



Department of Computer Science and Engineering

# Data Structures and Object-Oriented Design

(CSE – 2050)

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## CSE-2050 – Data Structures and Object-Oriented Design

Background

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### Background

- Variety of data structures
  - Stacks (LIFO)
    - All operations:  $O(1)$
  - Queues (FIFO)
    - Dequeue:  $O(n)$
  - Linked Lists
    - Removing tail element:  $O(n)$
  - Doubly-linked Lists
    - All operations:  $O(1)$
  - Hash Tables
    - Locating bucket ( $O(1)$ ), locating elements in bucket ( $O(n)$ )

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All the data structures we have studied so far are LINEAR

Breakthroughs come by thinking  
**nonlinearly!**



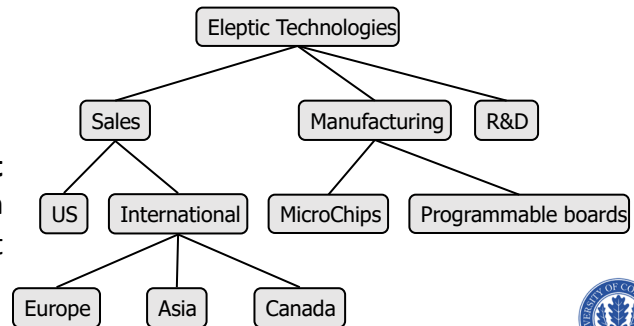
# Module 9

## Trees



## Trees

- In CS, Tree is an abstract data type that stores elements hierarchically.
- Non-linear data structure, relationship between objects/data are:
  - NOT defined as “before and after” relationship
  - Defined in hierarchical fashion - “above and below” relationship
- Examples:
  - Organizational Charts
  - File systems, etc
- Each element in a tree has a **parent** element and zero/more **children** elements, except the first/top element which is called **root**



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## Quick Recap of Recursion

Example: Adding K integers.

```

1 def sum(k):
2     if k > 0:
3         return sum(k - 1) + k
4     return 0
5 print(sum(5))

```

```

1 def sum(k):           k=0
2     if k > 0:
3         return sum(k - 1) + k
4     return 0
1 def sum(k):           k=1
2     if k > 0:
3         return sum(k - 1) + k
4     return 0
1 def sum(k):           k=2
2     if k > 0:
3         return sum(k - 1) + k
4     return 0
1 def sum(k):           k=3
2     if k > 0:
3         return sum(k - 1) + k
4     return 0
1 def sum(k):           k=4
2     if k > 0:
3         return sum(k - 1) + k
4     return 0
1 def sum(k):           k=5
2     if k > 0:
3         return sum(k - 1) + k
4     return 0

```

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## Quick Recap of Recursion

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```

1 def sum(k):
2     if k > 0:
3         return sum(k - 1) + k
4     return 0
5 print( 15 )

```

```

1 def sum(k):           k=0
2     if k > 0:
3         return sum(k - 1) + k
4     return 0
1 def sum(k):           k=1
2     if k > 0:
3         return sum(k - 1) + k
4     return 0
1 def sum(k):           k=2
2     if k > 0:
3         return sum(k - 1) + k
4     return 0
1 def sum(k):           k=3
2     if k > 0:
3         return sum(k - 1) + k
4     return 0
1 def sum(k):           k=4
2     if k > 0:
3         return sum(k - 1) + k
4     return 0
1 def sum(k):           k=5
2     if k > 0:
3         return sum(k - 1) + k
4     return 0

```

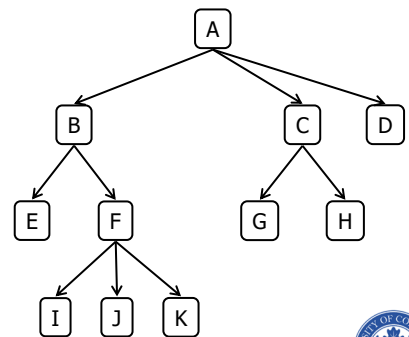
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## Trees Terminologies

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- **Root:** Highest-most node without parent (A)
- **Edge:** Connection between two nodes to show a relationship between them
- **Path:** A path is an ordered list of nodes that are connected by edges (from top to bottom)
- **Parent:** A node is a parent of all nodes it connects to with outgoing edges
- **Children:** The set of nodes which have incoming edges from a parent node
- **Sibling:** Nodes that are children of the same parent



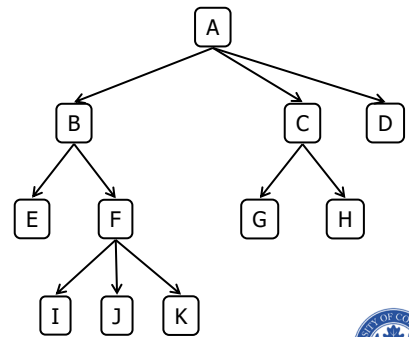
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## Trees Terminologies

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- **Descendant** of node (x): all nodes for which there is path from x. (child, grandchild, grand-grandchild)
- **Ancestors** of node (x): all nodes which x is a descendant of (parent, grandparent, grand-grandparent)
- **Leaf Node**: Nodes which have no children (J, K, etc)
- **Subtree**: Set of nodes and edges comprised of a parent and all descendants of that parent (C-G-H)



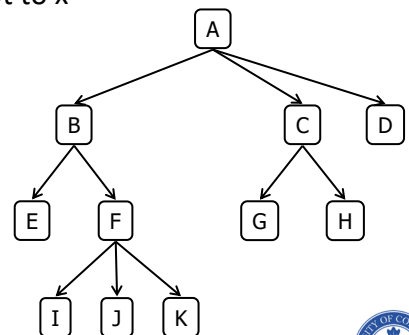
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## Trees Terminologies

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- **Height** of a node x: number of edges in longest path from the node x to a leaf
  - Height of a tree in this example is 3 (from root to leaf)
  - Height of B is 2 (from B to leaf)
- **Depth/Level** of node x: Number of edges in path from root to x
  - Depth of B is 1
  - Depth of J is 3
- **Degree** of a node: The number of its children
- **Degree** of a tree: The number of nodes in it



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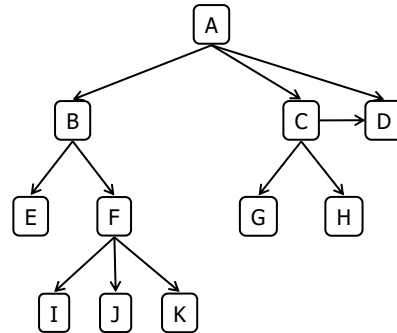
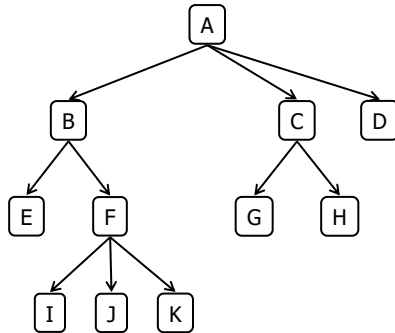


## Trees Terminologies

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- In a tree, there must only be a single path from the root node to any other node

This is not a tree



## Trees Trees as Lists

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- Tree can be defined recursively as a root with zero or more children
  - Each children can be a subtree
- As same as we conceptualized other data structures with Lists, we can do that for Trees as well
- $$T = ['C',$$

$$['A',$$

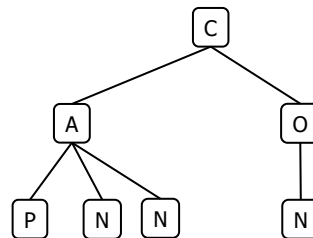
$$['P', 'N', 'T']$$

$$],$$

$$['O',$$

$$['N']$$

$$]$$



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Trees

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## Activity

Fill the table with corresponding values

```
T = ['C',
     ['A',
      ['P', 'N', 'T']
     ],
     ['O',
      ['Z']
     ]
]
```

```
def printtree(T):
    print(T[0])
    for child in range(1, len(T)):
        printtree(T[child])
```

printtree(t) calls	T[0]	T[child]

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Trees

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## Activity

## Solution

Fill the table with corresponding values

```
T = ['C',
     ['A',
      ['P', 'N', 'T']
     ],
     ['O',
      ['Z']
     ]
]
```

```
def printtree(T):
    print(T[0])
    for child in range(1, len(T)):
        printtree(T[child])
```

printtree(t) calls	T[0]	T[child]
1	C	['A', ['P', 'N', 'T']]
2	A	['P', 'N', 'T']
3	P	N
4	N	T
5	T	['O', ['Z']]
6	O	['Z']
7	Z	-

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Trees

Trees ADT

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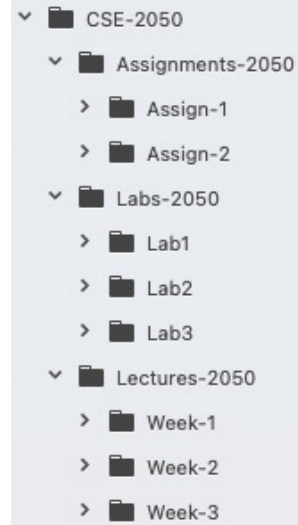
Very basic methods are:

**\_\_init\_\_(l):** Initializes a new tree with data, children (list) and parent.

**add\_child:** add a child to existing node

**get\_level:** get a level of the current node

**\_\_str\_\_():** Return a string representing the entire tree.



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Trees

Trees Implementation

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```

class TreeNode:
    def __init__(self, data):
        self.data = data
        self.children = []
        self.parent = None
  
```

```

def get_level(self):
    level = 0
    node_parent = self.parent
    while node_parent != None:
        level += 1
        node_parent = node_parent.parent
    return level
  
```

```

def add_child(self, child):
    child.parent = self
    self.children.append(child)
  
```

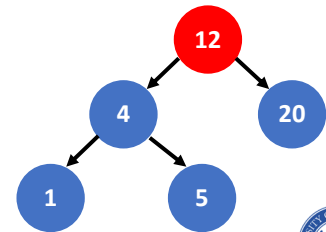
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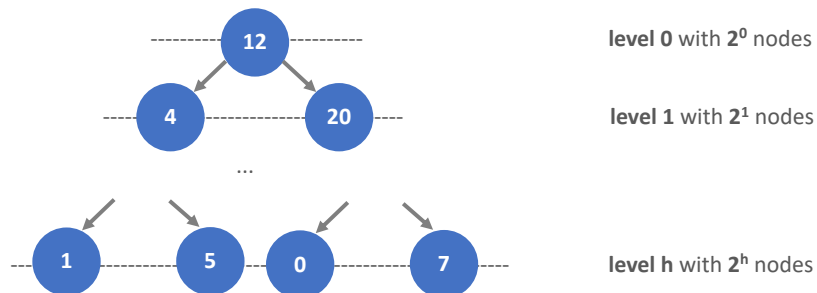
## Binary Search Trees

- Binary search trees are data structures to organize data efficiently
- Every node in the tree can have at most 2 children (left child and right child)
  - left child is smaller than the parent node
  - right child is greater than the parent node
- The new data is placed in sorted order so that the search and other operations can use the principle of binary search with  $O(\log n)$  running time
- We can access the root node exclusively as same as we can access head node of linked list
- All other nodes can be accessed via the root node



## Binary Search Trees

- Number of nodes in a complete binary tree with height  $h$

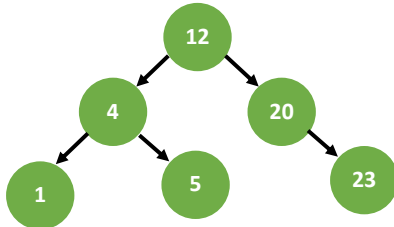


$$\begin{aligned}
 2^h &= N \\
 \log_2 2^h &= \log_2 N \\
 h &= \log_2 N \\
 h &= O(\log N)
 \end{aligned}$$



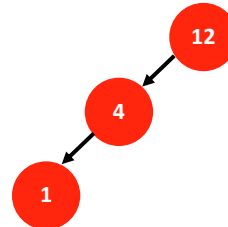
## Binary Search Trees

- Balanced and Imbalanced BST



BALANCED TREE

- Left and right nodes contain approximately same number of children
- operations are  $O(\log N)$  always



IMBALANCED TREE

- Number of children on both sides differ significantly
- $O(N)$  linear running time complexity



## Binary Search Trees Operations

Insert

Search

min

max

Delete

Traverse



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Trees

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Binary Search Trees


Operations

Insert

Insert(12)

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Trees

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Binary Search Trees


Operations

Insert

Insert(4)

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Trees

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Binary Search Trees

Operations


Insert

Insert(4)

Is new element smaller/greater than 12?



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Trees

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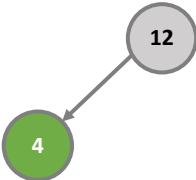
Binary Search Trees

Operations


Insert

Insert(4)

Smaller → place it on the left.



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Trees

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Binary Search Trees

Operations

Insert

Insert(8)

```
graph TD; 12((12)) --> 4((4));
```

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Trees

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Binary Search Trees

Operations

Insert

Insert(8)

Is new element smaller/greater than 12?

```
graph TD; 12((12)) --> 4((4));
```

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Trees

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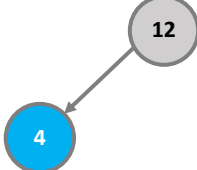
Binary Search Trees

Operations


Insert

Insert(8)

Smaller → check the next node on left.



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Trees

33

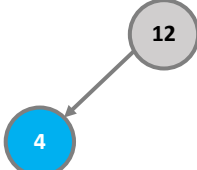
Binary Search Trees

Operations


Insert

Insert(8)

Is new element smaller/greater than 4?



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Trees

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Binary Search Trees

Operations

Insert

Insert(8)

Greater → place it on the right.

```
graph TD; 12((12)) --> 4((4)); 4 --> 8((8)); style 8 fill:#008000,stroke:#008000
```

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Trees

35

Binary Search Trees

Operations

Insert

```
graph TD; 12((12)) --> 4((4)); 4 --> 8((8));
```

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Trees

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Binary Search Trees

Operations

Insert

Insert(20)

```
graph TD; 12((12)) --> 4((4)); 4 --> 8((8));
```

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Trees

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Binary Search Trees

Operations

Insert

Insert(20)

Is new element smaller/greater than 12?

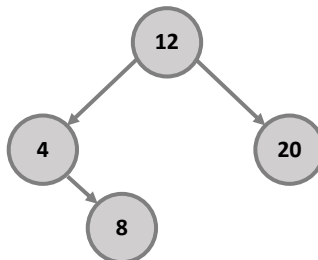
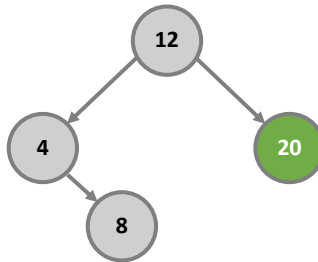
```
graph TD; 12((12)) --> 4((4)); 4 --> 8((8));
```

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Insert(20)

Greater → place it on the right.



