

Jan 10

Signal Transformation:

We know $x(t)$, How to draw $x(at+b)$?

1) scaling (a)

if $a > 1$, the signal compress (shrinks) along the axis

if $0 < a < 1$, the signal stretches (expand) along the time axis.

if $a < 0$, it also flips (mirrors) the signal about the vertical axis.

2) Shifting ($+b$):

if $b > 0$, the signal shift to the left (earlier in time).

if $b < 0$, the signal shifts to the right (later in time).

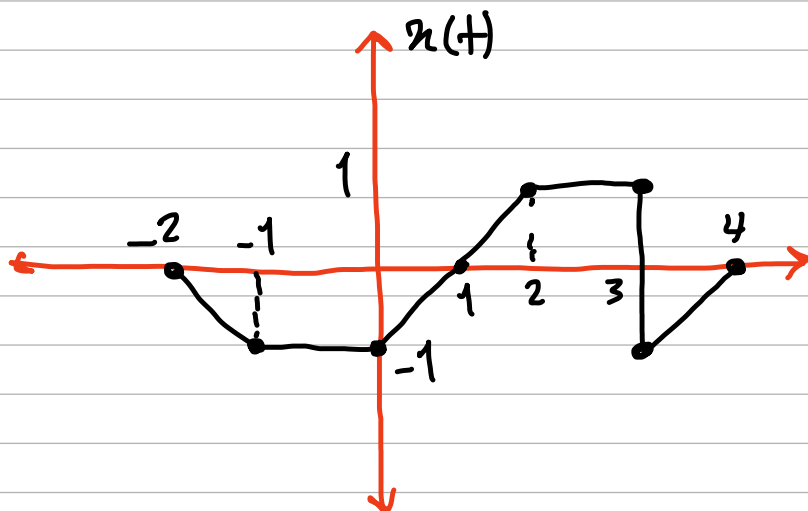
To draw $x(at+b)$, 1) shift by b
2) Scale by a

Double checking the critical point (peaks, zero crossing, discontinuities, etc).

$t' = at+b \rightarrow t = \frac{t'-b}{a}$, use this to determine where features of $x(t)$ map in $x(at+b)$

Question:

what is $x(2-t)$, $x(\frac{t}{2}-1)$, and $2x(-2t+3)+1$



phasor:

$$X(t) = \underbrace{A}_{\text{amplitude}} \cos(\underbrace{\omega t + \theta}_{\text{angular freq}}) = \text{Re} \left\{ \underbrace{A e^{j\theta}}_{\text{phasor}} e^{j\omega t} \right\}$$

phase angle

$$\sin(\omega t + \theta) = \cos(\omega t + \theta - \frac{\pi}{2})$$

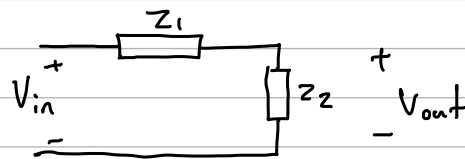
example: $x(t) = 5 \cos(100\pi t + \frac{\pi}{4}) \rightarrow X = 5 e^{j\frac{\pi}{4}}$

$$x(t) = 3 \sin(200\pi t + \frac{\pi}{6}) = 3 \cos(200\pi t + \frac{\pi}{6} - \frac{\pi}{2}) = 3 \cos(200\pi t - \frac{\pi}{3}) \Rightarrow X = 3 e^{-j\frac{\pi}{3}}$$

Capacitor: $i_C = C \frac{dv}{dt} \rightarrow I_C = j\omega C V_C \Rightarrow Z_C = \frac{1}{j\omega C}$

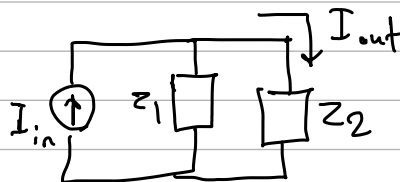
Inductor: $V = L \frac{di}{dt} \rightarrow V = j\omega L I \Rightarrow Z_L = j\omega L$

voltage divider:



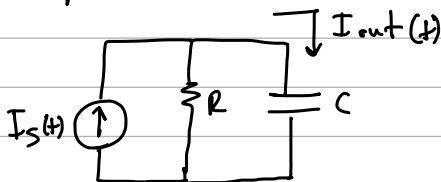
$$\frac{V_{out}}{V_{in}} = \frac{Z_2}{Z_1 + Z_2}$$

current divider



$$\frac{I_{out}}{I_{in}} = \frac{Z_1}{Z_1 + Z_2}$$

Example:



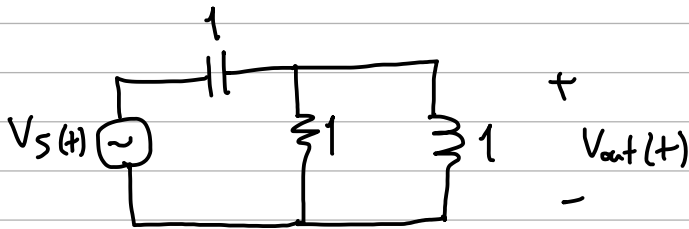
$$I_S(t) = A \cos(\omega t)$$

a) What is phasor of $I_S(t)$?

b) Find how I_{out} will relate to I_S in frequency domain?

c) compute $I_{out}(t)$

Example :



$$V_S(t) = 5 \cos\left(2t + \frac{\pi}{6}\right)$$

a) What is phasor of $V_S(t)$?

b) How V_{out} will relate to V_S in frequency domain?

c) Compute $V_{out}(t)$