

ECE 65: Components & Circuits Lab

Lecture 10

Bipolar Junction Transistor (BJT)

Introduction

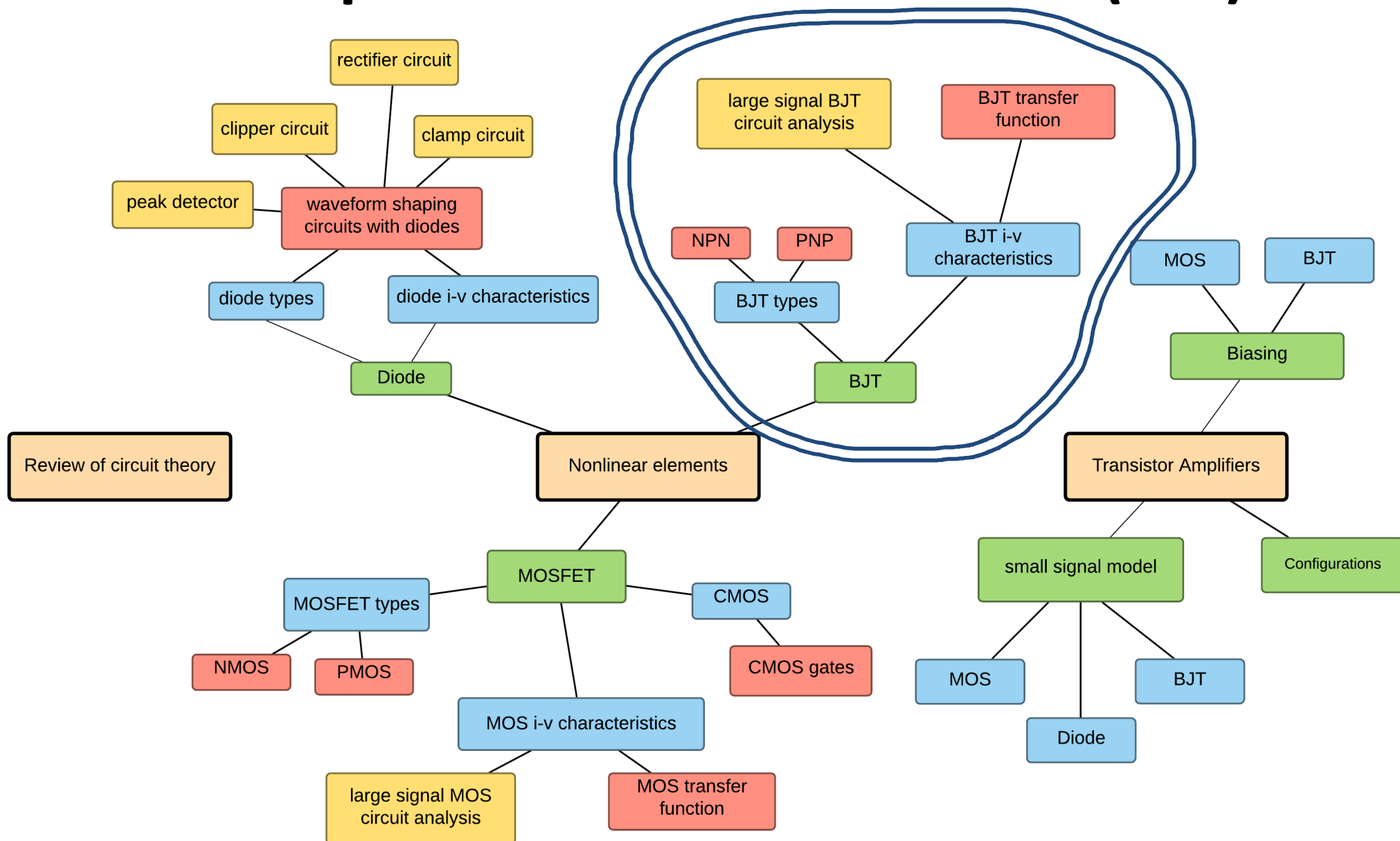
Reference notes: section 3.1

Sedra & Smith (7th Ed): sections 6.1,6.2

Saharnaz Baghdadchi

Course map

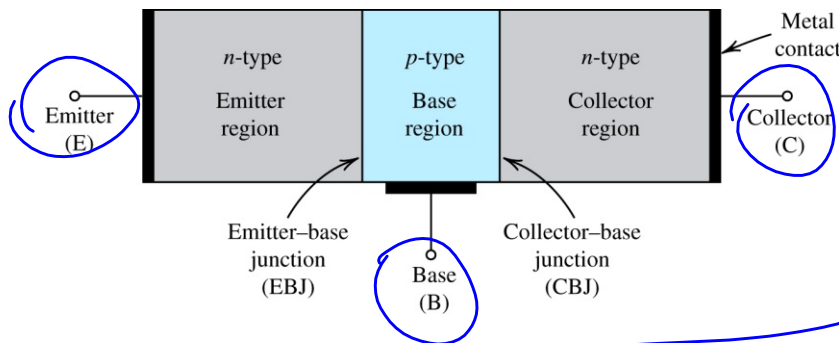
3. Bipolar Junction Transistor (BJT)



