

Complex numbers 006

Problem has been graded.

Hint: Solve this symbolically as much as you can and only plug in numbers at the very end.

Find P and Q .

Note: We've used bold capital letters to denote complex variables. The $*$ operator stands for complex conjugate. The $\text{Re}[]$ and $\text{Im}[]$ operators stand for taking the real part and imaginary part respectively.

Solve without a calculator

$$\begin{aligned} \mathbf{V}_0 &= ae^{j\frac{\pi}{6}} & \mathbf{Z}_1 &= 2 + j & \mathbf{Z}_2 &= bj \\ \mathbf{I}_1 &= \frac{\mathbf{V}_0}{\mathbf{Z}_1} & \mathbf{V}_1 &= \mathbf{Z}_2 \cdot \mathbf{I}_1 & \mathbf{S} &= \frac{1}{2} \cdot \mathbf{V}_1 \cdot \mathbf{I}_1^* \\ P &= \text{Re}[\mathbf{S}] & Q &= \text{Im}[\mathbf{S}] \end{aligned}$$

Given Variables:

$a : 2$.

$b : 1$.

Calculate the following:

$P(.) :$

0



$Q(.) :$

0.4



Hint: Work this out symbolically first and only plug in numbers later.