

ECE 65: Components & Circuits Lab

Lecture 23

Common-emitter / Common-source amplifier parameters

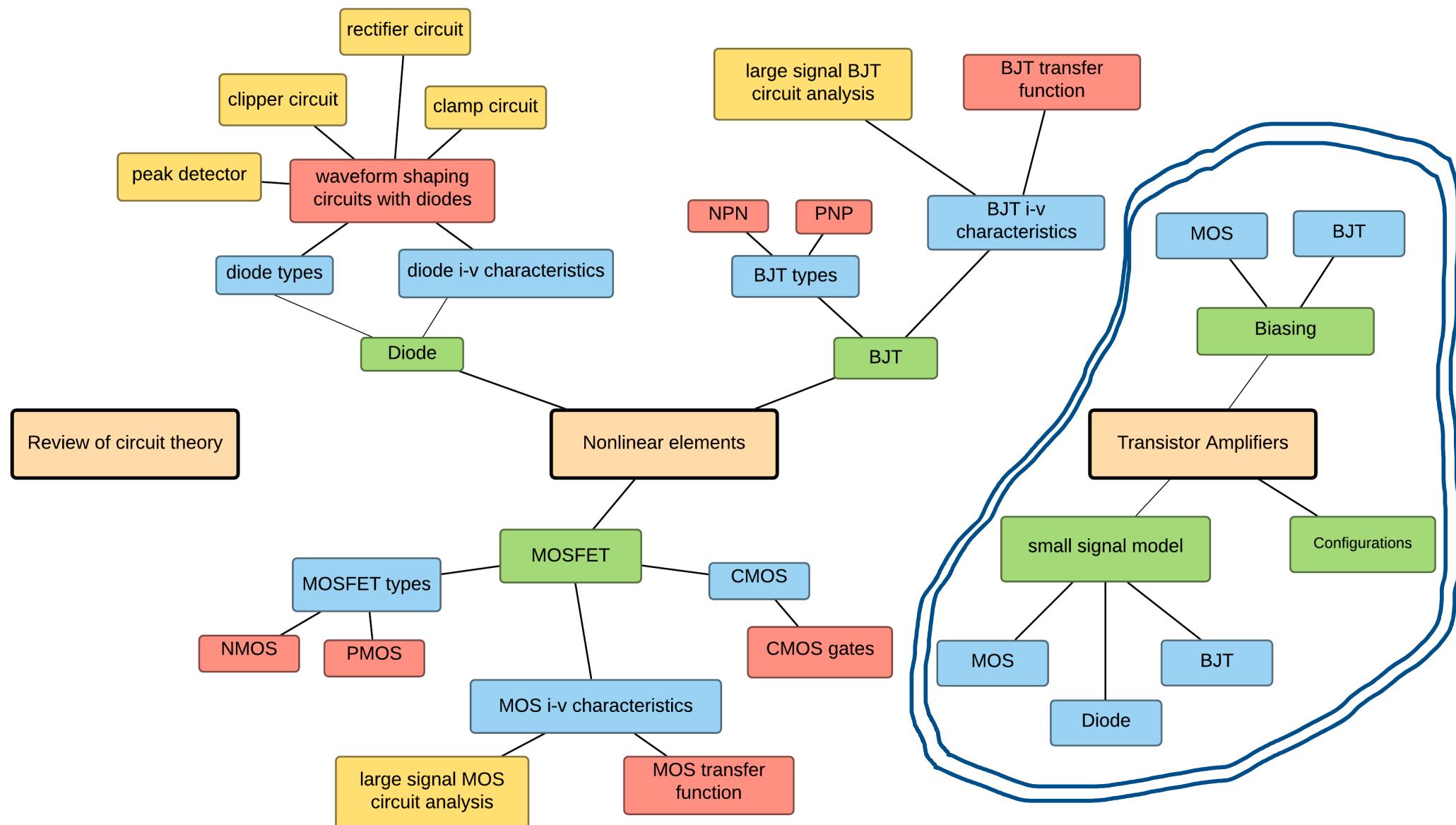
Reference notes: sections 6.1, 6.2

Sedra & Smith (7th Ed): sections 7.3

Saharnaz Baghdadchi

Course map

6. Transistor Amplifier Configurations



What are the amplifier parameters?

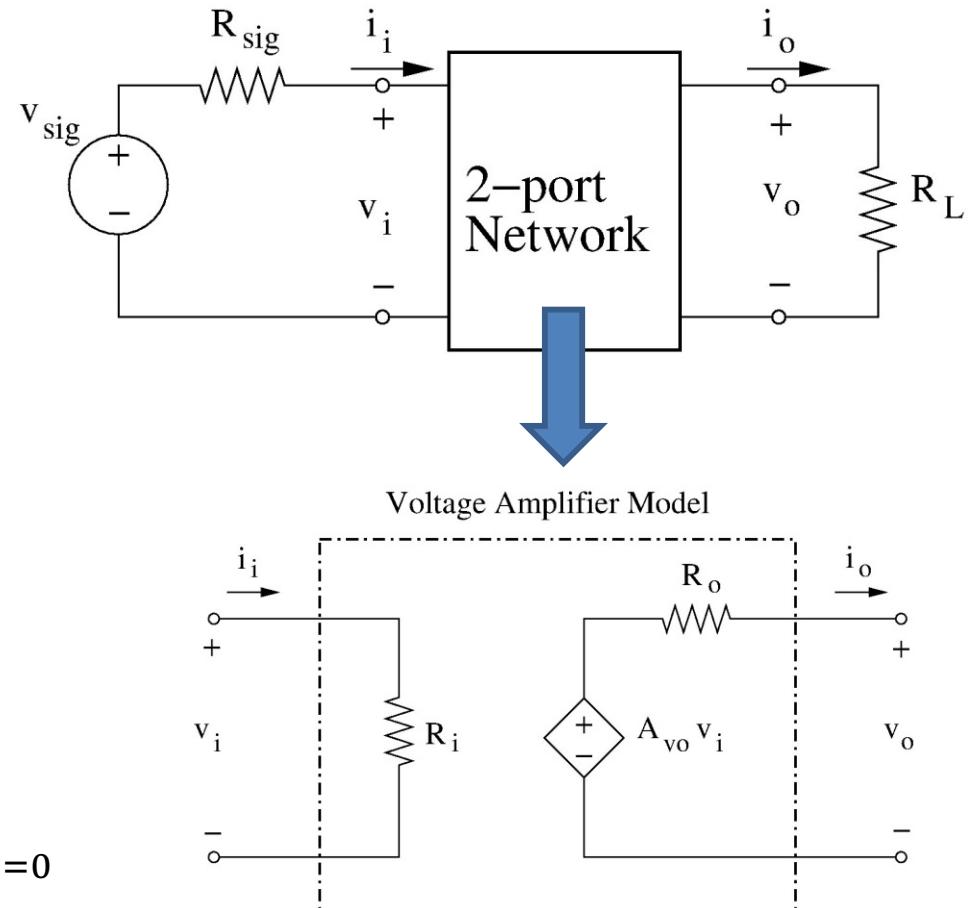
Voltage Gain of the Circuit: $A = \frac{v_o}{v_{sig}}$

Voltage Gain of the Amplifier: $A_v = \frac{v_o}{v_i}$

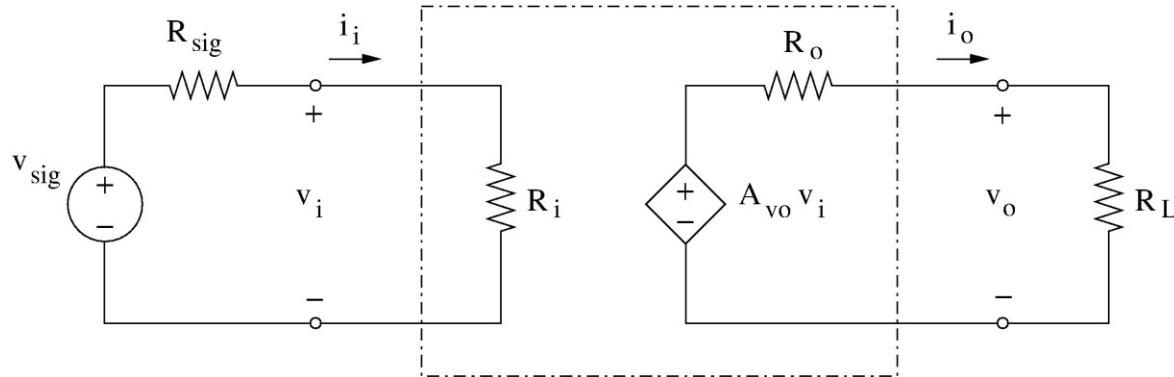
Open-loop Gain: $A_{vo} = \frac{v_o}{v_i} \Big|_{R_L \rightarrow \infty}$