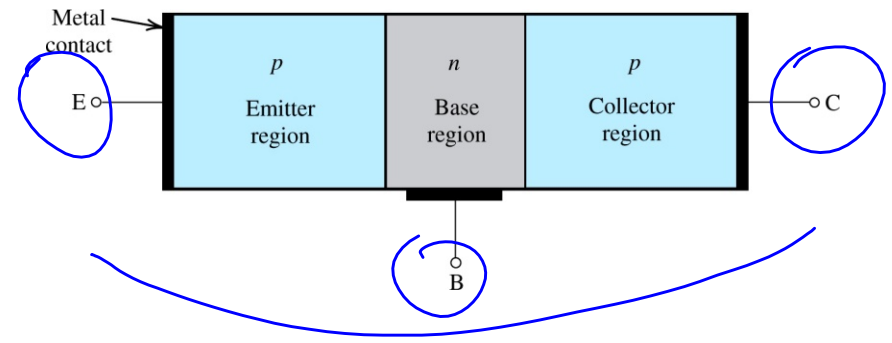
A BJT consists of three regions

Simplified physical structure

NPN transistor



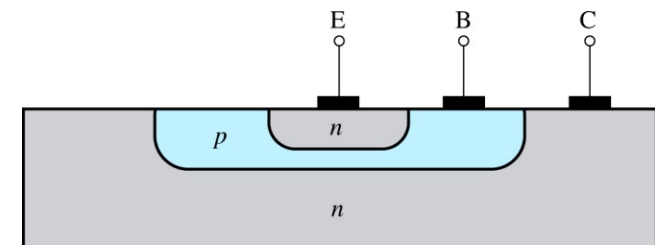
PNP transistor



Device construction is NOT symmetric

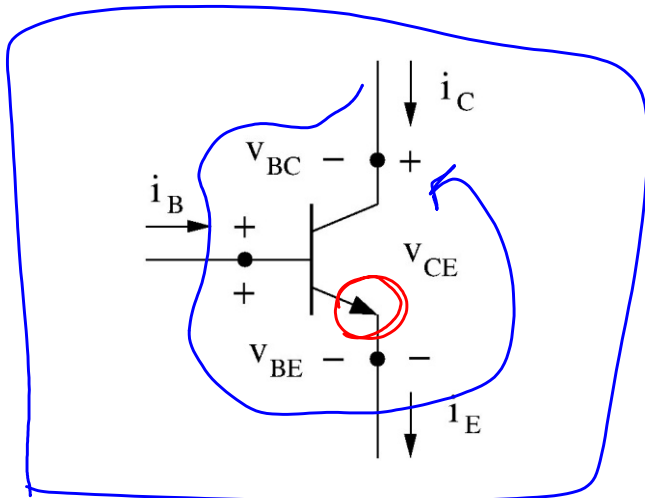
- “Thin” base region (between E & C)
- Heavily doped emitter
- Large area collector

An implementation on an IC (NPN)



NPN BJT $i v$ parameters

NPN transistor



**Circuit symbol and
Convention for current directions**

$$\text{KCL: } i_E = i_C + i_B$$

$$\text{KVL: } v_{BC} = v_{BE} - v_{CE}$$

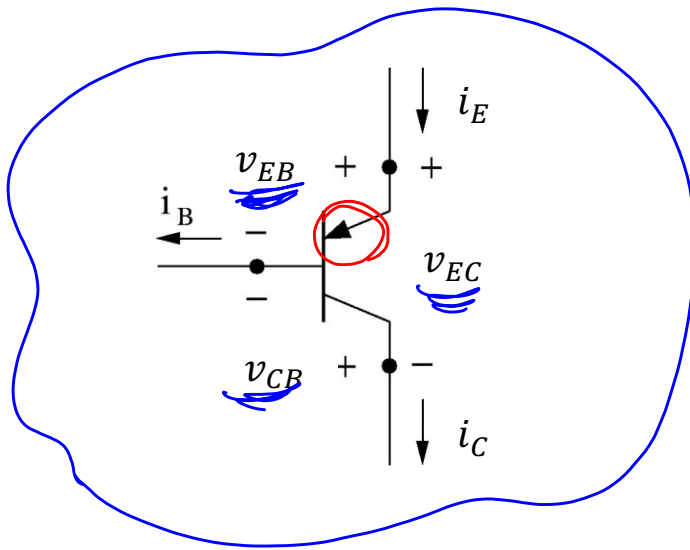
Note:

$$v_{CE} = v_C - v_E$$

BJT $i v$ characteristics is the relationship among (i_B , i_C , v_{BE} , and v_{CE})

PNP BJT iv parameters

PNP transistor



$$\text{KCL: } i_E = i_C + i_B$$

$$\text{KVL: } v_{CB} = \underline{v_{EB}} - v_{EC}$$

Note:

$$\underline{v_{EC} = v_E - v_C}$$

Compared to a NPN:

- 1) Current directions are reversed
- 2) Voltage subscripts switched

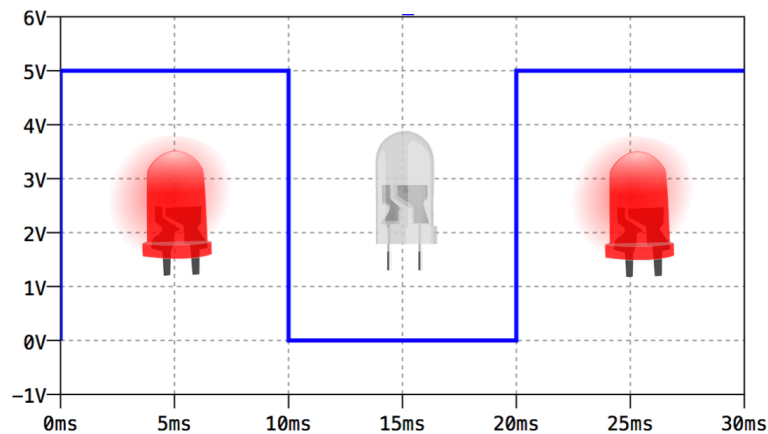
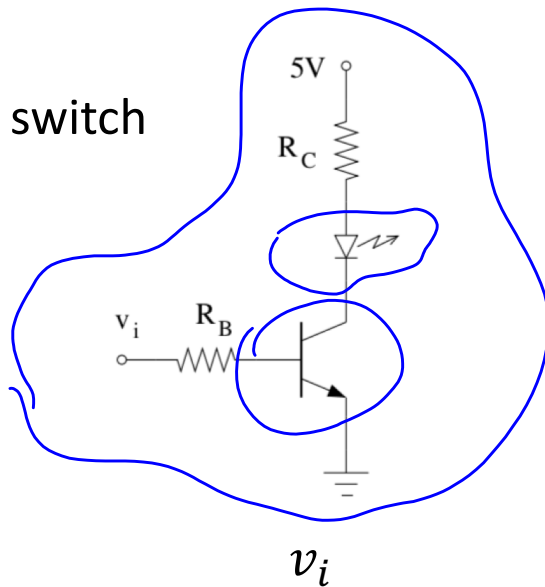
BJT modes of operation and applications

