



Department of Computer Science and Engineering

Data Structures and Object-Oriented Design

(CSE – 2050)

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CSE-2050 – Data Structures and Object-Oriented Design

Recap

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Announcements

- Updates in syllabus
 - Office hours
 - Schedule
 - Assignment due date extended
 - Exam 1 date announced

Weeks	Modules	Assignments Schedule
8/29 – 9/2	Mod 1 – Basic Python	
9/5 – 9/9	Mod 2 – Object-oriented Programming & testing	
9/12 – 9/16	Mod 3 – Running Time Analysis	Assignment 1 release
9/19 – 9/23	Mod 4 – Linear Data Structures	
9/27	Assignment 1 Due	
9/29	Exam 1	

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Week 4 – 09/19 – 09/23 – Lecture 1



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Recap

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Quick Recap

- Learnt the identity to evaluate the sum of all K integers
- Asymptotic Analysis
 - Allow us to measure performance in terms of input size
- Big-O notation
 - Allow us to ignore lower order terms and constants

```

12 def sum_clever(k):
13     total = k*(k+1)//2
14     return total
15
16 print(sum_clever(3))
17 print(sum_clever(6))
18 print(sum_clever(7))
19 print(sum_clever(100))

```

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Running Time Analysis

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Activity # 6 (1/2)

Calculate the time complexity (Big-O) for the following codes

```

1 #Practice question 1
2 def func(L):
3     x = 0
4     for i in L:
5         for j in L:
6             x += i * j
7     return x

```

Handwritten analysis: $1 + n(n \times 3) + 1 = 3n^2 + 2 \Rightarrow O(n^2)$

```

1 # Practice question 2
2 a = 0
3 b = 0
4 for i in range(N):
5     a = a + random()
6     x += 1
7 for i in range(M):
8     b = b + random()

```

Handwritten analysis: $3N \checkmark$, $3M \checkmark$, $N+M \Rightarrow O(N+M)$

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Activity # 6 (2/2)

5

Calculate the time complexity (Big-O) for the following codes

```

1 #Practice question 3
2 a = 0;
3 for i in range(N):
4     for j in reversed(range(i,N)):
5         a = a + i + j;

```

Handwritten analysis for Practice question 3:

For $i = 0$, j ranges from $N-1$ down to 0 .
 For $i = 1$, j ranges from $N-2$ down to 0 .
 ...
 For $i = N-1$, j ranges from 0 down to 0 .
 The total number of iterations is the sum of the first N natural numbers: $1 + 2 + 3 + \dots + N = \frac{N(N+1)}{2}$.
 Therefore, the time complexity is $O(N^2)$.

```

1 # Practice question 4
2 i = 1
3 while i <= n:
4     print(i)
5     i *= 2

```

Handwritten analysis for Practice question 4:

The loop variable i starts at 1 and doubles in each iteration: $1, 2, 4, 8, \dots$.
 The number of iterations is the number of times i can be doubled before exceeding n , which is $\log_2 n$.
 Therefore, the time complexity is $O(\log n)$.

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Types of functions

6

- | | | |
|-------------------------|---|----------------------------------|
| • Constant Functions | → | $O(1)$ |
| • Logarithmic Functions | → | $O(\log n)$ |
| • Linear Functions | → | $O(n)$ |
| • $n \log n$ | → | $O(n \log n)$ |
| • Quadratic Functions | → | $O(n^2)$ |
| • Polynomial Functions | → | $O(n^k)$ for some constant k . |
| • Exponential Functions | → | $O(2^n)$ |
| • Factorial Functions | → | $O(n!)$ |

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Module 4

Linear Data Structures

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Abstract Data Types (ADT)

What is Data Structure?

