

Circuit theorems 001

Problem has been graded.

A linear system has two inputs, v_a and v_b ,
and one output, v_{out} .

When $v_a = v_1$ and $v_b = v_2$, then $v_{out} = v_3$.

When $v_a = v_4$ and $v_b = v_5$, then $v_{out} = v_6$.

What is v_{out} , when $v_a = v_7$ and $v_b = v_8$?

Given Variables:

$v1 : 3 \text{ V}$

$v2 : 6 \text{ V}$

$v3 : 12 \text{ V}$

$v4 : 3 \text{ V}$

$v5 : 4 \text{ V}$

$v6 : 48 \text{ V}$

$v7 : 3 \text{ V}$

$v8 : 2 \text{ V}$

Calculate the following:

$v_{out} (\text{V}) :$

A linear system has two inputs, v_a and v_b , and one output, v_{out} .

$$v_1 = 8 \text{ V}$$

When $v_a = v_1$ and $v_b = v_2$, then $v_{out} = v_3$.

$$v_2 = 0 \text{ V}$$

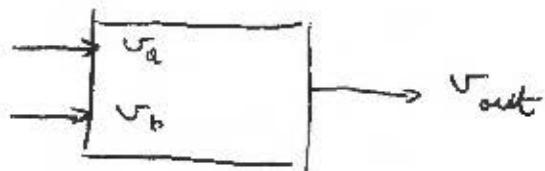
When $v_a = v_4$ and $v_b = v_5$, then $v_{out} = v_6$.

$$v_3 = 56 \text{ V}$$

What is v_{out} , when $v_a = v_7$ and $v_b = v_8$?

$$v_4 = 0 \text{ V}$$

$$v_5 = -9 \text{ V}$$



$$v_6 = 45 \text{ V}$$

$$v_7 = 5 \text{ V}$$

$$v_8 = 8 \text{ V}$$

$$a \cdot v_a + b v_b = v_{out}$$

$$\begin{cases} a \cdot 8 + b \cdot 0 = 56 \\ a \cdot 0 + b(-9) = 45 \end{cases}$$

$$\Rightarrow \begin{cases} a = \frac{56}{8} = 7 \\ b = \frac{45}{-9} = -5 \end{cases}$$

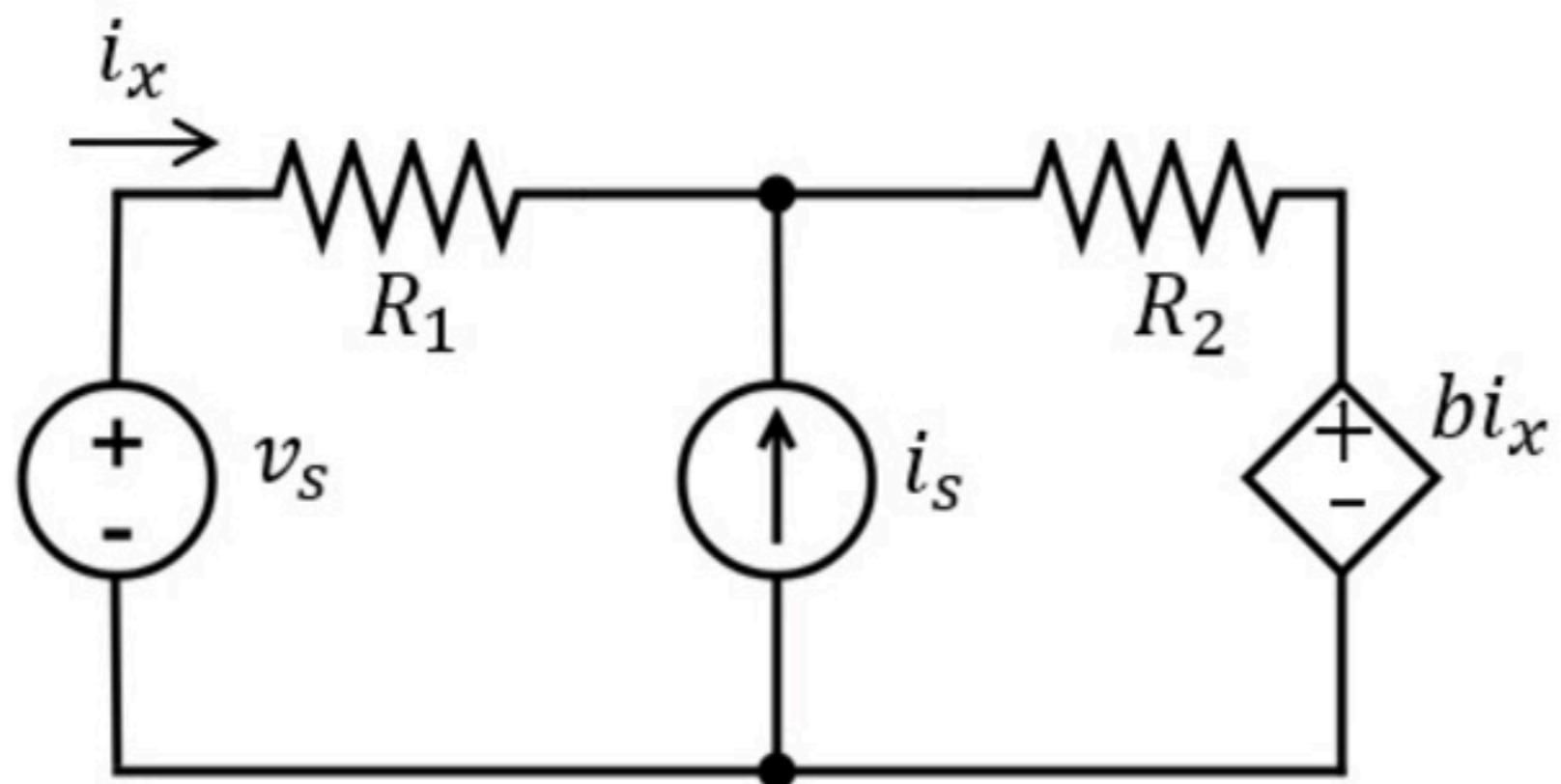
$$\Rightarrow a \cdot v_a + b v_b = 7 \cdot 5 + (-5) \cdot 8 \\ = -5 \text{ V}$$

$$v_{out} = -5 \text{ V}$$

Circuit theorems 002

Problem has been graded.

Use superposition to find i_x .



Given Variables:

$R_1 : 3 \text{ ohm}$

$R_2 : 4 \text{ ohm}$

$b : 4 \text{ V/A}$

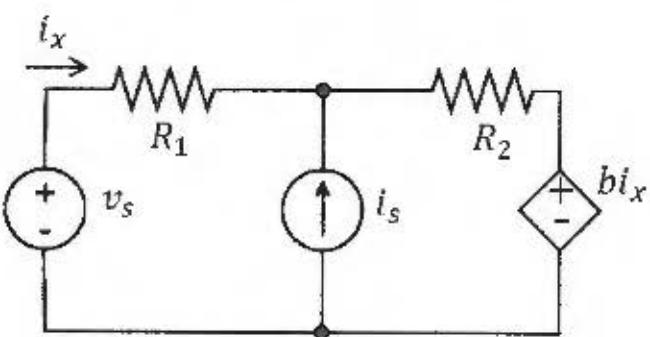
$v_s : 15 \text{ V}$

$i_s : 1 \text{ A}$

Calculate the following:

$i_x (\text{A}) :$

Use superposition to find i_x .