Cut-off

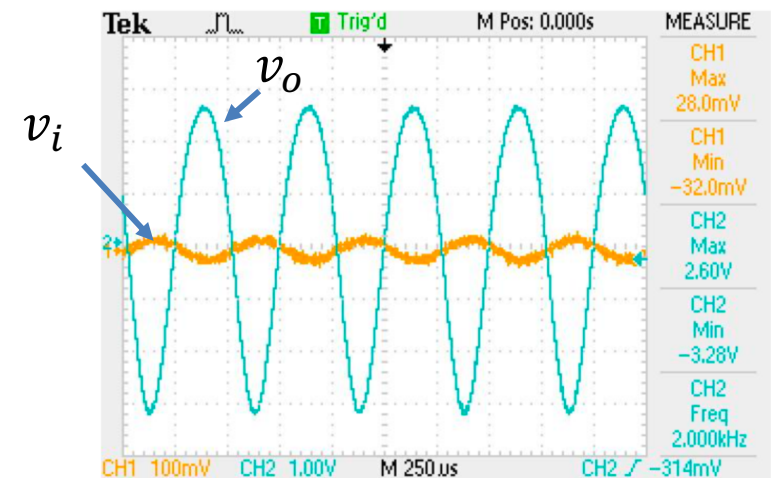
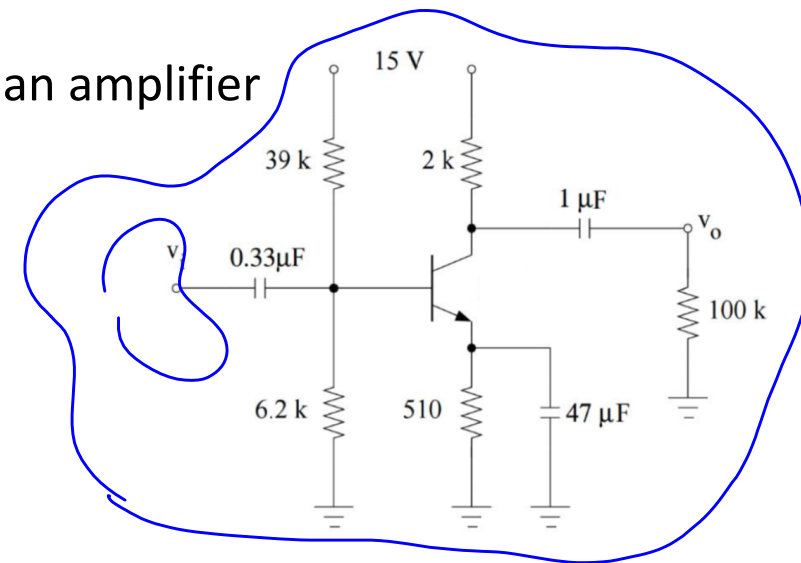
Saturation

Active

BJT as a switch

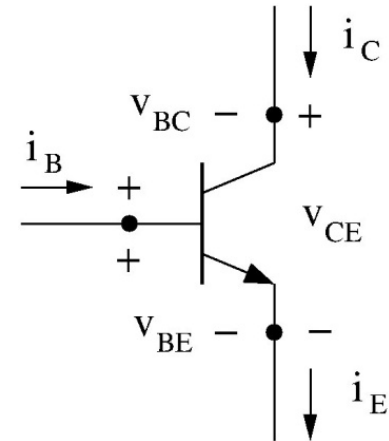


BJT as an amplifier



BJT operation in the cut-off mode

Operation of a BJT requires the presence of emitter-generated electrons near the BC junction (thus, the BE junction should be forward biased).



A BJT is called to be in “cut-off” if the BE junction is NOT forward biased.

In this case, $i_B = 0$ and $i_C = 0$ regardless of any voltage applied to the BC junction.

Cut-off mode:

$$i_B = 0$$

$$i_C = 0$$

$$i_E = 0$$

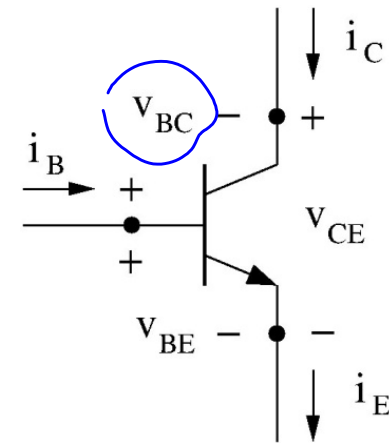
BJT operation in the active mode

BE junction is forward biased: $v_{BE} = V_{D0}$

BC junction is reverse biased: $v_{BC} \leq 0$

Since $v_{BC} = v_{BE} - v_{CE} \rightarrow$

$$v_{CE} \geq V_{D0}$$



A BJT operates in active mode when $v_{CE} \geq V_{D0}$ and $v_{BE} = V_{D0}$

Active mode:

$$i_B \geq 0$$

$$v_{BE} = V_{D0}$$

$$i_C = \beta i_B$$

$$v_{CE} \geq V_{D0}$$

for NPN: $v_{EB} = V_{D0}$

for PNP
 $\rightarrow v_{EC} \geq V_{D0}$

BJT operation in the saturation mode

BE junction is forward biased: $v_{BE} = V_{D0}$

In **soft saturation**:

BC junction is forward biased and $0 < v_{BC} \leq 0.4 \text{ V}$ (for Si)