It is a technique to *structure* data so that it can be utilized efficiently using:

- Some protocols or rules
- Implementation via programming
- ADT → *abstraction* of a data structure that provides only the *interface* to which the data must adhere
- Interface does not give any details about the implementation or programming language
 - What data we are dealing with
 - What operations can be performed on that data



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Linear Data Structures


Abstract Data Types (ADT)

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In ADT,

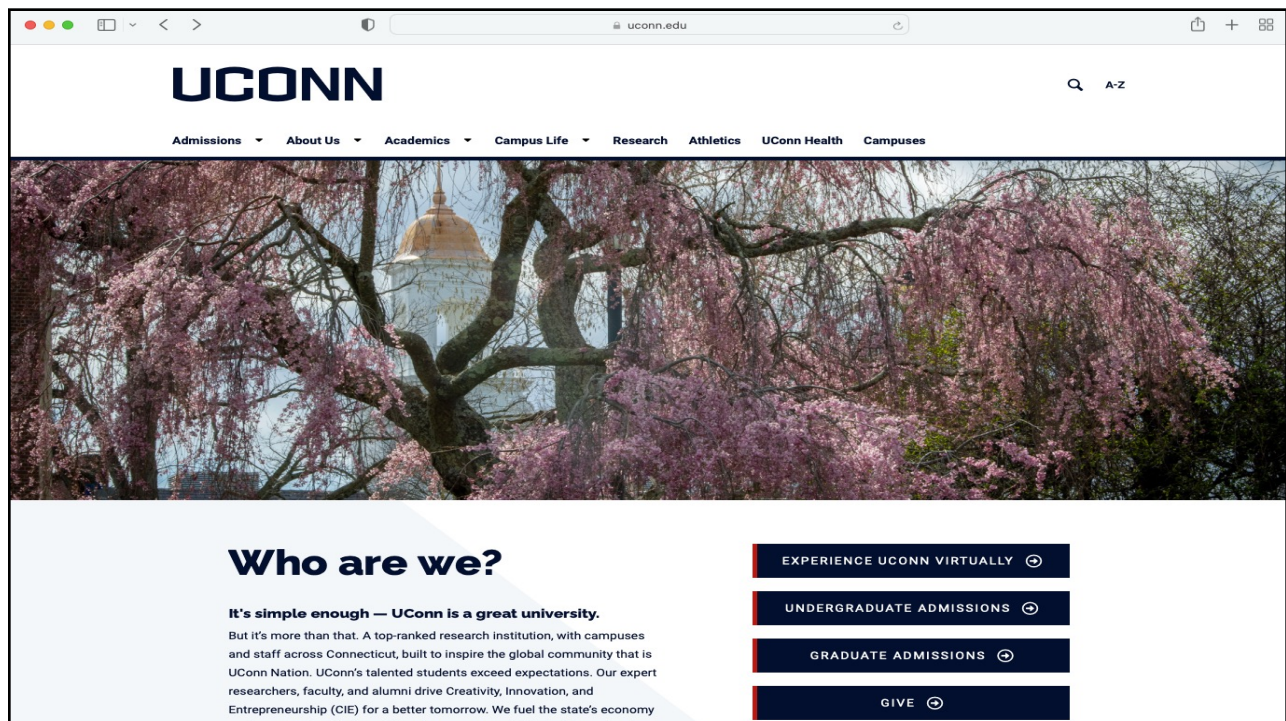
1. What input it takes
2. What methods (or operations) it supports on the data
3. What is the expected output

- Sometimes, ADT also describe error situations and what happens if an error occurs.
 - The implementation of ADT is called “Data Structure” or “Concrete Data Structure”.
- Concept of Encapsulation will be used to implement data structure

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The screenshot shows the UConn website homepage. At the top is the UConn logo and a navigation menu with links: Admissions, About Us, Academics, Campus Life, Research, Athletics, UConn Health, and Campuses. Below the menu is a large banner image of a building with a dome, partially obscured by pink cherry blossoms. Under the banner, the heading "Who are we?" is followed by the text: "It's simple enough — UConn is a great university. But it's more than that. A top-ranked research institution, with campuses and staff across Connecticut, built to inspire the global community that is UConn Nation. UConn's talented students exceed expectations. Our expert researchers, faculty, and alumni drive Creativity, Innovation, and Entrepreneurship (CIE) for a better tomorrow. We fuel the state's economy". To the right of this text are four dark blue buttons with white text and right-pointing arrows: "EXPERIENCE UCONN VIRTUALLY", "UNDERGRADUATE ADMISSIONS", "GRADUATE ADMISSIONS", and "GIVE".

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Linear Data Structures


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Last-In-First-Out (LIFO)



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Linear Data Structures

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Stack ADT

A **stack** is a collection of objects that are inserted and removed according to the **last-in, first-out (LIFO)** principle.