Input Resistance: $R_i = \frac{v_i}{i_i}$

Output Resistance of Amplifier: $R_o = -\frac{v_o}{i_o} \Big|_{v_i=0}$



Observations on the amplifier parameters

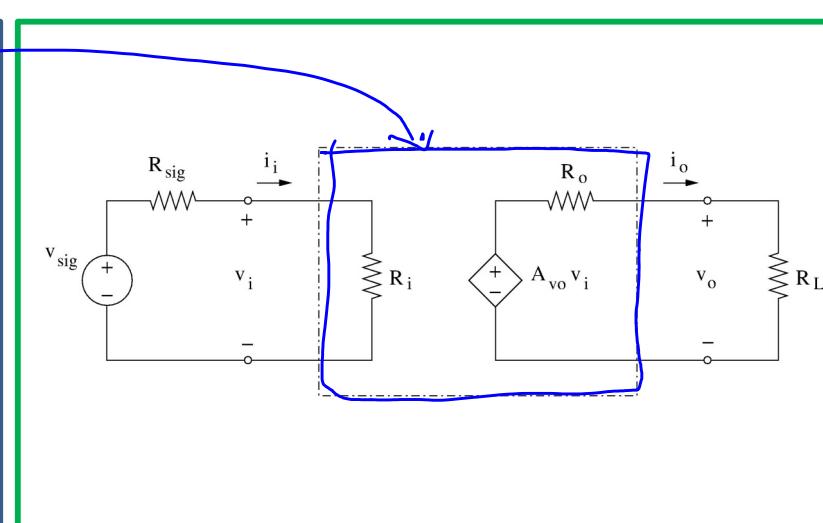
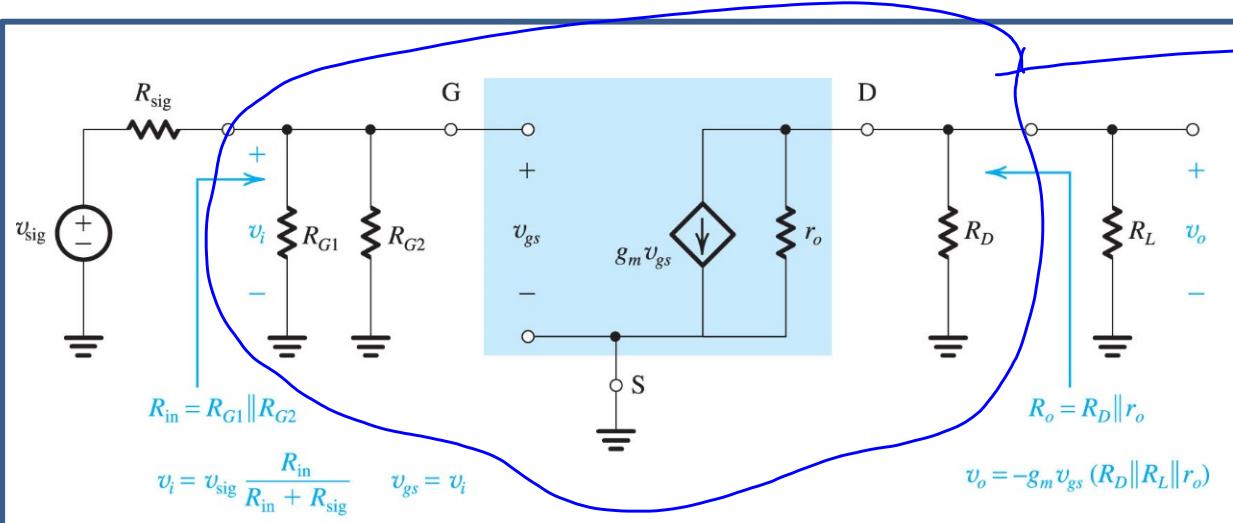
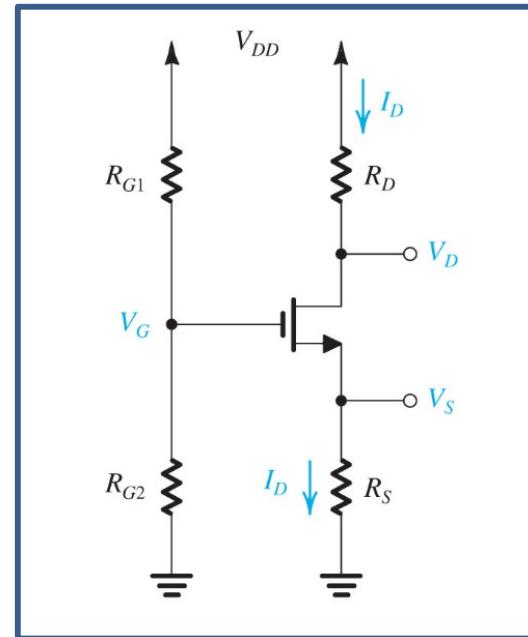
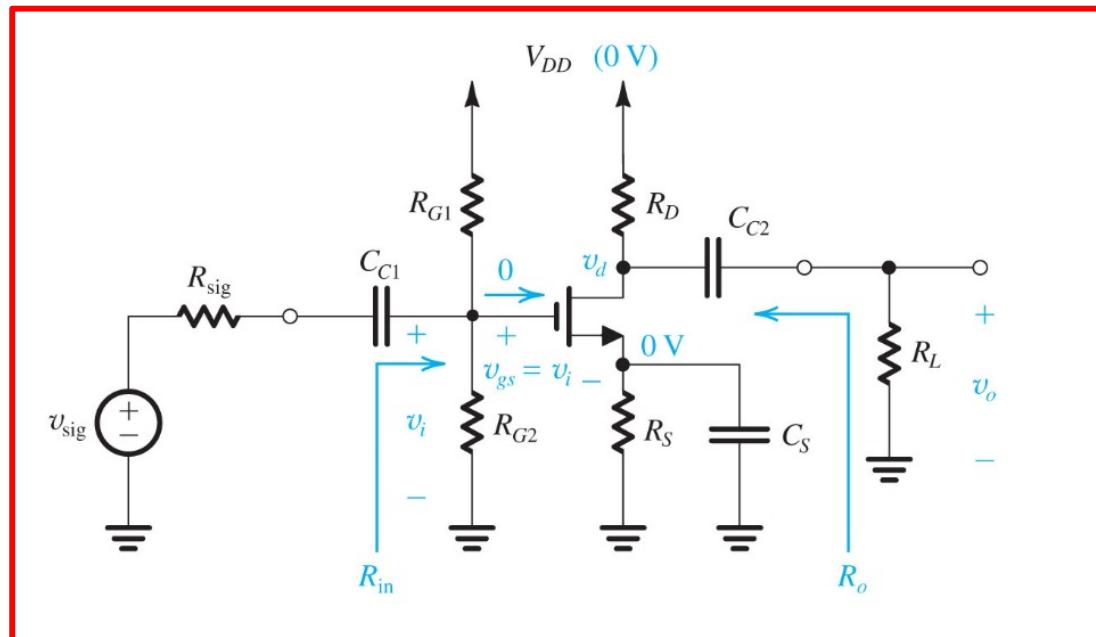


$$A = \frac{v_o}{v_{sig}} = \frac{v_i}{v_{sig}} \times \frac{v_o}{v_i} = \frac{R_i}{R_i + R_{sig}} A_v \quad \text{When } R_{sig} = 0, A = A_v$$

$$A_v = \frac{v_o}{v_i} = \frac{R_L}{R_L + R_o} A_{vo} \quad \text{When } R_L = \infty, A_v = A_{vo}$$

A_{vo} is the maximum possible gain of the amplifier

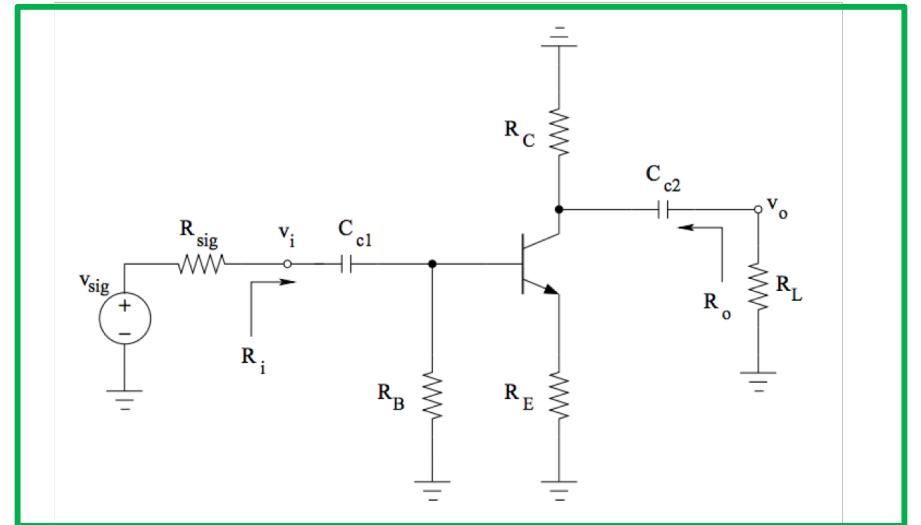
From an amplifier circuit to the building block representation



Equations of A_{vo} , R_o , R_i for the common-emitter with an emitter resistance BJT amplifier

Please follow the derivations of the below parameters from the reference notes.

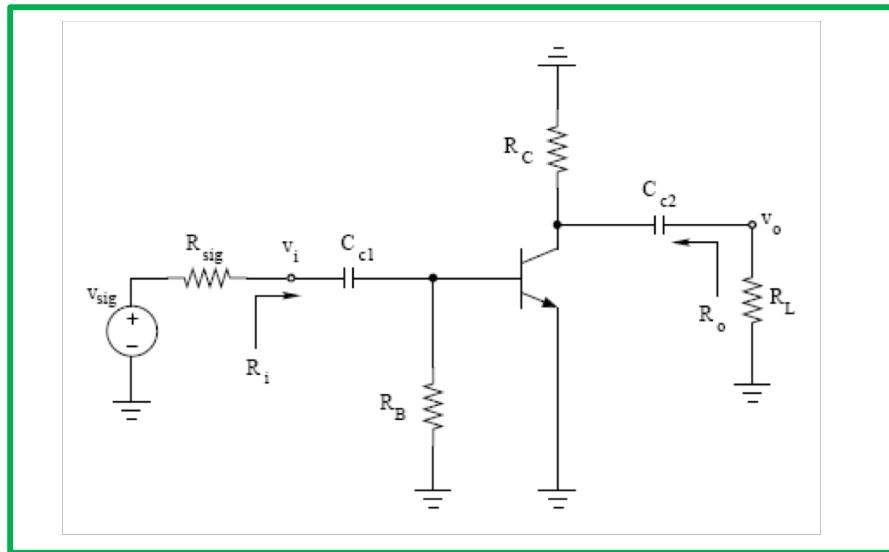
$$A_{vo} = \frac{-R_C}{R_E + (1 + R_C / r_o) \frac{R_E + r_\pi}{\beta}}$$



$$R_o = \left[\frac{\left(\frac{1}{g_m} \right) || r_o}{R_C || r_o} + \frac{r_\pi || R_E}{R_C} \right]^{-1} [(r_\pi || R_E) + (1/g_m) || r_o]$$

$$R_i = R_B || \left[R_E + r_\pi + \frac{\beta R_E}{1 + (R_E + R_C || R_L) / r_o} \right]$$

Common-emitter BJT amplifier parameters



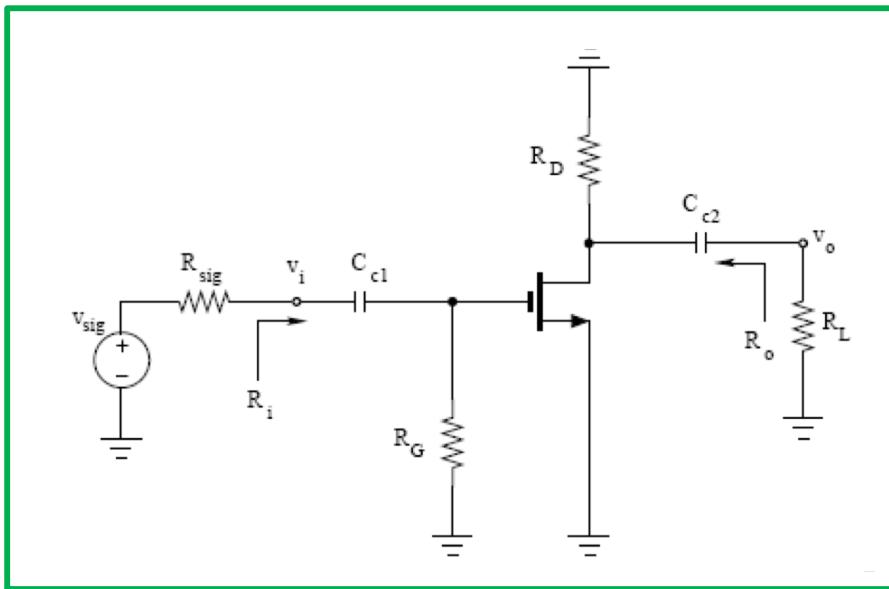
The amplifier parameters derived for the common emitter amplifier with an emitter resistor can be used for this amplifier by setting $R_E = 0$.

