variable 'scores'. Be sure to use the layers
   you prior implemented.
 h1, cache1 = affine_relu_forward(X, self.params['W1'], self.params['b1'])
 scores, cache2 = affine_forward(h1, self.params['W2'], self.params['b2'])
 # END YOUR CODE HERE
 # If y is None then we are in test mode so just return scores
 if y is None:
   return scores
 loss, grads = 0, {}
 # YOUR CODE HERE:
    Implement the backward pass of the two-layer neural net. Store
    the loss as the variable 'loss' and store the gradients in the
    'grads' dictionary. For the grads dictionary, grads['W1'] holds
    the gradient for W1, grads['b1'] holds the gradient for b1, etc.
    i.e., grads[k] holds the gradient for self.params[k].
 #
    Add L2 regularization, where there is an added cost 0.5*self.reg*W^2
    for each W. Be sure to include the 0.5 multiplying factor to
    match our implementation.
    And be sure to use the layers you prior implemented.
 loss, ds = softmax_loss(scores, y)
 dreg = self.reg * 0.5*(np.sum(self.params['W1'] ** 2) + np.sum(self.params['W2'] ** 2))
 loss += dreg
 d_h1, grads['W2'], grads['b2'] = affine_backward(ds, cache2)
 grads['W2'] += self.reg * self.params['W2']
 dx, grads['W1'], grads['b1'] = affine_relu_backward(d_h1, cache1)
 grads['W1'] += self.reg * self.params['W1']
 # ------ #
 # END YOUR CODE HERE
```

return loss, grads class FullyConnectedNet(object): A fully-connected neural network with an arbitrary number of hidden layers, ReLU nonlinearities, and a softmax loss function. This will also implement dropout and batch normalization as options. For a network with L layers, the architecture will be {affine - [batch norm] - relu - [dropout]} x (L - 1) - affine - softmax where batch normalization and dropout are optional, and the  $\{\ldots\}$  block is repeated L - 1 times. Similar to the TwoLayerNet above, learnable parameters are stored in the self.params dictionary and will be learned using the Solver class. def \_\_init\_\_(self, hidden\_dims, input\_dim=3\*32\*32, num\_classes=10, dropout=0, use\_batchnorm=False, reg=0.0, weight\_scale=1e-2, dtype=np.float32, seed=None): Initialize a new FullyConnectedNet. Inputs: - hidden\_dims: A list of integers giving the size of each hidden layer. - input\_dim: An integer giving the size of the input. - num\_classes: An integer giving the number of classes to classify. - dropout: Scalar between 0 and 1 giving dropout strength. If dropout=1 then the network should not use dropout at all. - use batchnorm: Whether or not the network should use batch normalization. - req: Scalar giving L2 regularization strength. - weight scale: Scalar giving the standard deviation for random initialization of the weights. - dtype: A numpy datatype object; all computations will be performed using this datatype. float32 is faster but less accurate, so you should use float64 for numeric gradient checking. - seed: If not None, then pass this random seed to the dropout layers. This will make the dropout layers deteriminstic so we can gradient check the model. self.use\_batchnorm = use\_batchnorm self.use\_dropout = dropout < 1</pre> self.reg = reg self.num\_layers = 1 + len(hidden\_dims) self.dtype = dtype self.params = {} # YOUR CODE HERE: Initialize all parameters of the network in the self.params dictionary. The weights and biases of layer 1 are W1 and b1; and in general the # # weights and biases of layer i are Wi and bi. The # biases are initialized to zero and the weights are initialized # so that each parameter has mean 0 and standard deviation weight\_scale. # # BATCHNORM: Initialize the gammas of each layer to 1 and the beta # parameters to zero. The gamma and beta parameters for layer 1 should be self.params['gamma1'] and self.params['beta1']. For layer 2, they # should be gamma2 and beta2, etc. Only use batchnorm if self.use\_batchnorm is true and DO NOT do batch normalize the output scores. 

layer\_dims = np.hstack((input\_dim, hidden\_dims, num\_classes))

