

OPTION 1 t EXPRESSED IN SECONDS

$$f(t) = 3 \cdot 10^3 \cdot t, \quad 0 \leq t < 2 \cdot 10^{-3}$$
$$= -\sqrt{6}, \quad 2 \cdot 10^{-3} \leq t < 4 \cdot 10^{-3}$$

$$\begin{aligned} \frac{1}{T} \int_0^T f^2(t) dt &= \frac{1}{4 \cdot 10^{-3}} \left[\int_0^{2 \cdot 10^{-3}} (3 \cdot 10^3 t)^2 dt + \int_{2 \cdot 10^{-3}}^{4 \cdot 10^{-3}} (-\sqrt{6})^2 dt \right] \\ &= \frac{1}{4 \cdot 10^{-3}} \left[9 \cdot 10^6 \cdot \frac{t^3}{3} \Big|_0^{2 \cdot 10^{-3}} + 6 \cdot 2 \cdot 10^{-3} \right] \\ &= \frac{1}{4 \cdot 10^{-3}} \left[\frac{9 \cdot 8 \cdot 10^{-3}}{3} + 12 \cdot 10^{-3} \right] \\ &= \frac{24 + 12}{4} = \frac{36}{4} = 9 \end{aligned}$$

$$\sqrt{\frac{1}{T} \int_0^T f^2(t) dt} = \boxed{V_{rms} = 3V}$$

OPTION 2 t EXPRESSED IN ms

$$f(t) = 3 \cdot t, \quad 0 \leq t < 2$$
$$= -\sqrt{6}, \quad 2 \leq t < 4$$

$$\begin{aligned} \frac{1}{T} \int_0^T f^2(t) dt &= \frac{1}{4} \left[\int_0^2 (3t)^2 dt + \int_2^4 (\sqrt{6})^2 dt \right] = \frac{1}{4} \left[9 \frac{t^3}{3} \Big|_0^2 + 6 \cdot 2 \right] \\ &= \frac{1}{4} \left[\frac{9 \cdot 8}{3} + 12 \right] = \frac{36}{4} = 9 \end{aligned}$$

$$\boxed{V_{rms} = 3V}$$