$$A_{vo} = -g_m(R_C \parallel r_o)$$

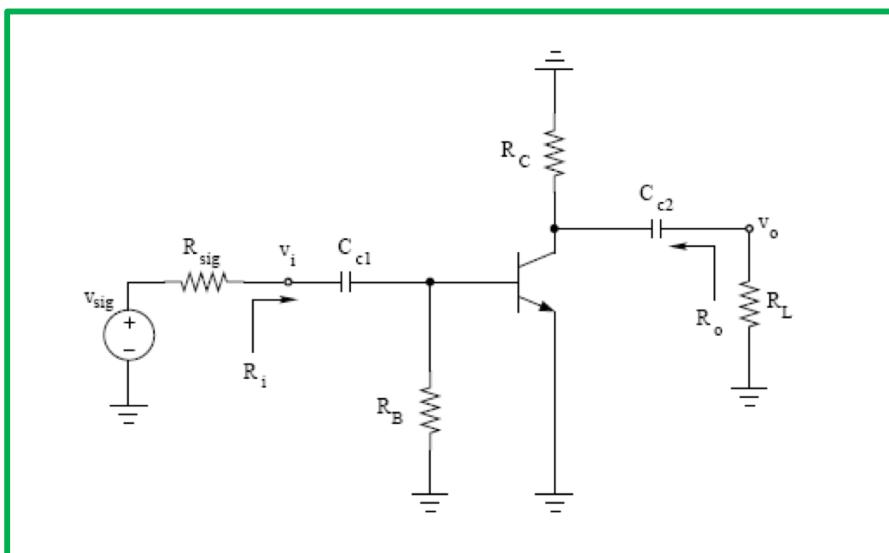
$$R_o = R_C \parallel r_o$$

$$R_i = R_B \parallel r_\pi$$

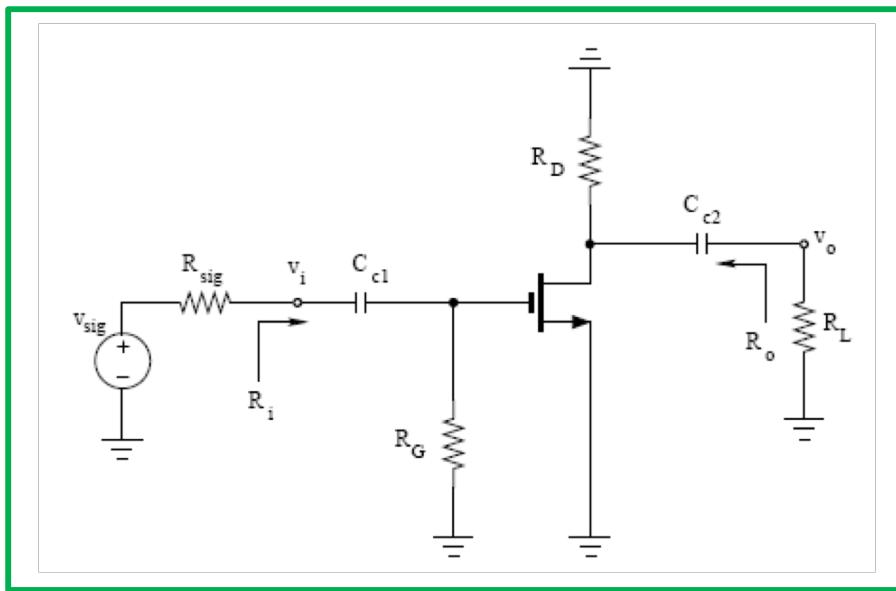
Common-Source MOS amplifier parameters



Compare it with the signal circuit for the common-emitter BJT amplifier:



Common-source MOS amplifier parameters



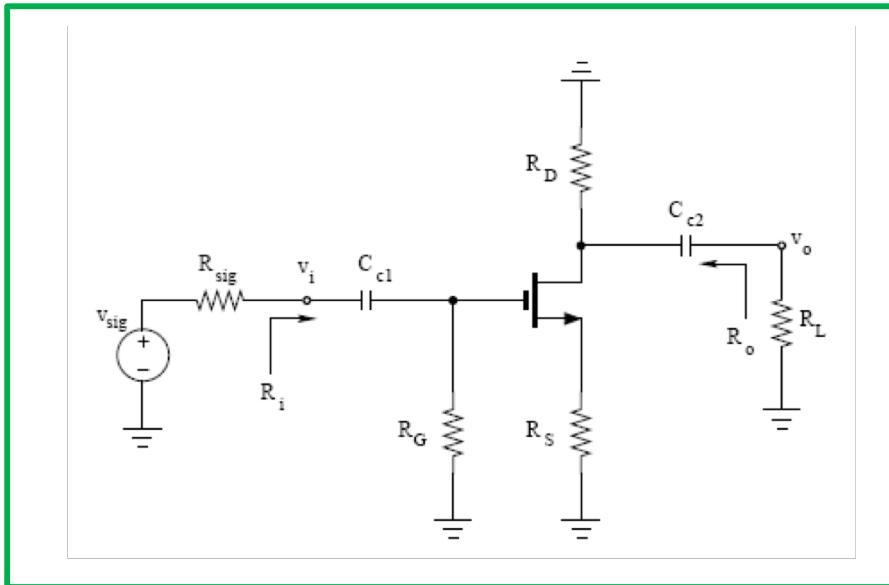
The common emitter BJT amplifier parameters can be used for this amplifier when R_B is replaced with R_G , and R_C is replaced with R_D , and $r_\pi \rightarrow \infty$.

$$A_{vo} = -g_m(R_D || r_o)$$

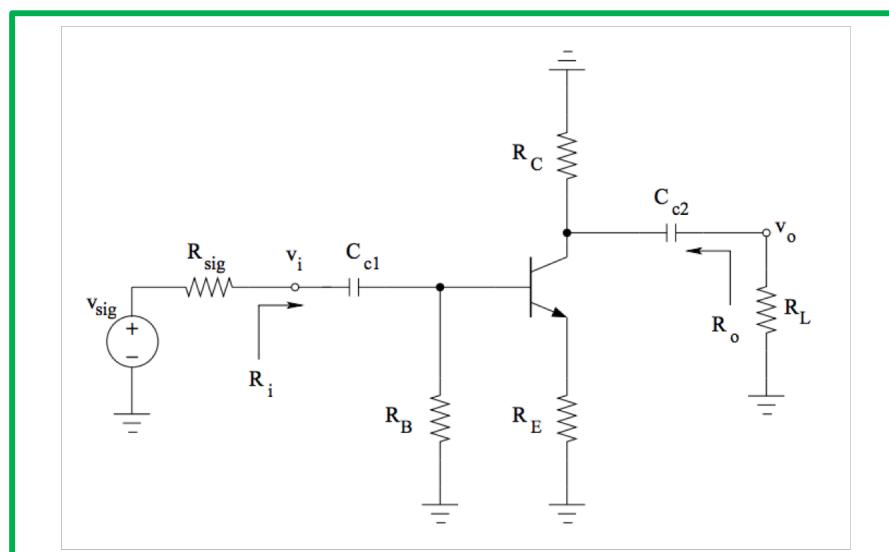
$$R_o = R_D || r_o$$

$$R_i = R_G$$

Common-source MOS with a source resistance amplifier parameters



Compare it with the signal circuit for the common-emitter with an emitter resistor BJT amplifier:

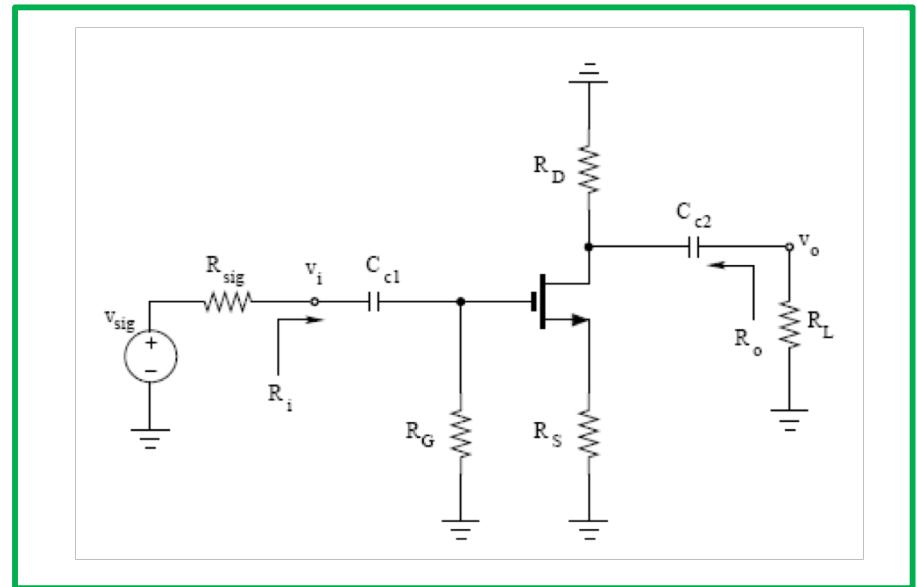


Common-source MOS with a source resistance

amplifier parameters

The common-emitter with an emitter resistor BJT amplifier parameters can be used for this amplifier when R_B is replaced with R_G , R_C is replaced with R_D ,

R_E is replaced with R_S , β/r_π is replaced with g_m and $r_\pi \rightarrow \infty$.



$$A_{vo} = \frac{-g_m R_D}{1 + g_m R_S + R_D / r_o}$$

$$R_o = R_D \parallel [r_o(1 + g_m R_S)]$$

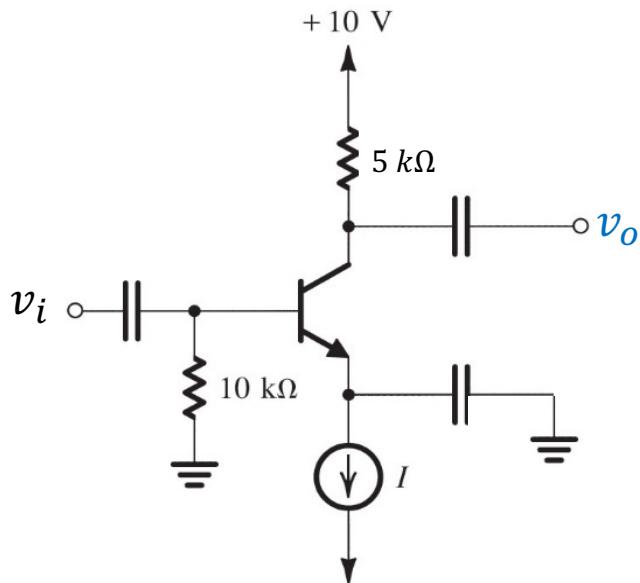
$$R_i = R_G$$

Some notes on *common-emitter* (CE) and *common-source* (CS) amplifiers:

- They have a high voltage gain.
- Ignoring R_G , CS has an infinite input resistance.
- Ignoring R_B , CE has a modest input resistance.
- Both CE and CS have a rather high output resistances.
- Adding R_S to the source of a CS or R_E to the emitter of a CE amplifier can have the benefits of raising the input resistance of CE amplifier, increasing linearity and increasing the amplifier bandwidth.

