

Lecture 11 Cache 2 Exercises

Q1:

Assume:

- A processor has a 64KB 2-way set associative cache
- The cache access uses physical addresses only
- A physical address is 48 bits long
- Each block holds 64 bytes of data
- Tag overhead includes the valid bit and tag bits

How much is the tag overhead in percent?

Solution:

The total number of cache blocks = $64\text{KB} / 64\text{B} = 1024$

Because 2-way set associative, the index bits in the address only need to identify each of the 512 ($=1024 / 2$) cache sets

Number of bits in index = $\log_2(1024 / 2) = 9$

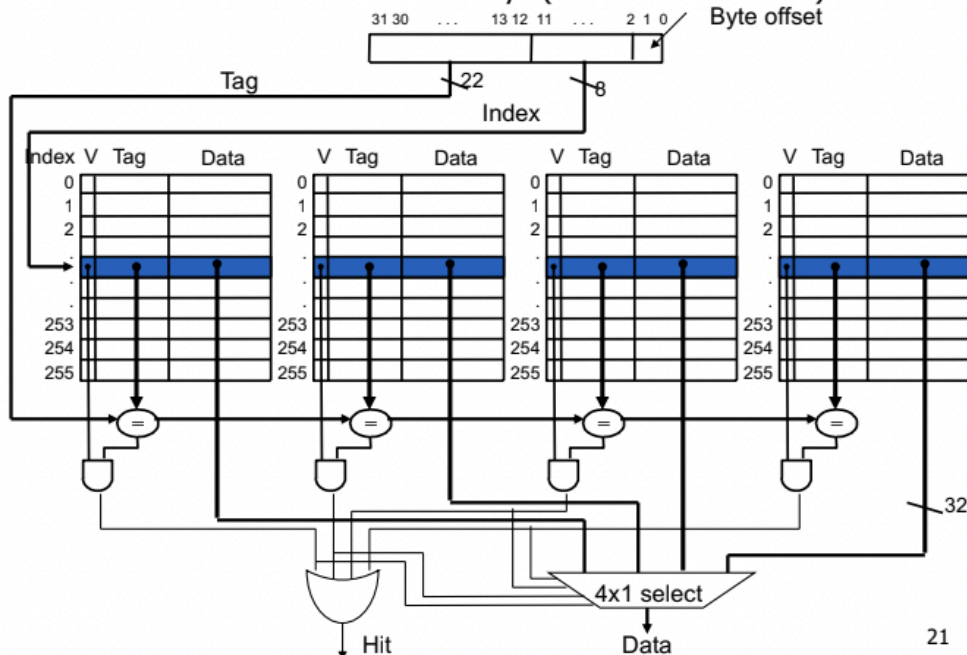
Number of bits in byte offset = $\log_2(64) = 6$

Number of bits in tag = $48 - 9 - 6 = 33$

Each cache block has a tag and a valid bit, i.e., with a 2-way set associative cache, each cache set has two tags and valid bits for each way, respectively

Example: 4-Way Set Associative Cache

- $2^8 = 256$ sets each with four ways (each with one block)



Therefore, tag overhead = $(33+1)/8/(64) * 100\% = 6.6\%$

Q2:

DAXPY is an acronym for a common double precision scientific loop of the form: $Y[i] = A \cdot X[i] + Y[i]$ where X and Y are arrays. Assume that X and Y are both 64 MB and our total cache capacity is 512 MB, and each array is stored sequentially in memory. We run the following loop:

```
extern double *X;
extern double *Y;
start_time = current_time();
for (outer = 0; outer < 100000; outer++){
    for (i=0; i< 8 * 1024 * 1024; i++){
        Y[i] = A*X[i] + Y[i];
    }
}
end_time = current_time();
duration = end_time - start_time;
```

When we analyze the performance counters, we find we are taking many last-level cache (LLC) misses. What can be done to the design to minimize the execution time of this code?

- A. Increase the associativity of the LLC
- B. Decrease the LLC line size
- C. Decrease the associativity of the LLC
- D. None of the above

Answer: A

Cache capacity $512\text{MB} > 64\text{MB} + 64\text{MB}$, so it is not capacity miss \rightarrow many misses can be conflict misses

So, increasing the associativity can help