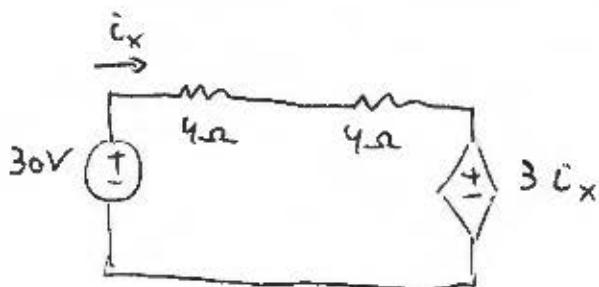
$$R_1 = 4 \text{ ohm}$$

$$R_2 = 4 \text{ ohm}$$

$$b = 3 \text{ V/A}$$

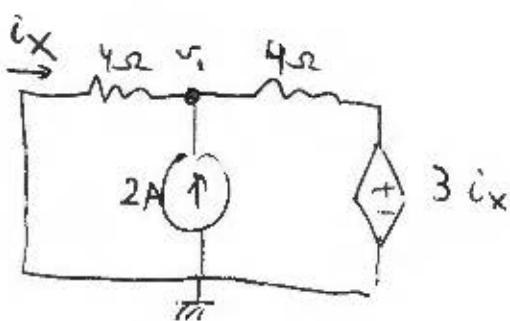
$$v_s = 30 \text{ V}$$

$$i_s = 2 \text{ A}$$



$$\text{KVL: } 30 = i_x \cdot 4 + i_x \cdot 4 + 3i_x$$

$$i_x = \frac{30}{11} \text{ A}$$



$$\text{node: } \frac{v_1}{4} - 2 + \frac{v_1 - 3i_x}{4} = 0$$

$$v_1 - 8 + v_1 - 3\left(-\frac{v_1}{4}\right) = 0$$

$$\text{if } v_1 = 32$$

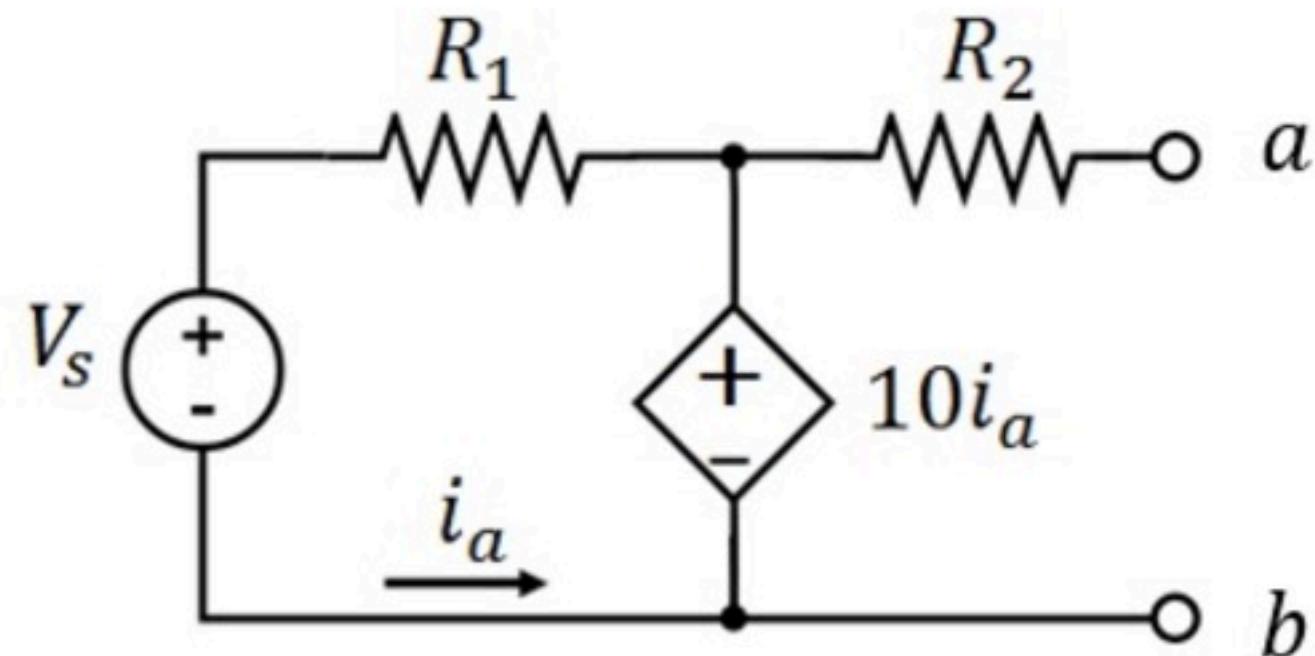
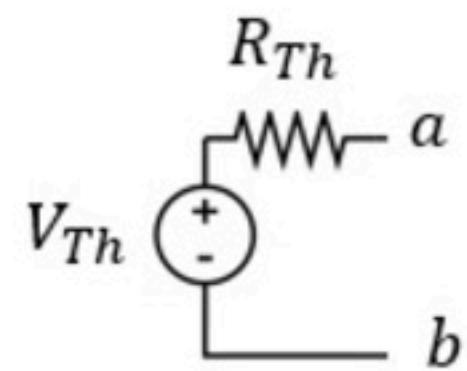
$$v_1 = \frac{32}{11} \Rightarrow i_x = -\frac{8}{11} \text{ A}$$

$$i_x = \frac{30}{11} - \frac{8}{11} = \frac{22}{11} \text{ A} \Rightarrow \boxed{i_x = 2 \text{ A}}$$

Circuit theorems 003

Unlimited Attempts.

Find the Thevenin equivalent model of this circuit, as seen between a and b.



Given Variables:

$R_1 : 9 \text{ ohm}$

$R_2 : 2 \text{ ohm}$

$V_s : 5 \text{ V}$

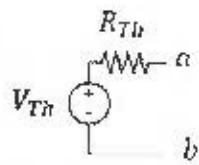
Calculate the following:

$V_{th} (\text{V}) :$

$R_{th} (\text{ohm}) :$

Hint: Find any two of V_{oc} , I_{sc} and R_{eq}

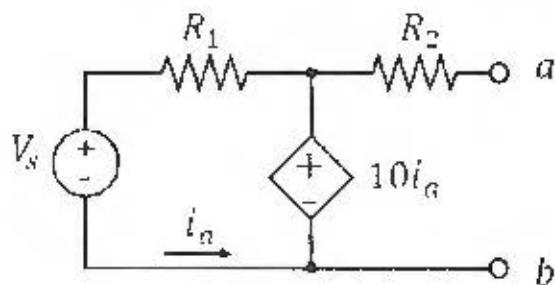
Find the Thevenin equivalent model of this circuit, as seen between a and b.



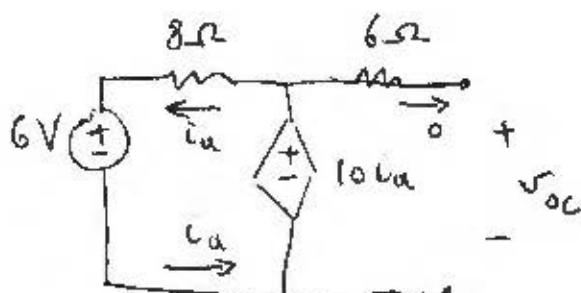
$$R_1 = 8 \text{ ohm}$$

$$R_2 = 6 \text{ ohm}$$

$$V_s = 6 \text{ V}$$



(*)

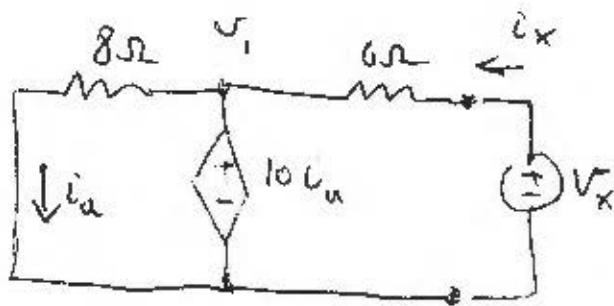


$$i_a = \frac{10i_a - 6}{8}$$

$$2i_a = 6 \Rightarrow i_a = 3 \text{ A}$$

$$V_{OC} = 10i_a = 30 \text{ V}$$

(*)



$$V_i = 10i_a = 8i_a$$

$$2i_a = 0 \Rightarrow i_a = 0$$

$$\Rightarrow i_x = \frac{V_x - 0}{6}$$

$$\Rightarrow \frac{V_x}{i_x} = 6 \Omega$$

$$R_{TH} = 6 \Omega$$

$$V_{TH} = 30 \text{ V}$$

Circuit theorems 004

Unlimited Attempts.

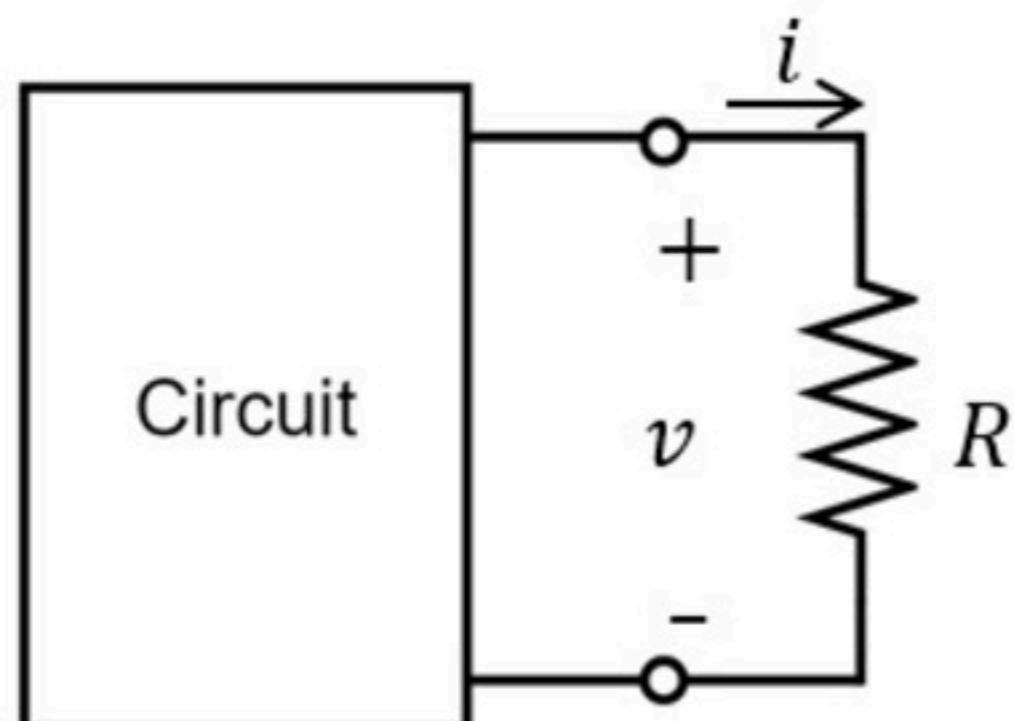
The box contains a linear circuit.

When $R = R_1$, we measure $i = I_1$.

When $R = R_2$, we measure $i = I_2$.

What value of $R = R_3$ results in $i = I_3$?

What is the maximum value of $i = i_{max}$ that can be achieved (assuming $R \geq 0$)?



Given Variables:

$R_1 : 1 \text{ ohm}$

$R_2 : 3 \text{ ohm}$

$I_1 : 10 \text{ A}$

$I_2 : 6 \text{ A}$

$I_3 : 2 \text{ A}$

Calculate the following:

$R_3 (\text{ohm}) :$

$i_{max} (\text{A}) :$

The box contains a linear circuit.

$$R_1 = 5 \text{ ohm}$$

When $R = R_1$, we measure $i = I_1$.

$$R_2 = 8 \text{ ohm}$$

When $R = R_2$, we measure $i = I_2$.

