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let f(+) be a periodic signal with period T, and frequency coefficient Fn.

 $f(+) \longleftrightarrow F_n$ 

① time shift:  $f'(t) = f(t-t_0) \longleftrightarrow F'_0 = F_0 e^{-jnw_0 t_0}$ 

2) time reversal:  $f'(+) = f(-+) \longleftrightarrow F'_n = F_n$ 

That is why if f(t) is even function (f'(t) = f(-t) = f(t)), we will have even frequency

coefficient (Fn'= Fn = Fn). The same for add functions.

3) time souling:  $f'(t) = f(at) \longleftrightarrow F'_n = F_n \qquad T_{new} = \frac{T}{\kappa}$ 

4 derivative:  $f'(t) = \frac{d}{dt} f(t) \longrightarrow F_n' = (jkw_n) F_n$ 

(5) Conjugate:  $f'(t) = f(t) \longleftrightarrow F_n' = F_n^*$ 

That is why if f(t) is real functions (f(t) = f(t)), we will have conjugate symmetry

 $(F'_n = F_n^* = F_n)$ . If f(t) is pure imaginary, we will have f'(t) = f'(t) = -f(t)

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Combining 2 and 5 says that

(6a) If f(+) is real and even, Fn is real and even.

(6b) If fltt is real and odd, Fn is imaginary and odd.

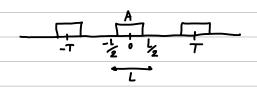
For f, (+) and f2(+) with period of T, and frequency response an and bn:

 $f_1(+) \longrightarrow a_n \qquad f_2(+) \longrightarrow b_n$ 

1) linearity: f(+) = Af(+) + Bf2(+) = Fn = Aan + Bbn

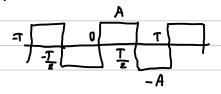
2) multiplication:  $f'(t) = f_1(t) f_2(t) = f$ 

pulse train



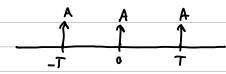
$$F_{n} = \begin{cases} n=0 : \frac{AL}{T} \\ n \neq 0 : \frac{A \sin(\frac{\pi L}{T}n)}{n\pi} = \frac{AL}{T} \sin(\frac{L}{T}n) \end{cases}$$

Square Wave



$$\begin{array}{c|c}
 & n = 0 & 0 \\
\hline
 & n = even & 0 \\
\hline
 & n = odd & \frac{2A}{jen}
\end{array}$$

delta train



$$F_n = \frac{A}{T}$$

parseval theorem:  $P_g = \frac{1}{T} \int |f(t)|^2 dt = \sum_{n=-\infty}^{\infty} |F_n|^2$ 

Example #1:
Consider two periodic signal with Fourier Series coefficient x(t) Es, ax and
y(t) is be. As usual, assume that x(t) has period T and thus fundamental frequency
$W_0 = \frac{2\eta}{T}$ . Use the properties of fourier series to answer following questions:
a) Find the period and FS coefficients of $y(t) = x(3t-5)$
b) Express $y(t)$ in terms of $X(t)$ if $b_k = 1 + (a_k - a_{-k}^*)$
c) Find the period and FS coefficients of $y(t) = x(1-t) \times (1)$ .
d) Compute 1 [   e junt n (3+-5)   2 dt

