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import numpy as np
import pdb
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use in the
ECE 239AS class at UCLA. This includes the descriptions of what code to
implement as well as some slight potential changes in variable names to be
consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
permission to use this code. To see the original version, please visit
cs231n.stanford.edu.
def affine_forward(x, w, b):
   Computes the forward pass for an affine (fully-connected) layer.
   The input x has shape (N, d_1, \ldots, d_k) and contains a minibatch of N
   examples, where each example x[i] has shape (d_1, \ldots, d_k). We will
   reshape each input into a vector of dimension D = d \ 1 * ... * d k, and
   then transform it to an output vector of dimension M.
   Inputs:
   - x: A numpy array containing input data, of shape (N, d 1, ..., d k)
   - w: A numpy array of weights, of shape (D, M)
   - b: A numpy array of biases, of shape (M,)
   Returns a tuple of:
   - out: output, of shape (N, M)
   - cache: (x, w, b)
   out = None
   # YOUR CODE HERE:
      Calculate the output of the forward pass. Notice the dimensions
      of w are D \times M, which is the transpose of what we did in earlier
      assignments.
   x reshape = x.reshape(x.shape[0], -1)
   out = np.dot(x_reshape, w) + b
   # END YOUR CODE HERE
   cache = (x, w, b)
   return out, cache
def affine_backward(dout, cache):
   Computes the backward pass for an affine layer.
   Inputs:
   - dout: Upstream derivative, of shape (N, M)
   - cache: Tuple of:
     - x: A numpy array containing input data, of shape (N, d_1, \ldots, d_k)
     - w: A numpy array of weights, of shape (D, M)
     - b: A numpy array of biases, of shape (M,)
   Returns a tuple of:
   - dx: Gradient with respect to x, of shape (N, d1, ..., d_k)
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- dw: Gradient with respect to w, of shape (D, M)
   - db: Gradient with respect to b, of shape (M,)
  x, w, b = cache
  dx, dw, db = None, None, None
  # YOUR CODE HERE:
     Calculate the gradients for the backward pass.
  # Notice:
     dout is N x M
     dx should be N x d1 x ... x dk; it relates to dout through multiplication with w, which is D x M
     dw should be D \times M; it relates to dout through multiplication with \times, which is N \times D after reshaping
     db should be M; it is just the sum over dout examples
  x_reshape = x_reshape(x_shape[0], -1)
  db = np.sum(dout, axis=0)
  dw = np.dot(x reshape.T, dout)
  dx = np.dot(dout, w.T).reshape(x.shape)
  # ============================ #
  # END YOUR CODE HERE
  return dx, dw, db
def relu forward(x):
  Computes the forward pass for a layer of rectified linear units (ReLUs).
  Input:
   - x: Inputs, of any shape
  Returns a tuple of:
  - out: Output, of the same shape as x
  # YOUR CODE HERE:
     Implement the ReLU forward pass.
  relu = lambda x: x * (x > 0)
  out = relu(x)
  # END YOUR CODE HERE
  cache = x
  return out, cache
def relu_backward(dout, cache):
  Computes the backward pass for a layer of rectified linear units (ReLUs).
  Input:
   - dout: Upstream derivatives, of any shape
   - cache: Input x, of same shape as dout
  Returns:
   - dx: Gradient with respect to x
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x = cache
   # YOUR CODE HERE:
      Implement the ReLU backward pass
   dx = dout * (x > 0)
   # END YOUR CODE HERE
   return dx
def batchnorm forward(x, gamma, beta, bn param):
   Forward pass for batch normalization.
   During training the sample mean and (uncorrected) sample variance are
   computed from minibatch statistics and used to normalize the incoming data.
   During training we also keep an exponentially decaying running mean of the mean
   and variance of each feature, and these averages are used to normalize data
   at test-time.
   At each timestep we update the running averages for mean and variance using
   an exponential decay based on the momentum parameter:
   running_mean = momentum * running_mean + (1 - momentum) * sample_mean
   running_var = momentum * running_var + (1 - momentum) * sample_var
   Note that the batch normalization paper suggests a different test-time
   behavior: they compute sample mean and variance for each feature using a
   large number of training images rather than using a running average. For
   this implementation we have chosen to use running averages instead since
   they do not require an additional estimation step; the torch7 implementation
   of batch normalization also uses running averages.