- A user may insert objects into a stack at any time
- Only access or remove the most recently inserted object that remains (at the so-called “top” of the stack)

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Linear Data Structures

Stack ADT

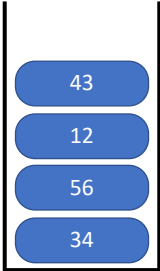
Operations

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PUSH


Add the element at the top of the stack

```
stack.push(34)
stack.push(56)
stack.push(12)
stack.push(43)
```



stack

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Linear Data Structures

Stack ADT

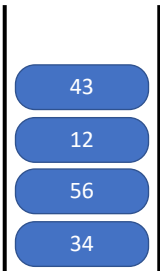
Operations

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POP


Returns and removes the element from the top of the stack

```
stack.pop( )
stack.pop( )
```



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Linear Data Structures

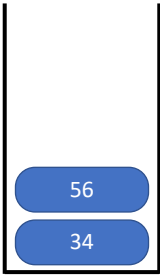
Stack ADT

Operations
PEEK/TOP


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Returns the element from the top of the stack without removing it

stack.peek()



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Linear Data Structures

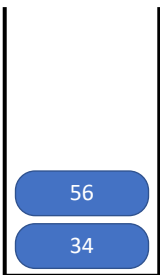
Stack ADT

Operations
is_empty

16


Returns True if stack does not contain any element

stack.is_empty()



stack

FALSE

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Linear Data Structures

Stack ADT

Operations

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Stack ADT

Operations

len

Returns the number of elements in the stack

stack.len ()


56

34

2

stack

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Linear Data Structures

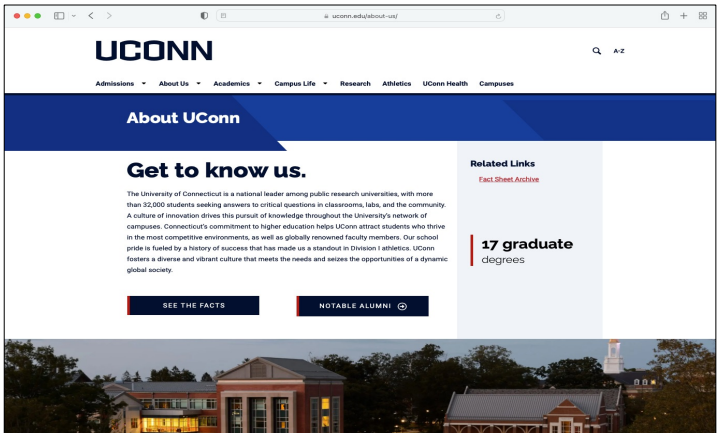
Stack ADT

Operations

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Stack ADT

Operations



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Stack ADT Implementation

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Stack ADT can be implemented easily with a list

- What OOP strategies are used?
 - Class, encapsulation, composition
- Bottom of stack → first element in the list
- Top of stack → last element in the list

All operations can be performed in constant time

```

Stack.py
1 class ListStack:
2     def __init__(self):
3         self._L = []
4
5     def push(self, item):
6         self._L.append(item)
7
8     def pop(self):
9         return self._L.pop()
10
11    def peek(self):
12        return self._L[-1]
13
14    def __len__(self):
15        return len(self._L)
16
17    def isempty(self):
18        return len(self) == 0
  
```

$O(1)$ $O(1)$ $O(1)$ $O(1)$ $O(1)$

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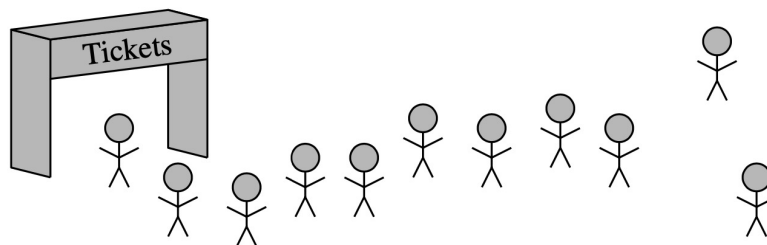
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Queue ADT

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A **queue** is a collection of objects that are inserted and removed according to the **first-in, first-out (FIFO)** principle.