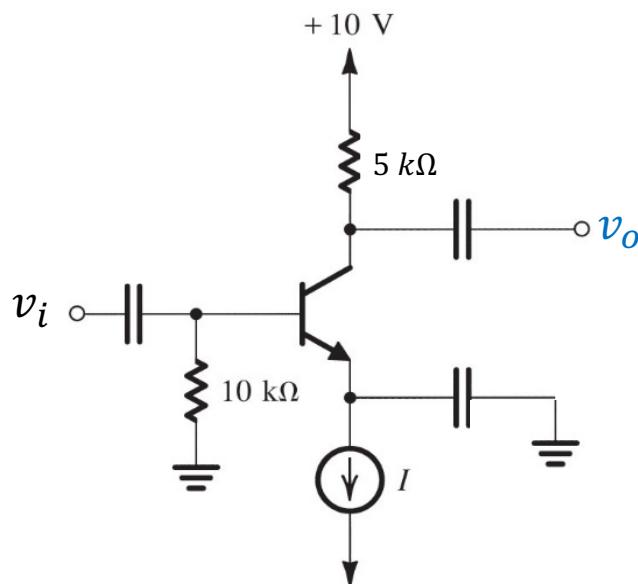
Lecture 23 reading quiz.

The below BJT common-emitter amplifier with $\beta = 100$ is fed with a signal source having a resistance of $5 \text{ k}\Omega$. A load resistor of $5 \text{ k}\Omega$ is connected to the output. In this amplifier, $R_i = 2 \text{ k}\Omega$, and $R_o = 5 \text{ k}\Omega$. $V_T = 25 \text{ mV}$. If the peak value of v_π (denoted by \hat{v}_π) is to be limited to 5 mV , what are the corresponding peak values of v_{sig} (denoted by \hat{v}_{sig}), and v_o (denoted by \hat{v}_o)?



Lecture 23 reading quiz.

$$R_i = R_B \parallel r_\pi = 2\text{k}\Omega$$

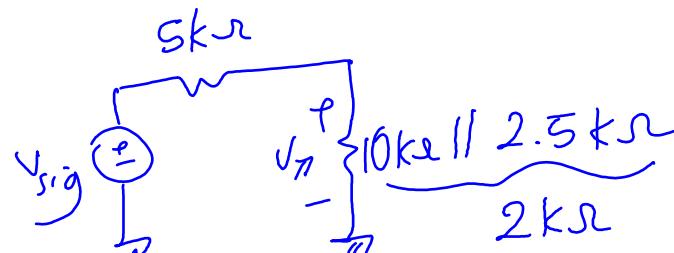
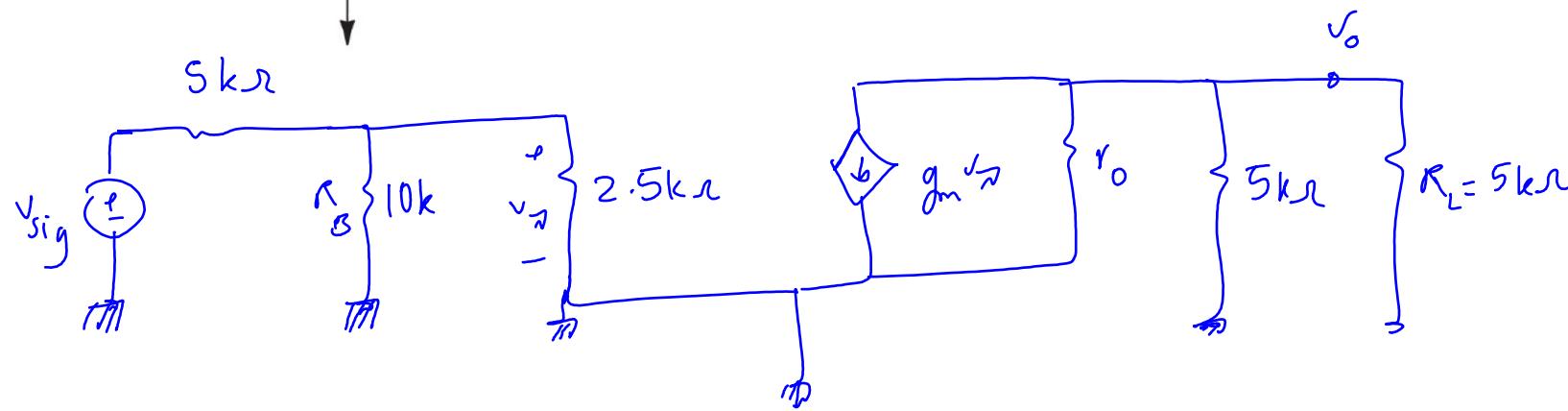


$$10\text{k}\Omega \parallel r_\pi = 2\text{k}\Omega \rightarrow r_\pi = 2.5\text{k}\Omega$$

$$r_\pi = \frac{V}{I} \rightarrow g_m = 40 \text{ mA/V}$$

$$R_o = R_C \parallel r_o = 5\text{k}\Omega, \quad R_c = 5\text{k}\Omega$$

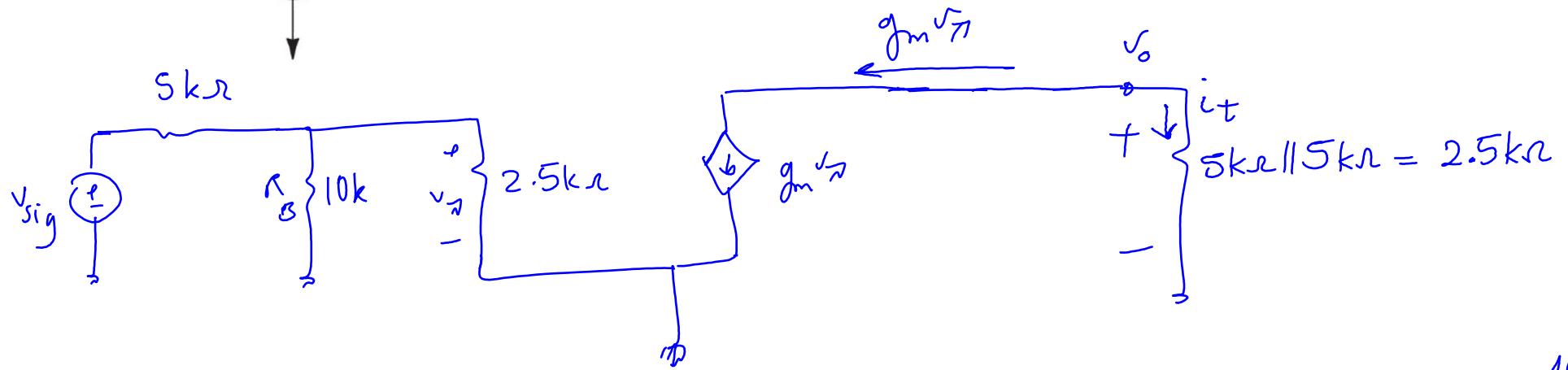
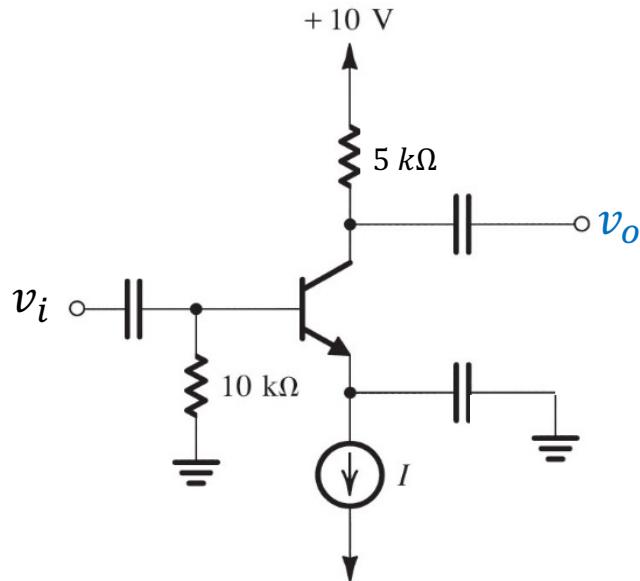
$$r_o = \infty$$



$$V_\pi = \frac{2\text{k}\Omega}{2\text{k}\Omega + 5\text{k}\Omega} \times V_{\text{Sig}} \Rightarrow V_\pi = \frac{2}{7} V_{\text{Sig}}$$

$$\hat{V}_{\text{Sig}} = \frac{7}{2} \times 5\text{mV} = 17.5 \text{ mV}$$

Lecture 23 reading quiz.



$$v_o = 2.5\text{ k}\Omega \times i_t$$

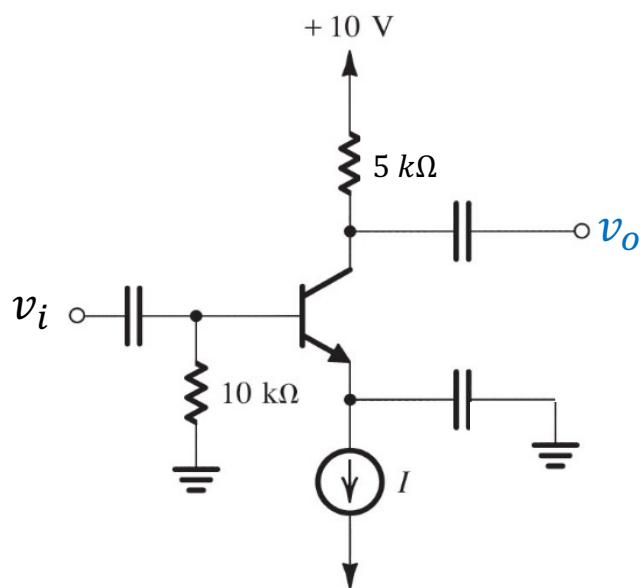
$$i_t = -g_m \sqrt{\pi}$$

$$v_o = -100 \sqrt{\pi}$$

$$v_o = -g_m \sqrt{\pi} \times 2.5\text{ k}\Omega = -40 \text{ mA} / \sqrt{2.5\text{ k}\Omega \times \sqrt{\pi}} = -40 \text{ mA} / \sqrt{2.5 \times 3.14} = -40 \text{ mA} / \sqrt{7.85} = -40 \text{ mA} / 2.8 = -14.3 \text{ V}$$

$$v_o = |100 \times 0.005 \text{ V}| = 0.5 \text{ V}$$

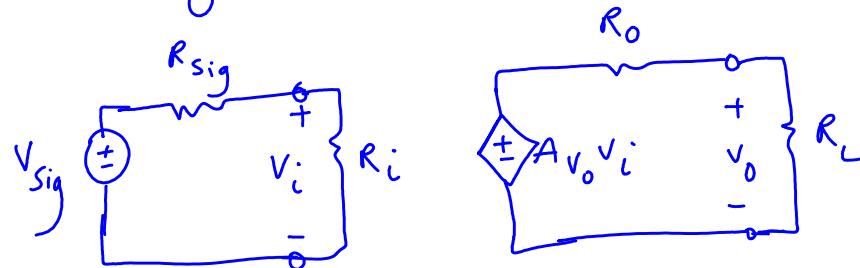
Lecture 23 reading quiz.



