CSE 415 Autumn 2019 Assignment 4

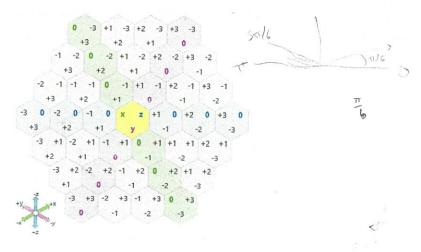
Last name: Gaywood	First name:_	Andrew	udi sanakan sa	
Due Thursday night October may be used on this assignment	and the same and t			ne late day
Do the following three exercises how to do them. Each is we		to take 20-30 min	utes each if	you know
- Branching factor = 1 Efficiency of S	max # of successors d: depth of clo Search Algorith		le bi	branch my factor
Suppose a binary tree-search ever, it could find a goal no				
~			level 0	
10			level l	v.
146 76	A A		level 2	
17 6	र्व हे र्व	à A À	level 3	
1716 22 0000	9999999	99999	level 4	
(a) (3 points) How many refollowing algorithms, to left-to-right order.)	node visitations in the transfind the goal node mark	ree above must be ted G? (Assume cl	e done by e hildren are	each of the handled in
DFS: 22	BFS: 13	IDDFS:	13	
(b) (9 points) Now for a conzations of the worst-cas		g N vertices, give	Big-Theta	characteri-
DFS: Q(N)	BFS: O(N)	IDDFS: 0	(0)	
	o(w) 1		L WOIST	branching factor is
	4,00 O(N)	1		brunching factor is
		(les memol	VI	

(c)	(6 points) Now for a general tree having N vertices, and any branching factor, including 1, or even irregular (varying numbers of children, but obviously always non-negative numbers), give Big-Theta characterizations of the worst-case running times:
	DFS: $\bigcirc(N)$ BFS: $\bigcirc(N)$ IDDFS: $\bigcirc(N^2)$
	(6 points) Using Big-Theta notation again, describe the amount of memory required by each algorithm for the general tree of N vertices.
0(68)	DFS: O(N) BFS: O(N) IDDFS: O(N) - O(N) O(N) (4 points) Suppose we now want to use graph-search versions of these algorithms. What
(e)	is an important benefit of BFS and IDDFS that DFS does not have?
	While DES can find a path to a goal node; it may not necessarily be the shortest path; BES & IDDES find the shortest path.
(f)	(3 points) What impact does a heuristic function have on the run time of the A* algorithm? Assume that the heuristic is admissible and that we don't consider the cost of
	computing the heuristic function itself. A heuristic function improves the runtime of the A* algorithme. If we do not consider the cost of the heuristic function.
	This is because the scenth is more informed & there force explores less irrelevant states
	explores less inclevant states
(g)	(4 points) What does an admissible heuristic do for us in the best and worst cases? (Consider the cost of computing the heuristic function as well as other issues.)
	In the best case, an admissible heuristic decreases the runtime of finding the 3 hortest path to the goal state. The cost of computing h (5) in the best case is less than
	the cost of a search without a neurismis,
	In the worst case the total cost of compiling the hewistic function in addition to finding the shortest path is worse than an aninformed search fluding the shortest path
	every tile, it is worse than UCS byc
	more time spent computing w/ same # of States

2 Heuristic Search

Imagine that you are part of a game-design team creating a game that takes place in a hexagonal grid world. Your job is to evaluate some heuristics proposed to help the monsters of the game do path planning.

The figure below shows a general hexagonal grid in which each cell is identifiable by a triple of coordinates: x (which tells how far it is from the origin on an axis that makes an angle of $\pi/6$ with the horizontal axis), y (which tells how far from the origin it is on an axis that makes an angle of $5\pi/6$ with the horizontal axis), and z (which tells how far down from the origin it is on the vertical axis). Note that there is (intentionally) some redundancy here. In particular, x + y + z = 0.



We define the distance between two adjacent cells as follows:

$$d((x_1, y_1, z_1), (x_2, y_2, z_2)) = |x_1 - x_2| + 2 \cdot |y_1 - y_2| + 4 \cdot |z_1 - z_2|$$

The monsters in the game need to perform path planning for two reasons. One is to escape from fighting with the protagonist. The other is to move towards the protagonist to make an attack. (Although the monsters should not be too intelligent, we will assume that they do need to know what the lowest-cost path is between their starting states and destination states.)