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Trees

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Binary Search Trees

Operations

Insert

Insert(27)

```
graph TD; 12((12)) --> 4((4)); 12 --> 20((20)); 4 --> 8((8));
```

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Trees

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Binary Search Trees

Operations

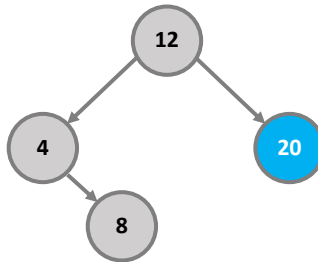
Insert

Insert(27)

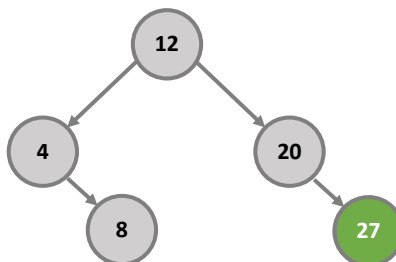
```
graph TD; 12((12)) --> 4((4)); 12 --> 20((20)); 4 --> 8((8));
```

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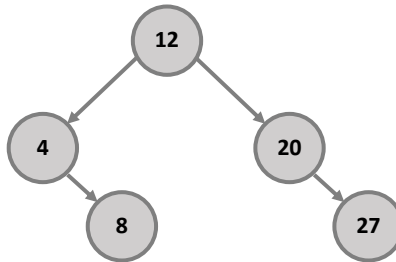
Insert(27)



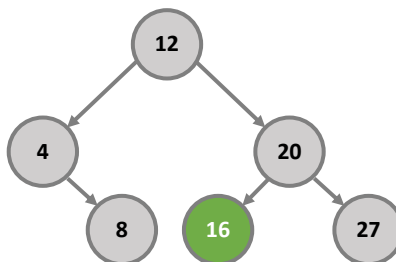
Insert(27)



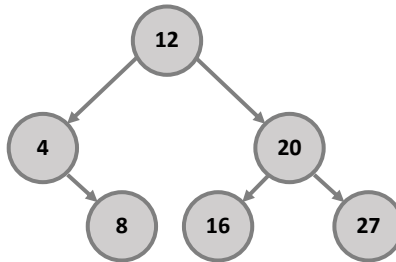
Insert(16)



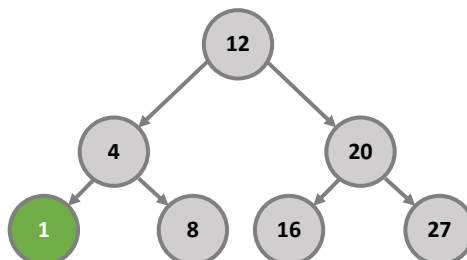
Insert(16)



Insert(1)



Insert(1)



## Binary Search Trees

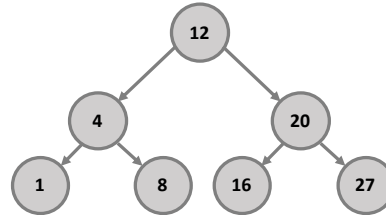
## Operations

## Insert

**Implementation**

**Create a Node** class encapsulating the following information:

- Actual data
- Parent node
- Left child
- Right child



```

class BSTNode:
    def __init__(self, data, parent = None):
        self.data = data
        self.parent = parent
        self.left = None
        self.right = None
  
```



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# Data Structures and Object-Oriented Design

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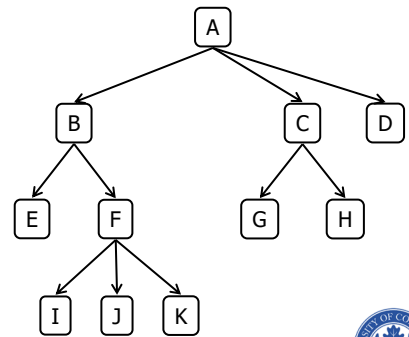
Office: UConn (Stamford), 305C  
email: [hasan.baig@uconn.edu](mailto:hasan.baig@uconn.edu)

## CSE-2050 – Data Structures and Object-Oriented Design

## Quick Recap

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- Overview of data structures studied so far
- Trees
  - Non linear data structure
- Terminologies
  - Root
  - Parent
  - Child
  - Leaf node
  - Depth/level
    - Number of edges from root to x
- Trees representation as a list



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## CSE-2050 – Data Structures and Object-Oriented Design

## Quick Recap

51

- Trees representation
  - As a list

```

T = ['C',
     ['A',
      ['P', 'N', 'T']
     ],
     ['O',
      ['Z']
     ]
    ]
  
```

- As a class

```

class TreeNode:
    def __init__(self, data):
        self.data = data
        self.children = []
        self.parent = None
  
```

```

def add_child(self, child):
    child.parent = self
    self.children.append(child)
  
```

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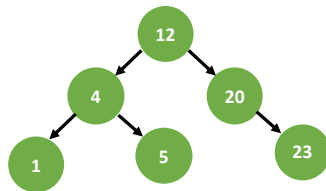


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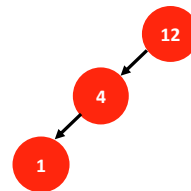
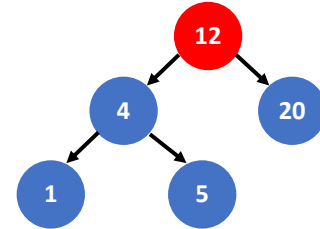
## Quick Recap

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- Binary Search Trees →
  - Each node can have at most two child
  - Left child is smaller than the parent
  - Right child is greater than the parent
- Balanced and Imbalanced Trees



BALANCED TREE



IMBALANCED TREE

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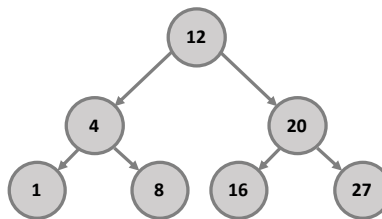


## CSE-2050 – Data Structures and Object-Oriented Design

## Quick Recap

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- BST Operations
  - Insert, Search, Delete, Traverse



```

class BSTNode:
    def __init__(self, data, parent = None):
        self.data = data
        self.parent = parent
        self.left = None
        self.right = None
  
```

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## Binary Search Trees

## Operations

## Insert

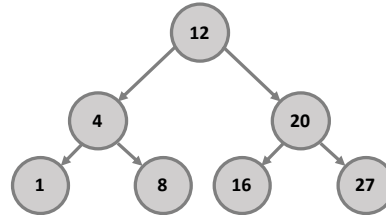
Implementation**Create a BinarySearchTree class**

1. Initialize the root node with None

**insert()** method

1. Add root node, if it does not exist
2. Check if the new element is greater/smaller than the current parent.
3. If left/right child does not exist, add the new node on appropriate side
4. If the child node exist, recursively execute step 2 and 3.

Note: Assume that the duplicate elements are not allowed



## Binary Search Trees

## Operations

## Insert

Implementation

```

class BinarySearchTree:
    def __init__(self):
        self.root = None

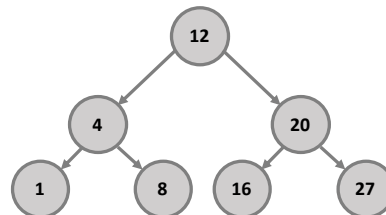
    def insert(self, data):
        if self.root is None:
            #if there is no root node
            self.root = BSTNode(data)
        else:
            #if root node exist, then add child at right location
            self._add_child(data, self.root)
  
```

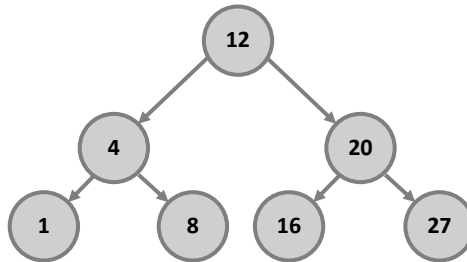
```

def _add_child(self, data, p_node):
    if data == p_node.data: #duplicate items cannot be added
        return

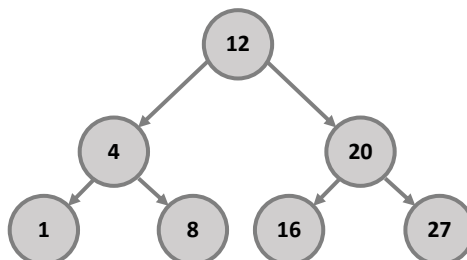
    if data < p_node.data: #the element is smaller than the root
        if p_node.left: #left child exist
            self._add_child(data, p_node.left)
        else: # left child does not exist
            p_node.left = BSTNode(data, p_node)

    else: #the element is greater than the root
        if p_node.right: #right child exists
            self._add_child(data, p_node.right)
        else: #right child does not exist
            p_node.right = BSTNode(data, p_node)
  
```



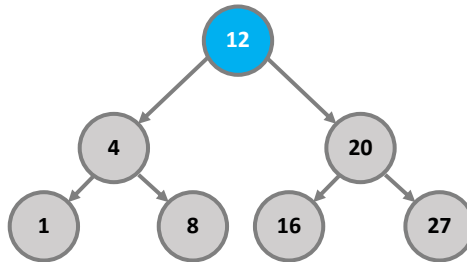


Search(8)

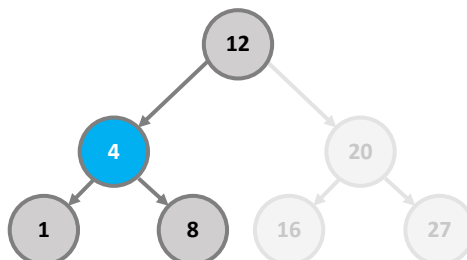


Search(8)

Is the element smaller/greater than the root?



Search(8)



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Trees

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Binary Search Trees    Operations

Search

Search(8)

```
graph TD; 12((12)) --> 4((4)); 12 --> 20((20)); 4 --> 1((1)); 4 --> 8((8)); 20 --> 16((16)); 20 --> 27((27)); style 8 stroke:#007bff,stroke-width:2px
```

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Trees

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Binary Search Trees    Operations

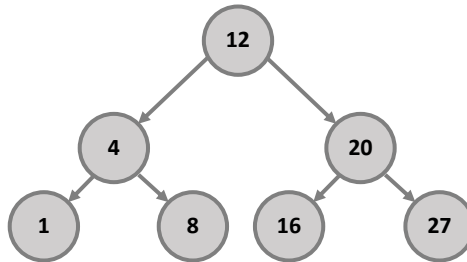
Search

Search(8)

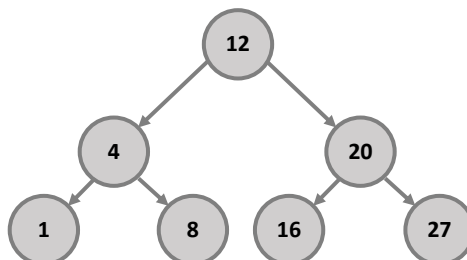
```
graph TD; 12((12)) --> 4((4)); 12 --> 20((20)); 4 --> 1((1)); 4 --> 8((8)); 20 --> 16((16)); 20 --> 27((27)); style 8 stroke:#008000,stroke-width:2px
```

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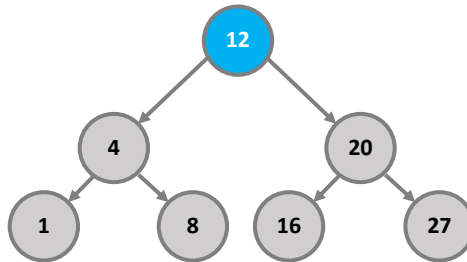




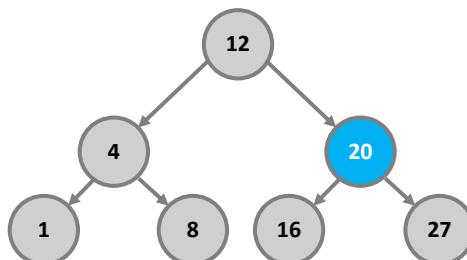
Search max()



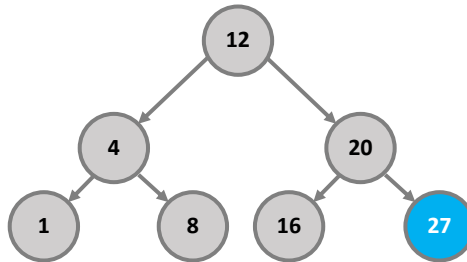
Search max()



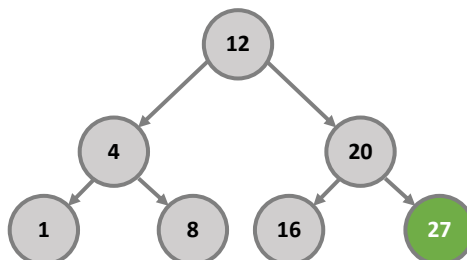
Search max()



Search max()



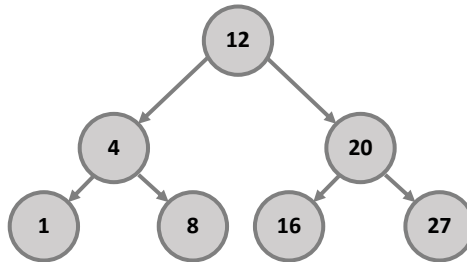
Search max()



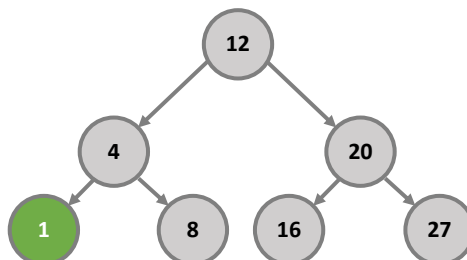
the **maximum** item in the binary search tree  
is the **rightmost** item in the tree



Search min()



Search min()



the **minimum** item in the binary search tree  
is the **leftmost** item in the tree





## Binary Search Trees

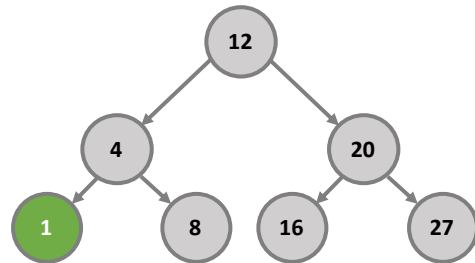
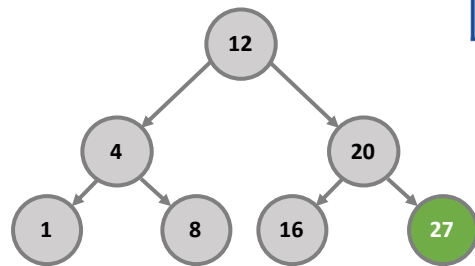
## Operations

## Search

**Implementation - get\_max()**

1. If root exist, proceed to step 2, else → None
2. For the current node, check if the right child exist
3. If right child does not exist, Return the current node data, else recurse step 2 again

Try it Yourself



## Binary Search Trees

## Operations

## Search

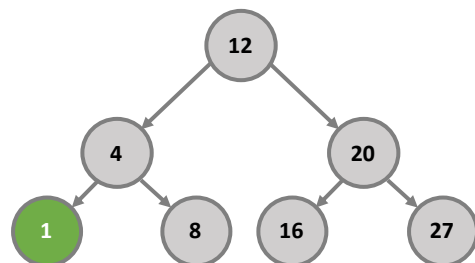
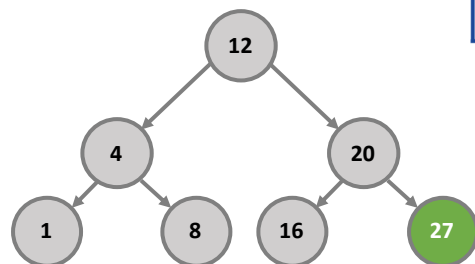
**Implementation - get\_max()**

```

def get_max(self):
    if self.root:
        return self._get_right_child(self.root)
    else:
        return None
  