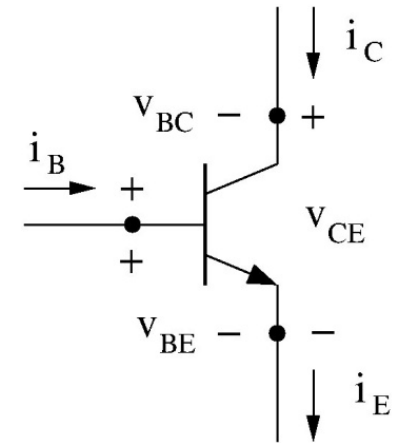
$$\text{Since } v_{BC} = v_{BE} - v_{CE} \rightarrow 0.3 \text{ V} \leq v_{CE} < 0.7 \text{ V}$$

In **deep saturation**:

BC junction is forward biased and $v_{BC} > 0.4 \text{ V}$ (for Si)

$$\text{Since } v_{BC} = v_{BE} - v_{CE} \rightarrow 0.1 \text{ V} < v_{CE} < 0.3 \text{ V}$$

We will use $v_{CE} \approx 0.2 \text{ V} = V_{sat}$ for Si



Deep saturation or saturation mode:

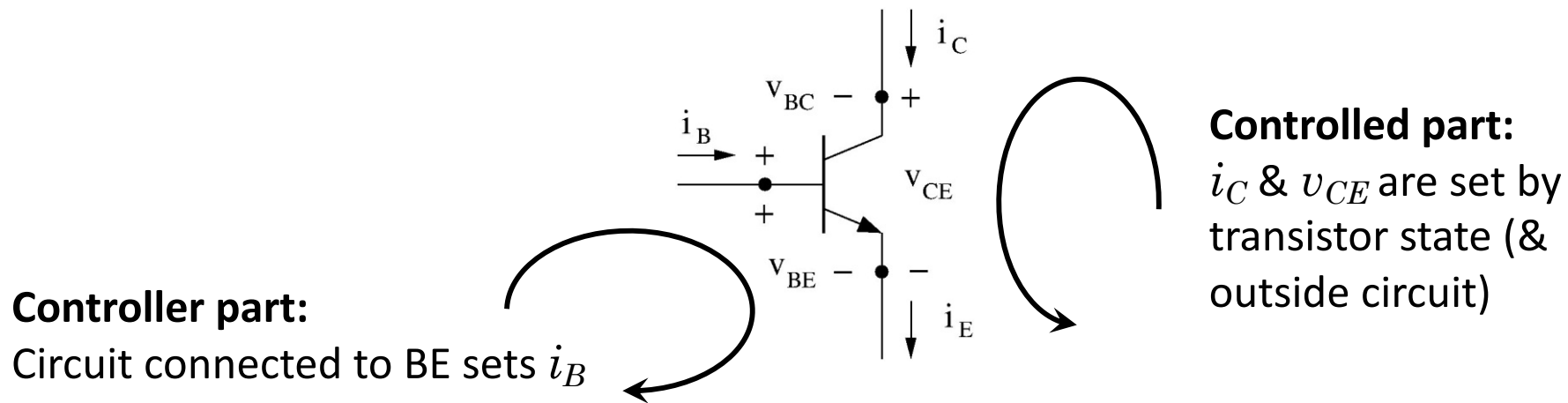
$$i_B \geq 0$$

$$v_{BE} = V_{D0}$$

$$i_C < \beta i_B$$

$$v_{CE} = V_{sat}$$

Transistor operates like a valve:



Controller part:

Circuit connected to BE sets i_B

Controlled part:

i_C & V_{CE} are set by transistor state (& outside circuit)

Cut-off ($i_B = 0$):

Valve Closed

$$i_C = 0$$

Active ($i_B > 0$):

Valve partially open

$$i_C = \beta i_B$$

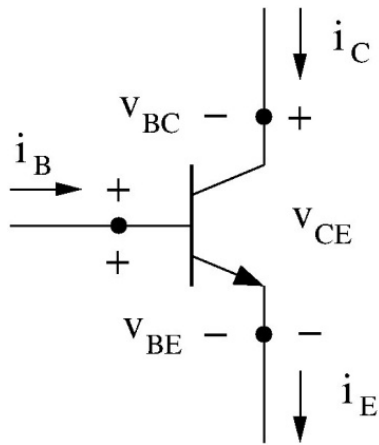
Saturation ($i_B > 0$):

Valve open

$$i_C < \beta i_B$$

i_C is limited by circuit connected to CE terminals, increasing i_B does not increase i_C

NPN BJT $i v$ equations



Cut-off :
BE is reverse biased

“Linear” model*

$$i_B = 0, \quad i_C = 0$$

$$v_{BE} < V_{D0}$$

Active:
BE is forward biased
BC is reverse biased

$$v_{BE} = V_{D0}, \quad i_B \geq 0$$

$$i_C = \beta i_B, \quad v_{CE} \geq V_{D0}$$

(Deep) Saturation:
BE is forward biased
BC is forward biased

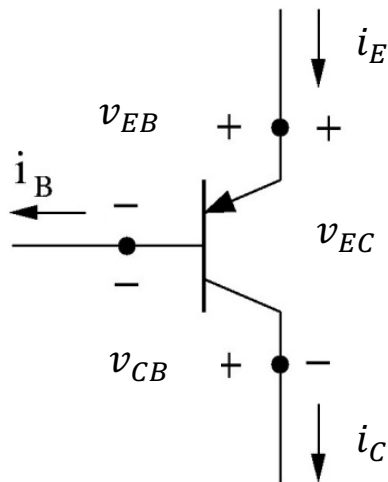
$$v_{BE} = V_{D0}, \quad i_B \geq 0$$

$$v_{CE} = V_{sat}, \quad i_C < \beta i_B$$

For Si, $V_{D0} = 0.7 \text{ V}$, $V_{sat} = 0.2 \text{ V}$

BJT Linear model is based on a diode “constant-voltage drop” model for the BE junction and ignores Early effect.