Another way of finding the peak value of v_o :

$$\hat{v}_o = |A| \hat{v}_{sig}$$

Voltage amplifier model:



$$A = \frac{v_o}{v_{sig}} = \frac{v_o}{v_i} \times \frac{v_i}{v_{sig}} = \left(\frac{R_L}{R_L + R_o} \times A_{v_o} \right) \left(\frac{R_i}{R_i + R_{sig}} \right)$$

$$A_{v_o} = -g_m R_c = - (40 \text{ mA/V}) \times 5k = -200 \text{ V/V}$$

$$A = \left(\frac{5k}{5k+5k} \times (-200 \text{ V/V}) \right) \left(\frac{2k}{2k+5k} \right) = -28.57 \text{ V/V} \rightarrow A = -28.57 \text{ V/V}$$

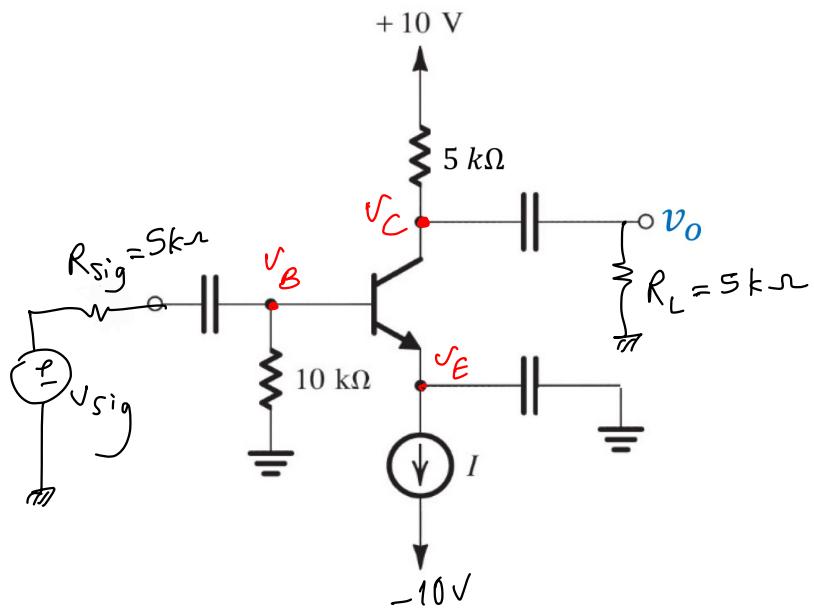
$$\hat{v}_o = |A| \hat{v}_{sig} = 28.57 \times 17.5 \text{ mV} = 0.5 \text{ V} \rightarrow \hat{v}_o = 0.5 \text{ V}$$

If v_{sig} is a sine wave with peak amplitude of 7 (mV),

$$v_{sig} = 7 \sin(\omega t) \text{ (mV)},$$

find and sketch all the instantaneous node voltages.

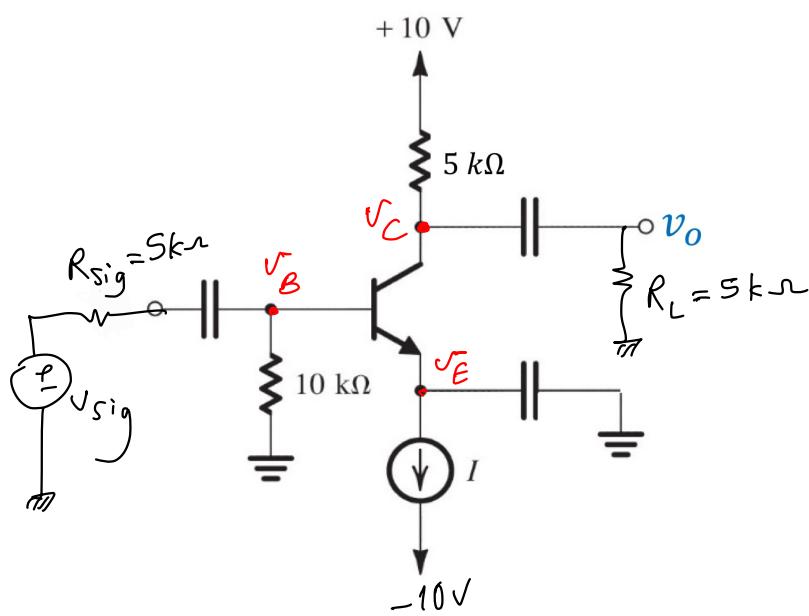
$$\text{Assume } v_{D_0} = 0.7 \text{ V}$$



If v_{sig} is a sine wave with peak amplitude of 7 (mV),

$$v_{sig} = 7 \sin(\omega t) \text{ (mV)}$$

find and sketch all the instantaneous node voltages



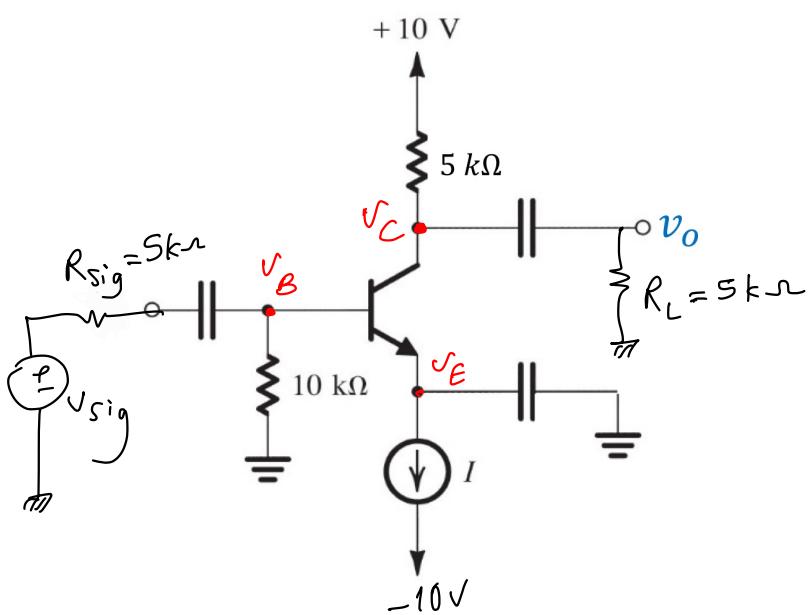
$$\begin{aligned}v_B &= V_B + v_b \\v_C &= V_C + v_c \\v_E &= V_E + v_e\end{aligned}$$

from the signal circuit
from Bias circuit

If v_{sig} is a sine wave with peak amplitude of 7 (mV),

$$v_{sig} = 7 \sin(\omega t) \text{ (mV)}$$

find and sketch all the instantaneous node voltages

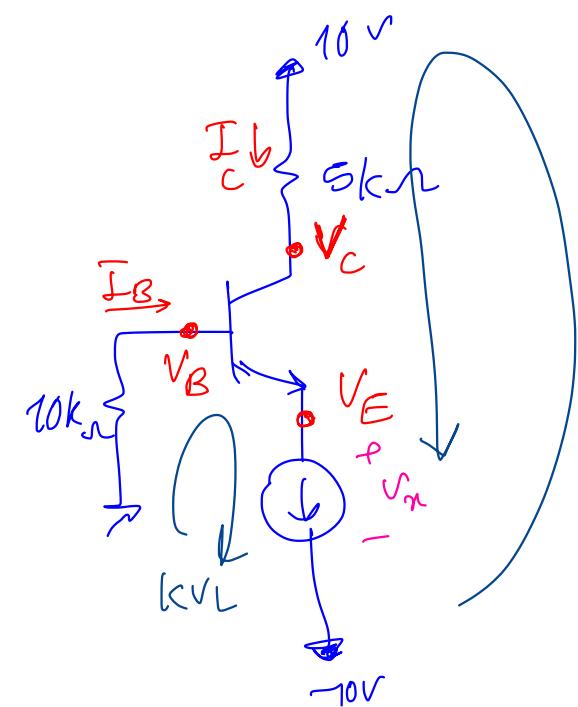


$$V_{BE} = 0.7V$$

$$V_B = -I_B \times 10k\Omega$$

$$I_C = 100 I_B$$

$$I_C = \frac{10V - V_C}{5k\Omega}$$

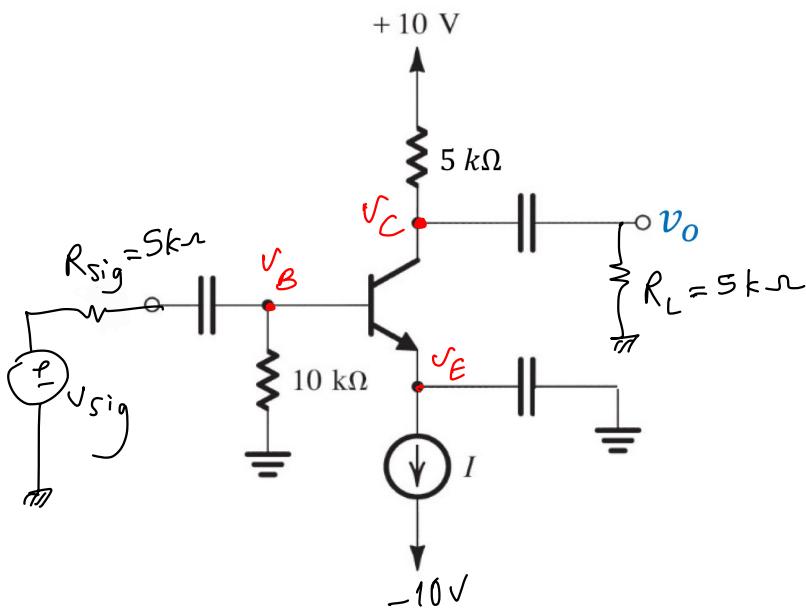


If V_{sig} is a sine wave with peak amplitude of 7 (mV),

$$V_{sig} = 7 \sin(\omega t) \text{ (mV)}$$

find and sketch all the instantaneous node voltages

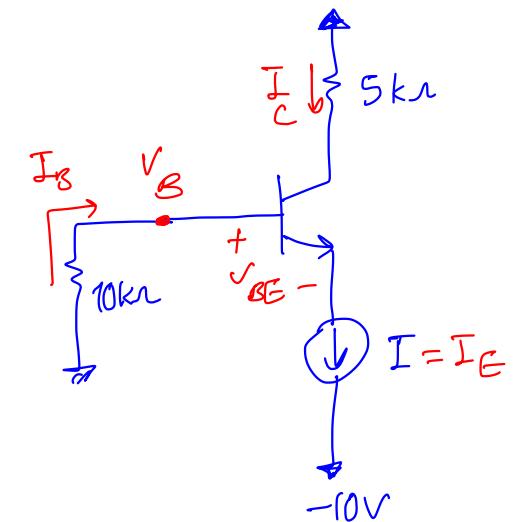
Bias circuit:



$$g_m = \frac{I_C}{V_T}$$

$$\Rightarrow I_C = g_m V_T$$

$$= 40 \text{ mA} \times 25 \text{ mV} = 1 \text{ mA}$$



$$I_B = \frac{I_C}{\beta} = \frac{1 \text{ mA}}{100} = 10 \mu\text{A}$$

If v_{sig} is a sine wave with peak amplitude of 7 (mV),

$$v_{sig} = 7 \sin(\omega t) \text{ (mV)}$$

find and sketch all the instantaneous node voltages

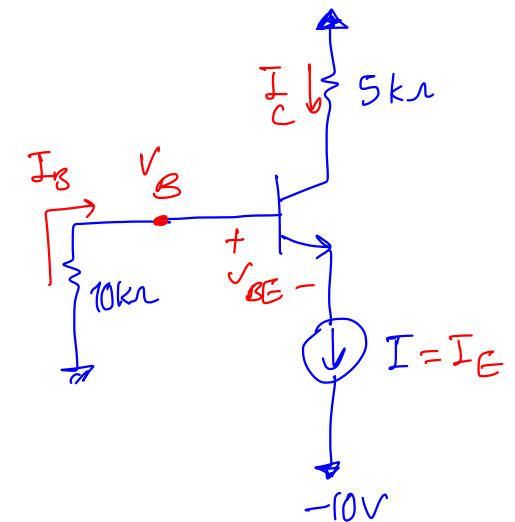
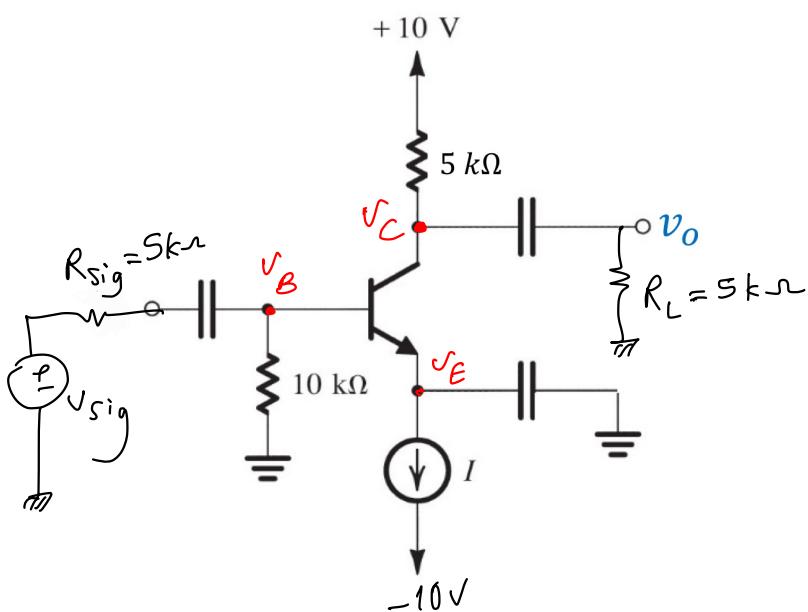
Bias circuit:

$$I_C = 1 \text{ mA}$$

$$I_B = 10 \text{ mA}$$

$$V_B = -10 \text{ k}\Omega \times 10 \text{ mA}$$

$$= -100 \text{ mV}$$

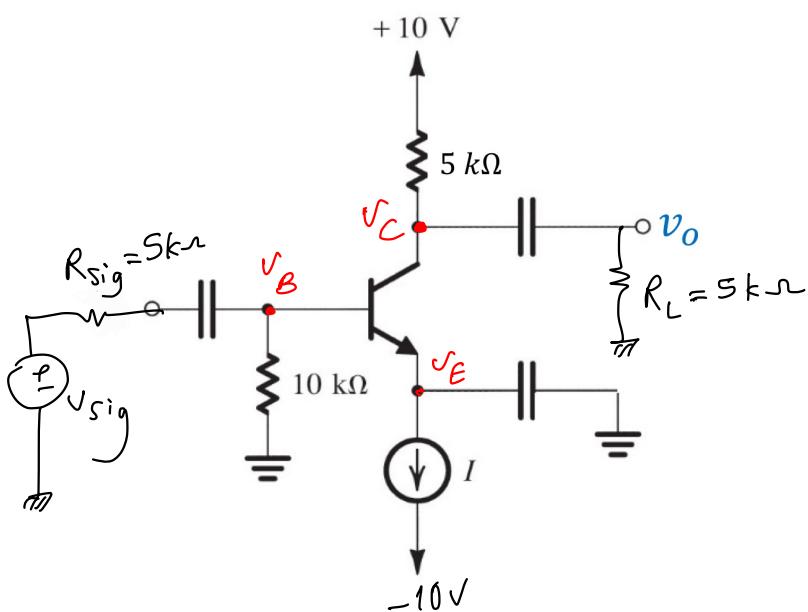


If v_{sig} is a sine wave with peak amplitude of 7 (mV),

$$v_{sig} = 7 \sin(\omega t) \text{ (mV)}$$

find and sketch all the instantaneous node voltages

Bias circuit:



$$I_C = 1 \text{ mA}$$

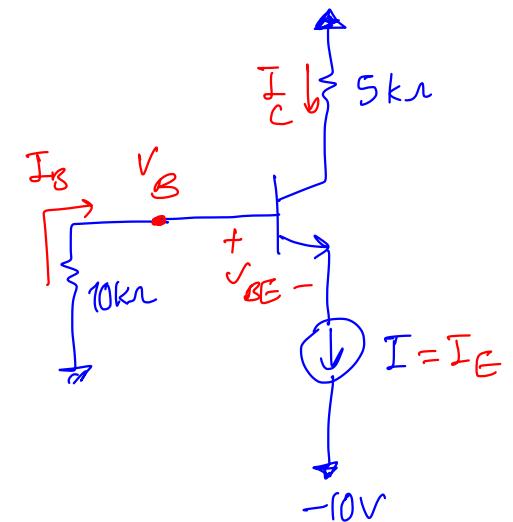
$$I_B = 10 \text{ } \mu\text{A}$$

$$V_B = -10 \text{ k}\Omega \times 10 \text{ } \mu\text{A}$$

$$= -100 \text{ mV}$$

$$V_{BE} = 0.7 \text{ V} = V_B - V_E \rightarrow V_E = V_B - 0.7 \text{ V}$$

$$\Rightarrow V_E = -800 \text{ mV}$$



If V_{sig} is a sine wave with peak amplitude of 7 (mV),

$$V_{\text{sig}} = 7 \sin(\omega t) \text{ (mV)}$$

find and sketch all the instantaneous node voltages

Bias circuit:

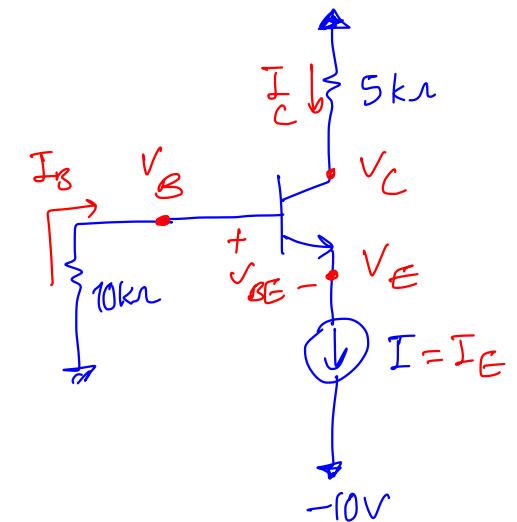
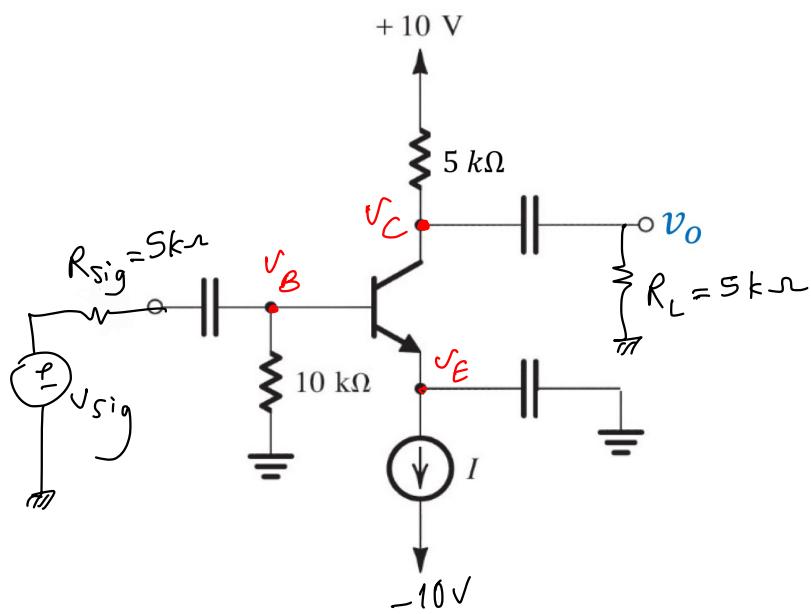
$$I_C = 1 \text{ mA}$$