```
for i in range(self.num layers):
     Wi = 'W' + str(i + 1)
     bi = 'b' + str(i + 1)
     self.params[Wi] = weight_scale * np.random.randn(layer_dims[i], layer_dims[i + 1])
     self.params[bi] = np.zeros(layer_dims[i + 1])
     if self.use batchnorm:
       if i == self.num layers - 1:
          break
       gamma_i = 'gamma' + str(i+1)
       beta i = 'beta' + str(i+1)
       self.params[gamma_i] = np.ones(hidden_dims[i], ) #Potentially make this a ( ,)
       self.params[beta_i] = np.zeros(hidden_dims[i], )
   # END YOUR CODE HERE
   # When using dropout we need to pass a dropout_param dictionary to each
   # dropout layer so that the layer knows the dropout probability and the mode
   # (train / test). You can pass the same dropout_param to each dropout layer.
   self.dropout_param = {}
   if self.use_dropout:
       self.dropout_param = {'mode': 'train', 'p': dropout}
   if seed is not None:
       self.dropout_param['seed'] = seed
   # With batch normalization we need to keep track of running means and
   # variances, so we need to pass a special bn_param object to each batch
   # normalization layer. You should pass self.bn_params[0] to the forward pass
   # of the first batch normalization layer, self.bn params[1] to the forward
   # pass of the second batch normalization layer, etc.
   self.bn params = []
   if self.use batchnorm:
       self.bn params = [{'mode': 'train'} for i in np.arange(self.num layers - 1)]
   # Cast all parameters to the correct datatype
   for k, v in self.params.items():
       self.params[k] = v.astype(dtype)
def loss(self, X, y=None):
   Compute loss and gradient for the fully-connected net.
   Input / output: Same as TwoLayerNet above.
   X = X.astype(self.dtype)
   mode = 'test' if y is None else 'train'
   # Set train/test mode for batchnorm params and dropout param since they
   # behave differently during training and testing.
   if self.dropout param is not None:
       self.dropout param['mode'] = mode
   if self.use batchnorm:
       for bn param in self.bn params:
           bn param[mode] = mode
   scores = None
   # YOUR CODE HERE:
     Implement the forward pass of the FC net and store the output
   #
      scores as the variable "scores".
   #
      BATCHNORM: If self.use batchnorm is true, insert a bathnorm layer
```

```
between the affine forward and relu forward layers. You may
  also write an affine batchnorm relu() function in layer utils.py.
 DROPOUT: If dropout is non-zero, insert a dropout layer after
  every ReLU layer.
cache = {}
dropout = self.dropout_param.get('p')
use_dropout = dropout is not None
hidden = np.copy(X)
#print('self.num_layers: ', self.num_layers)
for i in list(range(self.num_layers - 1)):
   Wi = 'W' + str(i + 1)
   bi = 'b' + str(i+1)
   ci = 'c' + str(i+1)
   if self.use batchnorm:
       gamma_i = 'gamma' + str(i+1)
       beta i = beta' + str(i+1)
       hidden, cache[ci] = affine batchnorm relu forward(hidden, self.params[Wi], self.params[bi],
          self.params[gamma i], self.params[beta i], self.bn params[i-1])
       hidden, cache[ci] = affine_relu_forward(hidden, self.params[Wi], self.params[bi])
   if use_dropout:
       hidden, dropout_cache = dropout_forward(hidden, self.dropout_param)
       cache[ci] = *cache[ci], dropout_cache
#print('self.params', self.params)
scores, cache['c' + str(self.num_layers)] = affine_forward(hidden, self.params['W' + str(self.num_layers)],
   self.params['b'+str(self.num layers)])
# END YOUR CODE HERE
# If test mode return early
if mode == 'test':
   return scores
loss, grads = 0.0, \{\}
# YOUR CODE HERE:
  Implement the backwards pass of the FC net and store the gradients
  in the grads dict, so that grads[k] is the gradient of self.params[k]
  Be sure your L2 regularization includes a 0.5 factor.
  BATCHNORM: Incorporate the backward pass of the batchnorm.
#
#
# DROPOUT: Incorporate the backward pass of dropout.
loss, ds = softmax loss(scores, y)
dh = np.copy(ds)
dh, dw, db = affine backward(dh, cache['c' + str(self.num layers)])
dreg = 0
grads['W'+str(self.num layers)] = dw
grads['b'+str(self.num layers)] = db
#print('dh', dh)
for i in range(self.num_layers-1, 0, -1):
   Wi = 'W' + str(i)
   bi = 'b' + str(i)
   ci = 'c' + str(i)
   #dreg += np.sum(self.params[Wi]**2)
   if use_dropout:
       dropout_cache = cache[ci][-1]
       dh = dropout_backward(dh, dropout_cache)
```

```
if not self.use batchnorm:
      _Cache = cache[ci][0], cache[ci][1]
      dh, dw, db = affine_relu_backward(dh, _Cache)
   else: #Use batch norm
      fc_cache = cache[ci][0]
      bn_cache = cache[ci][1]
      relu_cache = cache[ci][2]
      #print('dh', dh, 'relu_cache', relu_cache)
      dh = relu_backward(dh, relu_cache)
      dh, dgamma, dbeta = batchnorm_backward(dh, bn_cache)
      grads['gamma'+str(i)] = dgamma
      grads['beta'+str(i)] = dbeta
      dh, dw, db = affine_backward(dh, fc_cache)
   grads[Wi] = dw
   grads[bi] = db
   grads[Wi] += self.reg * self.params[Wi]
   dreg += np.sum(self.params[Wi]**2)
dreg *= 0.5 * self.reg
loss += dreg
# ----- #
# END YOUR CODE HERE
```

return loss, grads