PNP BJT $i v$ equations



“Linear” model

Cut-off :
EB is reverse biased

$$i_B = 0, \quad i_C = 0$$

$$v_{EB} < V_{D0}$$

Active:
EB is forward biased
CB is reverse biased

$$v_{EB} = V_{D0}, \quad i_B \geq 0$$

$$i_C = \beta i_B, \quad v_{EC} \geq V_{D0}$$

(Deep) Saturation:
EB is forward biased
CB is forward biased

$$v_{EB} = V_{D0}, \quad i_B \geq 0$$

$$v_{EC} = V_{sat}, \quad i_C < \beta i_B$$

$$\text{For Si, } V_{D0} = 0.7 \text{ V, } V_{sat} = 0.2 \text{ V}$$

BJT Linear model is based on a diode “constant-voltage drop” model for the BE junction and ignores Early effect.

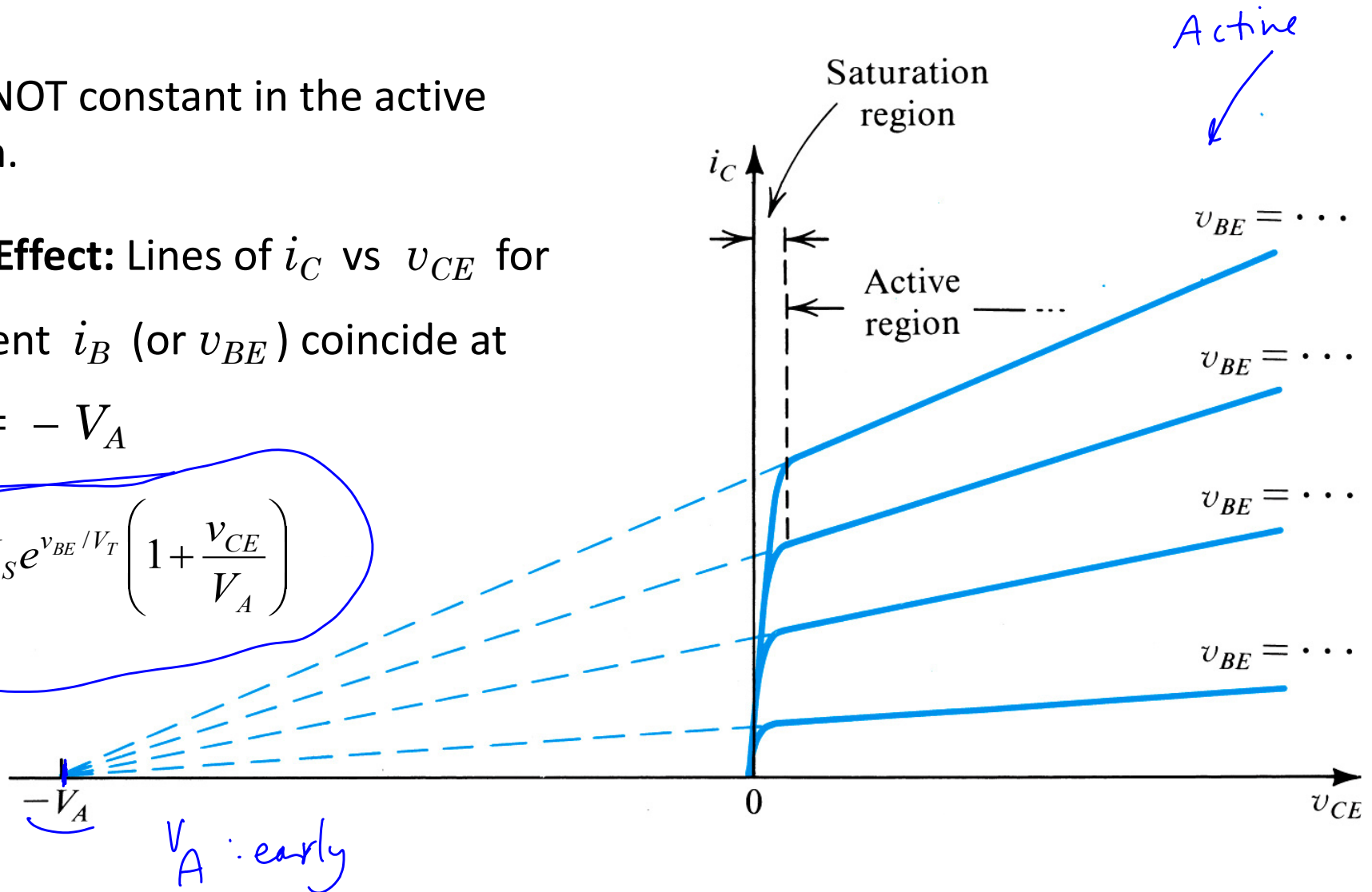
Early Effect modifies i_C characteristics in the active mode

i_C is NOT constant in the active region.

Early Effect: Lines of i_C vs v_{CE} for different i_B (or v_{BE}) coincide at

$$v_{CE} = -V_A$$

$$i_C = I_S e^{v_{BE}/V_T} \left(1 + \frac{v_{CE}}{V_A} \right)$$



Solving BJT circuits

(State of BJT is unknown before solving the circuit)

Assume BJT is in cut-off mode:

$$V_{D_0} = 0.7V, \beta = 100$$

$$i_B = 0, V_{BE} < V_{D_0}$$

$$\text{KVL: } 4V = 40k \times i_B + V_{BE}, i_B = 0, V_{BE} = 4V > 0.7V$$

Assumption was not correct. BJT is ON.