Suppose the operators are the following, in the sequence given. Note that only the state-transformation portion of each operator is shown here, but they all have a precondition that monsters are not allowed to go out of the grid or walk through walls. Also note that the order in which the operators are listed has significance during the various searches.

$$\phi_0: \ x \leftarrow x + 1 \text{ and } y \leftarrow y - 1.$$

$$\phi_1: \ z \leftarrow z + 1 \text{ and } y \leftarrow y - 1.$$

$$\phi_2: \ z \leftarrow z + 1 \text{ and } x \leftarrow x - 1.$$

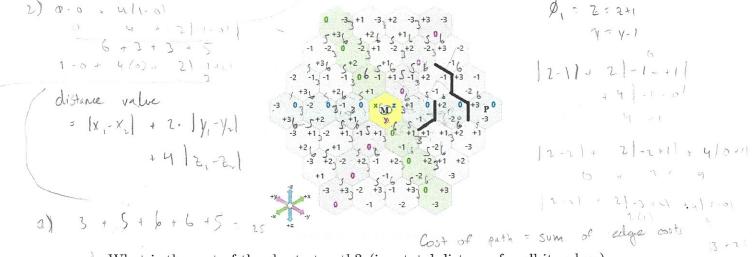
$$\phi_3: \ y \leftarrow y + 1 \text{ and } x \leftarrow x - 1.$$

$$\phi_4: \ y \leftarrow y + 1 \text{ and } z \leftarrow z - 1.$$

$$\phi_5: \ x \leftarrow x + 1 \text{ and } z \leftarrow z - 1.$$

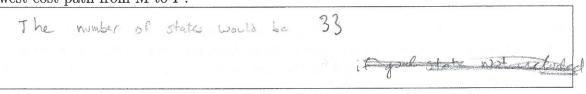
The cost of going from one cell to a neighbor depend on the operator. For example, applying ϕ_3 to state M leads to state (-1, +1, 0), so that the distance value, by the formula above, is 3. The cost of a path is, as usual, the sum of its edge costs.

(a) (6 points) Consider the problem of finding a lowest-cost path from M to P in the example game situation below. The thick black walls in the diagram represent barriers through which the monsters must not pass. (Therefore, the precondition for operator ϕ_0 is not satisfied at state (+1, -1, 0), and neither is the precondition for operator ϕ_1 , so that this state has only 4 successors.)



What is the cost of the shortest path? (i.e., total distance for all its edges)

(b) (6 points) What is the number of states that would be expanded by UCS to find a lowest-cost path from M to P?



17

5-13+2+1 11 7/5+, - 0+4+2 - 5 5 - 1 21 541 (c) (4 points) Consider the heuristic $h_x((x,y,z)) = \min(|x-x_g|,|y-y_g|,|z-z_g|)$, where (x_g, y_g, z_g) refer to the coordinates of the goal cell. Determine whether or not h_x is admissible and explain why it is or why it is not. is admissible: it Overestimate the actual distance; in the wast composents
stending the heriostic gives the actual distance.
No overestimation because the actual distances by k of components (d) (6 points) Determine how many states would be expanded by A^* using h_x to find a shortest path from M to P. number of states expanded would be (e) (5 points) Explain how the use of the heuristic is affecting the search (compared with Rather than servin beliebly, the hearth informs the algorithm whether it is gretting closer to or further from the god (f) (5 points) Propose another heuristic that you believe will outperform h_x . (Do not propose the exact distance defined above or function that includes it.) Give a formula to Define hemsylve define your function. Also give an argument for or against its admissibility. Why do you -> certain ages of believe it will outperform h_x ? hally, y, z) - max (1x-xg), 1y-yg), 1z-zg)) + barrier_condition)

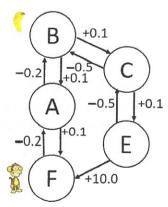
1 think this is admissable; it never overestimates the distance because of the way the distance is calculated. If the max is ox = 4; the goal is at least cost 4 away; if the max is oy = 3; blue goal is at least cost 4 away; it the max is oy = 3; blue goal is at least cost 4 away; etc.