- Elements can be inserted at the **back** in the queue
- Element, in **front**, that has been in the queue for longest can be removed




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Queue ADT	Operations	22
Q.enqueue(e)	Add element e to the back of queue Q.	Week 4 – 09/19 – 09/23 – Lecture 1 
Q.dequeue()	Remove and return the first element from queue Q; an error occurs if the queue is empty.	
Q.first() or Q.peek()	Return a reference to the element at the front of queue Q, without removing it; an error occurs if the queue is empty.	
Q.is empty():	Return True if queue Q does not contain any elements.	
len(Q)	Return the number of elements in queue Q. In Python, we implement this with the special method <code>__len__</code> .	
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Queue ADT	Operations	23																																													
	<table border="1"> <thead> <tr> <th>Operation</th> <th>Return Value</th> <th>first \leftarrow Q \leftarrow last</th> </tr> </thead> <tbody> <tr><td>Q.enqueue(5)</td><td>–</td><td>[5]</td></tr> <tr><td>Q.enqueue(3)</td><td>–</td><td>[5, 3]</td></tr> <tr><td>len(Q)</td><td>2</td><td>[5, 3]</td></tr> <tr><td>Q.dequeue()</td><td>5</td><td>[3]</td></tr> <tr><td>Q.is empty()</td><td>False</td><td>[3]</td></tr> <tr><td>Q.dequeue()</td><td>3</td><td>[]</td></tr> <tr><td>Q.is empty()</td><td>True</td><td>[]</td></tr> <tr><td>Q.dequeue()</td><td>“error”</td><td>[]</td></tr> <tr><td>Q.enqueue(7)</td><td>–</td><td>[7]</td></tr> <tr><td>Q.enqueue(9)</td><td>–</td><td>[7, 9]</td></tr> <tr><td>Q.first()</td><td>7</td><td>[7, 9]</td></tr> <tr><td>Q.enqueue(4)</td><td>–</td><td>[7, 9, 4]</td></tr> <tr><td>len(Q)</td><td>3</td><td>[7, 9, 4]</td></tr> <tr><td>Q.dequeue()</td><td>7</td><td>[9, 4]</td></tr> </tbody> </table>	Operation	Return Value	first \leftarrow Q \leftarrow last	Q.enqueue(5)	–	[5]	Q.enqueue(3)	–	[5, 3]	len(Q)	2	[5, 3]	Q.dequeue()	5	[3]	Q.is empty()	False	[3]	Q.dequeue()	3	[]	Q.is empty()	True	[]	Q.dequeue()	“error”	[]	Q.enqueue(7)	–	[7]	Q.enqueue(9)	–	[7, 9]	Q.first()	7	[7, 9]	Q.enqueue(4)	–	[7, 9, 4]	len(Q)	3	[7, 9, 4]	Q.dequeue()	7	[9, 4]	Week 4 – 09/19 – 09/23 – Lecture 1 
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Q.enqueue(3)	–	[5, 3]																																													
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Q.enqueue(4)	–	[7, 9, 4]																																													
len(Q)	3	[7, 9, 4]																																													
Q.dequeue()	7	[9, 4]																																													
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Queue ADT Implementation

Can easily use list to implement

→ inefficient

- Pop(0) → shift elements towards left to fill the gap
- Causes worst case behavior $O(n)$

```

1 class ListQueueSimple:
2     def __init__(self):
3         self._L = []
4
5     def enqueue(self, item):
6         self._L.append(item)
7
8     def dequeue(self):
9         return self._L.pop(0)
10
11    def peek(self):
12        return self._L[0]
13
14    def __len__(self):
15        return len(self._L)
16
17    def isempty(self):
18        return len(self._L) == 0

```

$O(1)$
 $O(n)$
 $O(1)$
 $O(1)$
 $O(1)$

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Queue ADT Implementation

Alternate approach – avoid the call to pop(0) entirely

- Use variable head to store the index of element in front of queue
- Dequeue element using head without removing it.
- → dequeue operation will run in $O(1)$ time
- There is a **drawback** of this approach!
 - Size of list → $O(m)$
 - m is the total number of enqueue operations

```

1 class ListQueueHead:
2     def __init__(self):
3         self._L = []
4         self._head = 0
5
6     def enqueue(self, item):
7         self._L.append(item)
8
9     def dequeue(self):
10        front_item = self.peek()
11        self._head += 1
12        return front_item
13
14    def peek(self):
15        return self._L[self._head]
16
17    def __len__(self):
18        return len(self._L)
19
20    def isempty(self):
21        return len(self._L) == 0