Assume BJT is in active mode.

$$i_C = \beta i_B, V_{CE} \geq V_{D_0}$$

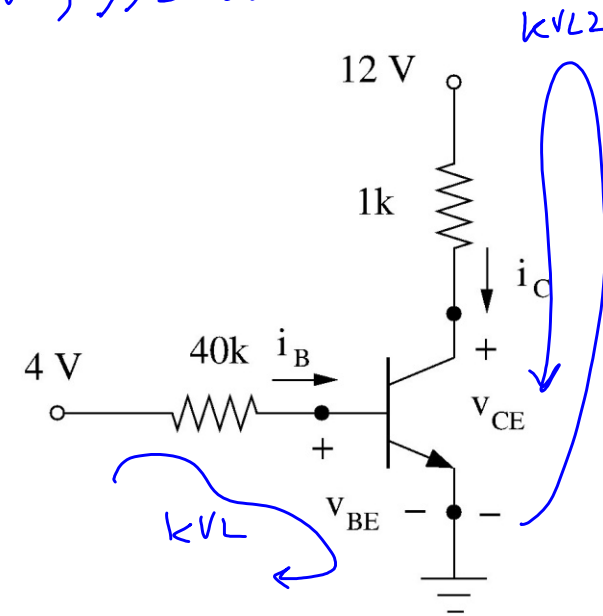
$$i_B = \frac{4V - 0.7}{40k} = 82.5 \mu A$$

$$i_C = 100 \times i_B = 8.25 \text{ mA}$$

KVL 2

$$12 = 1k \times i_C + V_{CE}, \quad 12 = 1k \times 8.25 \text{ mA} + V_{CE} \rightarrow V_{CE} = 3.75V > V_{D_0}$$

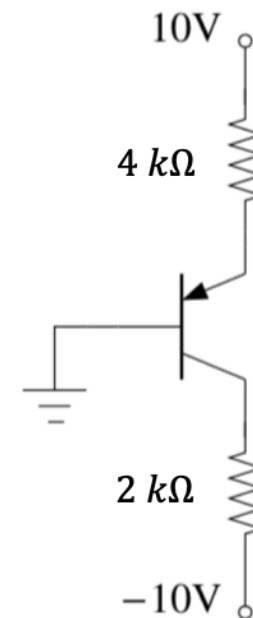
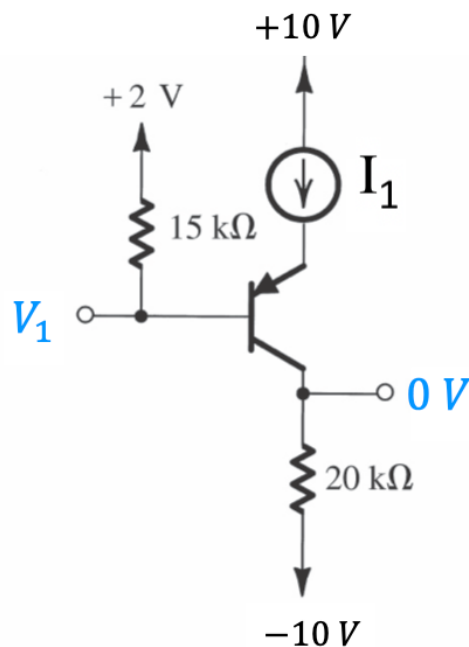
Assumption was correct and transistor operates in active mode



Note:

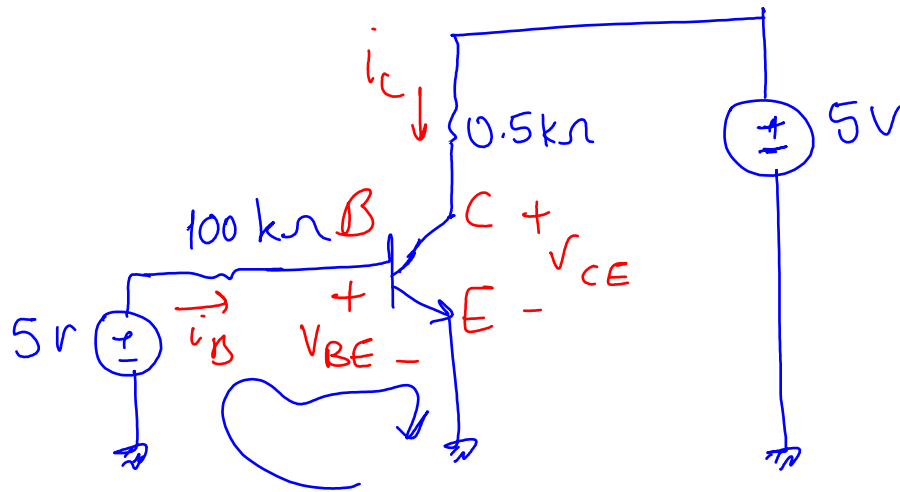
In the BJT and MOSFET circuits, to differentiate the applied node voltages from the measured node voltages:

We will show the measured node voltages in **blue color** and the DC or AC voltage sources connected to different nodes in **black color**.

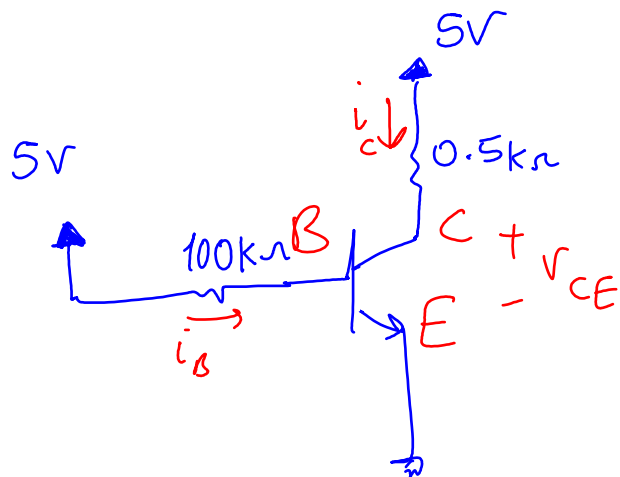
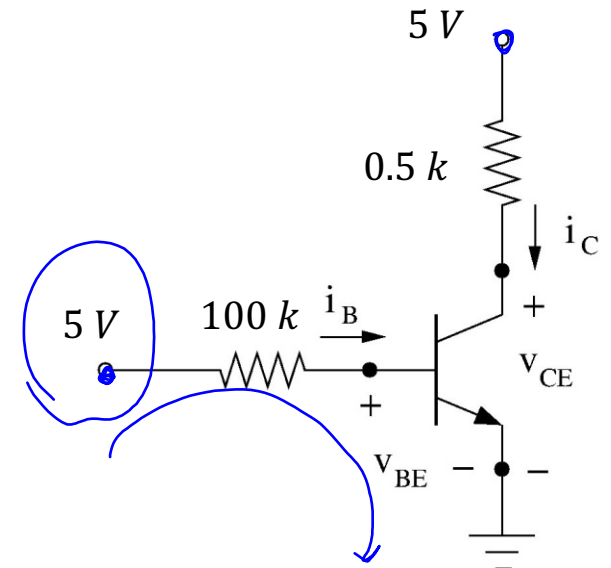


Lecture 10 reading quiz

Find the transistor parameters in this BJT circuit. ($\beta = 100$, $V_{D0} = 0.7V$).