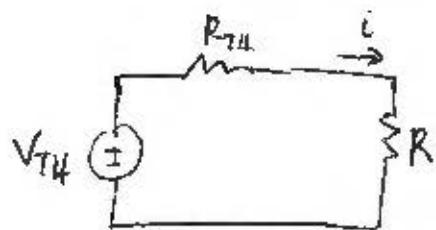
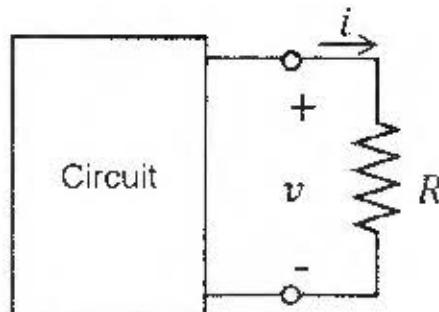
$$I_1 = 4 \text{ A}$$

What value of $R = R_3$ results in $i = I_3$?

$$I_2 = 3 \text{ A}$$

What is the maximum value of $i = i_{max}$ that can be achieved (assuming $R \geq 0$)?

$$I_3 = 2 \text{ A}$$



$$\textcircled{1} \quad I_1 = \frac{V_{TH}}{R_{TH} + 5} \Rightarrow 4 R_{TH} + 20 = V_{TH}$$

$$\textcircled{2} \quad I_2 = \frac{V_{TH}}{R_{TH} + 8} \Rightarrow 3 R_{TH} + 24 = V_{TH}$$

$$\textcircled{1} - \textcircled{2} \Rightarrow R_{TH} = 4 \Omega$$

$$V_{TH} = 36 \text{ V}$$

$$\textcircled{3} \quad I_3 = \frac{V_{TH}}{R_{TH} + R} = \frac{36}{4 + R} \Rightarrow R + R_{TH} = 18 \Rightarrow \boxed{R = 14 \Omega}$$

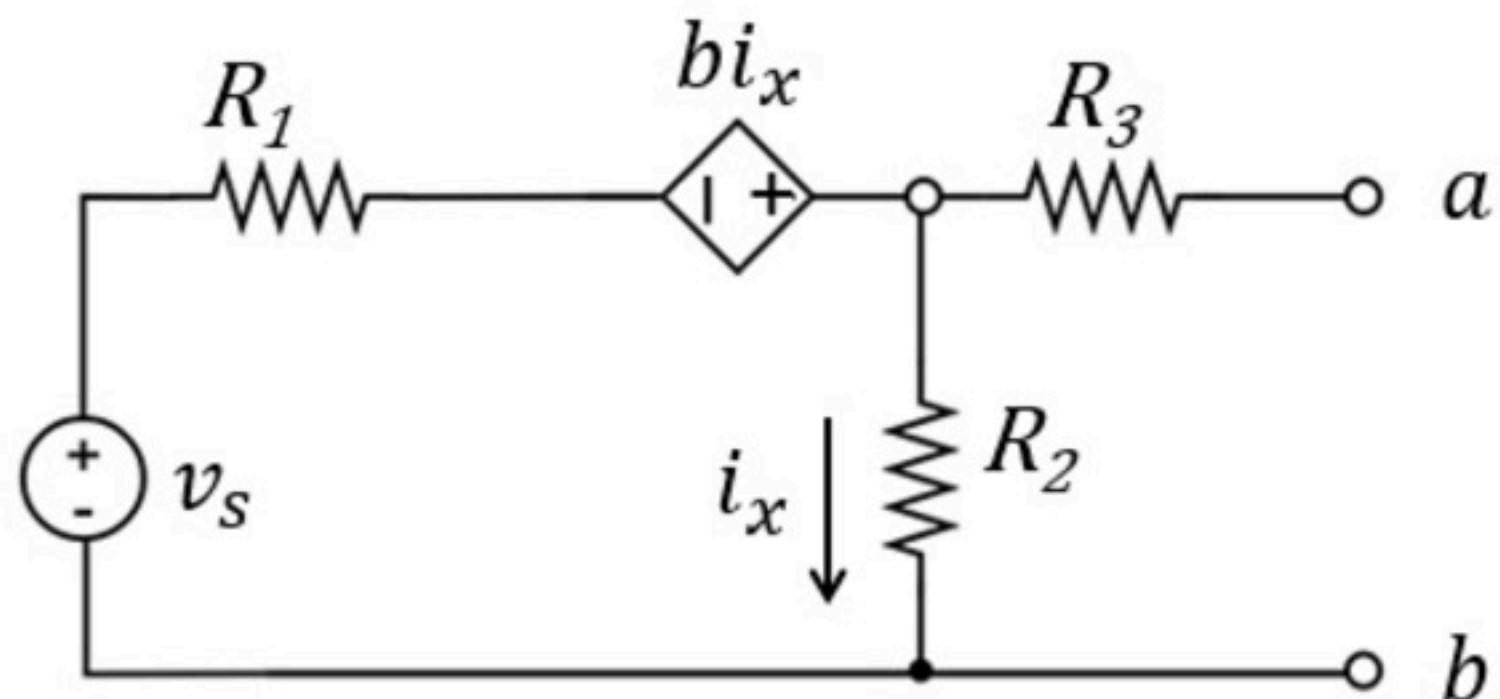
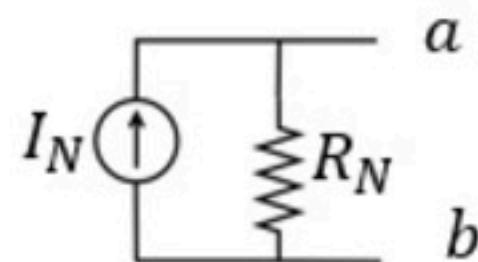
$$\textcircled{4} \quad i_{max} \text{ WHEN } R=0 \Rightarrow i_{max} = \frac{V_{TH}}{R_{TH}} = \frac{36}{4} = 9$$

$$\boxed{i_{max} = 9 \text{ A}}$$

Circuit theorems 005

Problem has been graded.

Find the Norton equivalent model of this circuit, as seen between a and b.



Given Variables:

$R_1 : 2 \text{ ohm}$

$R_2 : 6 \text{ ohm}$

$R_3 : 3 \text{ ohm}$

$v_s : 18 \text{ V}$

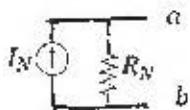
$b : 6 \text{ V/A}$

Calculate the following:

$I_N (\text{A}) :$

$R_N (\text{ohm}) :$

Find the Norton equivalent model of this circuit, as seen between a and b.



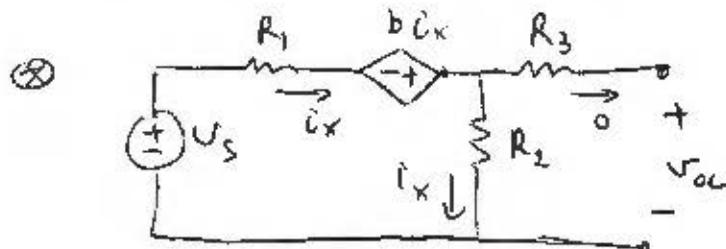
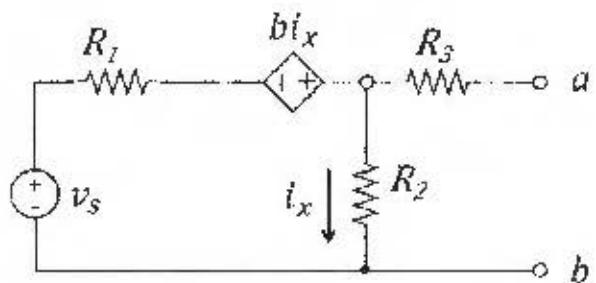
$$R_1 = 2 \text{ ohm}$$

$$R_2 = 4 \text{ ohm}$$

$$R_3 = 4 \text{ ohm}$$

$$v_s = 12 \text{ V}$$

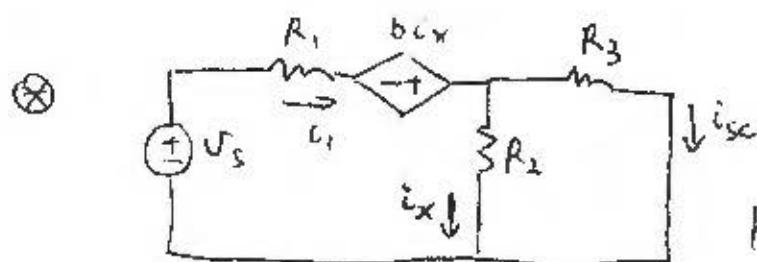
$$b = 2 \text{ A/V}$$



$$\text{KVL: } v_s - R_1 i_x + b i_x - R_2 i_x = 0$$

$$12 - 2i_x + 3i_x - 4i_x = 0$$

$$i_x = 3 \text{ A} \Rightarrow V_{oc} = R_2 i_x = 12 \text{ V}$$



$$i_x = \frac{R_3}{R_2 + R_3} i_1 = \frac{4}{8} i_1 \Rightarrow i_x = \frac{i_1}{2}$$