```

```

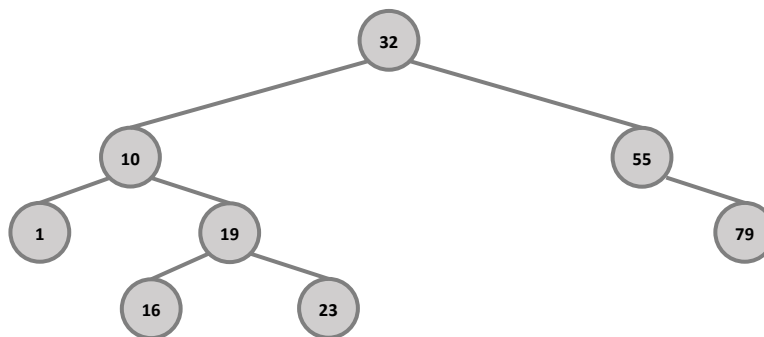
def _get_right_child(self, node):
    if node.right:
        return self._get_right_child(node.right)
    return node.data
  
```



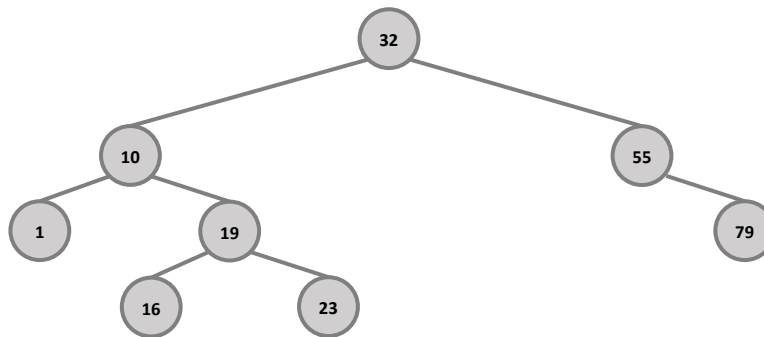
1. Deleting a leaf node → node having no children
2. Deleting a node with 1 child
3. Deleting a node with 2 children



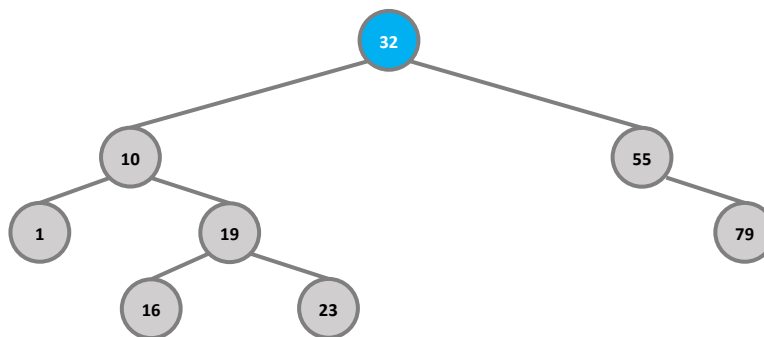
1. Deleting a leaf node → node having no children



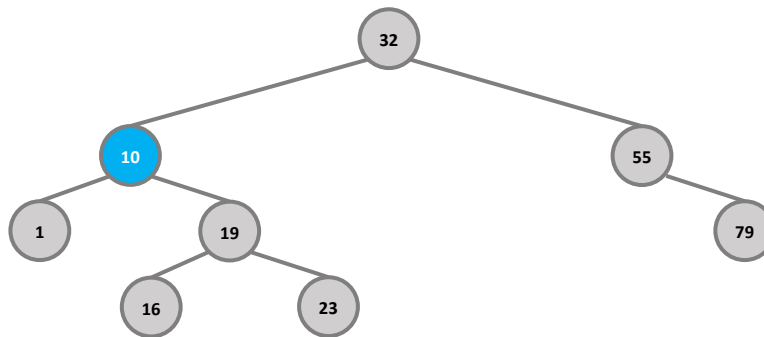
1. Deleting a leaf node → 23



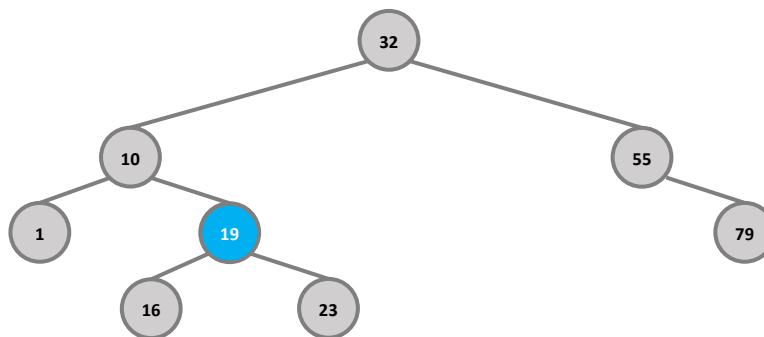
1. Deleting a leaf node → 23



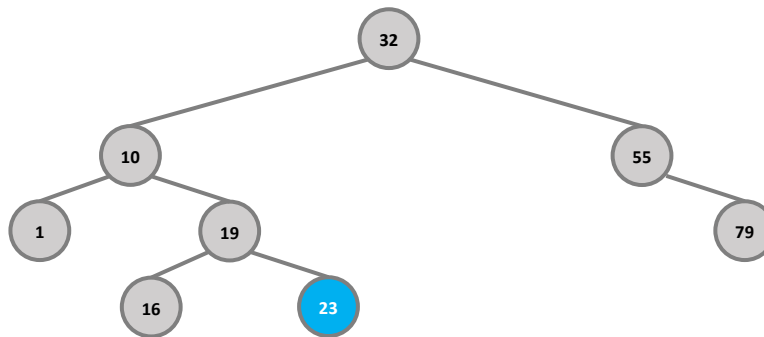
1. Deleting a leaf node  $\rightarrow$  23



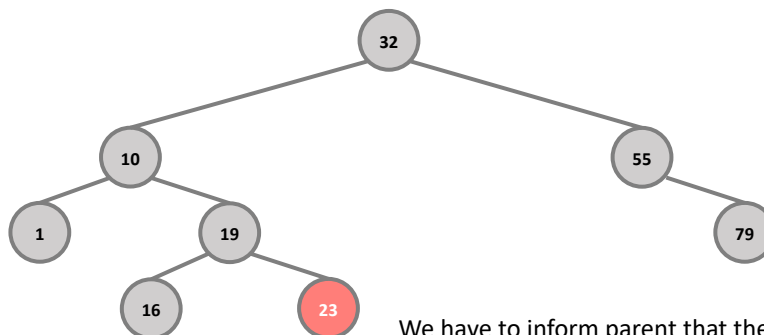
1. Deleting a leaf node  $\rightarrow$  23



1. Deleting a leaf node → 23



1. Deleting a leaf node → 23



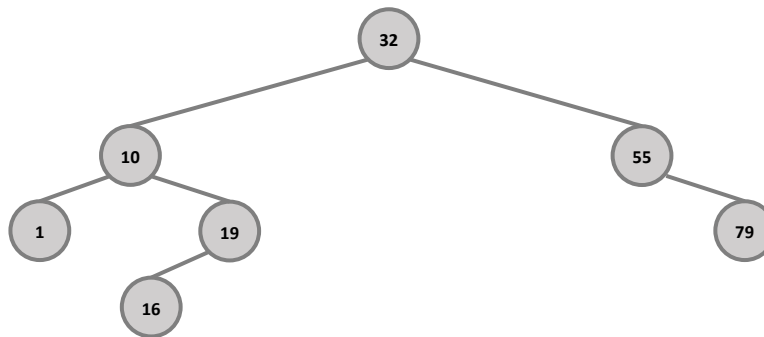
We have to inform parent that the child has been removed.

## Binary Search Trees

## Operations

## Delete

1. Deleting a leaf node → 23

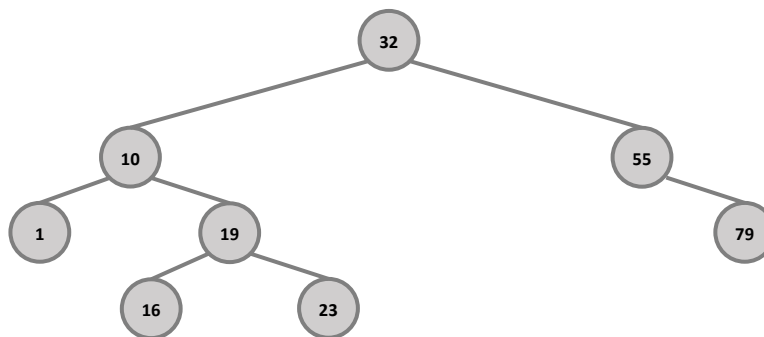


## Binary Search Trees

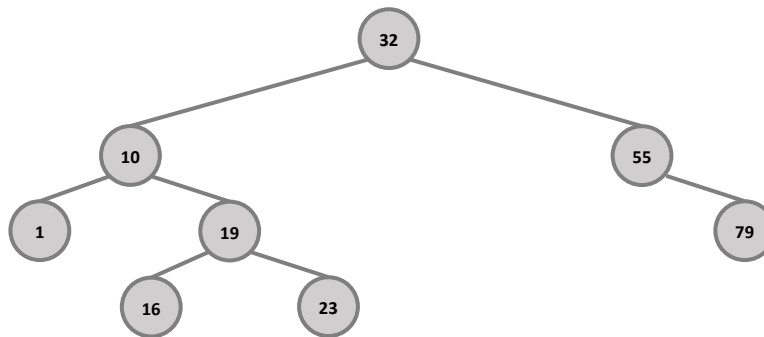
## Operations

## Delete

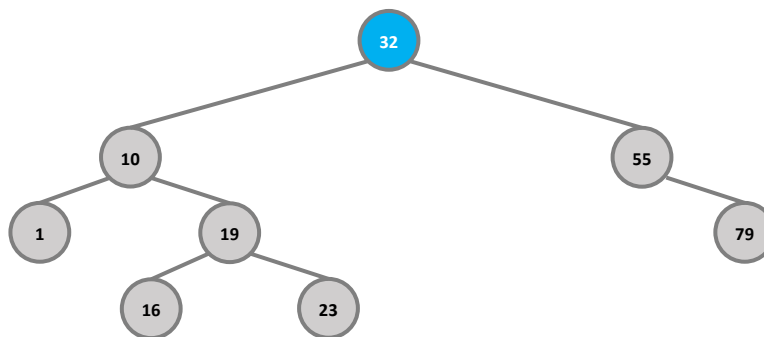
2. Deleting a node with one child



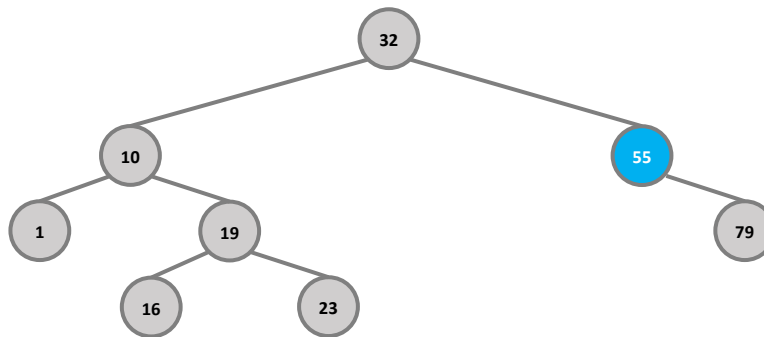
2. Deleting a node with one child → 55



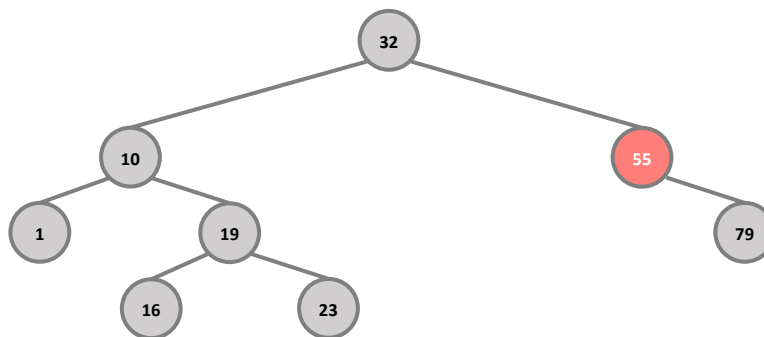
2. Deleting a node with one child → 55



2. Deleting a node with one child → 55



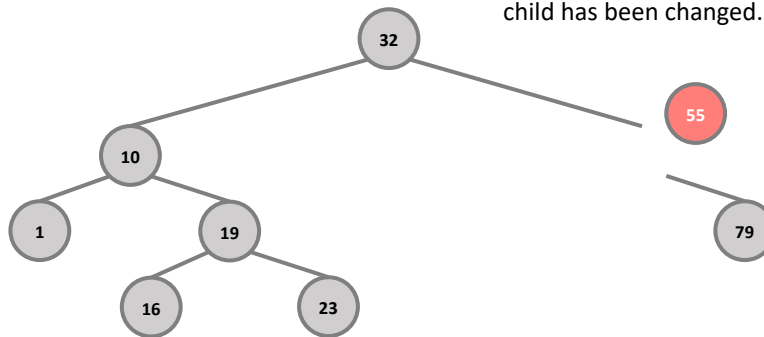
2. Deleting a node with one child → 55





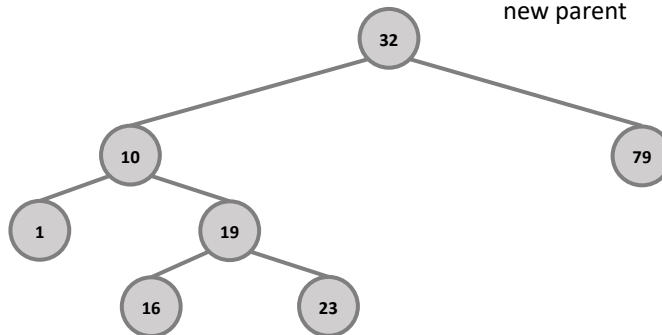
2. Deleting a node with one child → 55

We have to inform parent that the right (or left) child has been changed.