```

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Recap

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Quick Recap

- Abstract Data Types (ADT)
- Stacks – LIFO
 - Operations: PUSH, POP, PEEK, IS_EMPTY, LEN
 - Cost: $O(1)$
- Queues – FIFO
 - Operations: ENQUEUE, DEQUEUE, FIRST, IS_EMPTY, LEN
 - Cost: Dequeue $\rightarrow O(n)$
- To overcome this, we made use of head variable to dequeue the element in front of queue
 - Space issue

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Error Handling

- Displaying an error message is the correct behavior.
- Example: Executing a pop operation on an empty stack.

```
def pop(self):
    try:
        return self._L.pop()
    except:
        raise Exception("Trying to pop from empty stack.")
```

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Deque ADT

- Deque (pronounced as “deck”) is a **Doubly-Ended-QUEue** .
- Acts like a Stack and Queue
 - Add or remove elements from both the beginning and the end
- **addfirst(item)** - add item to the front of the deque.
- **addlast(item)** - add item to the end of the deque.
- **removefirst(item)** - remove and return the first item in the deque.
- **removelast(item)** - remove and return the last item in the deque.
- **len** - return the number of items in the deque.

```
class ListDeque:
    def __init__(self):
        self._L = []
    def addfirst(self, item):
        self._L.insert(0, item)
    def addlast(self, item):
        self._L.append(item)
    def removefirst(self):
        return self._L.pop(0)
    def removelast(self):
        return self._L.pop()
    def __len__(self):
        return len(self._L)
```

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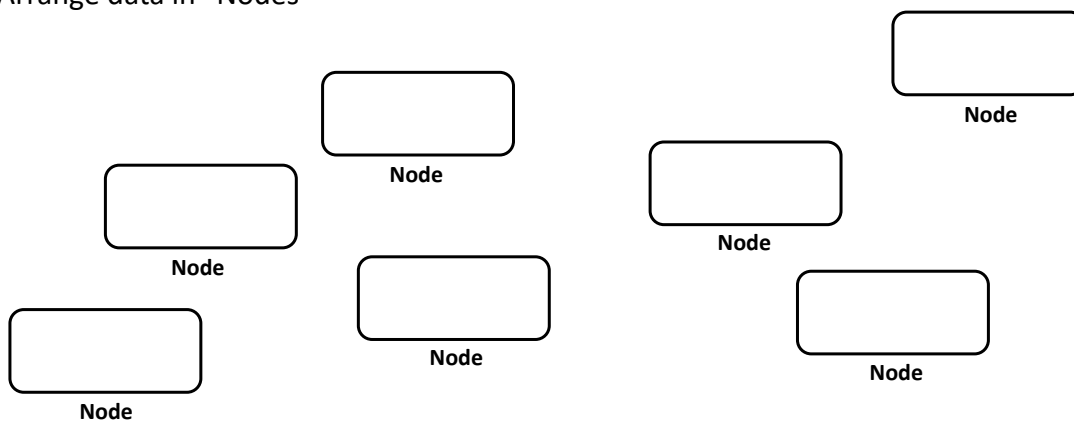
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Same problem of shifting elements towards right or left!
Only because of
The arrangement of items in a memory sequentially.

