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## ECE 65 Fall 2018 Midterm Exam Answer Sheet

### Problem 1. (10 points)

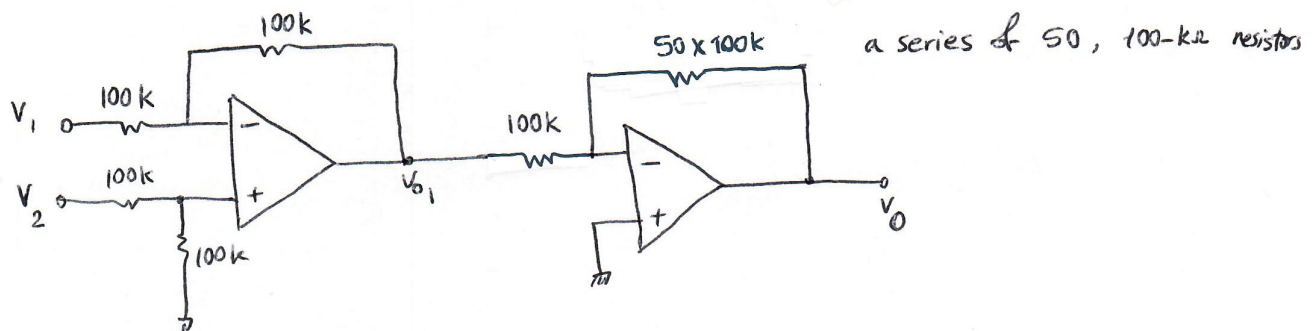
In a system, it is required to take the difference between two signals,

$$v_1 = 4 \sin(2\pi \times 50t) + 0.01 \sin(2\pi \times 2000t)$$

$$v_2 = 4 \sin(2\pi \times 50t) - 0.01 \sin(2\pi \times 2000t)$$

such that the 50-Hz component is eliminated and the 2000-Hz component is amplified with a gain of 40 dB. Design the circuit using **two** ideal op-amps and 100 k $\Omega$  resistors. Assume opamps have  $V_{sat} = \pm 10V$ .

One possible design is as following



$$V_{o1} = \frac{100k}{100k} (V_2 - V_1) = -0.02 \sin(2\pi \times 2000t)$$

$$V_o = -\frac{50 \times 100k}{100k} \times V_{o1} = 1 \sin(2\pi \times 2000t)$$

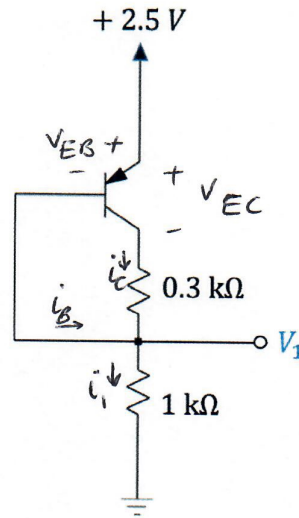
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**Problem 2.** (10 points)

In the following circuit, find the values of the collector and base currents and the node voltage

V1. Assume  $\beta = 100$ ,  $V_{D0} = 0.7 \text{ V}$ ,  $V_{sat} = 0.2 \text{ V}$ .



Assume BJT is off:  $V_{EB} < V_{D0}$  and  $i_B = 0$ ,  $i_C = 0$

$$\text{EB-KVL: } 2.5 \text{ V} = V_{EB} + 1 \text{ k} \times i_1$$

$$\text{KCL: } i_1 = i_B + i_C$$

$$i_B = i_C = 0 \rightarrow i_1 = 0 \rightarrow 2.5 \text{ V} = V_{EB} + 0 \rightarrow V_{EB} = 2.5 \text{ V} > V_{D0}$$

Assumption was wrong

BJT is ON, Assume Active mode of operation:  $i_C = \beta i_B$ ,  $V_{EC} \gg V_{D0}$   
 $V_{EB} = 0.7 \text{ V}$

$$i_1 = i_B + i_C = (1 + \beta) i_B$$

$$\text{EB-KVL: } 2.5 \text{ V} = 0.7 \text{ V} + 1 \text{ k} \times i_1 \rightarrow i_1 = 1.8 \text{ mA}$$

$$\rightarrow i_B = \frac{1.8 \text{ mA}}{101} = 17.8 \text{ } \mu\text{A}, \quad i_C = 1.78 \text{ mA}$$

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problem 2. cont.

$$EC - \text{kVL: } 2.5 = V_{EC} + 0.3k \times i_c + 1k \times i_1$$

$$2.5 = V_{EC} + 0.3k \times 1.78 \text{ mA} + 1k \times 1.8 \text{ mA}$$

$$\rightarrow V_{EC} = 0.166 \text{ V} < V_{D_0} \rightarrow \text{Assumption was wrong}$$