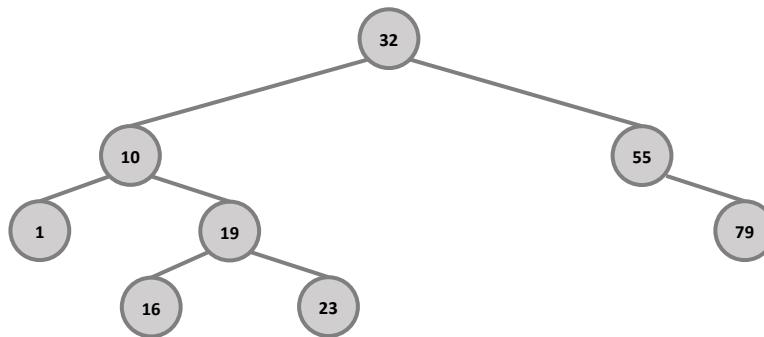


2. Deleting a node with one child → 55

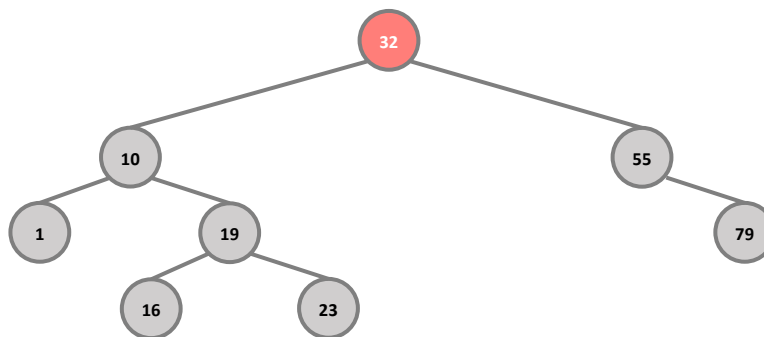
We also have to update “the child” about its new parent



## 3. Deleting a node with two child

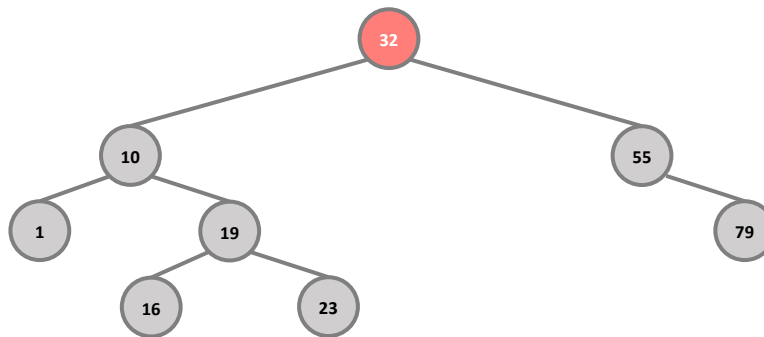


## 3. Deleting a node with two child → root node



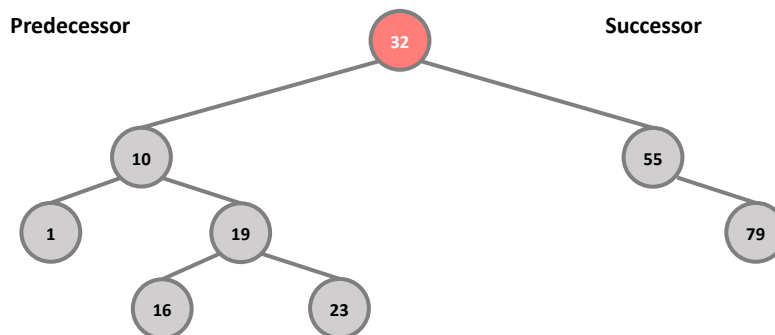
3. Deleting a node with two child  $\rightarrow$  root node

After deleting, what will be the new root?



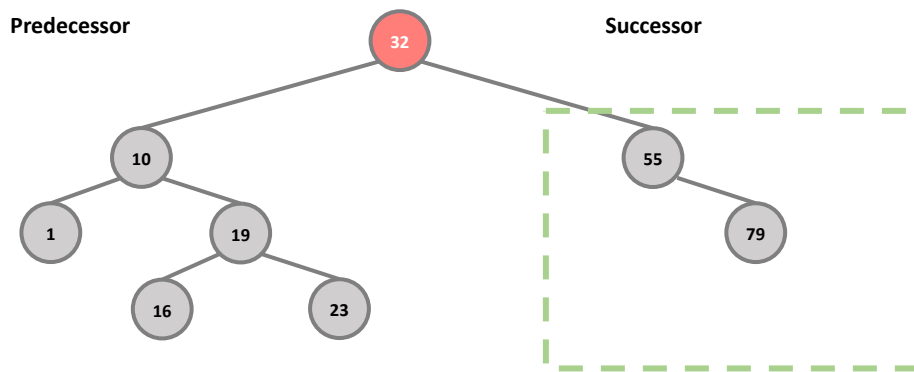
3. Deleting a node with two child  $\rightarrow$  root node

After deleting, what will be the new root?



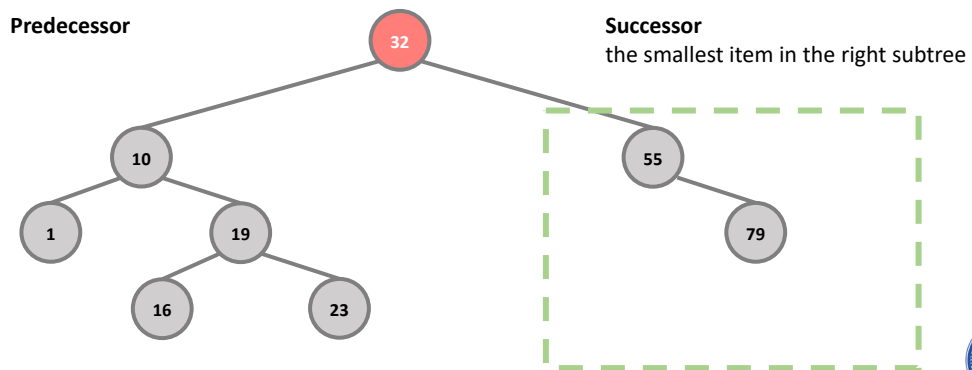
3. Deleting a node with two child  $\rightarrow$  root node

After deleting, what will be the new root?



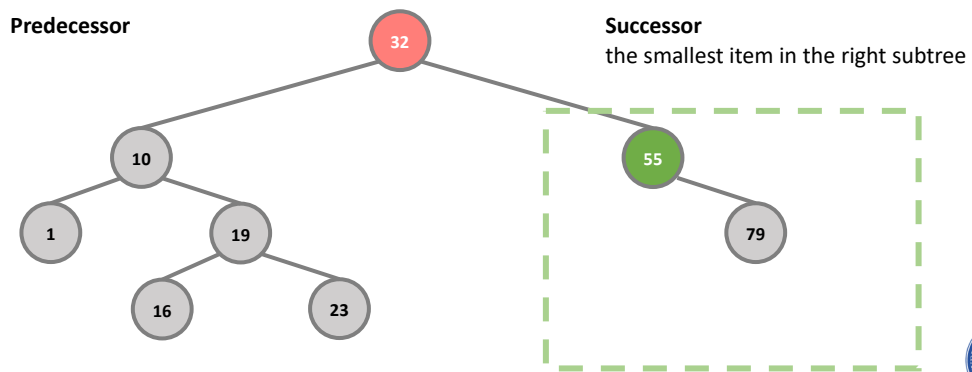
3. Deleting a node with two child  $\rightarrow$  root node

After deleting, what will be the new root?



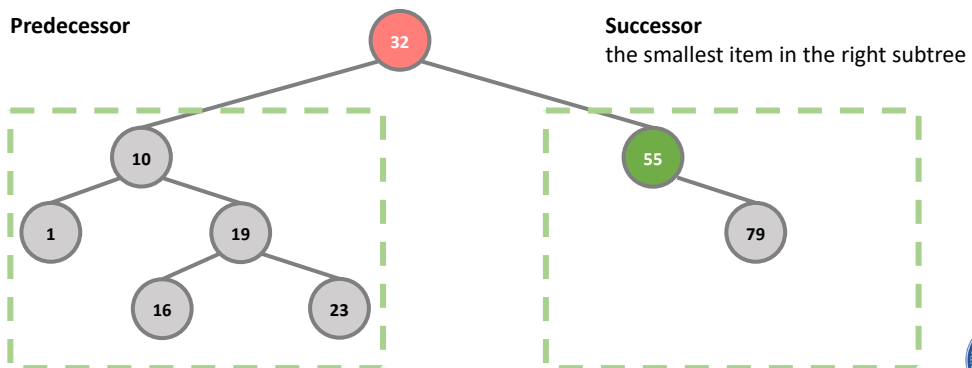
3. Deleting a node with two child  $\rightarrow$  root node

After deleting, what will be the new root?



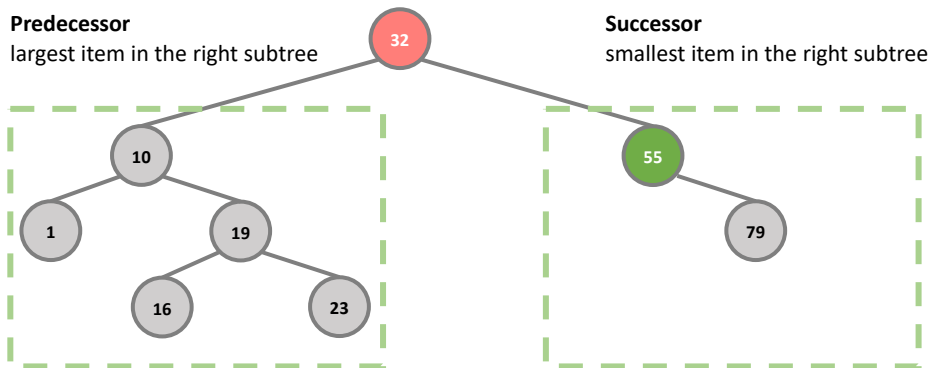
3. Deleting a node with two child  $\rightarrow$  root node

After deleting, what will be the new root?



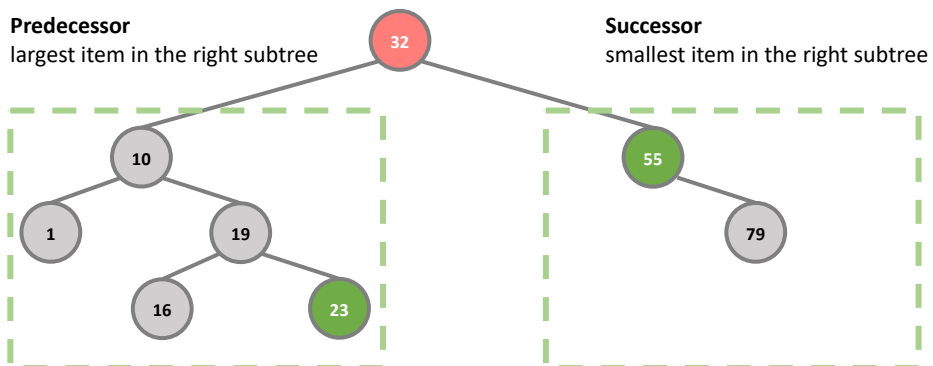
3. Deleting a node with two child  $\rightarrow$  root node

After deleting, what will be the new root?

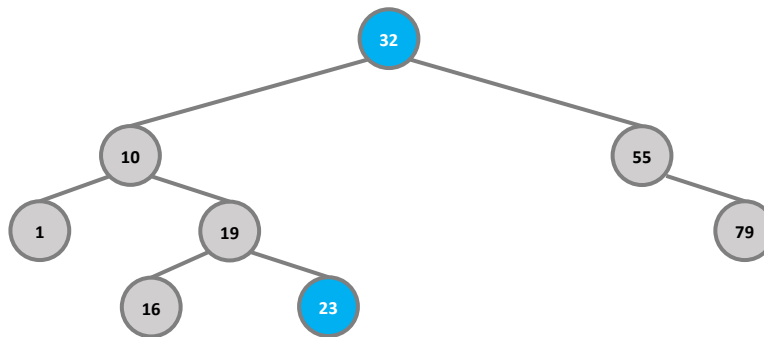


3. Deleting a node with two child  $\rightarrow$  root node

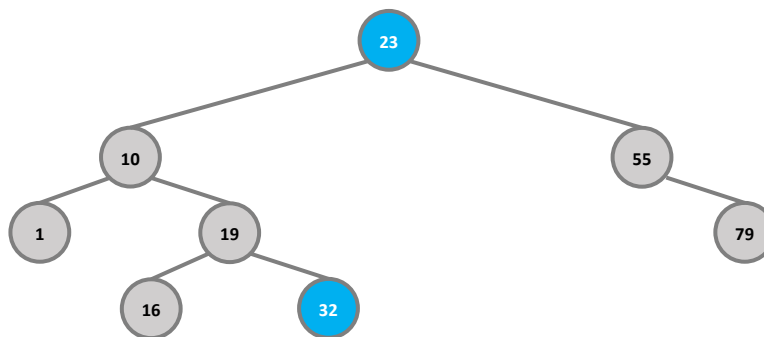
After deleting, what will be the new root?



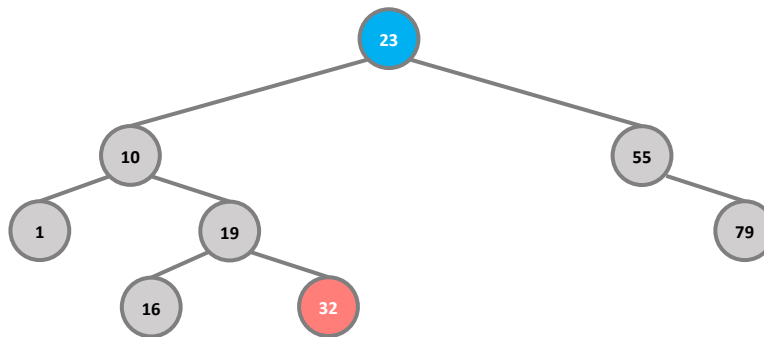
3. Deleting a node with two child  $\rightarrow$  root node



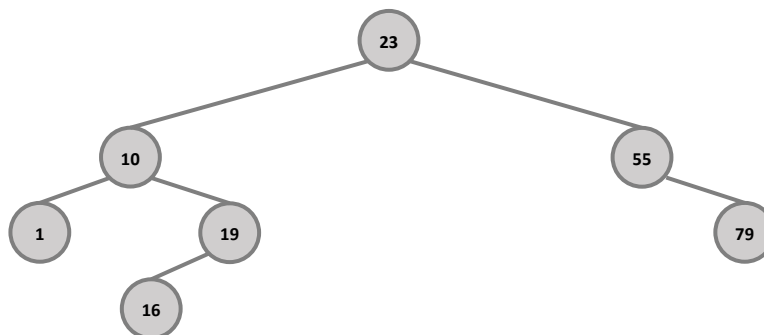
3. Deleting a node with two child  $\rightarrow$  root node



3. Deleting a node with two child  $\rightarrow$  root node



3. Deleting a node with two child  $\rightarrow$  root node



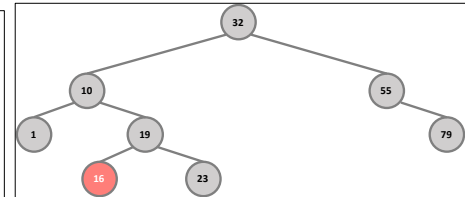
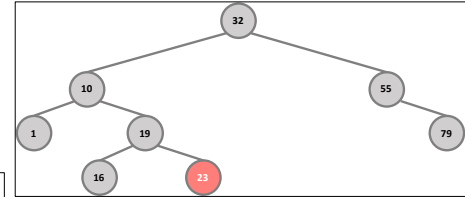


**Implementation - delete()****1. Deleting a leaf node**

```
def delete(self, data):
    if self.root:
        self.remove_node(data, self.root)
```

```
def remove_node(self, data, node):
    if node is None:
        return

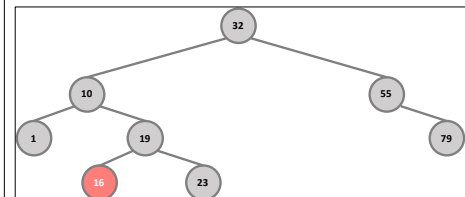
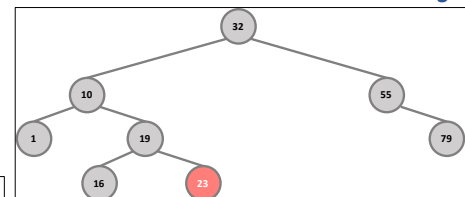
    if data < node.data:
        self.remove_node(data, node.left)
    elif data > node.data:
        self.remove_node(data, node.right)
```

