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Programming Assignment 2 Report  
CSCI338

**The approach that you took to implementing this algorithm, i.e., were you able to implement the algorithm exactly as described in the book, did you need to make any modifications to it, etc?**

I believe I implemented the algorithm as described in the book. I had to implement a few changes in order to make it work, such as creating helper methods and a Point class.

Methods/classes I created:

`class Point()`: An object that holds x and y coordinates

`sortByX(p)`: This is a helper method to sort a list of points by x coordinate. It's used as a key for the `sorted(points, key=sortByX)` call.

`stripClosest(strip, size, d)`: This method deals with determining the closest pairs middle strip of points. Parameters: Strip: A y coordinate sorted list of points in the middle strip. Size: the size of Strip. d: minimum distance to 'beat'

`closestPairs(Px, Py, n)`: This is the bulk of the solution. It is the recursive part. Parameters: Px: Points sorted by x coordinate. Py: Points sorted by y coordinate. n: the size of Px

`distance(p1, p2)`: This method determines the distance between two points. Parameters: p1: a point. p2: a point.

`bruteForce(p, n)`: The brute force method. This method is used when the list of points is less than 3. Parameters: p: A list of points. n: the size of p.

**A description of anything that I should know about your program. This could be limitations like, it only works for XXX files, but not YYY file, or challenges that prevented you from completing the assignment.**

There were no issues getting my problem to work for a specific type of files. The only error I noticed was with rounding/truncating the results at the end. Because the points were so close together, rounding to 4 decimal places yielded a distance result of 0.0 for some of the larger .pts files. (I noticed this with 65536.pts) When you do not round (to change this to not round, modify line 196 from

```
print("Closest Distance: "+str(closestDistanceRounded)) to  
print("Closest Distance: "+str(closestDistance)) the result is correct.
```

I believe this issue is a limitation of Python Floats, as when the rounded value is not used, the result is outputted in scientific notation. (for 65536.pts, it yields a result of 4.368065933567342e-05)

This is also an issue when reporting the points if they are very small floating point numbers: for example, in 65536.pts, Point1X is reported back as 2.8e-05 and Point2X is reported as 3.9e-05 due to being such a small floating point number.

An analysis comparing and contrasting the theoretical analysis of EfficientClosestPair (from the book), with your experimental analysis. Does your experimental analysis support the theoretical analysis from the book? Why or why not? You should include plots to support your conclusions.

I believe that my implementation followed the  $n\log N$  theoretical analysis from the book.

We followed the book's algorithm, and the time efficiency did not exponentially increase. D

| numOfPoints | averageTimeInSeconds | nLognForSpecificPoints | logN       | n2         |
|-------------|----------------------|------------------------|------------|------------|
| 8           | 0.0000918865         | 7.224719896            | 0.90308999 | 64         |
| 128         | 0.00118103           | 269.7228761            | 2.10720997 | 16384      |
| 256         | 0.002634144          | 616.5094311            | 2.40823997 | 65536      |
| 512         | 0.00842123           | 1387.14622             | 2.70926996 | 262144     |
| 1024        | 0.014666796          | 3082.547156            | 3.01029996 | 1048576    |
| 2048        | 0.035039759          | 6781.603742            | 3.31132995 | 4194304    |
| 4096        | 0.052797461          | 14796.22635            | 3.61235995 | 16777216   |
| 8192        | 0.087168503          | 32058.49042            | 3.91338994 | 67108864   |
| 65536       | 0.864873886          | 315652.8287            | 4.81647993 | 4294967296 |