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Lecture 10 reading quiz

Find the transistor parameters in this BJT circuit. ($\beta = 100$, $V_{D0} = 0.7V$).

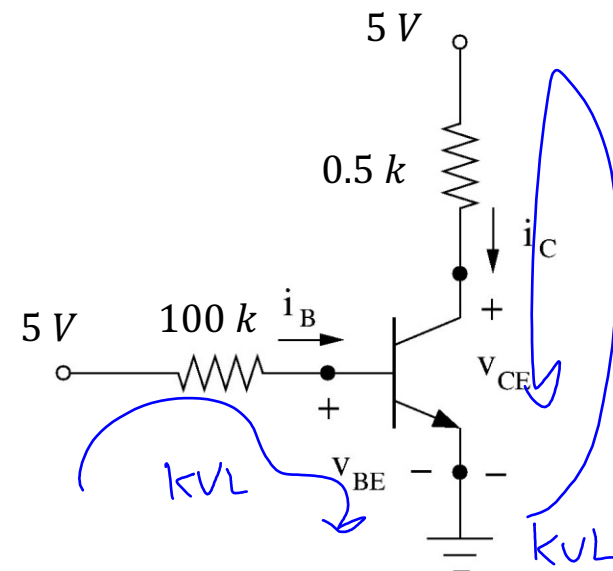
Assume BJT is in cut-off

$$i_B = 0, V_{BE} < 0.7V$$

$$\text{BE - KVL: } 5V = 100k\Omega \times i_B + V_{BE}$$

$$5V = 0 + V_{BE} \rightarrow V_{BE} = 5V > 0.7V$$

\Rightarrow assumption was wrong.



Assuming BJT is in active mode: $i_C = \beta i_B$, $V_{CE} \geq V_{D0}$.

$$\text{CE KVL: } 5 = 0.5k\Omega \times i_C + V_{CE}, \quad i_C = \beta i_B, \quad i_B = \frac{5V - 0.7V}{100k\Omega}$$

$$i_B = 43 \mu A$$

$$V_{CE} = 2.85V > 0.7V$$

Assumption was correct!

$$\rightarrow i_C = 100 \times 43 \mu A = 4.3 \text{ mA}$$

Clicker question 1.

What is the region of the operation of this transistor? (Assume Si BJT with $\beta = 100$, $V_{sat} = 0.2 V$)

Find i_B and v_{CE} .

$$i_B = i_E - i_C = 1.2 - 1 = 0.2 \text{ mA}$$

A. Saturation

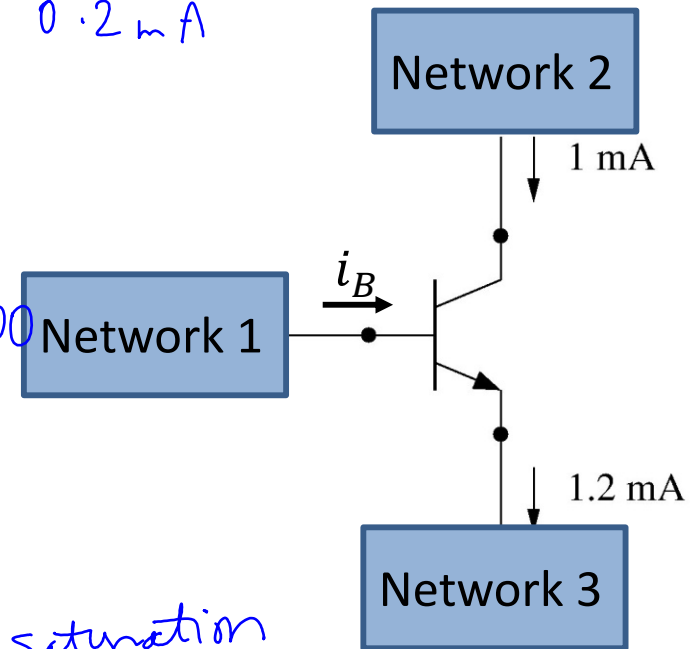
B. Active

C. ~~Cut-Off~~

$$\frac{i_C}{i_B} = \frac{1 \text{ mA}}{0.2 \text{ mA}} = 5 < 100$$

$$\Rightarrow i_C < \beta i_B$$

\Rightarrow BJT is in saturation



Cut-off :

$$i_B = 0, \quad i_C = 0$$

$$v_{BE} < V_{D0}$$

Active:

$$v_{BE} = V_{D0}, \quad i_B \geq 0$$

$$i_C = \beta i_B, \quad v_{CE} \geq V_{D0}$$

Saturation:

$$v_{BE} = V_{D0}, \quad i_B \geq 0$$

$$v_{CE} = V_{sat}, \quad i_C < \beta i_B$$

Clicker question 2.

What is the collector current in this BJT circuit. ($\beta = 100$, $V_{D0} = 0.7V$, $V_{sat} = 0.2V$).