$$\text{KVL: } v_s - R_1 i_1 + b i_x - R_2 i_x = 0$$

$$12 - 2 \cdot 2 \cdot i_x + 2 \cdot i_x - 4i_x = 0$$

$$6i_x = 12 \Rightarrow i_x = 2 \text{ A}$$

$$I_{sc} = i_1 - i_x = 2 \text{ A}$$

$$V_{oc} = 12 \text{ V}$$

$$I_{sc} = 2 \text{ A}$$

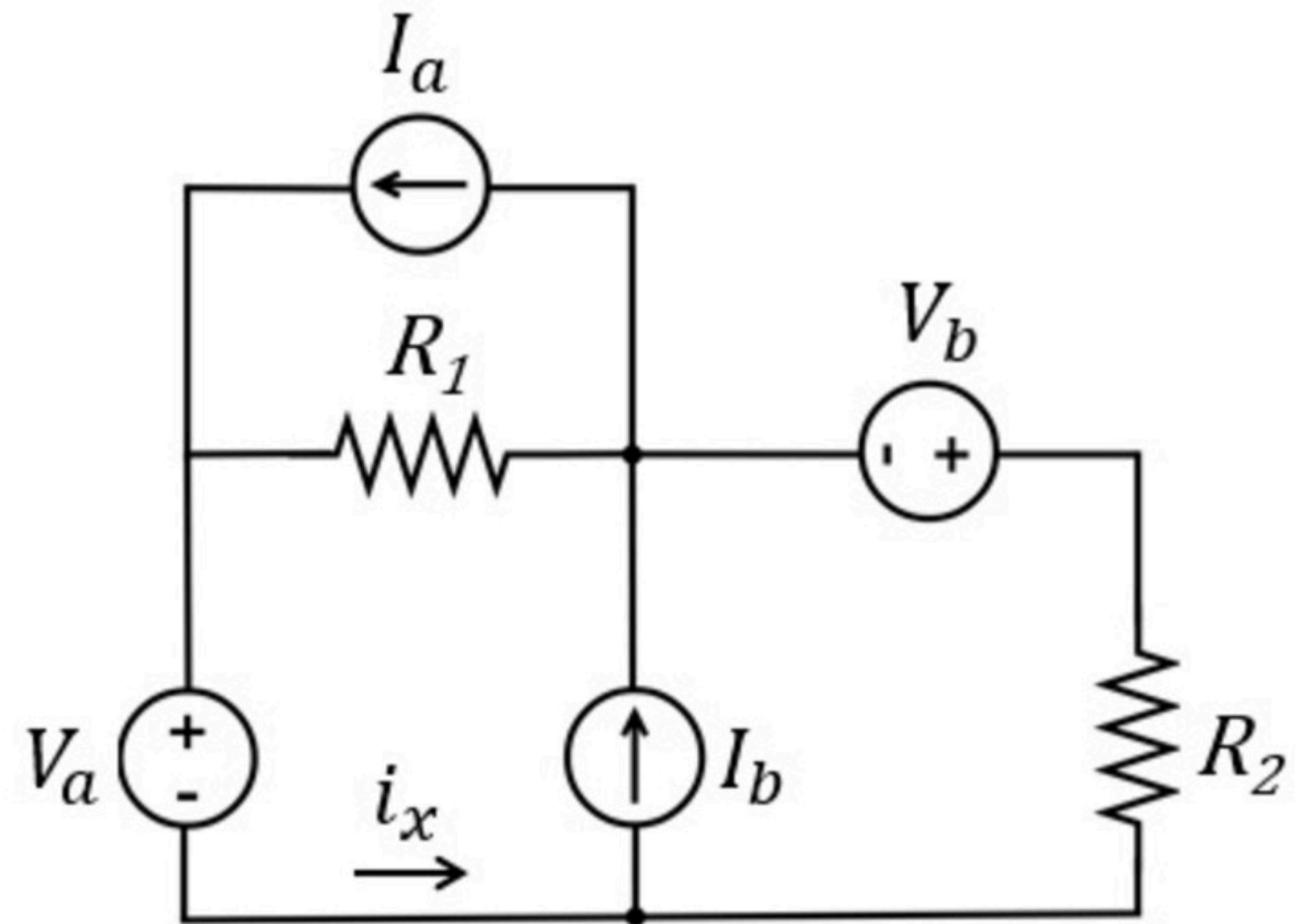
$$\Rightarrow I_N = 2 \text{ A}$$

$$R_N = \frac{V_{oc}}{I_{sc}} = 6 \text{ ohm} \Rightarrow R_N = 6 \text{ ohm}$$

Circuit theorems 006

Problem has been graded.

Use source transformations to find the current i_x .



Given Variables:

$V_a : 12 \text{ V}$

$V_b : 6 \text{ V}$

$I_a : 5 \text{ A}$

$I_b : 2 \text{ A}$

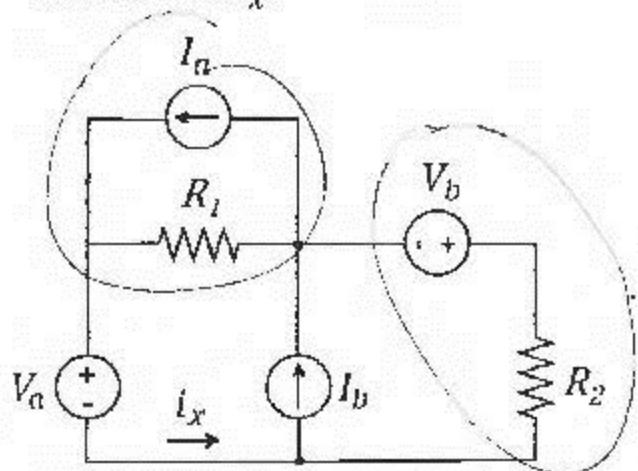
$R_1 : 15 \text{ ohm}$

$R_2 : 12 \text{ ohm}$

Calculate the following:

$i_x (\text{A}) :$

Use source transformations to find the current i_x .



$$V_a = 12 \text{ V}$$

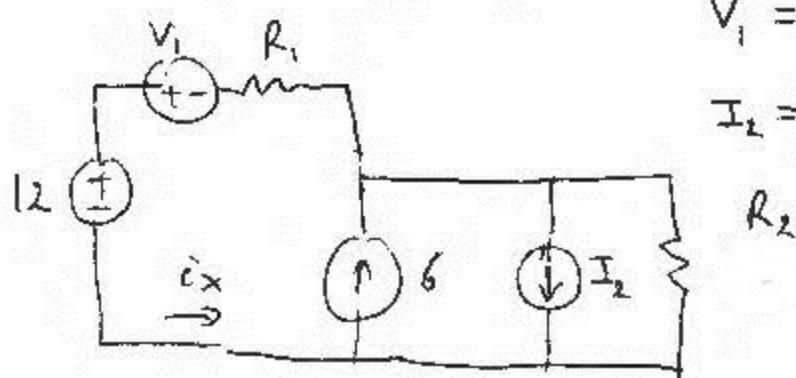
$$V_b = 6 \text{ V}$$

$$I_a = 4 \text{ A}$$

$$I_b = 6 \text{ A}$$

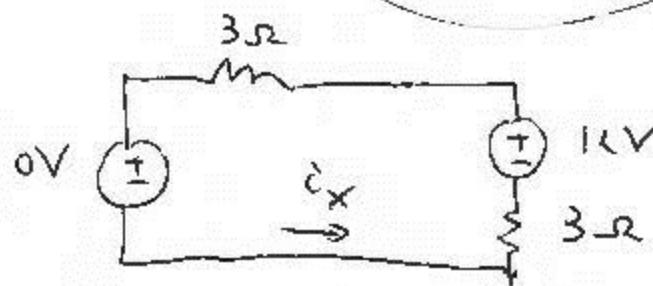
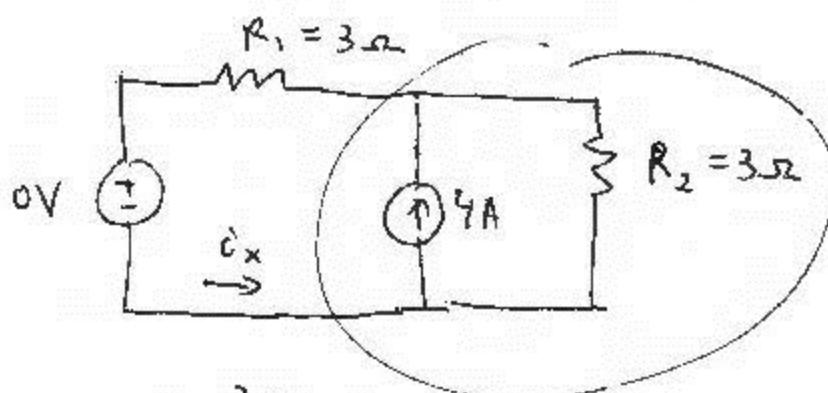
$$R_1 = 3 \text{ ohm}$$

$$R_2 = 3 \text{ ohm}$$



$$V_1 = I_a \cdot R_1 = 4 \cdot 3 = 12 \text{ V}$$

$$I_L = \frac{V_b}{R_2} = \frac{6}{3} = 2 \text{ A}$$



$$i_x = \frac{12 \text{ V}}{6 \text{ ohm}} = 2 \text{ A}$$

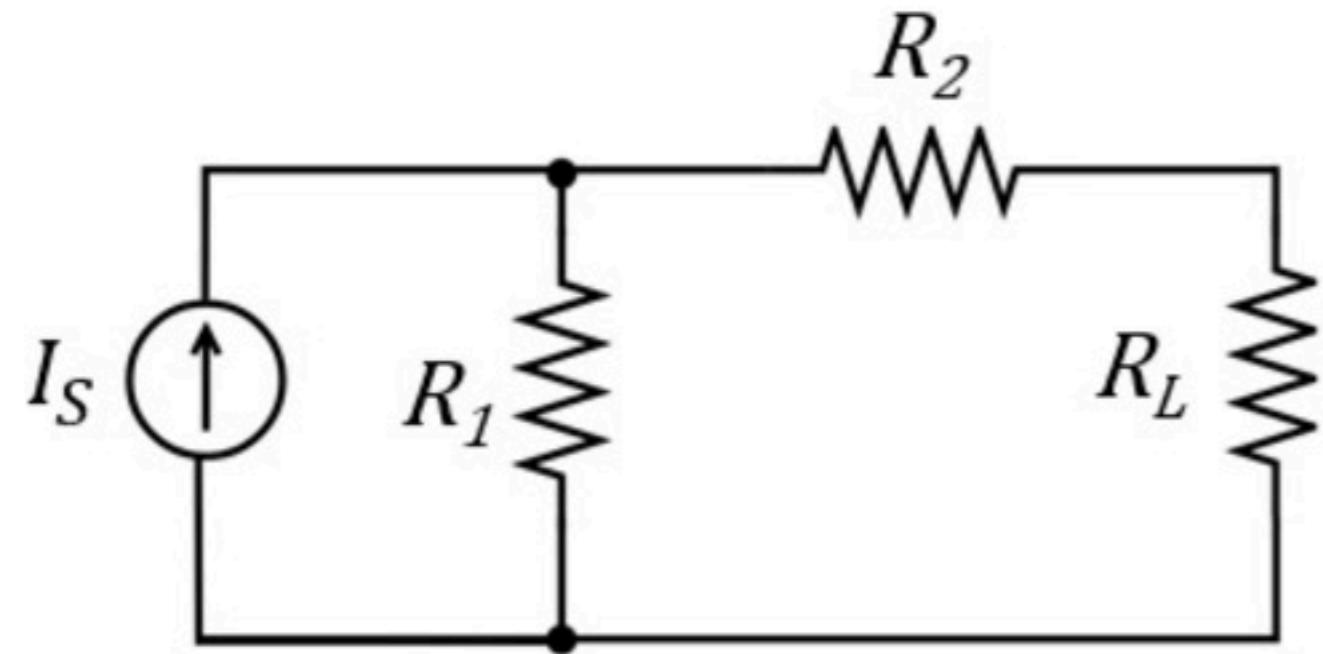
$i_x = 2 \text{ A}$

Circuit theorems 007

Unlimited Attempts.

Find the R_L for maximum power transfer.

