

This circuit contains a capacitor (which we will cover in detail later in this course) with a voltage v_C across it. Voltage v_2 and current i_1 will satisfy the equations shown below (as we will also see later). Find the coefficients A , D and E .

$$V_s = 15 \text{ V}$$

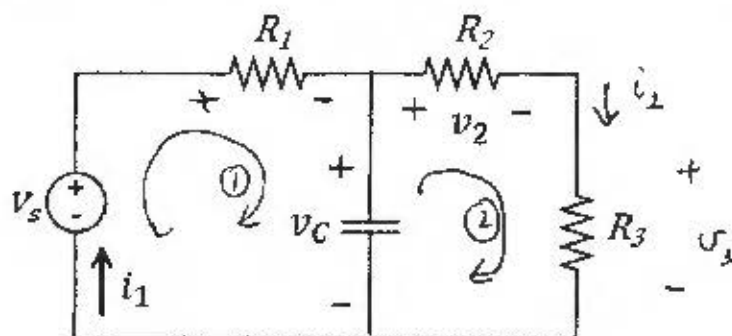
$$R_1 = 10 \, \Omega$$

$$R_2 = 15 \, \Omega$$

$$R_3 = 5 \, \Omega$$

$$v_C = 10 - 10 \cdot e^{-20t} \text{ V}$$

$$v_2 = A + B \cdot e^{-20t} \text{ V} \quad i_1 = D + E \cdot e^{-20t} \text{ A}$$



$$\text{KVL in } \textcircled{1} : v_s - v_{R_1} - v_C = 0 \quad v_{R_1} = i_1 \cdot R_1$$

$$\Rightarrow i_1 = \frac{1}{R_1} \cdot (v_s - v_C) = \frac{1}{10} \left(15 - 10 + 10 e^{-20t} \right) \\ = \frac{1}{10} \left(5 + 10 e^{-20t} \right)$$

$$\boxed{D = 0.5} \quad \boxed{E = 1}$$

$$\text{KVL in } \textcircled{2} : v_C - v_2 - v_3 = 0$$

$$v_2 = i_2 \cdot R_2$$

$$v_3 = i_2 \cdot R_3$$

$$\Rightarrow v_C = v_2 + v_3 = i_2 (R_2 + R_3)$$

$$\Rightarrow v_2 = R_2 \cdot i_2 = v_C \cdot \frac{R_2}{R_2 + R_3} \\ = v_C \cdot \frac{15}{20}$$

\leadsto THIS COULD ALSO BE FOUND DIRECTLY WITH VOLTAGE DIVIDER

$$\Rightarrow v_2 = 7.5 - 7.5 e^{-20t}$$

$$\boxed{A = 7.5} \quad \boxed{B = -7.5}$$