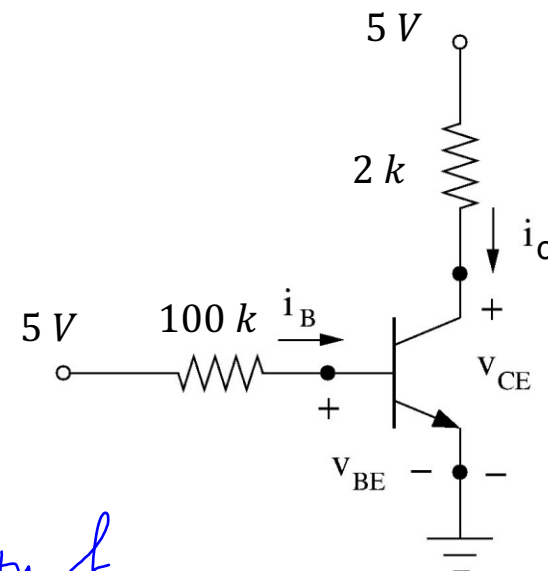
$$i_B = \frac{5 - 0.7}{100k} = 43 \mu A$$

$$i_B = 43 \mu A$$

Assume active mode of operation:

$$i_C = \beta i_B = 4.3 mA$$

we need to check the validity of this assumption.



Cut-off :

$$i_B = 0, \quad i_C = 0$$

$$v_{BE} < V_{D0}$$

Active:

$$v_{BE} = V_{D0}, \quad i_B \geq 0$$

$$i_C = \beta i_B, \quad v_{CE} \geq V_{D0}$$

Saturation:

$$v_{BE} = V_{D0}, \quad i_B \geq 0$$

$$v_{CE} = V_{sat}, \quad i_C < \beta i_B$$

Clicker question 2.

What is the collector current in this BJT circuit. ($\beta = 100$, $V_{D0} = 0.7V$, $V_{sat} = 0.2V$).

$$i_B = \frac{5 - 0.7}{100k} = 43 \mu A$$

$$i_C = \beta i_B = 4.3 mA$$

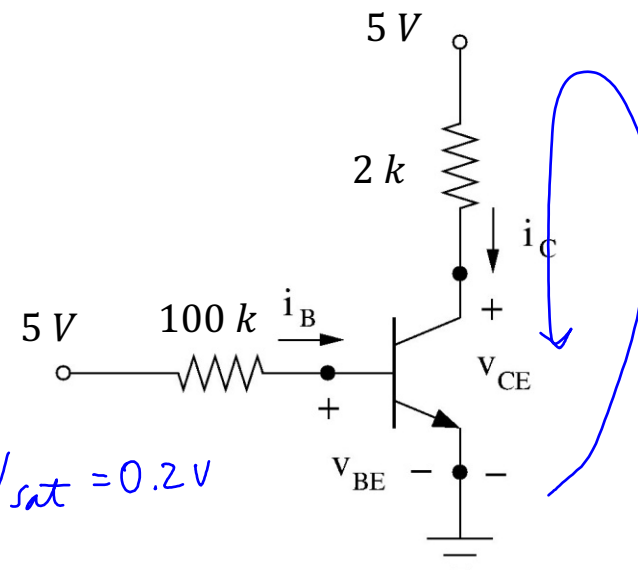
$$CE \text{ KVL: } 5 = 2k \times i_C + V_{CE}$$

$$\rightarrow V_{CE} = -3.6 < 0.7V$$

$$\text{Assume sat.} \rightarrow V_{CE} = V_{sat} = 0.2V$$

$$CE \text{ KVL: } 5V = 2k \times i_C + 0.2$$

$$\rightarrow i_C = 2.4 mA \quad \text{check} \Rightarrow i_C < \beta i_B \quad 2.4 mA < 100 \times 43 \mu A$$



A. $i_C = 4.3 mA$

B. $i_C = 2.4 mA$

C. $i_C = 2 mA$

D. $i_C = 2.15 mA$

Cut-off :

$$i_B = 0, \quad i_C = 0$$

$$v_{BE} < V_{D0}$$

Active:

$$v_{BE} = V_{D0}, \quad i_B \geq 0$$

$$i_C = \beta i_B, \quad v_{CE} \geq V_{D0}$$

Saturation:

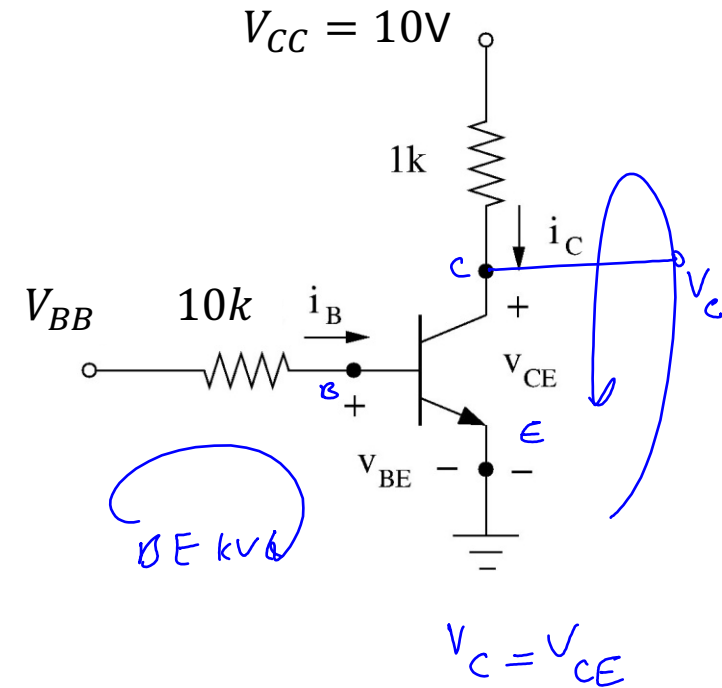
$$v_{BE} = V_{D0}, \quad i_B \geq 0$$

$$v_{CE} = V_{sat}, \quad i_C < \beta i_B$$

Discussion question 1.

Find the value of voltage V_{BB} that results in the transistor operating in the active region with $V_C = 5V$.

(Assume Si transistor with $\beta = 100$ and $V_{sat} = 0.2 V$).



$$V_{CE} = V_C - V_E = V_C - 0 = V_C$$

$$CE\ KVL: 10 = 1k \times i_C + V_{CE} \rightarrow i_C = 5\text{ mA}$$

$$i_B = 50\ \mu A$$

$$BE\ KVL: V_{BB} = 10k \times i_B + \underbrace{V_{BE}}_{0.7V} \rightarrow V_{BB} = 1.2V$$