Find the max power transferred to R_L .



Given Variables:

$I_S : 12 \text{ A}$

$R_1 : 4 \text{ ohm}$

$R_2 : 12 \text{ ohm}$

Calculate the following:

$R_L (\text{ohm}) :$

$P_{\max} (\text{W}) :$

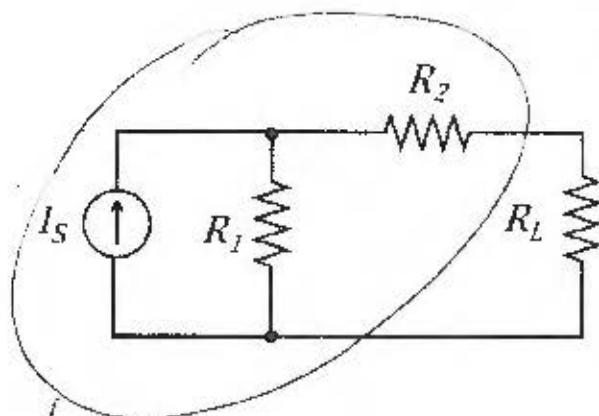
Hint: Replace the circuit (without the load) by its Thevenin model.

Find the R_L for maximum power transfer.

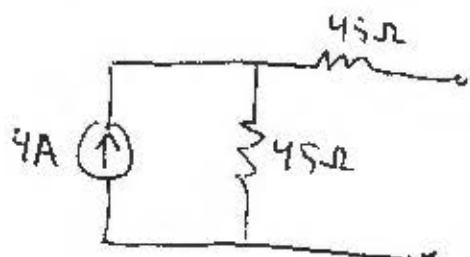
$$I_s = 4 \text{ A}$$

Given I_s , find the max power transferred to R_L .

$$R_1 = 45 \text{ ohm}$$

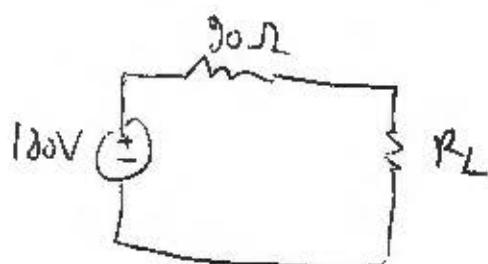


FIND THEVENIN MODEL



$$V_{oc} = 4 \cdot 45 = 180 \text{ V}$$

$$R_{TH} = 45 + 45 = 90 \text{ ohm}$$



FOR MAX POWER
TRANSFER

$$R_L = R_{TH} = 90 \text{ ohm}$$

$$R_L = 90 \text{ ohm}$$

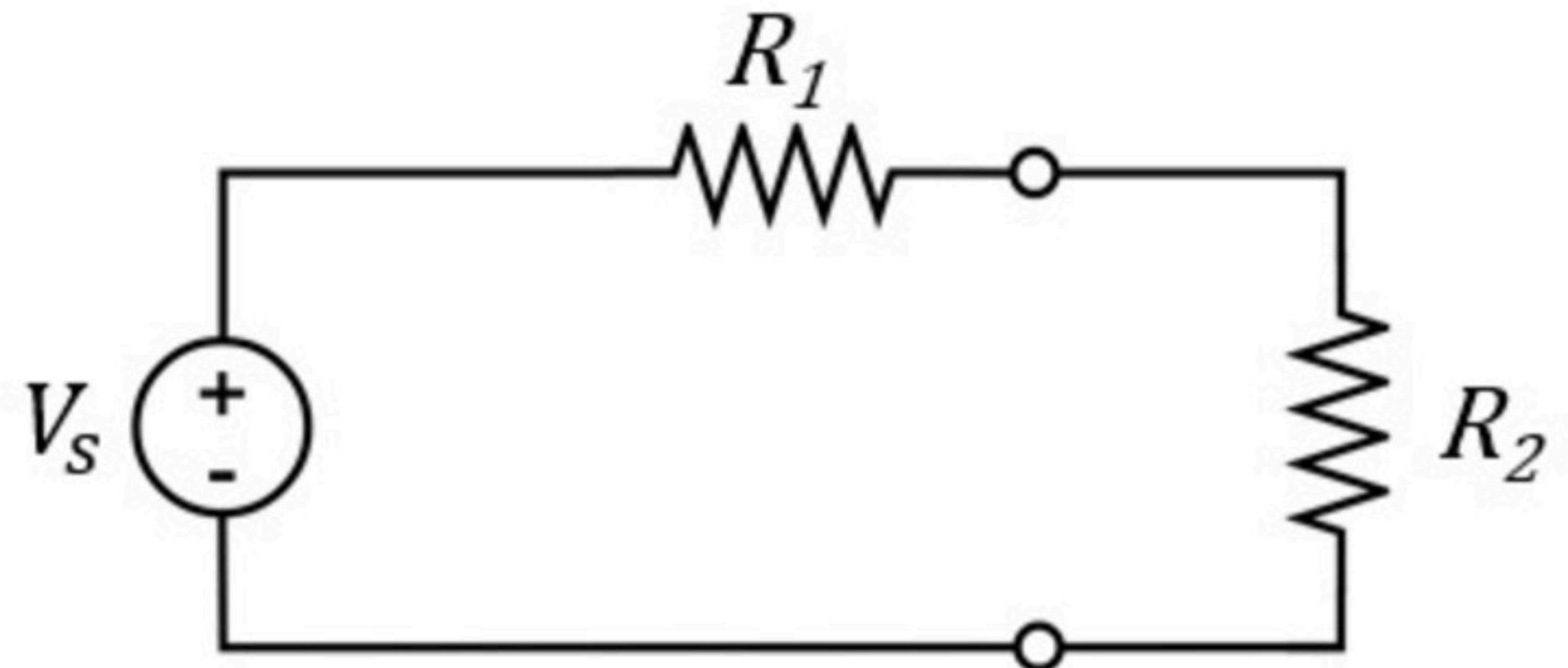
$$P = R_L \cdot i^2 \quad i = \frac{180}{90 + R_L} \approx 1 \text{ A}$$

$$P_{MAX} = 90 \text{ W}$$

Circuit theorems 008

Problem has been graded.

Determine the resistance R_1 such that the power dissipated in R_2 is maximum.



Given Variables:

$V_s : 12 \text{ V}$

$R_2 : 7 \text{ ohm}$

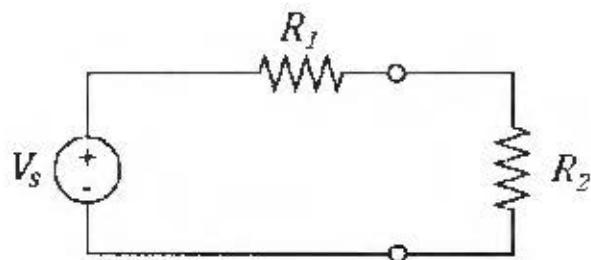
Calculate the following:

$R_1 \text{ (ohm) :}$

Determine the resistance R_1 such that the power dissipated in R_2 is maximum.

$V_s = 12 \text{ V}$

$R_2 = 3 \text{ ohm}$



$$I = \frac{V_s}{R_1 + R_2}$$

$$\begin{aligned} P &= R_2 I^2 \\ &= \frac{R_2 V_s^2}{(R_1 + R_2)^2} \end{aligned}$$

$$P = \frac{3 \cdot 144}{(R_1 + 3)^2}$$

$$\frac{dP}{dR_1} = -2 \cdot \frac{3 \cdot 144}{(R_1 + 3)^3} = 0 \Leftrightarrow R_1 = \infty$$

→ ALWAYS DECREASING

P_{MAX} WHEN

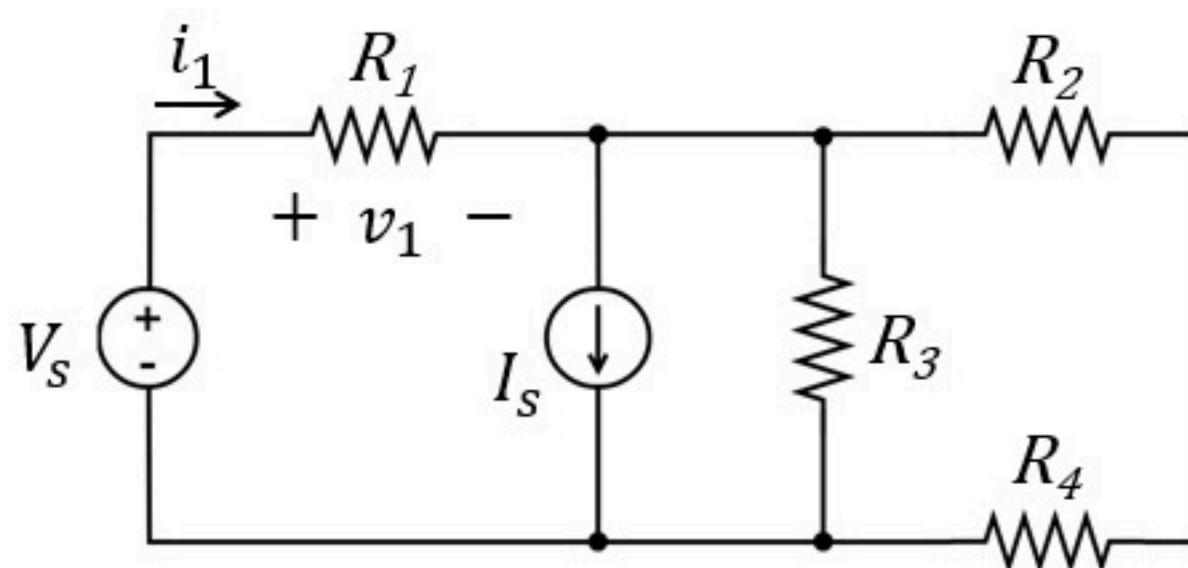
$$R_1 = 0 \text{ ohm}$$

Circuit theorems 009

Unlimited Attempts.

The resistance R_1 is a variable resistor that can take on values in the range $0 \leq R_1 \leq 24\Omega$.