Assume saturation:  $V_{EC} = 0.2 \text{ V}$ ,  $i_c < \beta i_B$

$$EC - \text{kVL: } 2.5 \text{ V} = 0.2 + 0.3k \times i_c + 1k \times i_1$$

$$EB - \text{kVL: } 2.5 \text{ V} = 0.7 \text{ V} + 1k \times i_1 \rightarrow \boxed{i_1 = 1.8 \text{ mA}} \quad \text{not changed}$$

$$\rightarrow 2.3 \text{ V} = 0.3k \times i_c + 1.8 \text{ V} \rightarrow \boxed{i_c = 1.67 \text{ mA}}$$

$$i_B = i_1 - i_c = 0.13 \text{ mA}, \quad \beta i_B = 13 \text{ mA} > i_c \quad \checkmark$$

$$\boxed{i_B = 0.13 \text{ mA}}$$

Assumption is correct.

BJT is in saturation

$$\boxed{V_1 = i_1 \times 1k = 1.8 \text{ V}}$$

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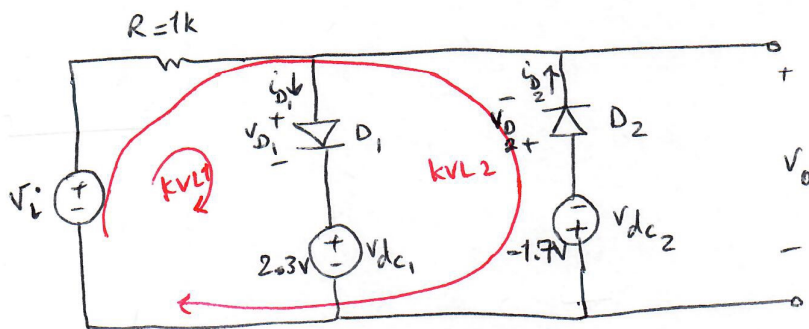
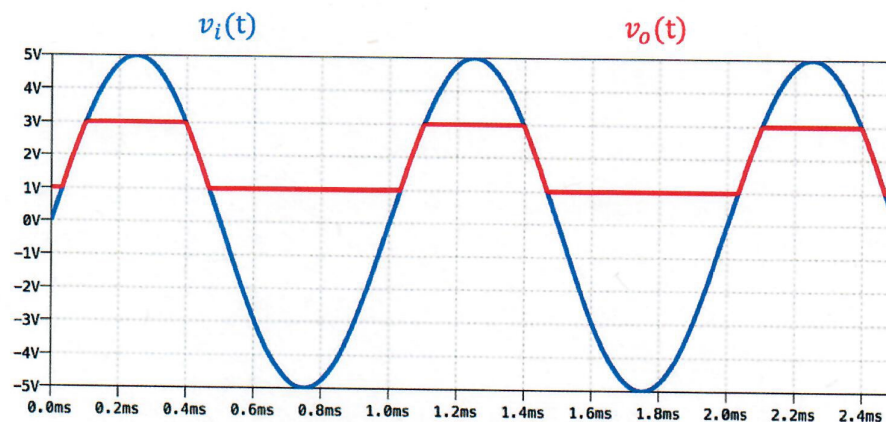
**Problem 3. (10 points)**

**Part a. (8 points)**

- I. Design a two-port network using diodes (a diode waveform shaping circuit) that would generate the output waveform shown in the below graph when the input signal  $v_i = 5 \sin(\omega t)$  is applied to the network. On the graph,  $v_i(t)$  is drawn in blue color and  $v_o(t)$  is drawn in red color.

You can use regular PN junction diodes, Zener diodes, voltage sources and any other circuit elements in your design.

- II. Draw the transfer function for this circuit.



When  $D_1$  is ON and  $D_2$  is OFF,  $v_{D1} = 0.7$ ,  $i_{D1} \geq 0$ ,  $v_{D2} < 0.7$ ,  $i_{D2} = 0$

$$v_o = v_{D1} + v_{dc1} = v_{D1} + 2.3V = 3V \rightarrow \boxed{v_o = 3V}$$

$$\text{KVL1: } i_{D1} = \frac{v_i - (v_{D1} + v_{dc1})}{R}, \quad i_{D1} \geq 0 \rightarrow \boxed{v_i \geq 3V}$$

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When  $D_2$  is ON and  $D_1$  is off,  $i_{D_2} \geq 0$ ,  $v_{D_2} = 0.7$ ,  $v_{D_1} < 0.7$ ,  $i_{D_1} = 0$