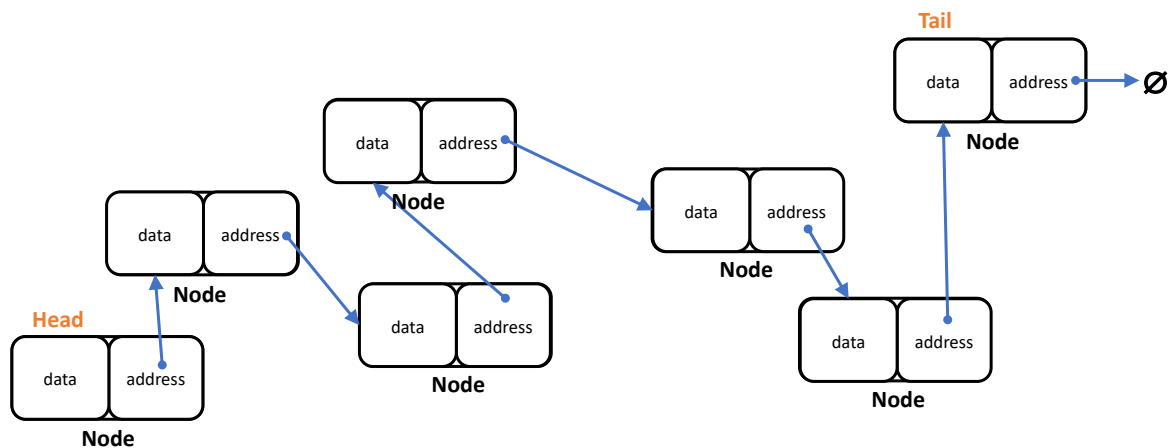
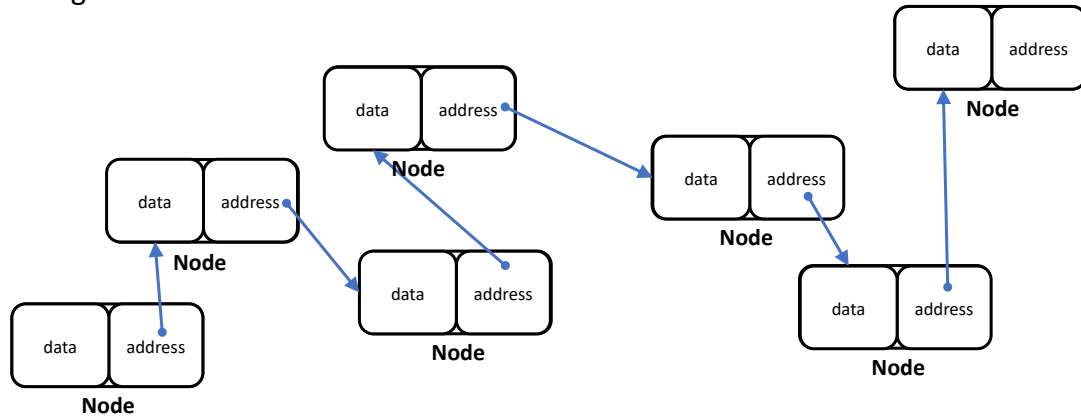


Drop the idea of storing elements sequentially in a memory.

Arrange data in “Nodes”

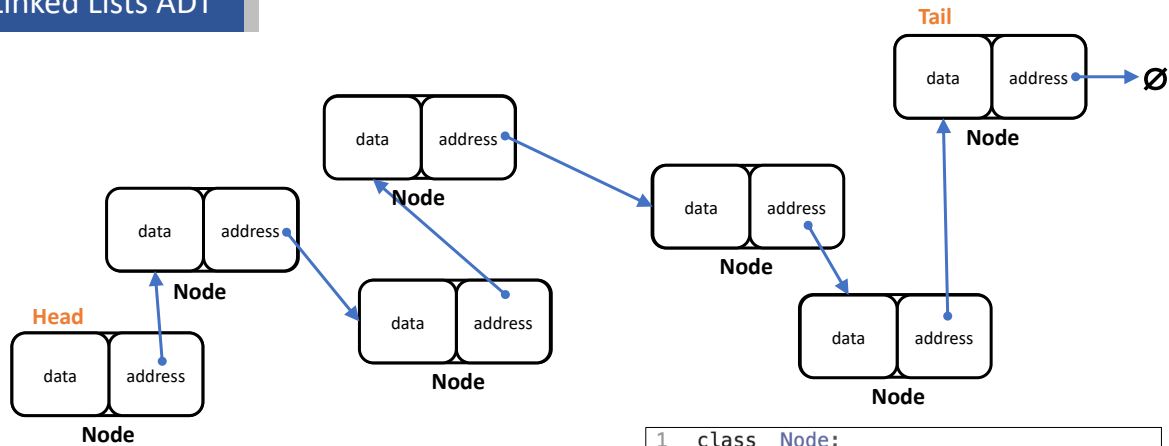


Arrange data in “Nodes”



Linked Lists ADT

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- Data is arranged in distributed nodes
- Each node contains the element (data) + the address of next node