1. Find the value of $R_1 = R_{1a}$ that maximizes current i_1 and the resulting maximum current $i_1 = i_{1a}$.
2. Find the value of $R_1 = R_{1b}$ that maximizes voltage v_1 and the resulting maximum voltage $v_1 = v_{1b}$.
3. Find the value of $R_1 = R_{1c}$ that maximizes the power received by R_1 and the resulting maximum power P_{1c} .



Given Variables:

$V_s : 36 \text{ V}$

$I_s : 2 \text{ A}$

$R_2 : 12 \text{ ohm}$

$R_3 : 18 \text{ ohm}$

$R_4 : 24 \text{ ohm}$

Calculate the following:

$i_{1a} (\text{A}) :$

$R_{1a} (\text{ohm}) :$

$v_{1b} (\text{V}) :$

$R_{1b} (\text{ohm}) :$

$P_{1c} (\text{W}) :$

$R_{1c} (\text{ohm}) :$

Hint: Replace the circuit (without R_1) by its Thevenin model.

The resistance R_1 is a variable resistor that can take on values in the range $0 \leq R_1 \leq 24\Omega$.

$$V_s = 12 \text{ V}$$

- Find the value of $R_1 = R_{1a}$ that maximizes current i_1 and the resulting current $i_1 = i_{1a}$.

$$I_s = 3 \text{ A}$$

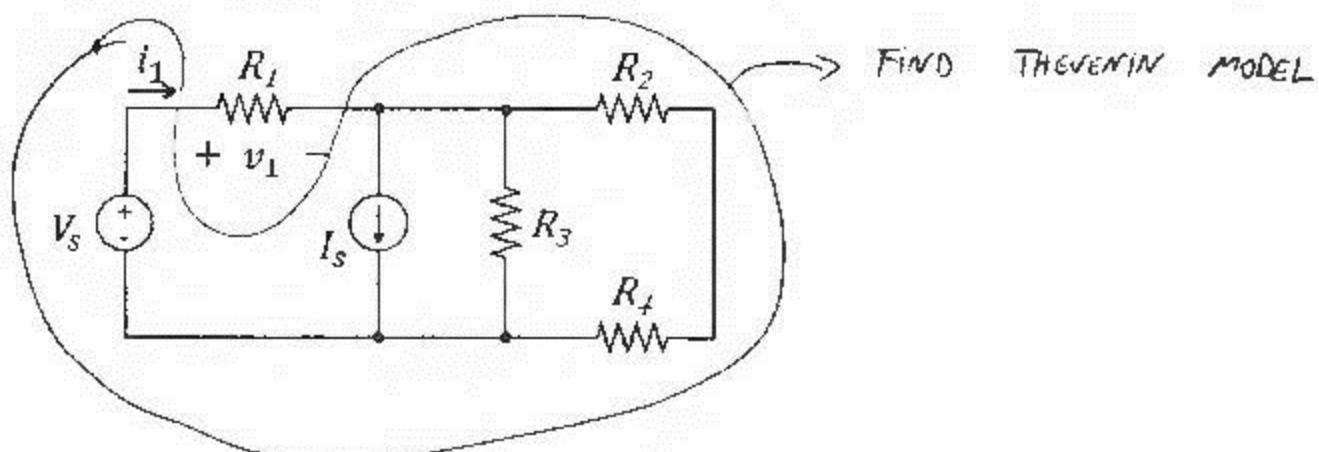
- Find the value of $R_1 = R_{1b}$ that maximizes voltage v_1 and the resulting current $v_1 = v_{1b}$.

$$R_2 = 12 \Omega$$

- Find the value of $R_1 = R_{1c}$ that maximizes the power received by R_1 and the resulting power P_{1c} .

$$R_3 = 18 \Omega$$

$$R_4 = 24 \Omega$$



$$\textcircled{1} \quad \text{Circuit: } \begin{array}{c} 12 \\ \parallel \\ 18 \quad 24 \end{array} \Rightarrow R_{TH} = 18 // (12 + 24) = \left(\frac{1}{18} + \frac{1}{36} \right)^{-1} = \left(\frac{3}{36} \right)^{-1} = 12 \Omega$$



$$\Rightarrow \begin{array}{c} 12\Omega \\ \parallel \\ 48V \\ \text{---} \\ R_1 \\ \text{---} \\ v_1 \end{array}$$

$$\textcircled{1} \quad R_1 = 0 \quad i_1 = \frac{48}{12} = 4 \Rightarrow i_1 = 4A$$

$$\textcircled{2} \quad R_1 = 24\Omega \quad v_1 = 48 \cdot \frac{24}{24+12} = 48 \cdot \frac{2}{3} = 32 \quad v_1 = 32V$$

$$\textcircled{3} \quad R_1 = R_{TH} \Rightarrow R_1 = 12\Omega$$

$$i_1 = \frac{48}{24} = 2A \Rightarrow P = i^2 R = 4 \cdot 12$$

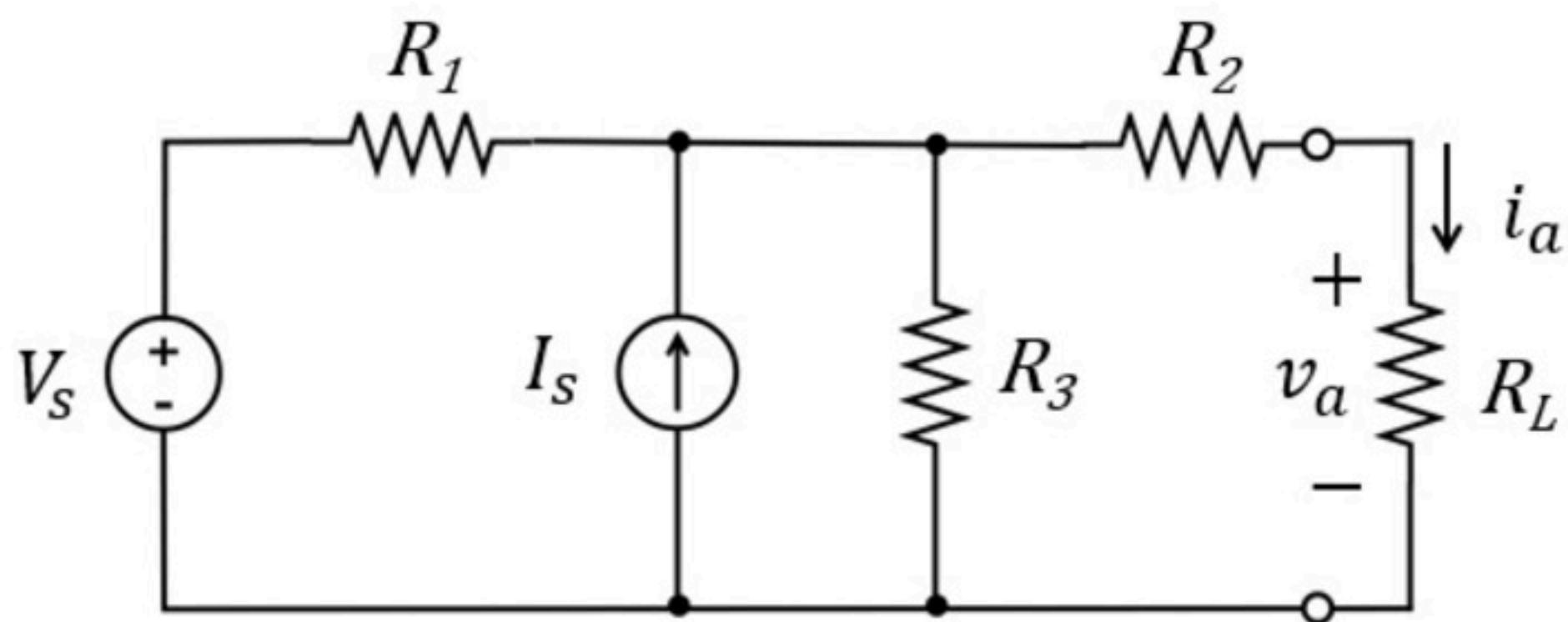
$$P = 48W$$

Circuit theorems 010

Unlimited Attempts.

Find (and think about how to minimize your calculations)

1. The value of $v_a = v_{a1}$ when $R_L = 12 \Omega$
2. The value of $R_L = R_{L2}$ that results in $v_a = 4 \text{ V}$
3. The value of $R_L = R_{L3}$ that results in $i_a = 1 \text{ A}$



Given Variables:

$V_s : 12 \text{ V}$

$I_s : 1 \text{ A}$

$R_1 : 6 \text{ ohm}$

$R_2 : 8 \text{ ohm}$

$R_3 : 12 \text{ ohm}$

Calculate the following:

$v_{a1} (\text{V}) :$

$R_{L2} (\text{ohm}) :$

$R_{L3} (\text{ohm}) :$

Find (and think about how to minimize your calculations)

1. The value of $v_a = v_{a1}$ when $R_L = 12 \Omega$
2. The value of $R_L = R_{L2}$ that results in $v_a = 4 V$
3. The value of $R_L = R_{L3}$ that results in $i_a = 1 A$