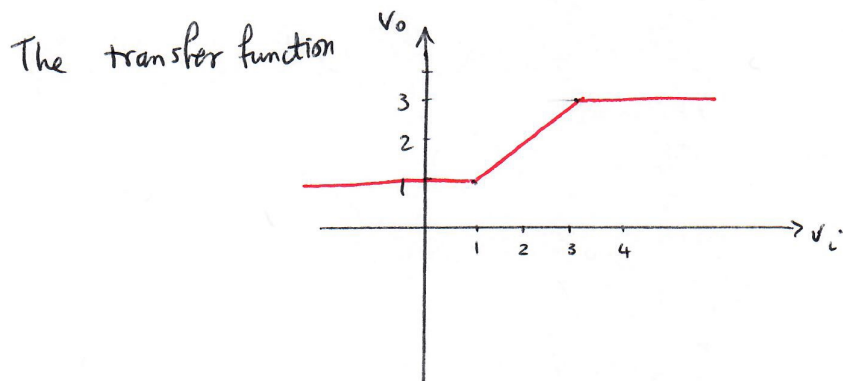
$$V_o = -v_{D_2} - v_{dc_2} = -0.7 - (-1.7V) = 1V \rightarrow \boxed{V_o = 1V}$$

$$\text{KVL2: } v_i = -R i_{D_2} - v_{D_2} - v_{dc_2}$$

$$i_{D_2} \geq 0 \rightarrow \frac{-v_i - v_{D_2} - v_{dc_2}}{R} \geq 0 \rightarrow \frac{-v_i - 0.7 - (-1.7)}{1k} \geq 0$$

$$\rightarrow \boxed{v_i \leq 1V}$$

For  $\boxed{1V < v_i < 3V}$ ,  $D_1$  &  $D_2$  are off &  $\boxed{V_o = v_i}$





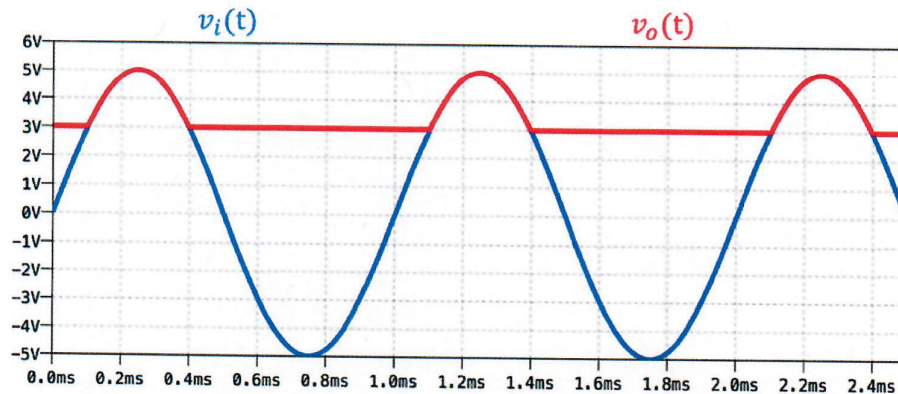
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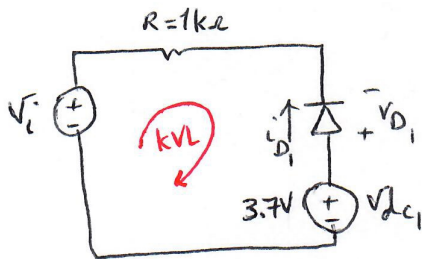
**Part b. (2 points)**

Design a two-port network using diodes (a diode waveform shaping circuit) that would generate the output waveform shown in the below graph when the input signal  $v_i = 5 \sin(\omega t)$  is applied to the network. On the graph,  $v_i(t)$  is drawn in blue color and  $v_o(t)$  is drawn in red color.

You can use regular PN junction diodes, Zener diodes, voltage sources and any other circuit elements in your design.



From the graph, when  $v_i \geq 3V \rightarrow v_o = v_i$  and when  $v_i \leq 3V \rightarrow v_o = 3V$



when  $D_1$  is ON:  $V_{D_1} = 0.7V$ ,  $i_{D_1} \geq 0$

$$\text{KVL: } v_i = -i_{D_1} \times 1k\Omega - V_{D_1} + V_{dc1}$$

$$i_{D_1} = \frac{-v_i - V_{D_1} + V_{dc1}}{1k\Omega} \geq 0$$

$$\rightarrow v_i \leq -V_{D_1} + V_{dc1}$$

$$v_i \leq -0.7 + 3.7 = 3V$$

$$V_o = -V_{D_1} + V_{dc1} = 3V$$

$$\rightarrow \boxed{v_i \leq 3V} \text{ and } \boxed{v_o = 3V}$$

for  $v_i > 3V$ ,  $D_1$  is off and  $i_{D_1} = 0 \rightarrow V_o = 0 + v_i = v_i$ ,  $\boxed{V_o = v_i}$