**Implementation - delete()****1. Deleting a leaf node**

```
else: #once the required node to be deleted is found
    if node.left is None and node.right is None:
        print(f"Removing a leaf node with data: {node.data}")
        parent = node.parent

        if parent is not None:
            if parent.right == node:
                parent.right = None
            if parent.left == node:
                parent.left = None
        else: #if the element we are removing is root
            self.root = None

    del node
```



**Implementation - delete()****2. Deleting a node with one child (on right)**

```

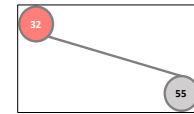
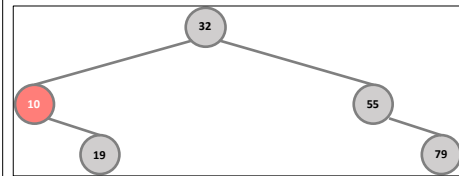
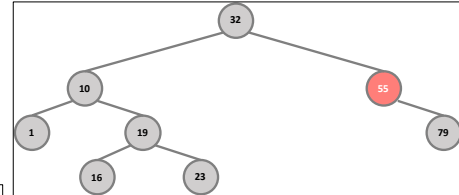
elif node.left is None and node.right is not None:
    print(f"Removing node having a right child with data: {node.data}")
    parent = node.parent

    if parent is not None:
        if parent.right == node:
            parent.right = node.right
        if parent.left == node:
            parent.left = node.right
    else:
        self.root = node.right

    node.right.parent = parent

del node

```

**Implementation - delete()****2. Deleting a node with one child (on right)**

```

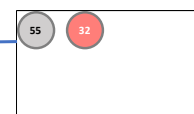
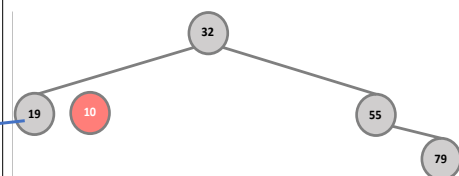
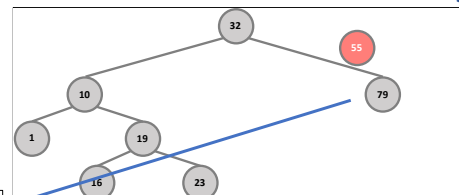
elif node.left is None and node.right is not None:
    print(f"Removing node having a right child with data: {node.data}")
    parent = node.parent

    if parent is not None:
        if parent.right == node:
            parent.right = node.right
        if parent.left == node:
            parent.left = node.right
    else:
        self.root = node.right

    node.right.parent = parent

del node

```



## Binary Search Trees

## Operations

## Delete

**Implementation - delete()**

## 2. Deleting a node with one child (on right)

```

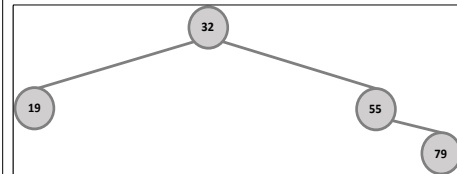
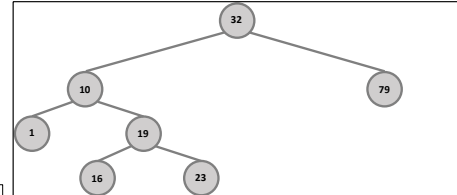
elif node.left is None and node.right is not None:
    print(f"Removing node having a right child with data: {node.data}")
    parent = node.parent

    if parent is not None:
        if parent.right == node:
            parent.right = node.right
        if parent.left == node:
            parent.left = node.right
    else:
        self.root = node.right

    node.right.parent = parent

del node

```



## Binary Search Trees

## Operations

## Delete

**Implementation - delete()**

## 2. Deleting a node with one child (on left)

```

elif node.left is not None and node.right is None:
    print(f"Removing node having a left child with data: {node.data}")
    parent = node.parent

    if parent is not None:
        if parent.right == node:
            parent.right = node.left
        if parent.left == node:
            parent.left = node.left
    else:
        self.root = node.left

    node.left.parent = parent

del node

```



## Binary Search Trees

## Operations

## Delete

**Implementation - delete()****3. Deleting a node with two children**

```

else: #when both children are present
    print(f"Removing node having the left child ({node.left.data}) \
and right child ({node.right.data})")

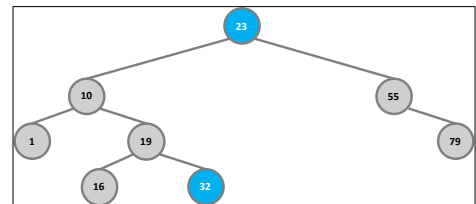
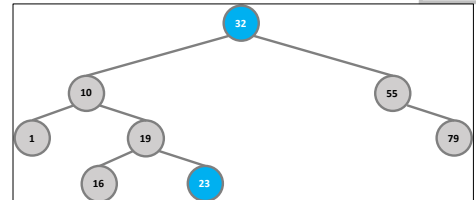
    predecessor = self.get_predecessor(node.left)
    print("predecessor before: ", predecessor.data)
    predecessor.data, node.data = node.data, predecessor.data
    print("predecessor after: ", predecessor.data)
    self.remove_node(data, predecessor)

def get_predecessor(self, node):
    if node.right:
        return self.get_predecessor(node.right)

    return node

```

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## Binary Search Trees

## Traversal

Tree traversal means visiting every node of the binary search tree exactly once in  $O(n)$  linear running time.

## 1. Pre-order traversal

Visit **root** node first, then **left**-subtree and finally **right**-subtree

## 2. Post-order traversal

Visit **left**-subtree first, then **right**-subtree, and finally the **root** node

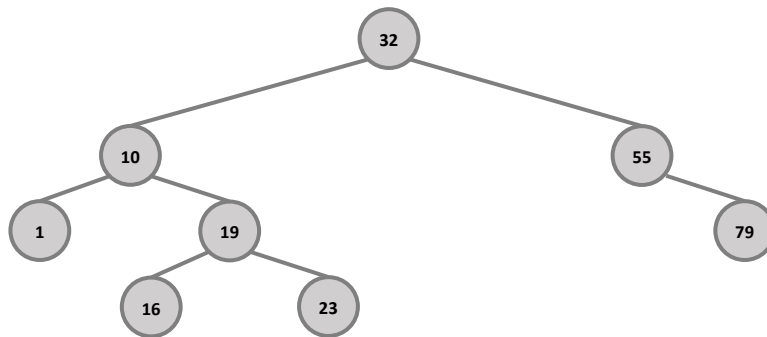
## 3. In-order traversal

Visit **left**-subtree first, then **root** node, and finally **right**-subtree

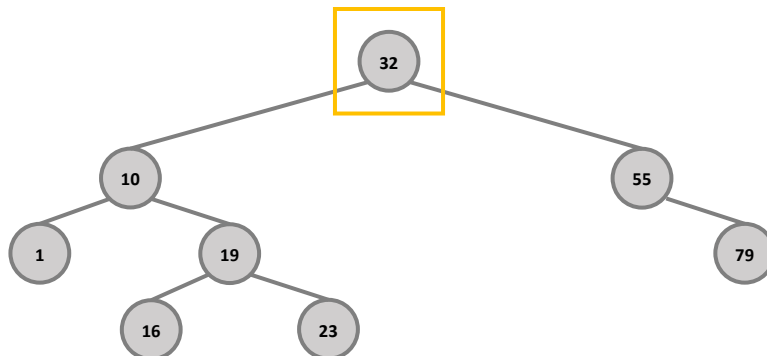
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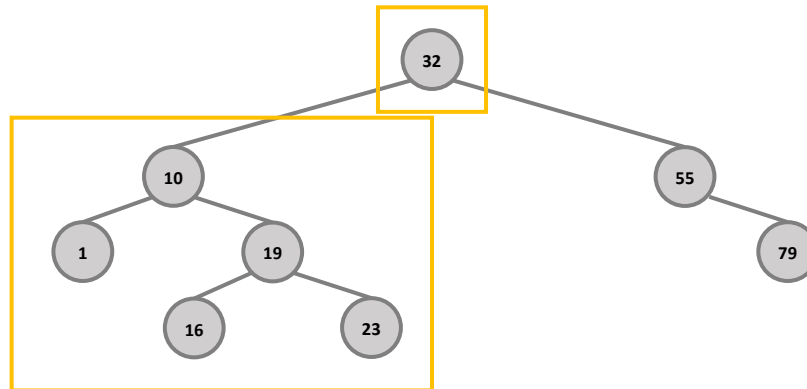
Root node → left subtree → right subtree



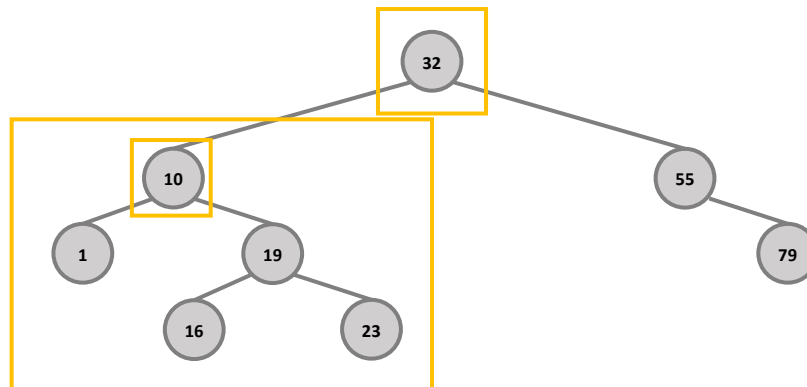
Root node → left subtree → right subtree



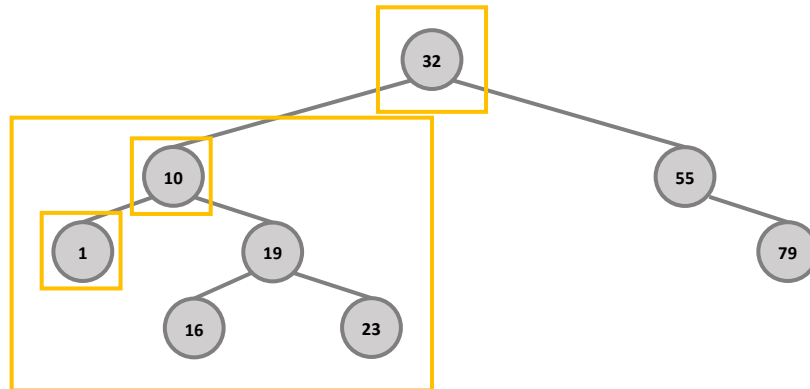
Root node → left subtree → right subtree



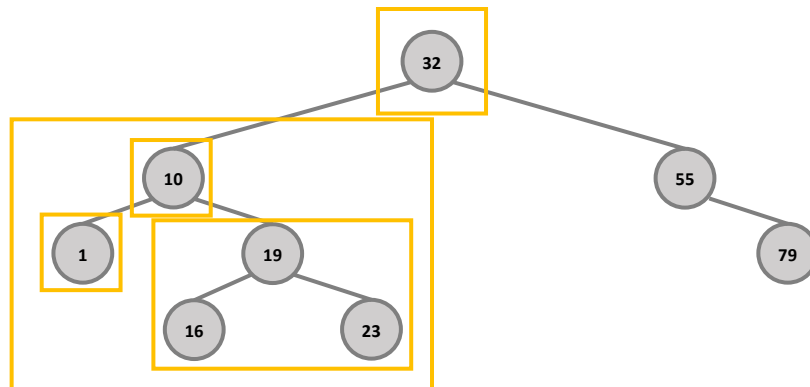
Root node → left subtree → right subtree



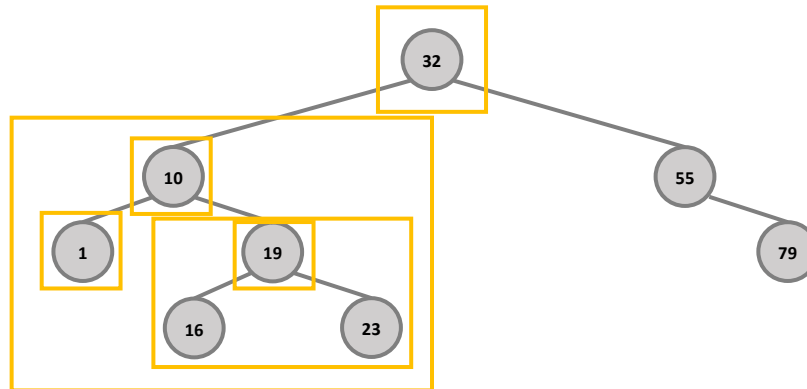
Root node → left subtree → right subtree



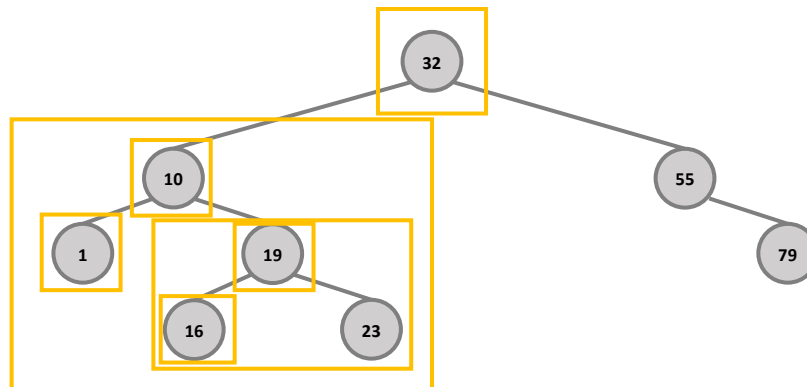
Root node → left subtree → right subtree



Root node → left subtree → right subtree

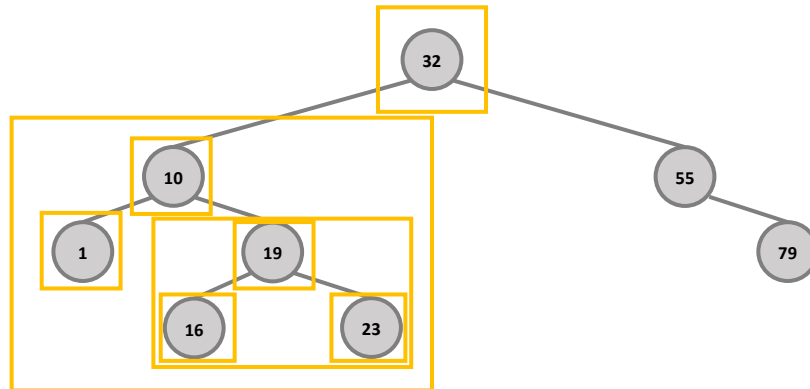


Root node → left subtree → right subtree

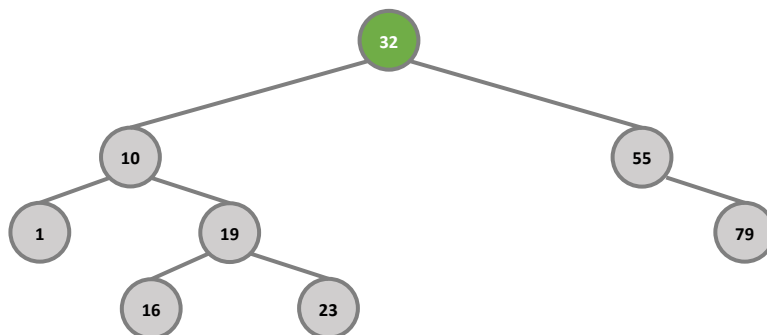




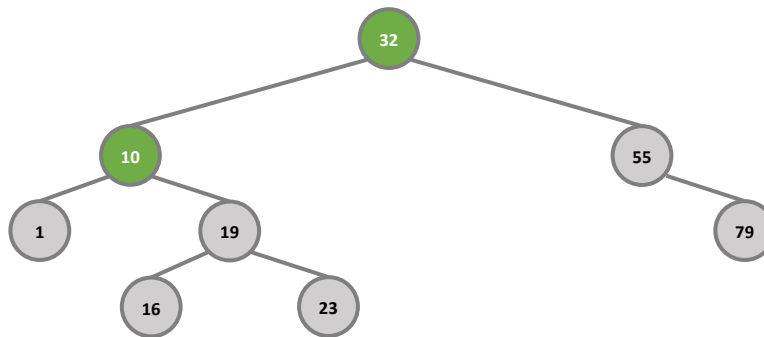
Root node → left subtree → right subtree