$$I_B = 10 \mu\text{A}$$

$$V_B = -100 \text{ mV}$$

$$V_E = -800 \text{ mV}$$

$$V_C = 10 \text{ V} - 5 \text{k}\Omega \times I_C = 5 \text{ V}$$

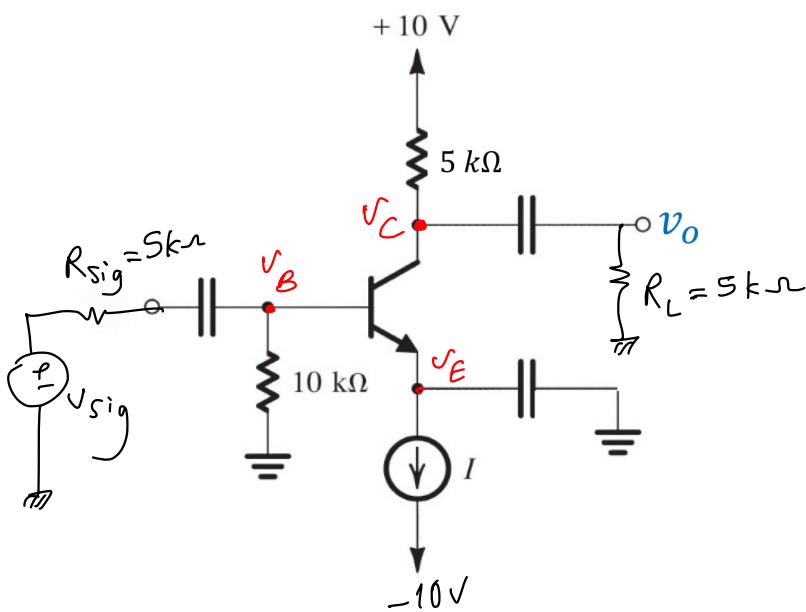


If V_{sig} is a sine wave with peak amplitude of 7 (mV),

$$V_{\text{sig}} = 7 \sin(\omega t) \text{ (mV)}, \text{ use } V_{D_0} = 0.7 \text{ V}$$

find and sketch all the instantaneous node voltages

Bias circuit:



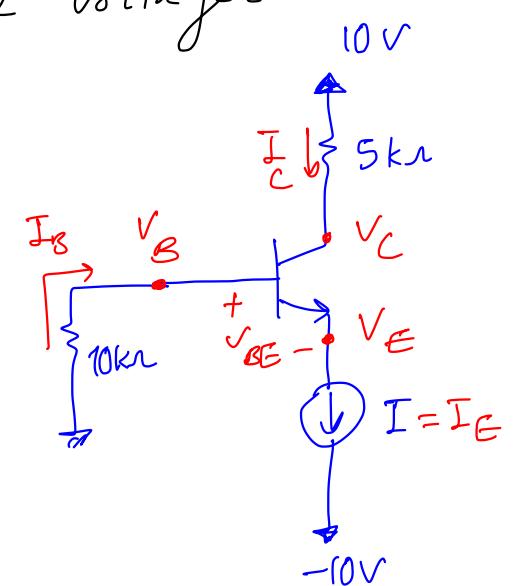
$$I_C = 1 \text{ mA}$$

$$I_B = 10 \mu\text{A}$$

$$V_B = -100 \text{ mV}$$

$$V_E = -800 \text{ mV}$$

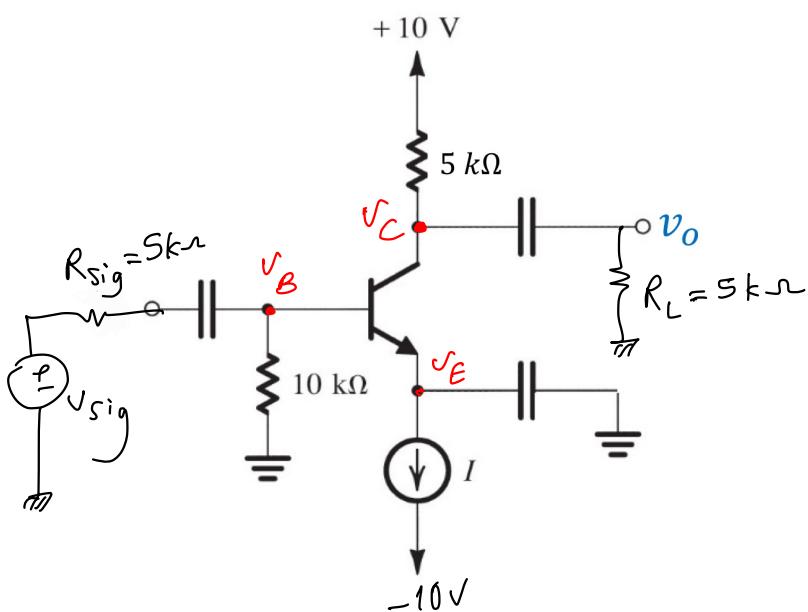
$$V_C = 5 \text{ V}$$



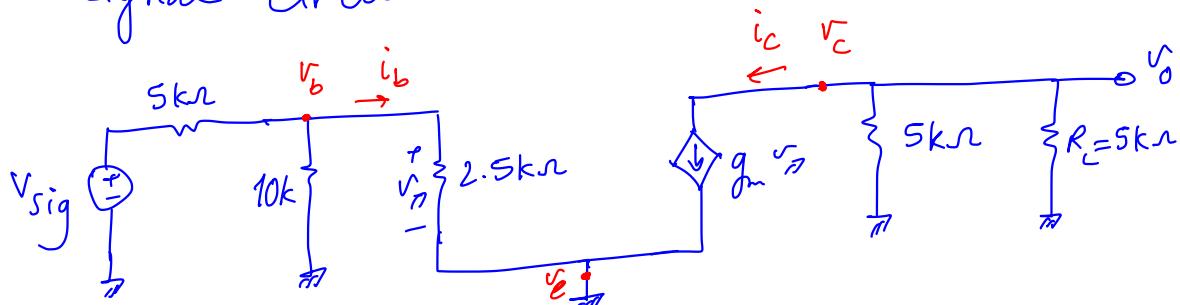
If v_{sig} is a sine wave with peak amplitude of 7 (mV),

$$v_{sig} = 7 \sin(\omega t) \text{ (mV)}$$

find and sketch all the instantaneous node voltages



signal circuit:



$$v_b = v_{\pi} = \frac{(10k \parallel 2.5k)}{(10k \parallel 2.5k) + 5k} \times v_{sig} = \frac{2}{7} v_{sig}$$

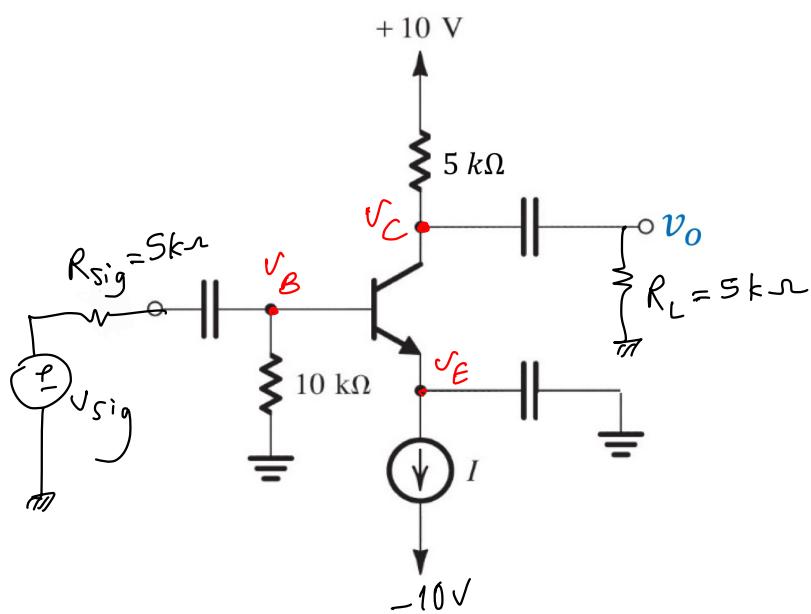
$$\Rightarrow v_b = \frac{2}{7} \times 7 \sin(\omega t) \text{ (mV)} = 2 \sin \omega t \text{ (mV)}$$

$v_e = 0$, the emitter in the signal circuit is grounded

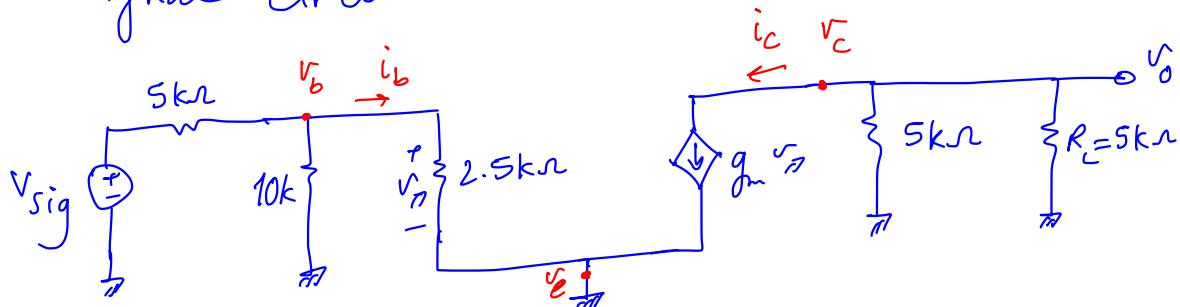
If v_{sig} is a sine wave with peak amplitude of 7 (mV),

$$v_{sig} = 7 \sin(\omega t) \text{ (mV)}$$

find and sketch all the instantaneous node voltages



signal circuit:



$$v_C = v_0 = -100 \frac{v}{\pi} \quad (\text{as previously calculated})$$

$$\Rightarrow v_C = -200 \sin(\omega t) \text{ (mV)}$$

If v_{sig} is a sine wave with peak amplitude of 7 (mV),

$$v_{sig} = 7 \sin(\omega t) \text{ (mV)}$$

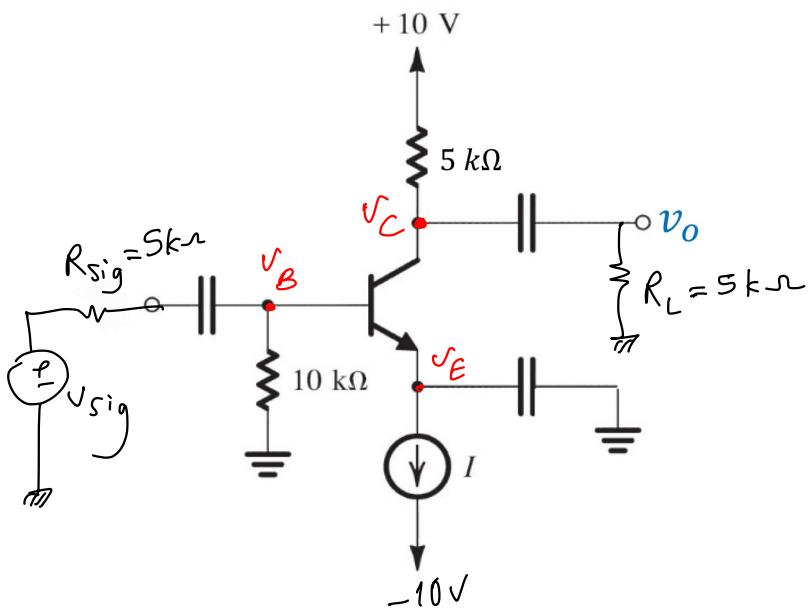
find and sketch all the instantaneous node voltages