   Input:
   - x: Data of shape (N, D)
   - gamma: Scale parameter of shape (D,)
   - beta: Shift paremeter of shape (D,)
   - bn_param: Dictionary with the following keys:
     - mode: 'train' or 'test'; required
     - eps: Constant for numeric stability
     - momentum: Constant for running mean / variance.
     - running_mean: Array of shape (D,) giving running mean of features
     - running_var Array of shape (D,) giving running variance of features
   Returns a tuple of:
   - out: of shape (N, D)
   - cache: A tuple of values needed in the backward pass
   mode = bn param['mode']
   eps = bn_param.get('eps', 1e-5)
   momentum = bn_param.get('momentum', 0.9)
   N, D = x.shape
   running mean = bn param.get('running mean', np.zeros(D, dtype=x.dtype))
   running_var = bn_param.get('running_var', np.zeros(D, dtype=x.dtype))
   out, cache = None, None
   if mode == 'train':
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# ----- #
      # YOUR CODE HERE:
         A few steps here:
          (1) Calculate the running mean and variance of the minibatch.
          (2) Normalize the activations with the running mean and variance.
      #
          (3) Scale and shift the normalized activations. Store this
             as the variable 'out'
      #
          (4) Store any variables you may need for the backward pass in
             the 'cache' variable.
      mean_sample = np.mean(x, axis=0)
      var_sample = np.var(x, axis=0)
      running mean = momentum * running mean + (1 - momentum) * mean sample
      running_var = momentum * running_var + (1 - momentum) * var_sample
      xhat = (x - mean_sample) / np.sqrt(var_sample + eps)
      out = gamma * xhat + beta
      cache = (x, xhat, mean_sample, var_sample, gamma, beta, eps)
      # END YOUR CODE HERE
      elif mode == 'test':
      # YOUR CODE HERE:
      # Calculate the testing time normalized activation. Normalize using
        the running mean and variance, and then scale and shift appropriately.
      # Store the output as 'out'.
      outhat = (x - running_mean) / np.sqrt(running_var + eps)
      out = outhat * gamma + beta
      # ----- #
      # END YOUR CODE HERE
      else:
      raise ValueError('Invalid forward batchnorm mode "%s"' % mode)
   # Store the updated running means back into bn param
   bn param['running mean'] = running mean
   bn_param['running_var'] = running var
   return out, cache
def batchnorm_backward(dout, cache):
   Backward pass for batch normalization.
   For this implementation, you should write out a computation graph for
   batch normalization on paper and propagate gradients backward through
   intermediate nodes.
   Inputs:
   - dout: Upstream derivatives, of shape (N, D)
   - cache: Variable of intermediates from batchnorm forward.
   Returns a tuple of:
   - dx: Gradient with respect to inputs x, of shape (N, D)
   - dgamma: Gradient with respect to scale parameter gamma, of shape (D,)
   - dbeta: Gradient with respect to shift parameter beta, of shape (D,)
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dx, dgamma, dbeta = None, None, None
   # YOUR CODE HERE:
     Implement the batchnorm backward pass, calculating dx, dgamma, and dbeta.
   N, D = dout.shape
   x, xhat, sample_mean, var_sample, gamma, _, eps = cache
   dgamma = np.sum(dout * xhat, axis=0)
   dbeta = np.sum(dout, axis=0)
   dxhat = gamma * dout
   var sample eps = 1/np.sqrt(var sample + eps)
   dx = var_sample_eps * (1/N) * gamma * (dout * N - dbeta - (xhat * dgamma))
   # END YOUR CODE HERE
   return dx, dgamma, dbeta
def dropout_forward(x, dropout_param):
   Performs the forward pass for (inverted) dropout.
   Inputs:
   - x: Input data, of any shape
   - dropout_param: A dictionary with the following keys:
    - p: Dropout parameter. We keep each neuron output with probability p.
    - mode: 'test' or 'train'. If the mode is train, then perform dropout;
      if the mode is test, then just return the input.
    - seed: Seed for the random number generator. Passing seed makes this
      function deterministic, which is needed for gradient checking but not in
      real networks.
   Outputs:
   - out: Array of the same shape as x.