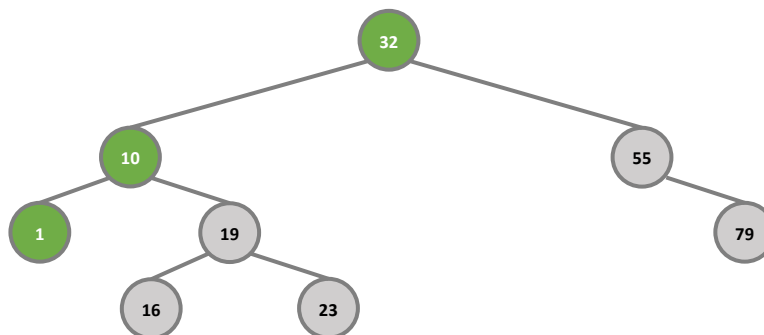
Root node → left subtree → right subtree



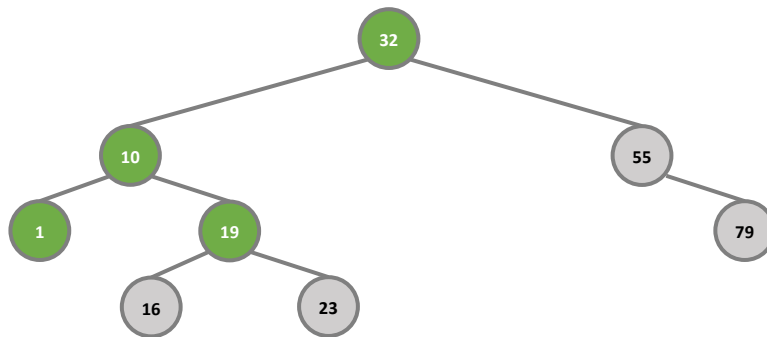
Root node → left subtree → right subtree



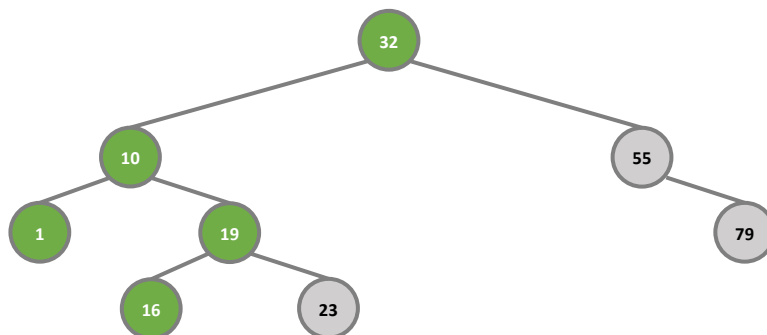
Root node → left subtree → right subtree



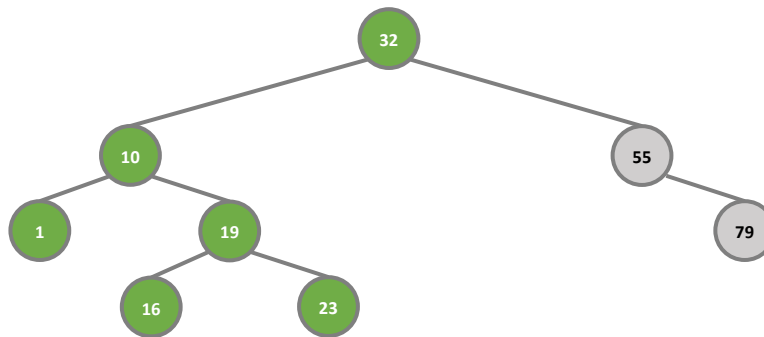
Root node → left subtree → right subtree



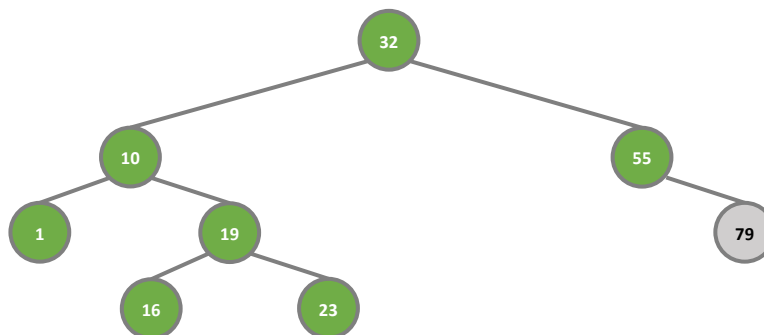
Root node → left subtree → right subtree



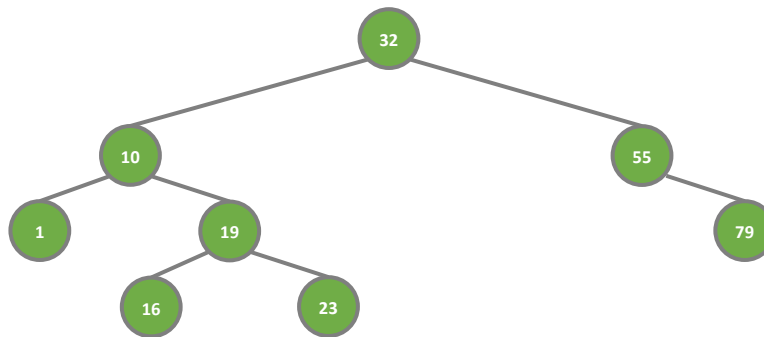
Root node → left subtree → right subtree



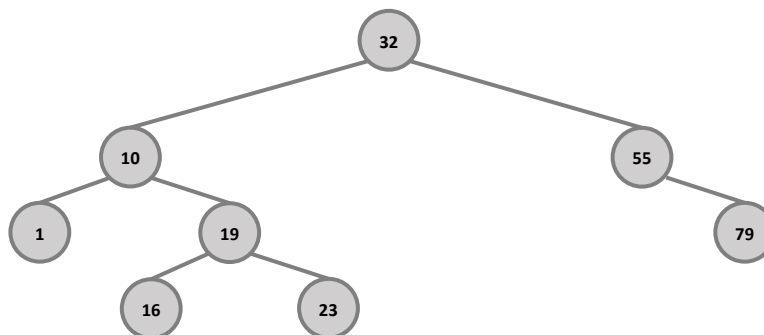
Root node → left subtree → right subtree



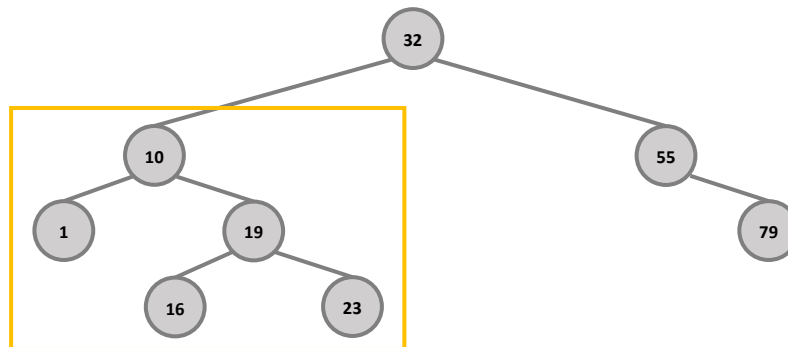
Root node → left subtree → right subtree



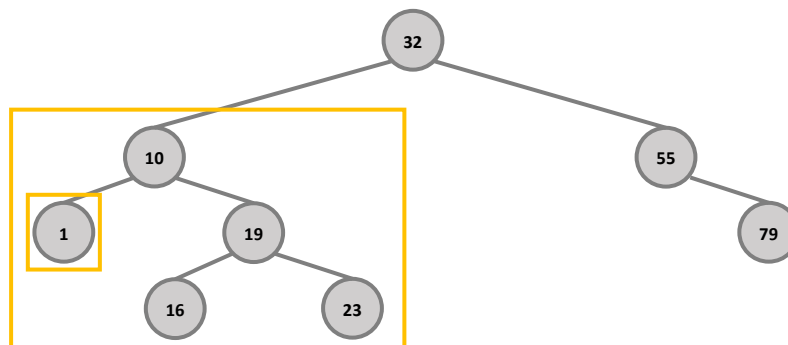
Left subtree → Right subtree → Root node