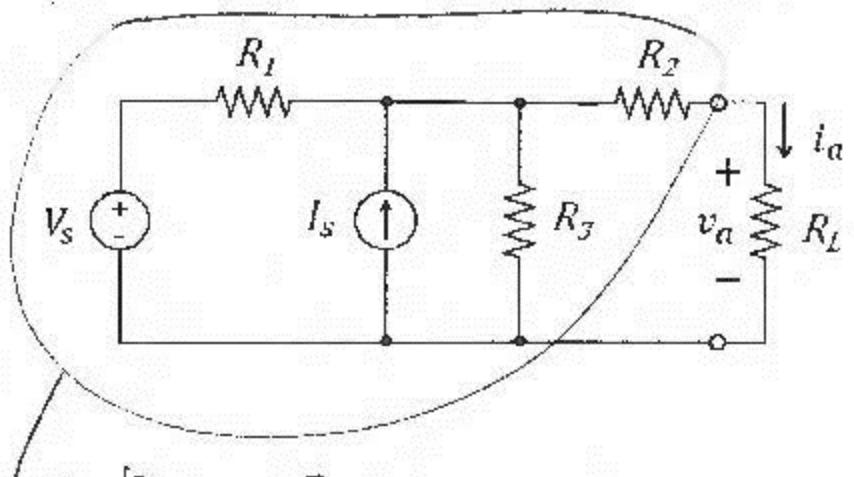
$$V_s = 12 V$$

$$I_s = 2 A$$

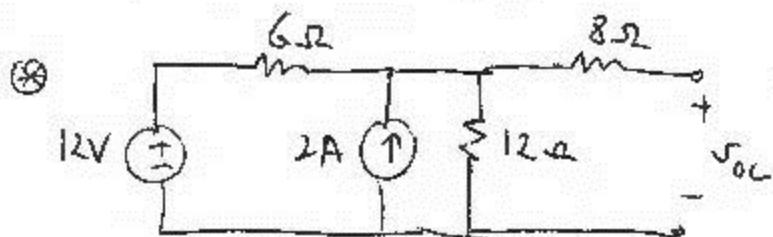
$$R_1 = 6 \Omega$$

$$R_2 = 8 \Omega$$

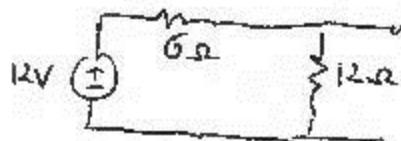
$$R_3 = 12 \Omega$$



FIND THEVENIN MODEL

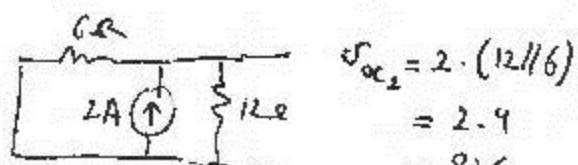


→ SUPERPOSITION

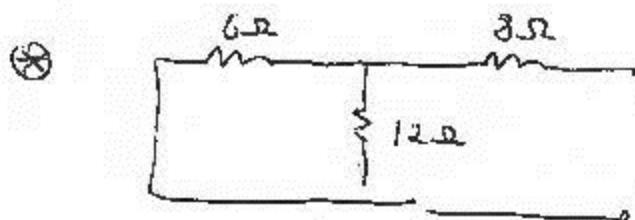


$$V_{oc1} = \frac{12 \cdot 12}{48} = 8 V$$

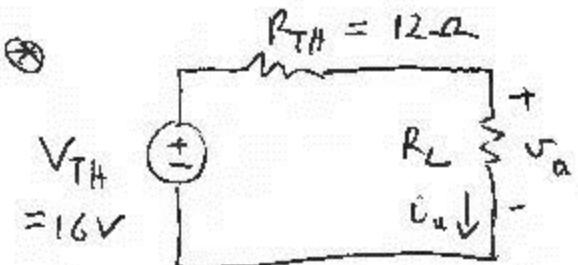
$$\Rightarrow V_{oc} = 16 V$$



$$V_{oc2} = 2 \cdot (12/6) = 2 \cdot 4 = 8 V$$



$$R_{th} = (6//12) + 8 = 4 + 8 = 12 \Omega$$



$$\textcircled{1} \quad v_a = \frac{16 \cdot 12}{12 + 12} = \frac{16 \cdot 12}{24} = 8 \quad \boxed{v_a = 8 V}$$

$$\textcircled{2} \quad v_a = 16 \cdot \frac{R_L}{R_L + 12} = 4 \Rightarrow 12R_L = 4 \cdot 12 \Rightarrow \boxed{R_L = 4 \Omega}$$

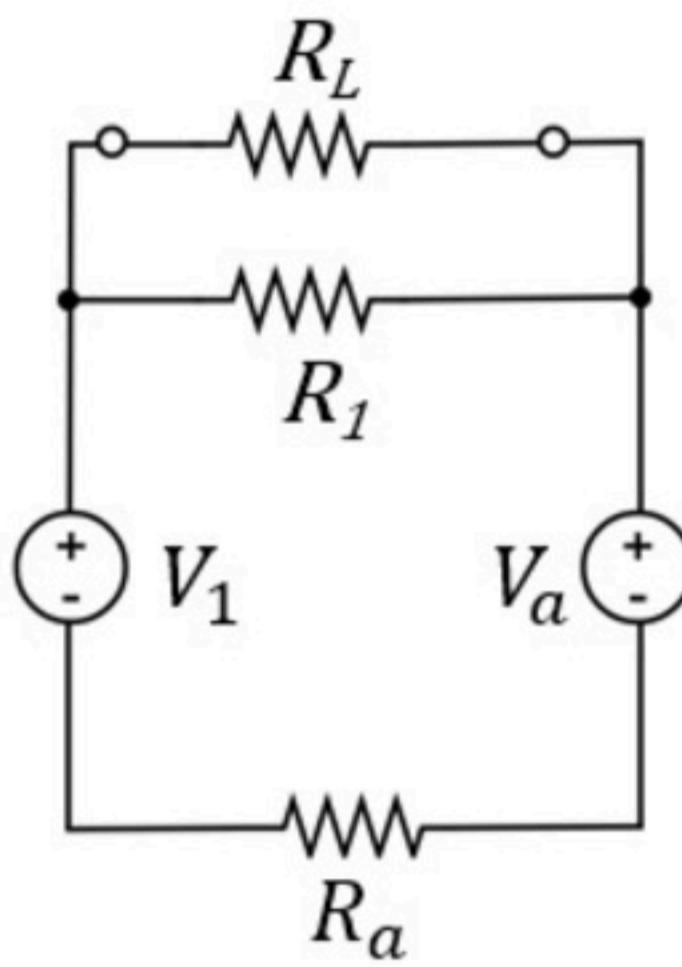
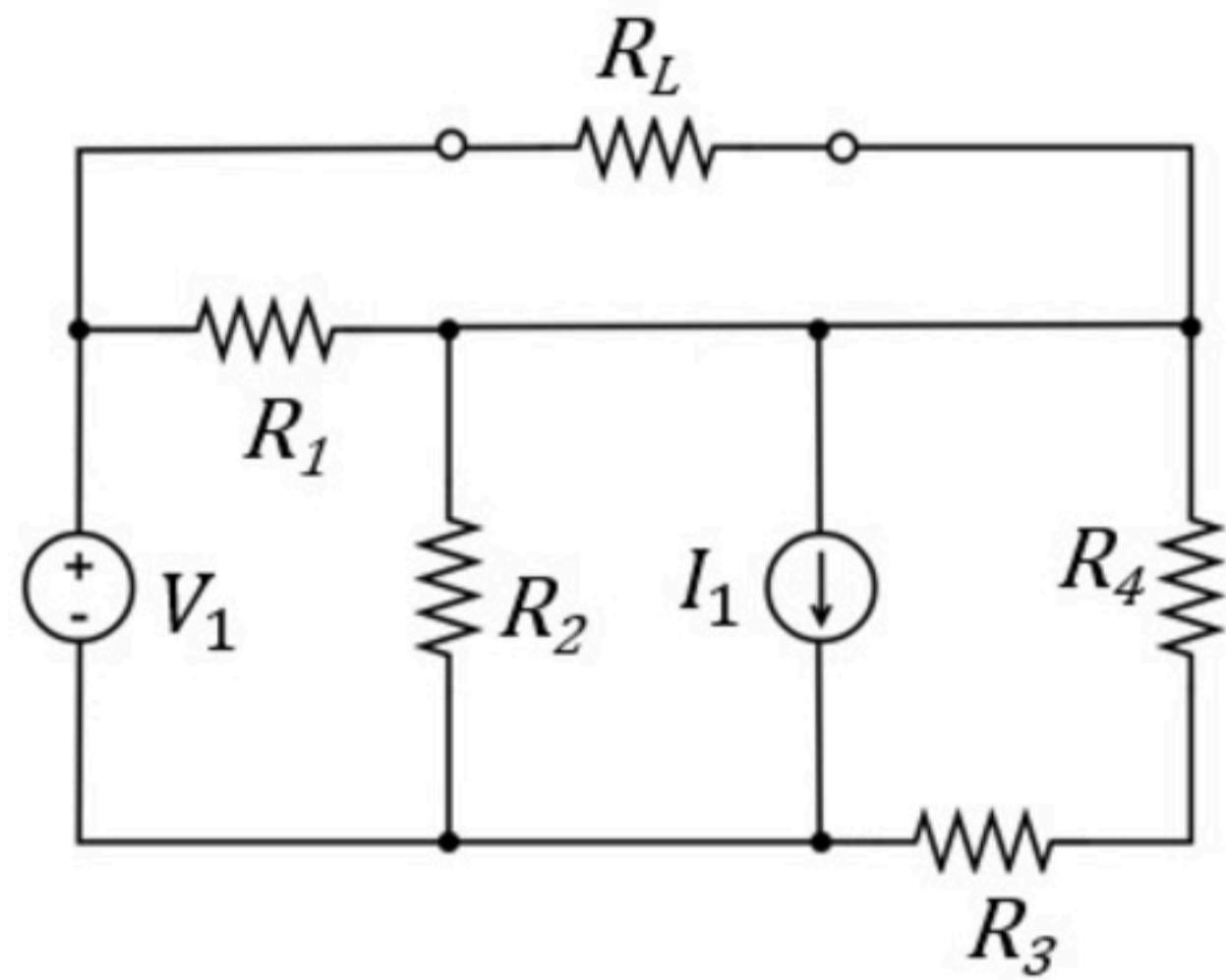
$$\textcircled{3} \quad i_a = \frac{16}{R_L + 12} = 1 \Rightarrow \boxed{R_L = 4 \Omega}$$

Circuit theorems 011

Unlimited Attempts.

The circuit on the right was created by applying source transformations to the circuit on the left.

Find the values of V_a and R_a .