Decare it gives a larger heristic value and is still admissable it outperforms by. tile. burnier noifibres let 5: # of adjacent barriers in directional hemisphere of gonli (g) (3 points) How many states will be expanded by A* using your heuristic to find a shortest path from M to P? barrier condition 19 States are expanded burrier-condition 421 M 8, 9= [7,8,8,9,9,10,] A 9, 3, 3, 2,9,9,10,3 7 M 8

hex)- mux + barrer cons JH 1 162 19 + gal

3 Markov Decision Processes

Consider a situation in which a robot monkey is in a room in which some bananas are hanging from the ceiling. The monkey can move its left arm to any one of 3 different places, and it might be holding or not holding bananas in either of two states. The monkey starts out not holding bananas with left hand low (state F). It can try to raise its hand, and so it can transition to state A. However, this monkey has a somewhat unreliable body, and most actions are only effective with probability 0.7. (Then, with probability 0.3, the arm goes a different way. But there is 0 probability of staying in the same state.) The action of raising the hand from state F, however, is the one completely reliable and deterministic action, so the next state after that action is guaranteed to be state A. If the monkey again tries to raise his hand from state A, there is a 0.7 probability of arriving in state B, which is roughly where the bananas are. There is a probability of 0.3 that the action will cause the monkeys hand to move back down to state F. From state B, the monkey has a choice of action: (G) grab the bananas and go down to state C, or (D) leave the bananas and go down to state A. (These again are nondeterministic, so action G in state B goes to C with probability 0.7 and to state A with probability 0.3; action D in state B goes to A with probability 0.7 and to C with probability 0.3.) From state C, the monkey can go to state E or back up to state B. From state E, the monkey can finally get the bananas all the way down and consume them, for a reward of +10. Note that the other rewards are either effort-consuming (raising the hand or raising it and the bananas for rewards of -0.2 or -0.5) or somewhat easier, lowering the hand (for rewards 0f 0.1).



(a) (10 points) Create a table representing the function T(s, a, s') for this MDP. Assume that there are three possible actions: U, D and G. U means try to go up, and D means try to go down. G means try to grab the bananas (and go down from B to C). Action U is applicable only at states A, C, E, and F. Action D is applicable only at states A, B, C, and E. Action G is only applicable at state B. In this table you do not have to provide an explicit entry for any T(s, a, s') whose value is 0. Hint: there should be 17 entries in your table.

w fan TLS €5 T (5, a, s') 5 EA 5 6 u 1.0 A U 0,7 U 1) F B B D 0 B 9 3 6 0,3 u 4 E 1) E 0,7 3 0 0,3 1 U 0,7 U F 1) E F 0,7 E 0 6 0.3

(b) (5 points) Create a table representing the function R(s, a, s'). There should be one explicit entry here for each explicit entry you gave in part (a).

January Lion	TOT OCCUPATIONS	7 7 4 6	are m pare (a).	
SES	$\alpha \in A$	5'65	(R(5, a 5')	
F	u'	A	-0,1	
A	The second section of the sect	I B	-012	
A	u	F	401	
A	D	F	40.1	
A	D	B	-0.2	
3	D -	A	40-1	
8	D	-	+0.1	A CONTRACTOR OF THE CONTRACTOR
3	(7	-	10,1	
B	Lon	A	10.1	
L	V	3	-0,5	The same of the sa
hard	1	¥	+0-1	
L	5	t t	+0,1	
<u></u>	T.	T _k	-0.5	
£	4	6	-015	
£	W.	f.	+ 10.0	
£	1)	r	410.0	
6	0	r-	-0,5	

(c) (10 points) Create a table representing the expected reward for taking action a in state s. Call this function $Q_1(s, a)$. Note: if action a is not allowed in state s then $S_1(s, a) = 0$. The expected reward is the *expectation* of the reward from state s given that the action

Q, (s, a)

is s. Because of the nondeterminism in the actions, this is normally a weighted sum of the possible rewards out of s, and the weight corresponding to action a is usually the

largest of the weights. Hint: there should be 9 entries in your table

5 65	aEA	Expected weight	Expected	remore	
F	w	-60	mg 0, 2		
A	W	-0,2	-0.11		
A	(m)	toit	+0.01		
B		10,1	+0.1		
)	D	+0.1	+ 0,1		
	V T	-0.5	-0.32		
	0	1011	- 9.08		
E	u D	C-015	+2,65		
10 may 1 may	V	7-10,0	16.85		
	Standon and the standard stand	C. S.			

(d) (5 points) What is the total reward corresponding to the following episode, where the monkey starts in state A and makes the transitions below?

$$A-D-F-U-A-U-B-D-A-U-B-G-C-D-B-G-C-D-E-D-C-D-E-D-F-U-A$$

(Add up all the actual rewards here; do not use expected rewards.)

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