   - cache: A tuple (dropout_param, mask). In training mode, mask is the dropout
    mask that was used to multiply the input; in test mode, mask is None.
   p, mode = dropout_param['p'], dropout_param['mode']
   if 'seed' in dropout param:
      np.random.seed(dropout_param['seed'])
   mask = None
   out = None
   if mode == 'train':
      # ----- #
      # YOUR CODE HERE:
         Implement the inverted dropout forward pass during training time.
         Store the masked and scaled activations in out, and store the
         dropout mask as the variable mask.
      # ------ #
      mask = np.random.uniform(low=0, high=1, size = x.shape) > p
      out = x * mask
      # END YOUR CODE HERE
      # ============================ #
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elif mode == 'test':
    # ------ #
    # YOUR CODE HERE:
      Implement the inverted dropout forward pass during test time.
    out = x
    # END YOUR CODE HERE
    cache = (dropout param, mask)
  out = out.astype(x.dtype, copy=False)
  return out, cache
def dropout backward(dout, cache):
  Perform the backward pass for (inverted) dropout.
  Inputs:
  - dout: Upstream derivatives, of any shape
  - cache: (dropout_param, mask) from dropout_forward.
  dropout_param, mask = cache
  mode = dropout param['mode']
  dx = None
  if mode == 'train':
    # YOUR CODE HERE:
      Implement the inverted dropout backward pass during training time.
    dx = dout * mask
    # END YOUR CODE HERE
    # ------ #
  elif mode == 'test':
    # YOUR CODE HERE:
      Implement the inverted dropout backward pass during test time.
    dx = dout
    # ----- #
    # END YOUR CODE HERE
    return dx
def svm_loss(x, y):
  Computes the loss and gradient using for multiclass SVM classification.
  Inputs:
  - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
   for the ith input.
  - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
   \theta \leftarrow y[i] \leftarrow C
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Returns a tuple of:
    - loss: Scalar giving the loss
    - dx: Gradient of the loss with respect to x
   N = x.shape[0]
    correct_class_scores = x[np.arange(N), y]
    margins = np.maximum(0, x - correct_class_scores[:, np.newaxis] + 1.0)
   margins[np.arange(N), y] = 0
    loss = np.sum(margins) / N
    num_pos = np.sum(margins > 0, axis=1)
    dx = np.zeros_like(x)
    dx[margins > 0] = 1
    dx[np.arange(N), y] -= num pos
    dx /= N
    return loss, dx
def softmax_loss(x, y):
    Computes the loss and gradient for softmax classification.
    Inputs:
    - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
     for the ith input.
    - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
     0 <= y[i] < C
    Returns a tuple of:
    - loss: Scalar giving the loss
    - dx: Gradient of the loss with respect to x
    probs = np.exp(x - np.max(x, axis=1, keepdims=True))
    probs /= np.sum(probs, axis=1, keepdims=True)
    N = x.shape[0]
    loss = -np.sum(np.log(probs[np.arange(N), y])) / N
    dx = probs.copy()
    dx[np.arange(N), y] -= 1
    dx /= N
    return loss, dx
def affine batchnorm relu forward(x, w, b, gamma, beta, bn param):
 Convenience layer that performs an affine transform, batch normalization,
 and ReLU.
 Inputs:
  - x: Array of shape (N, D1); input to the affine layer
  - w, b: Arrays of shape (D2, D2) and (D2,) giving the weight and bias for
    the affine transform.
  - gamma, beta: Arrays of shape (D2,) and (D2,) giving scale and shift
   parameters for batch normalization.
  - bn_param: Dictionary of parameters for batch normalization.
  Returns:
  - out: Output from ReLU, of shape (N, D2)
  - cache: Object to give to the backward pass.
 a, fc cache = affine forward(x, w, b)
 a_bn, bn_cache = batchnorm_forward(a, gamma, beta, bn_param)
 out, relu cache = relu forward(a bn)
 cache = (fc_cache, bn_cache, relu_cache)
 return out, cache
def affine batchnorm relu backward(dout, cache):
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Backward pass for the affine-batchnorm-relu convenience layer.

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fc_cache, bn_cache, relu_cache = cache
da_bn = relu_backward(dout, relu_cache)
da, dgamma, dbeta = batchnorm_backward(da_bn, bn_cache)
dx, dw, db = affine_backward(da, fc_cache)
return dx, dw, db, dgamma, dbeta
```