The instantaneous node voltages:

$$v_B = V_B + v_b = [-100 + 2 \sin(\omega t)] \text{ (mV)}$$

$$v_c = V_c + v_c = [5000 - 200 \sin(\omega t)] \text{ (mV)}$$

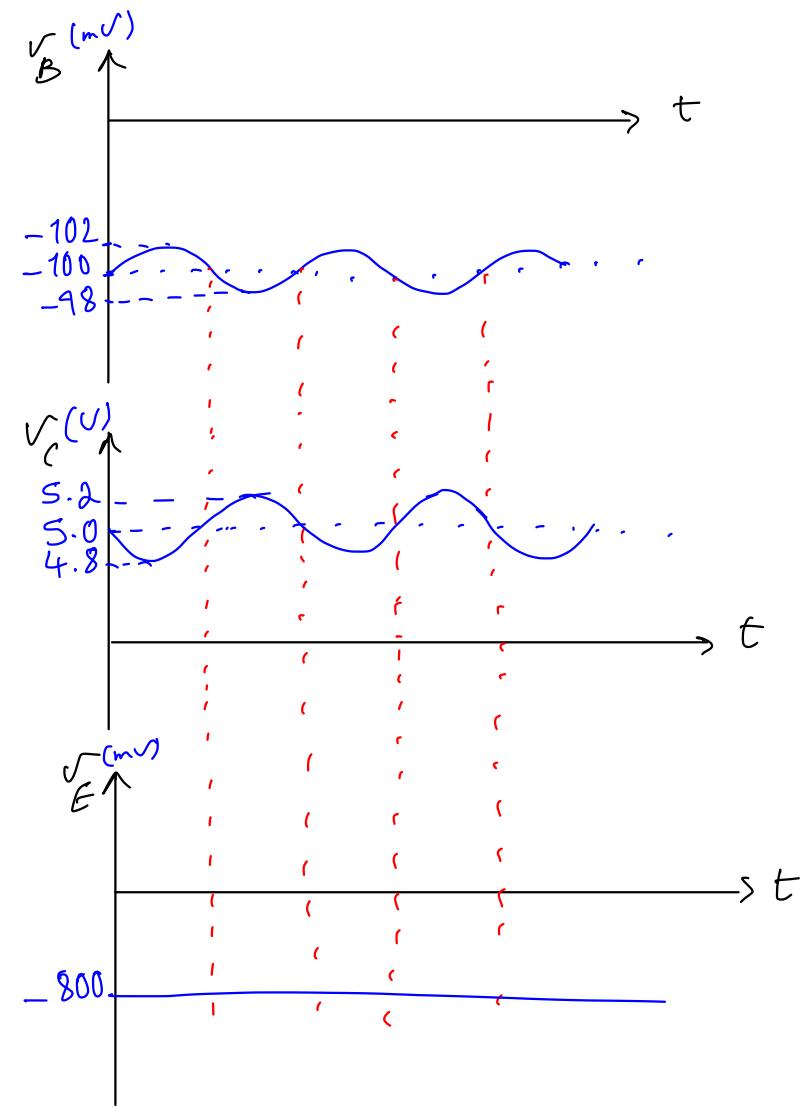
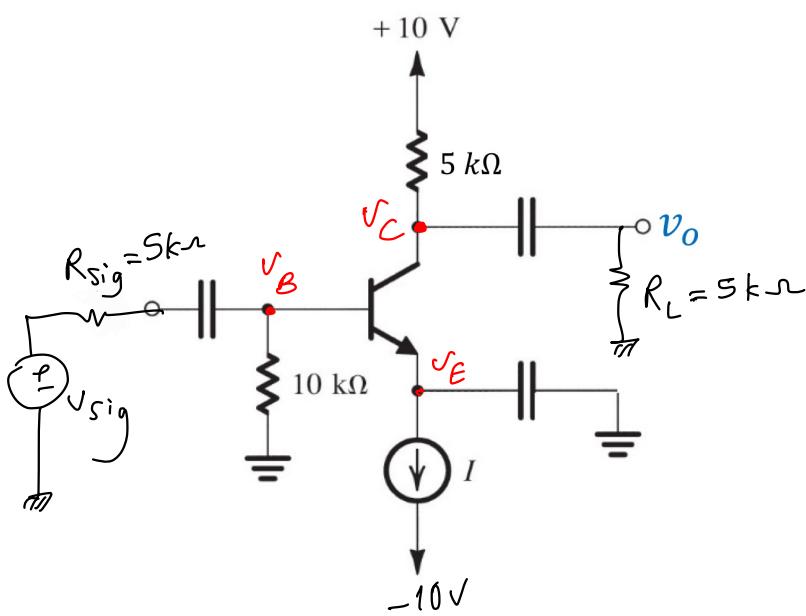
$$v_E = V_E + v_e = -800 \text{ mV}$$



If v_{sig} is a sine wave with peak amplitude of 7 (mV),

$$v_{sig} = 7 \sin(\omega t) \text{ (mV)}$$

find and sketch all the instantaneous node voltages

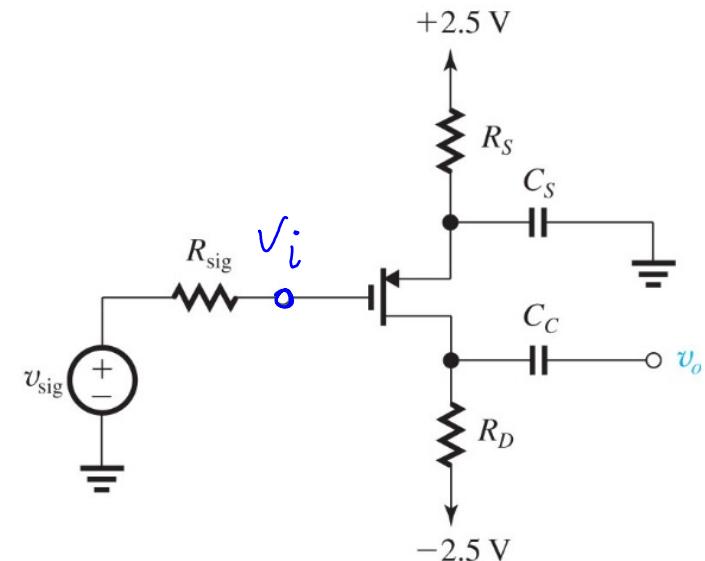


Clicker question 1.

Amplifier design problem

The PMOS in the below common-source amplifier circuit has $V_{tp} = -0.7 \text{ V}$ and $\lambda = 0$.

1. Select a value for R_S to bias the transistor at $I_D = 0.3 \text{ mA}$ and $V_{OV} = 0.3 \text{ V}$.
2. Select a value for R_D that results in $A_V = -10 \text{ V/V}$.

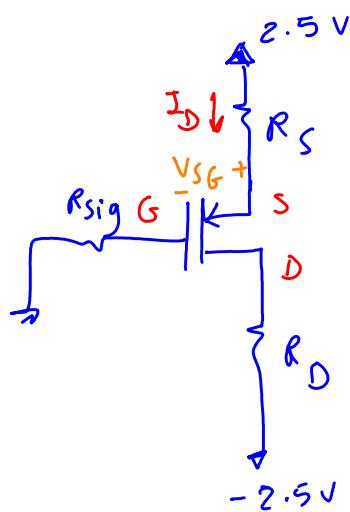


Clicker question 1.

The PMOS in the below common-source amplifier circuit has $V_{tp} = -0.7 \text{ V}$ and $\lambda = 0$.

1. Select a value for R_S to bias the transistor at $I_D = 0.3 \text{ mA}$ and $V_{OV} = 0.3 \text{ V}$.

Bias circuit:



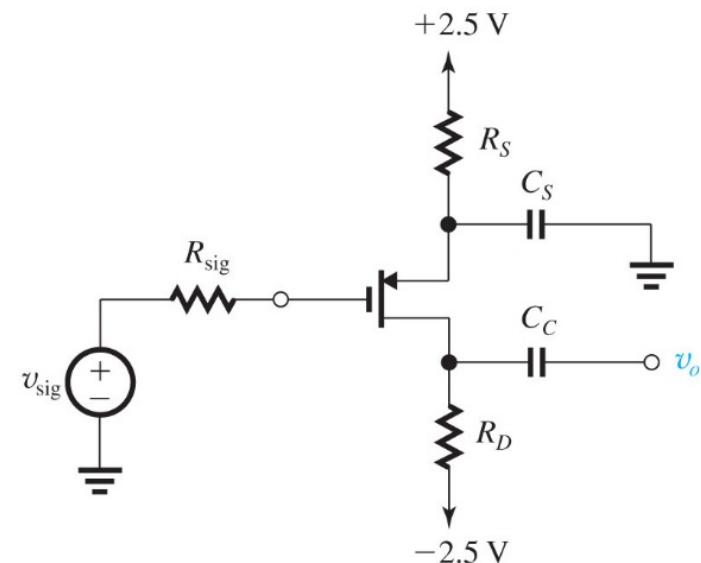
$$\text{Since } I_G = 0 \rightarrow V_G = 0$$

$$V_{OV} = V_{SG} - |V_{tp}|$$

$$V_{SG} = 0.3 \text{ V} + 0.7 \text{ V} = 1 \text{ V}$$

$$V_{SG} = V_S - V_G = V_S = 1 \text{ V}$$

$$\boxed{V_S = 1 \text{ V}} \rightarrow R_S = \frac{2.5 \text{ V} - 1 \text{ V}}{0.3 \text{ mA}} = 5 \text{ k}\Omega$$



Clicker question 1.

The PMOS in the below common-source amplifier circuit has $V_{tp} = -0.7 \text{ V}$ and $\lambda = 0$.

1. Select a value for R_S to bias the transistor at $I_D = 0.3 \text{ mA}$ and $V_{OV} = 0.3 \text{ V}$.
2. Select a value for R_D that results in $A_V = -10 \text{ V/V}$.

$$A_{V_0} = -g_m R_D = -10 \frac{\text{V}}{\text{V}}$$

$$g_m = \frac{2 I_D}{V_{OV}} = \frac{2 \times 0.3 \text{ mA}}{0.3 \text{ V}} = 2 \text{ mA/V}$$

$$2 (\text{mA/V}) R_D = 10 \rightarrow R_D = 5 \text{ k}\Omega$$