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```

1 class _Node:
2     """ Node class to create
3         individual linked list nodes """
4     def __init__(self, element, next):
5         self._element = element
6         self._next = next

```

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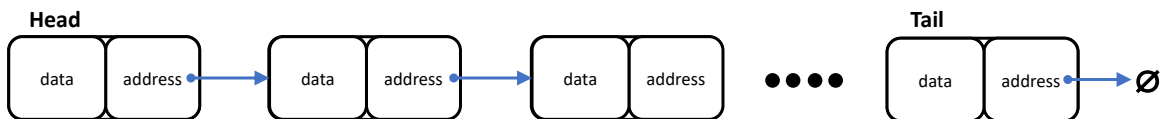


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Linked Lists ADT **Singly Linked List**

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- Most simplest form of linked list
- First node is the head node. Last node is the tail node.



- Tail node can be determined by :
 - checking its pointer to next node \rightarrow None
 - Traversing the list
- Since the next reference of a node can be viewed as a *link* or a *pointer* \rightarrow traversal is also referred to as “link hopping” or “pointer hopping”

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Linked Lists ADT

Singly Linked List

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- Minimally, instance of a linked list must keep a reference of **head** node
- Also keep the reference of a **tail** node.
→ Traversal can help us get to the tail node → $O(n)$
- Size of the linked list can also be continuously monitored
→ Traversal can help us count the nodes → $O(n)$

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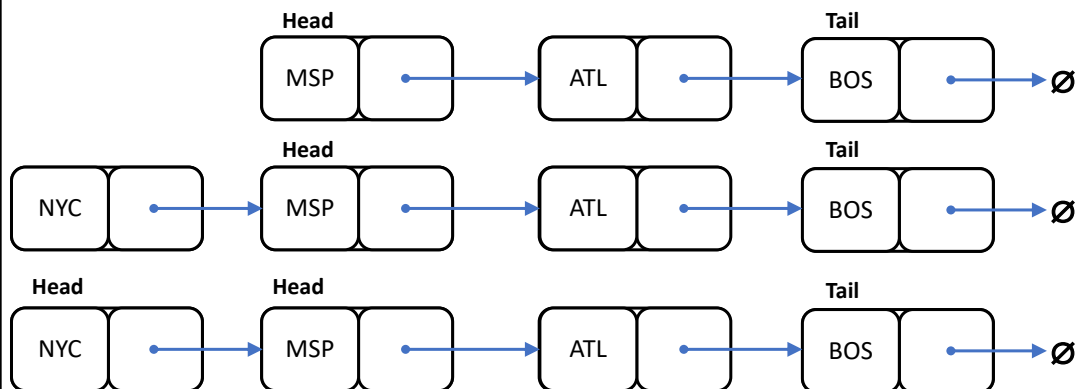
Linked Lists ADT

Singly Linked List

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Inserting element at:

The HEAD of linked list



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Inserting element at:

The HEAD of linked list

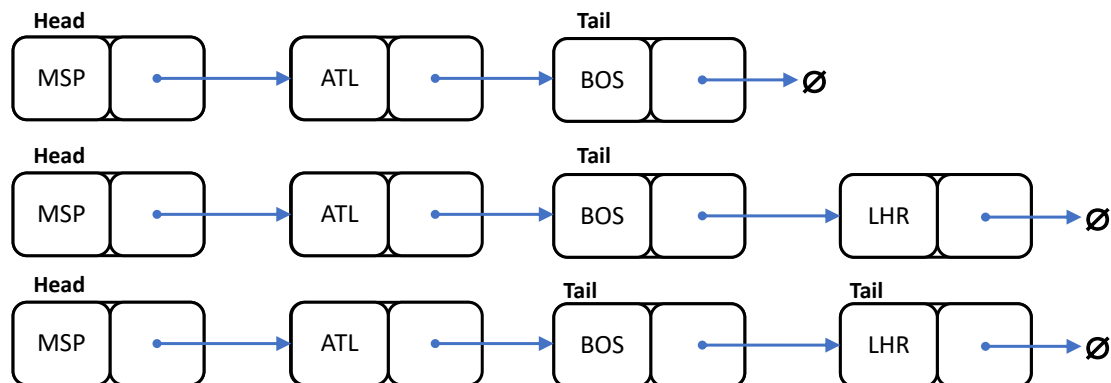
Pseudocode:

1. Create a node with an element
`newest = _Node(element)`
2. Set the newest node next reference to the current head node:
`newest._next = L.head`
3. Set the variable "head" to refer the newest node as the head node
`L.head = newest`
4. Update the size of the list
`L.size += 1`



Inserting element at:

The TAIL of linked list



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Linked Lists ADT	Singly Linked List	40
<div style="background-color: #003366; color: white; padding: 5px; text-align: center; margin-bottom: 10px;">Inserting element at:</div> <p>The TAIL of linked list</p> <p>Pseudocode:</p> <ol style="list-style-type: none"> 1. Create a node with an element <code>newest = Node(element)</code> 2. Set the newest node next reference to None <code>newest.next = None</code> 3. Set the next node reference of current tail to point to the newest node <code>L.tail.next = newest</code> 4. Set the variable "tail" to reference to newest node <code>L.Tail = newest</code> 4. Update the size of the list <code>L.size += 1</code> 		

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Linked Lists ADT	Singly Linked List	41
<div style="background-color: #003366; color: white; padding: 5px; text-align: center; margin-bottom: 10px;">Deleting element from:</div> <p>The HEAD of linked list</p>		

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Linear Data Structures

Linked Lists ADT

Singly Linked List

Deleting element from:

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The TAIL of linked list