Left subtree → Right subtree → Root node



Left subtree → Right subtree → Root node

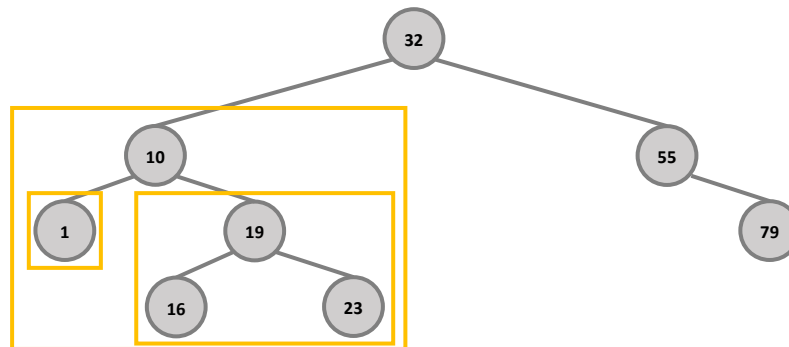


## Binary Search Trees

## Traversal

## Post-order

Left subtree → Right subtree → Root node



Hasan Baig

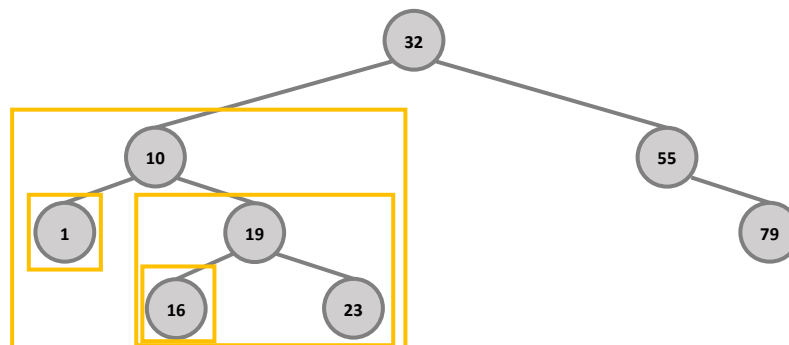


## Binary Search Trees

## Traversal

## Post-order

Left subtree → Right subtree → Root node



Hasan Baig

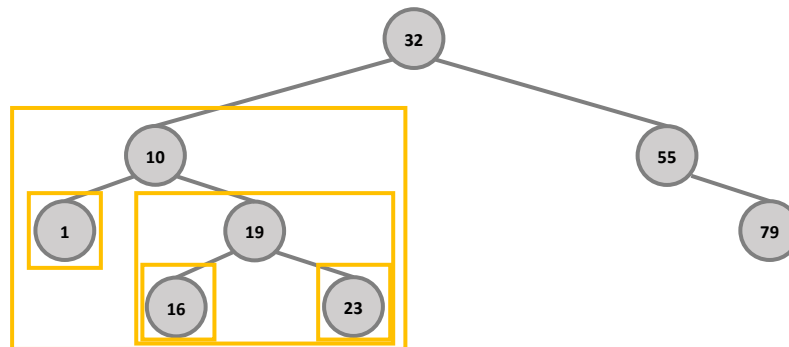


## Binary Search Trees

## Traversal

## Post-order

Left subtree → Right subtree → Root node



Hasan Baig

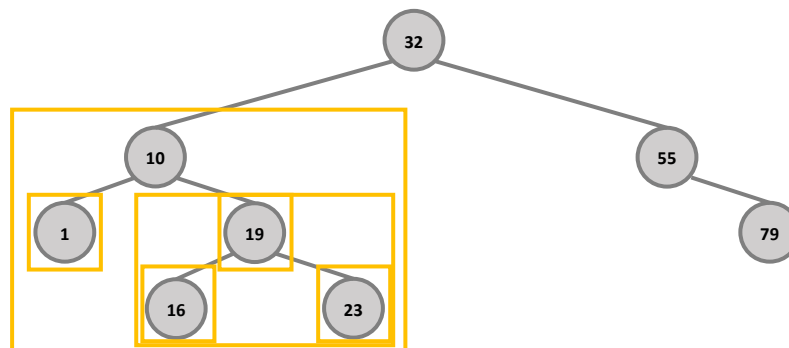


## Binary Search Trees

## Traversal

## Post-order

Left subtree → Right subtree → Root node



Hasan Baig



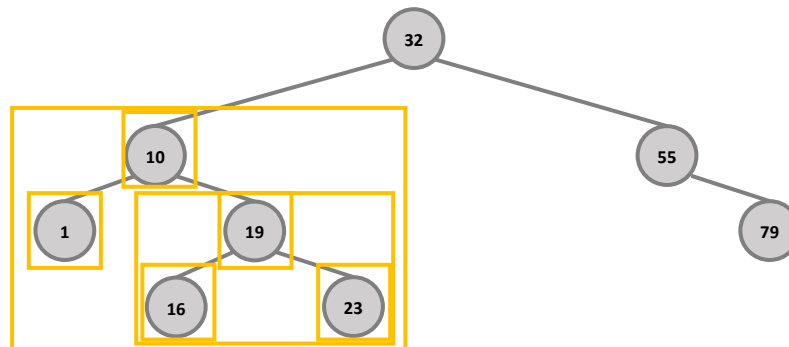


## Binary Search Trees

## Traversal

## Post-order

Left subtree → Right subtree → Root node

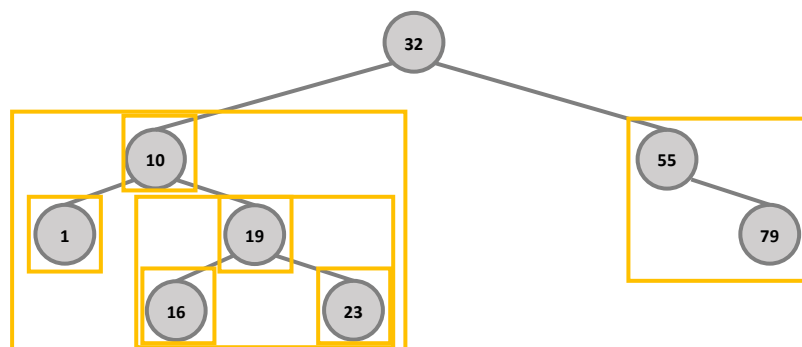


## Binary Search Trees

## Traversal

## Post-order

Left subtree → Right subtree → Root node



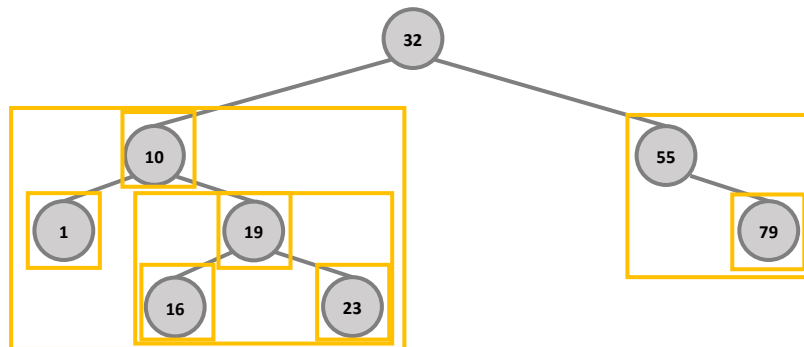
## Binary Search Trees

## Traversal

## Post-order

136

Left subtree → Right subtree → Root node



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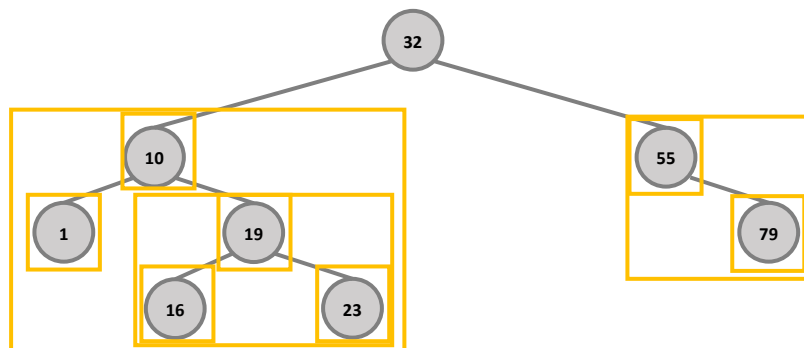
## Binary Search Trees

## Traversal

## Post-order

137

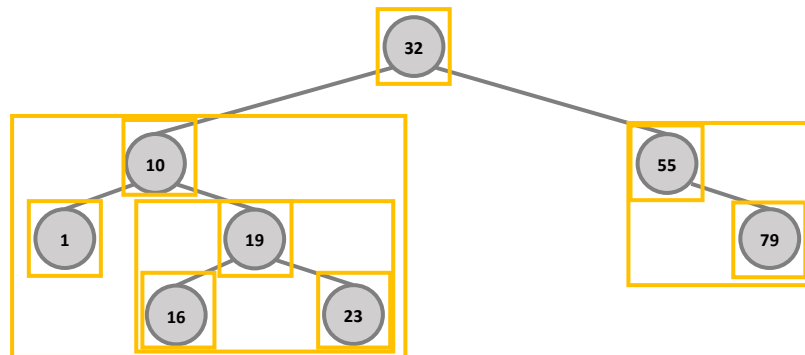
Left subtree → Right subtree → Root node



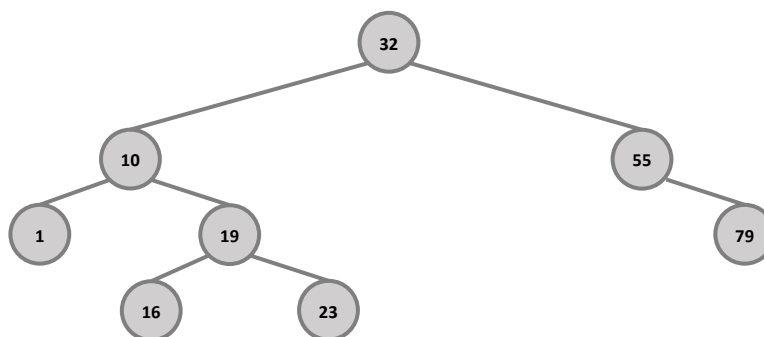
Hasan Baig



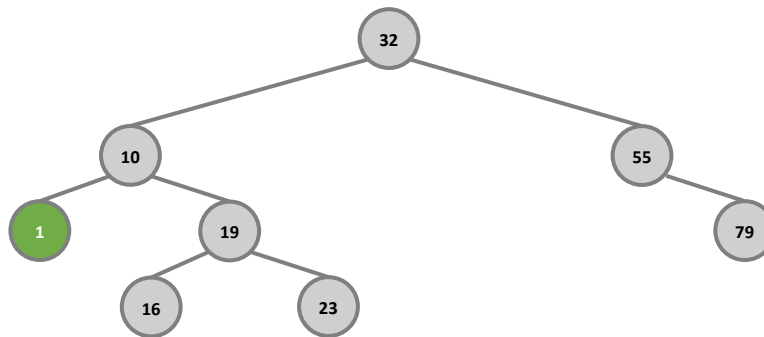
Left subtree → Right subtree → Root node



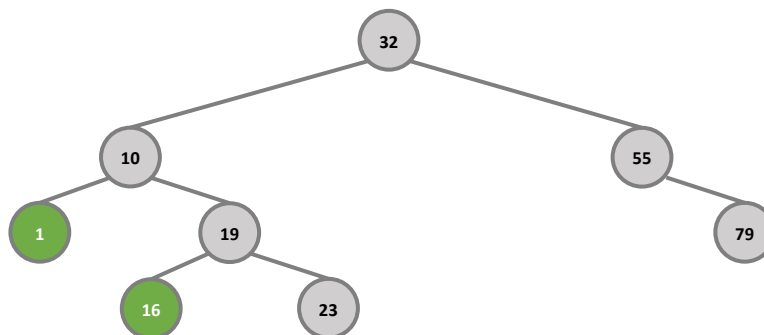
Left subtree → Right subtree → Root node



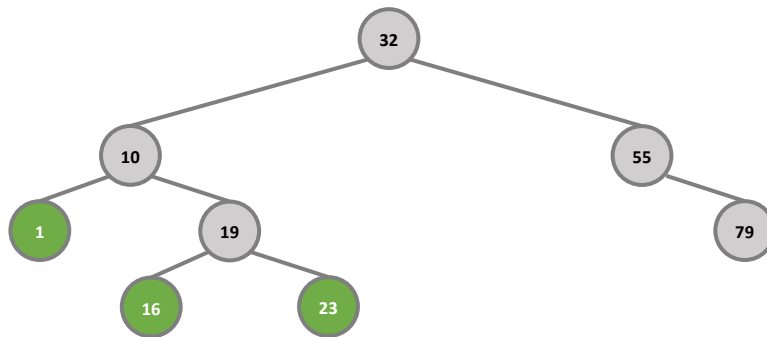
Left subtree → Right subtree → Root node



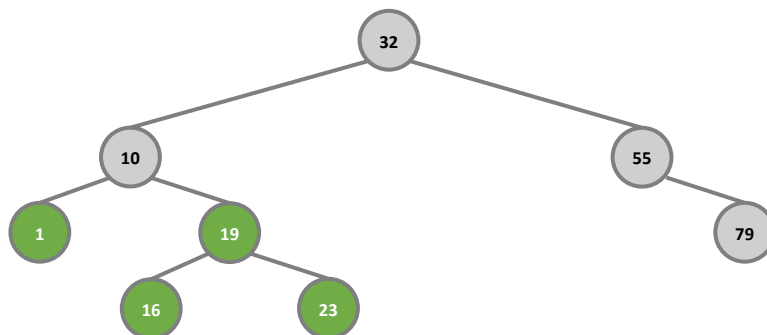
Left subtree → Right subtree → Root node



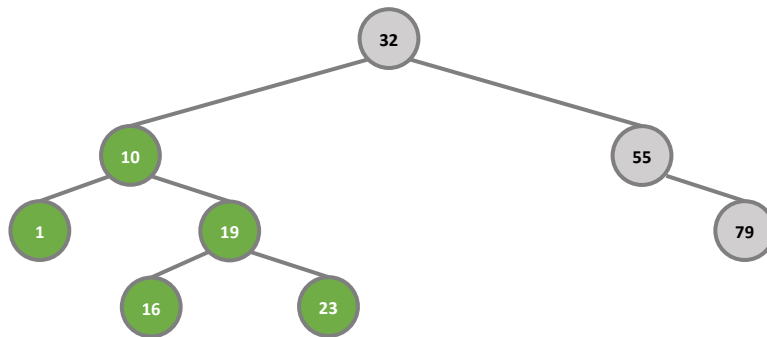
Left subtree → Right subtree → Root node



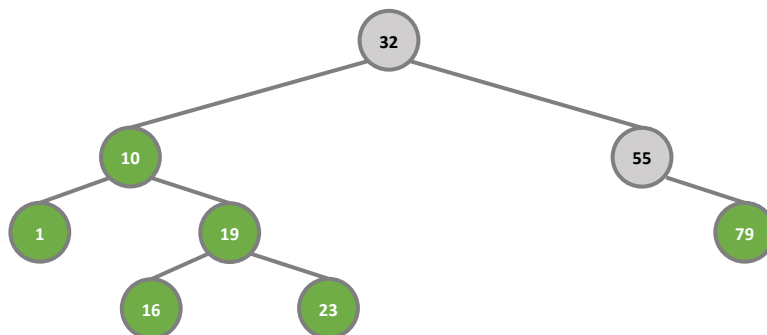
Left subtree → Right subtree → Root node



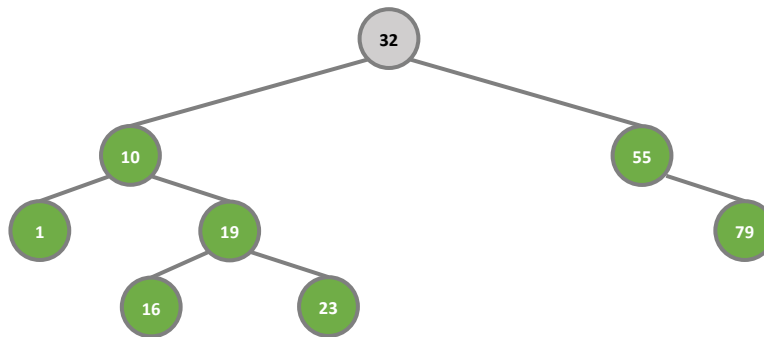
Left subtree → Right subtree → Root node



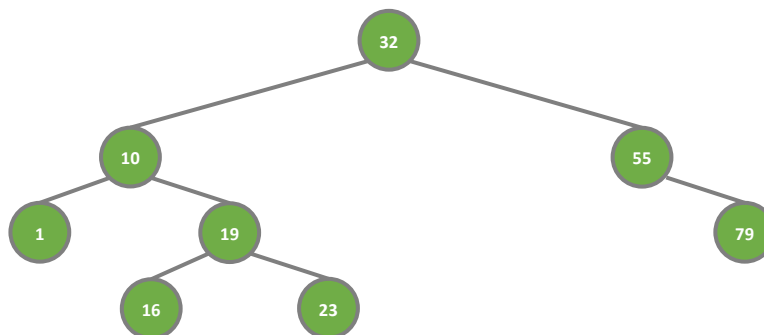
Left subtree → Right subtree → Root node



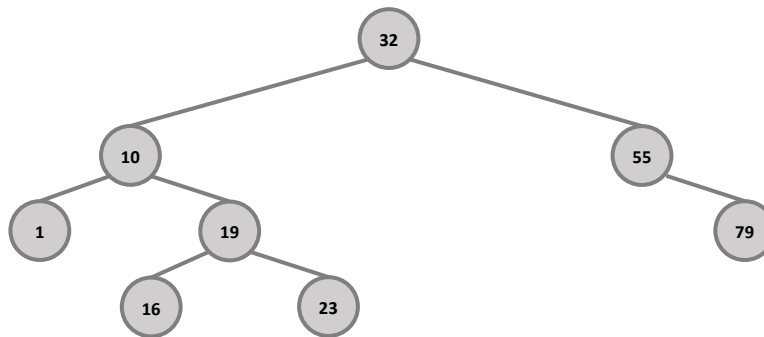
Left subtree → Right subtree → Root node



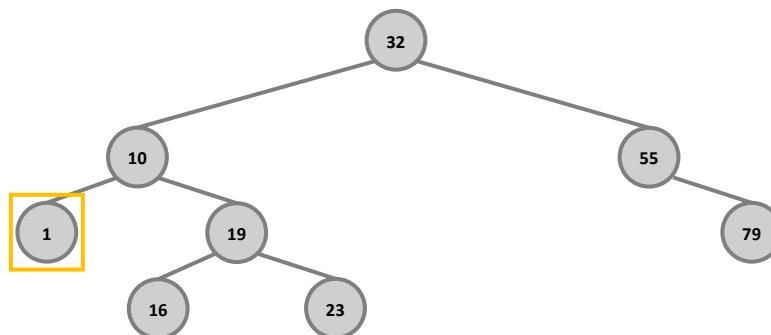
Left subtree → Right subtree → Root node



