

Lecture 2 Performance Exercises

Q1:

Short answers

(a) If a given program runs on a processor with a higher clock frequency, does it imply that the processor always executes more instructions per second (compared to a processor with a lower clock frequency)? Why?

(b) If a processor executes more of a given program's instructions per second, does it imply that the processor always finishes the program faster (compared to running a program that executes fewer instructions per second)? Why?

Solution:

(a) No. Instructions per second is also impacted by program, compiler, ISA.

(b) No. Instruction count can be different.

Q2:

Assume a program has the following instruction type breakdown:

40% memory, latency is 4 cycles

50% adds, latency is 2 cycles

10% multiplies, latency is 18 cycles

If you could pick one type of instructions to make twice as fast (half of latency) in the next-generation of this processor, which instruction type would you pick? What is the speedup?

Solution 1:

Base CPI: $40\% \cdot 4 + 50\% \cdot 2 + 10\% \cdot 18 = 4.4$

Pick one type of instructions to make twice as fast (half of latency):

Make memory instructions 2x faster: New CPI = $40\% \cdot 2 + 50\% \cdot 2 + 10\% \cdot 18 = 3.6$

Make add instructions 2x faster: New CPI = $40\% \cdot 4 + 50\% \cdot 1 + 10\% \cdot 18 = 3.9$

Make multiplies 2x faster: New CPI = $40\% \cdot 4 + 50\% \cdot 2 + 10\% \cdot 9 = 3.5$

Therefore, I will pick to optimize multiply instructions.

Speedup = Base CPI / New CPI = $4.4 / 3.5 = 1.257$

Solution 2:

Calculate Base CPI: Assume a program has a total of 100 instructions, then

40 are memory instructions, will take $40 \cdot 4 = 160$ cycles

50 are adds, will take a total of $50 \cdot 2 = 100$ cycles

10 are multiplies, will take $10 \cdot 18 = 180$ cycles

The total number of cycles to run the program with 100 instructions = $160 + 100 + 180 = 440$ cycles

So Base CPI = $440 / 100 = 4.4$

Pick one type of instructions to make twice as fast (half of latency):

Make memory instructions 2x faster: New total cycles = $40*2 + 50*2 + 10*18 = 360$,

So New CPI = $360 / 100 = 3.6$

You may calculate New CPIs with other optimizations in the same way...and get the same results as solution 1.

Solution 3:

You may calculate IPC instead of CPI, and should reach the same conclusion.

Q3:

Assume a typical program has the following instruction type breakdown:

30% loads, latency is 4 cycles

10% stores, latency is 4 cycles

50% adds, latency is 2 cycles

8% multiplies, latency is 16 cycles

2% divides, latency is 50 cycles

If you could pick one type of instruction to make twice as fast (half the latency) in the next-generation of this processor, which instruction type would you pick? Why?

Solution:

The same as Q2, you may pick either one of the methods to solve the problem. In the following, I show one of the solutions.

Base CPI = ?

Pick one type of instructions to make twice as fast (half of latency):

Make loads 2x faster: New CPI = ?

Make stores 2x faster: New CPI = ?

Make adds 2x faster: New CPI = ?

Make multiplies 2x faster: New CPI = ?

Make divides 2x faster: New CPI = ?

	Base	loads	stores	adds	mults	divs
Loads 30%*4	1.2	0.6	1.2	1.2	1.2	1.2

Stores 10%*4	0.4	0.4	0.2	0.4	0.4	0.4
Adds 50%*2	1.0	1.0	1.0	0.5	1.0	1.0
Mults 8%*16	1.28	1.28	1.28	1.28	0.64	1.28
Divs 2%*50	1.0	1.0	1.0	1.0	1.0	0.5
CPI	4.88	4.28	4.68	4.38	4.24	4.38

Therefore, I would pick the multiplies to make twice as fast, because it reduces the CPI the most,

by 15% over the Base case, because

$$\text{Speedup} = \text{Base CPI} / \text{New CPI} = 4.88 / 4.24 = 1.15$$