```

graph LR
    Head[Head] --> NYC[NYC]
    NYC --> MSP[MSP]
    MSP --> ATL[ATL]
    ATL --> Tail[Tail]
    Tail --> EmptySet[∅]
  
```

- We cannot easily delete the last node of a singly linked list
 - Though, we can hold a reference to the Tail node
 - There is no way to determine the node preceding to the Tail node
- List traversal may help, but takes $O(n)$ time

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Linear Data Structures

Activity # 7

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Write a pseudocode (steps) for implementing the Stack ADT using Linked List.

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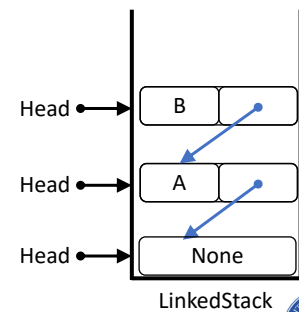
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Write a pseudocode (steps) for implementing the Stack ADT using Linked List.

1. Start off with an instance of `ListStack` with:
 `head = None`
2. PUSH operation → Create an instance of the private
 Node class with:
 `head = _Node("A", head)`
2. PUSH operation → Create an instance of the private
 Node class with:
 `head = _Node("B", head)`

For each PUSH operation, increase the size to keep track of the stack size

```
1 class _Node:
2     """ Node class to create
3     individual linked list nodes """
4     def __init__(self, element, next):
5         self._element = element
6         self._next = next
```



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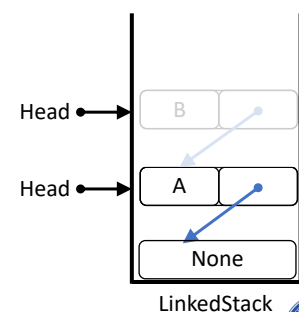


Write a pseudocode (steps) for implementing the Stack ADT using Linked List.

To POP the element from stack

1. Get the element of "head" node
 `read_element = head`
2. Set the next head node to the "next" pointer of the
 current head node
 `head = head._next`
2. Reduce the size of the stack and return the
 `read_element`
 `size -= 1`
 `return read_element`

```
1 class _Node:
2     """ Node class to create
3     individual linked list nodes """
4     def __init__(self, element, next):
5         self._element = element
6         self._next = next
```



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Linear Data Structures


Linked Lists ADT
Queue ADT as Linked List
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LinkedQueue

1. Start off by creating an instance of `LinkedQueue` with:

```
head = None
tail = None
```

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Linked Lists ADT
Queue ADT as Linked List
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LinkedQueue

A

→

∅

Head
 ↗


↘
 Tail

Enqueue → Create an instance of a private class `Node` with:

```
newest = _Node("A", None)
if it is the first element then
    head = newest
```

- Set the element as a Tail
tail = newest
- Increase the size of queue

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LinkedQueue

Head Tail Tail

Enqueue → Create an instance of a private class Node with:
 newest = _Node("B", None)
 if it is the first element then
 head = newest
 else
 tail._next = newest

- Set the element as a Tail
tail = newest
- Increase the size of queue

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LinkedQueue

Head Head Tail

Dequeue → Read the element
 read_element = head._element

- Update the head variable to be set to the next node
head = head._next
if it was the last element in queue
tail = None
- Reduce the size of queue
- Return read_element

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