Left subtree → Root node → Right subtree

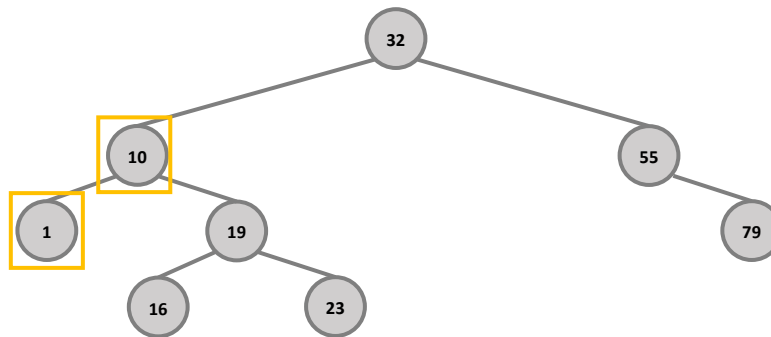


Left subtree → Root node → Right subtree

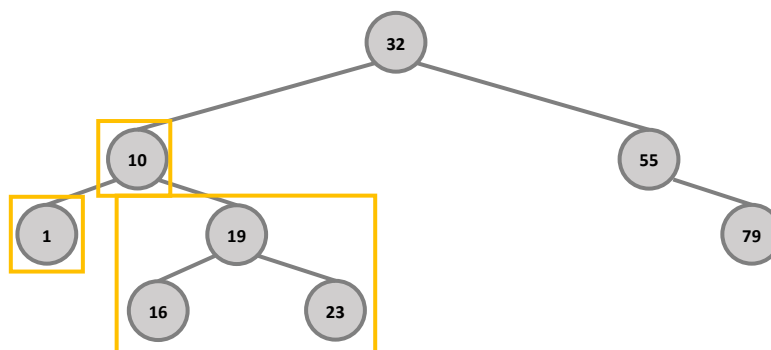




Left subtree → Root node → Right subtree



Left subtree → Root node → Right subtree



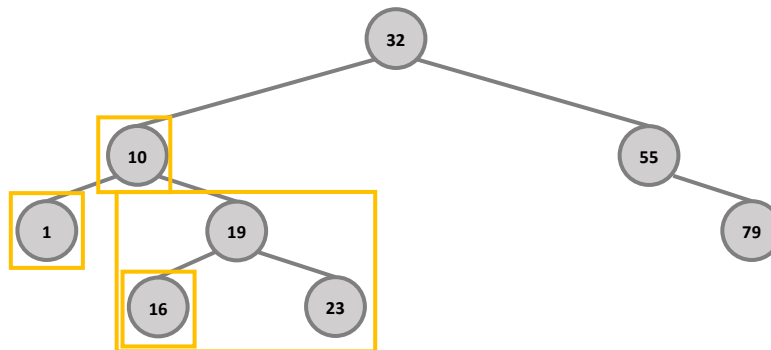
## Binary Search Trees

## Traversal

## In-order

152

Left subtree → Root node → Right subtree



Hasan Baig



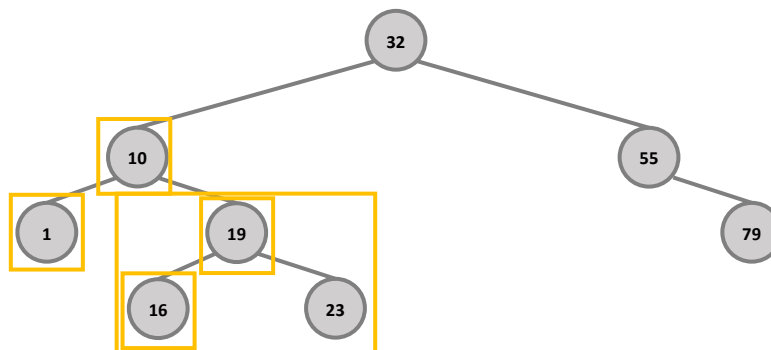
## Binary Search Trees

## Traversal

## In-order

153

Left subtree → Root node → Right subtree



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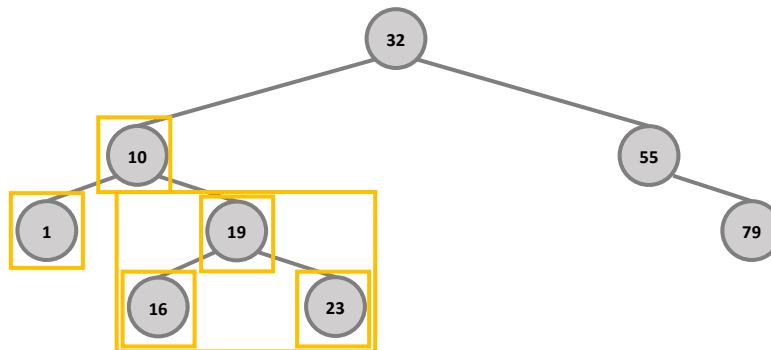


## Binary Search Trees

## Traversal

## In-order

Left subtree → Root node → Right subtree

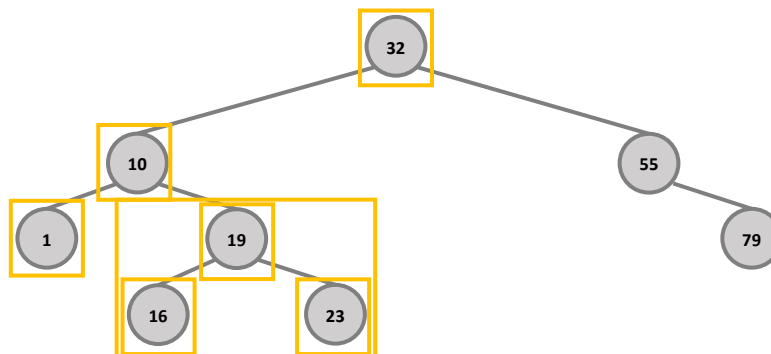


## Binary Search Trees

## Traversal

## In-order

Left subtree → Root node → Right subtree



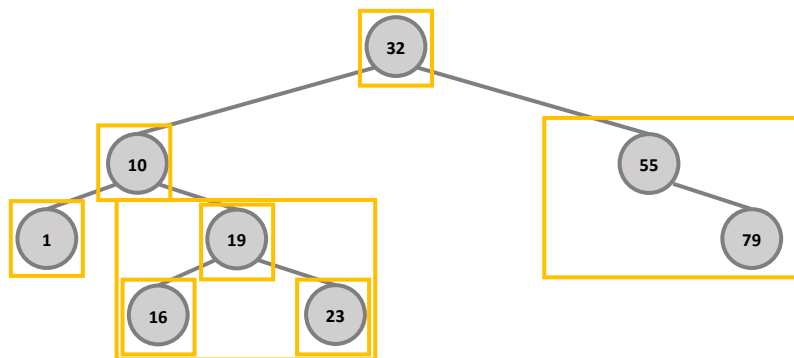
## Binary Search Trees

## Traversal

## In-order

156

Left subtree → Root node → Right subtree



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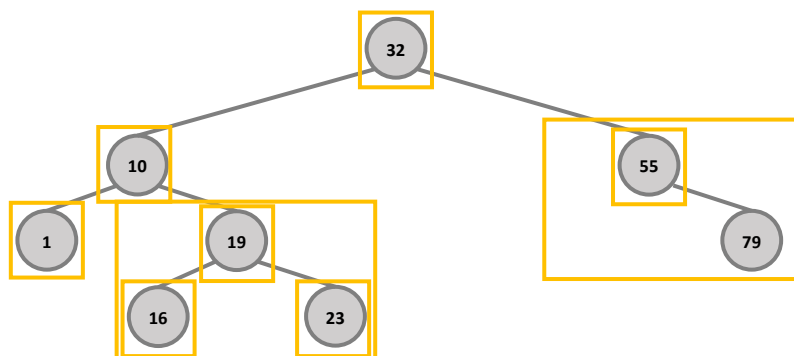
## Binary Search Trees

## Traversal

## In-order

157

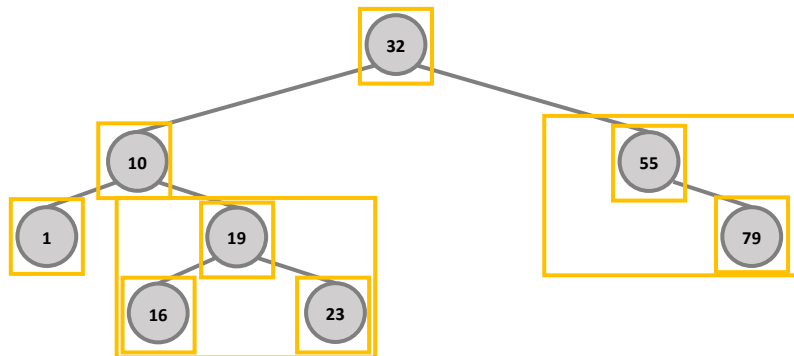
Left subtree → Root node → Right subtree



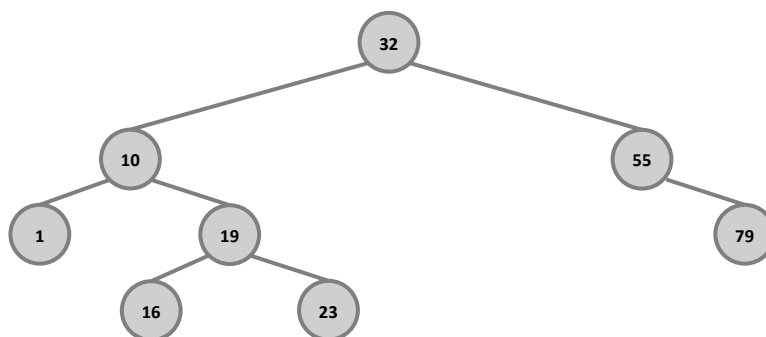
Hasan Baig



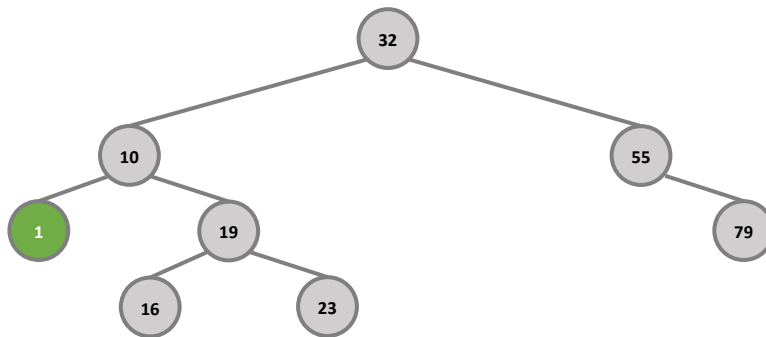
Left subtree → Root node → Right subtree



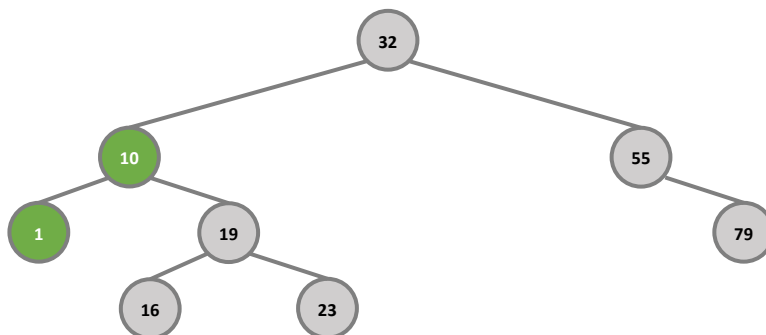
Left subtree → Root node → Right subtree



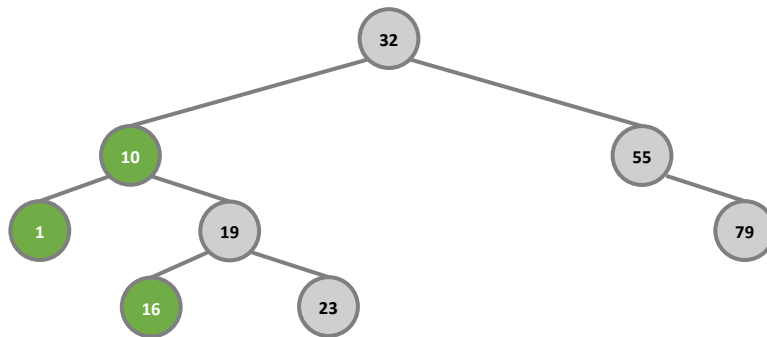
Left subtree → Root node → Right subtree



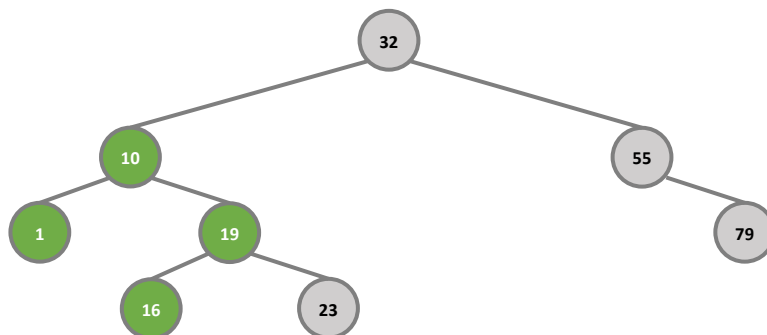
Left subtree → Root node → Right subtree



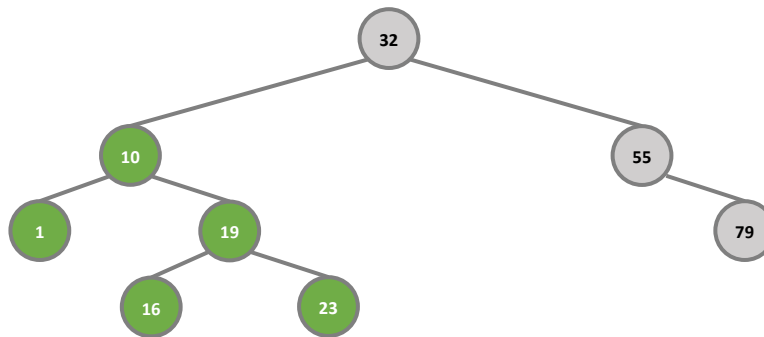
Left subtree → Root node → Right subtree



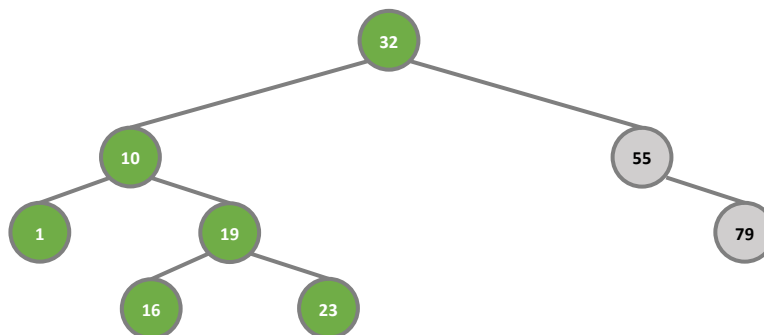
Left subtree → Root node → Right subtree



Left subtree → Root node → Right subtree

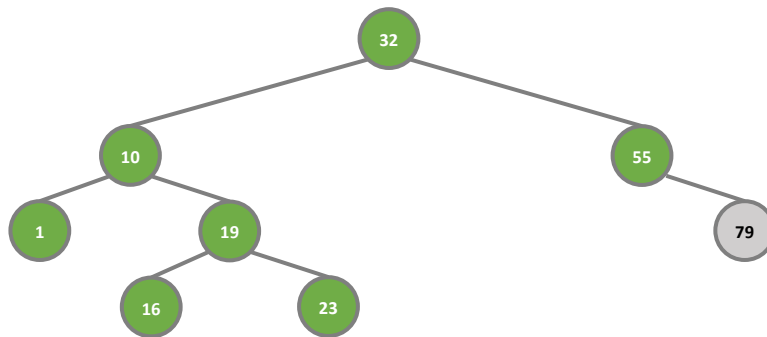


Left subtree → Root node → Right subtree

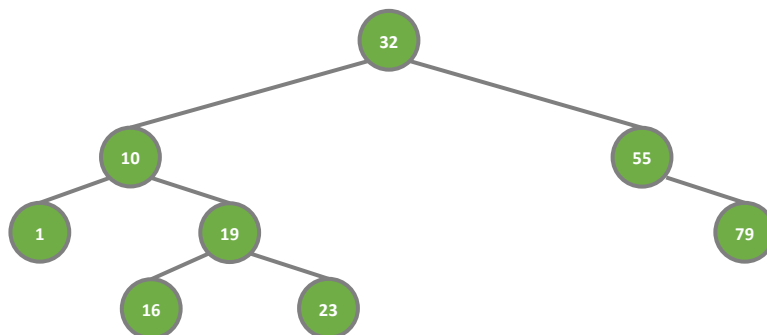




Left subtree → Root node → Right subtree



Left subtree → Root node → Right subtree



Left subtree → Root node → Right subtree



## Binary Search Trees

## Traversal

## In-order

**Pre-order**

- Root node → left subtree → right subtree

32, 10, 1, 19, 16, 23, 55, 79

**Post-order**

- Left subtree → Right subtree → Root node

1, 16, 23, 19, 10, 79, 55, 32

**In-order**

- Left subtree → Root node → Right subtree

1, 10, 16, 19, 23, 32, 55, 79

- Returns elements in sorted order