Given Variables:

$V_1 : 20 \text{ V}$

$I_1 : 2 \text{ A}$

$R_1 : 14 \text{ ohm}$

$R_2 : 6 \text{ ohm}$

$R_3 : 1 \text{ ohm}$

$R_4 : 11 \text{ ohm}$

Calculate the following:

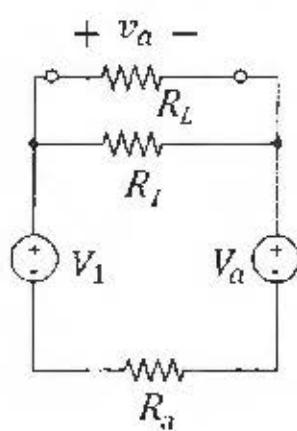
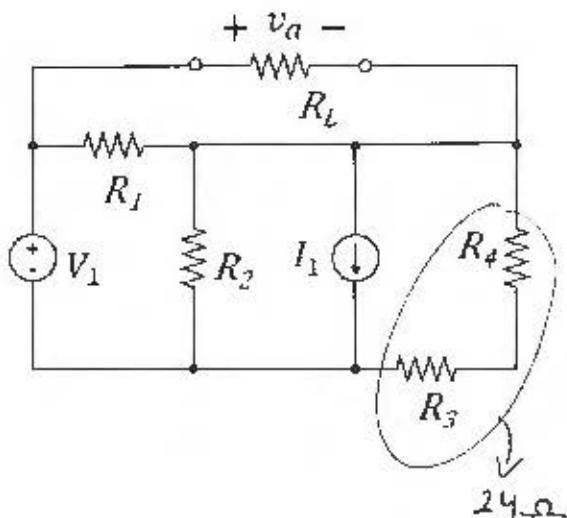
$R_a (\text{ohm}) :$

$V_a (\text{V}) :$

Hint: Make sure you use the correct transformations.

The circuit on the right was created by applying source transformations on the left circuit.

Find the values of V_a and R_a .



$$V_1 = 17 \text{ V}$$

$$I_1 = 2 \text{ A}$$

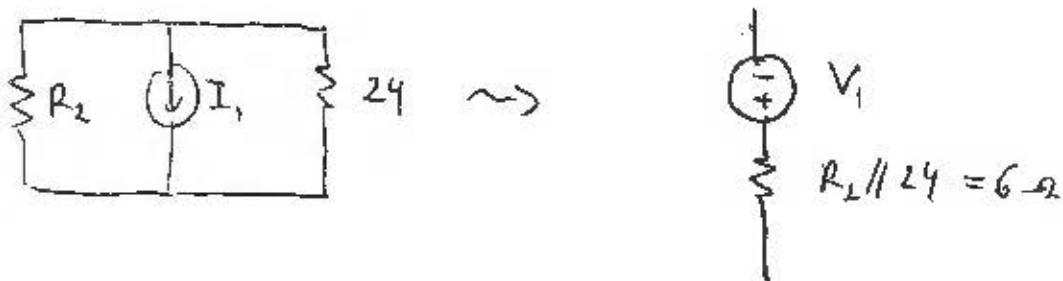
$$R_1 = 22 \text{ ohm}$$

$$R_2 = 8 \text{ ohm}$$

$$R_3 = 12 \text{ ohm}$$

$$R_4 = 12 \text{ ohm}$$

$$R_2 // 24 = \left(\frac{1}{8} + \frac{1}{24} \right)^{-1} = \left(\frac{3}{24} + \frac{1}{24} \right)^{-1} = 6 \text{ ohm}$$



$$V_i = I_1 \cdot (R_2 // 24) = 2 \cdot 6 = 12 \text{ V}$$

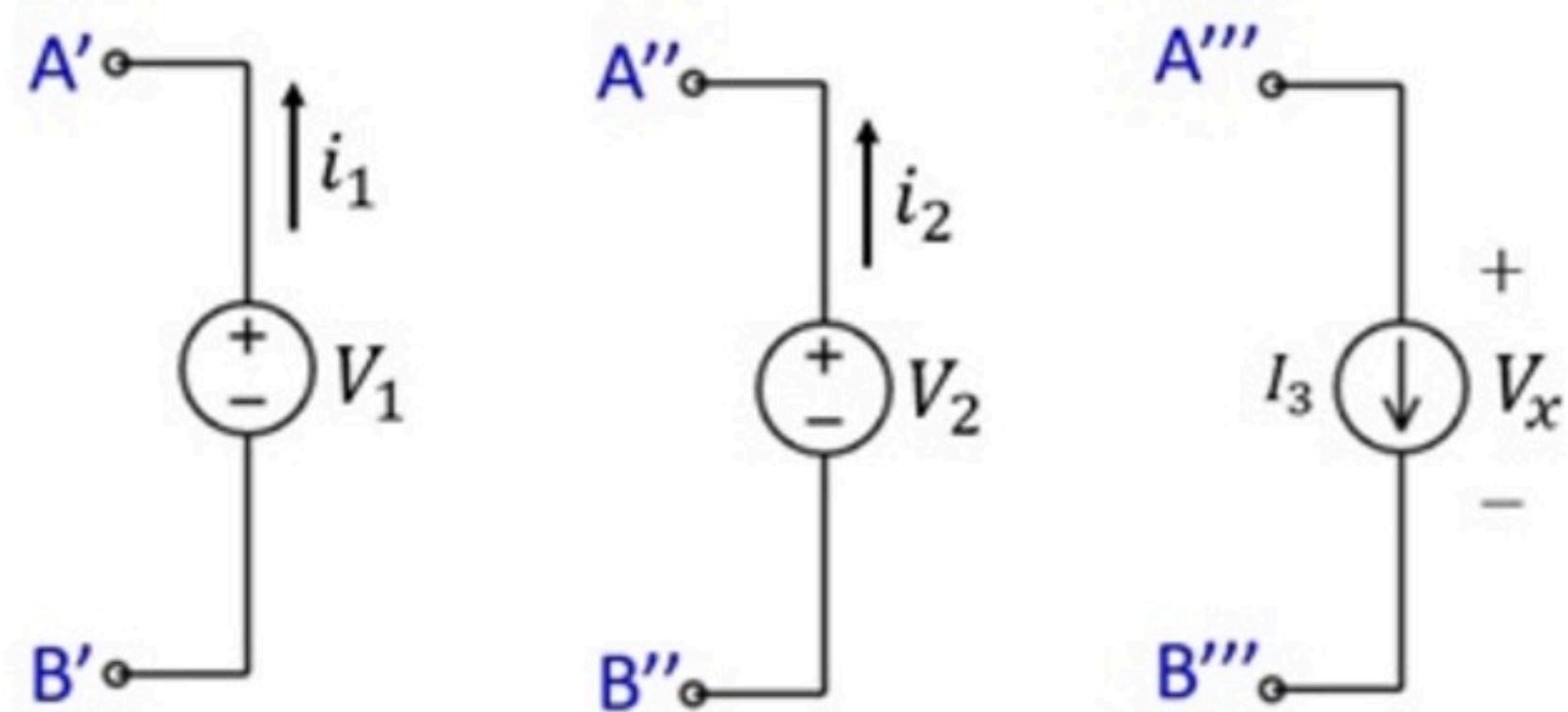
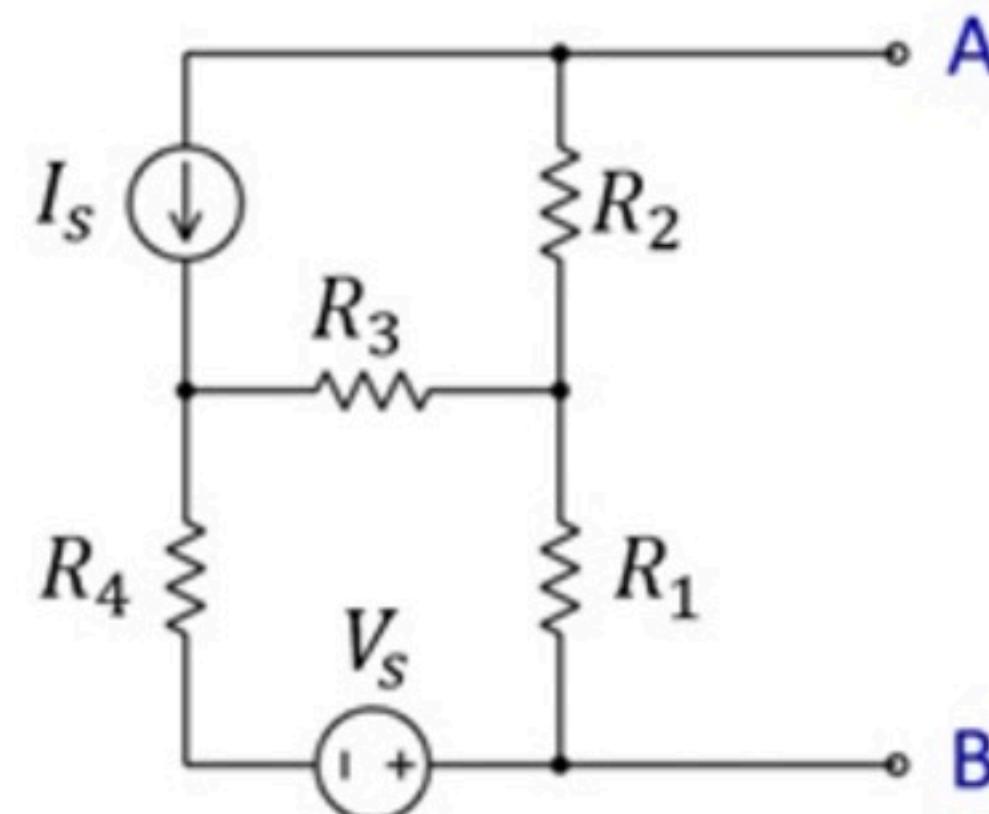
$$\boxed{V_a = 12 \text{ V}}$$

$$\boxed{R_a = 6 \text{ ohm}}$$

Circuit theorems 013

No more attempts left.

Consider the circuit on the left. You are not given the values of V_S , I_S , R_1 , R_2 or R_3 .



You are told the value of current i_1 if V_1 is attached to this circuit, with A connected to A' and B connected to B'.

You are also told the value of current i_2 if V_2 is attached, with A connected to A'' and B connected to B''. However, in this case, the independent sources were first turned off (i.e., $V_S = 0$ and $I_S = 0$).

Your task is to find V_x if current source I_3 is connected to the original circuit (i.e., with the independent sources V_S and I_S not turned off), with A connected to A''' and B connected to B'''.

Given Variables:

$V_1 : 6 \text{ V}$

$i_1 : 12 \text{ A}$

$V_2 : 12 \text{ V}$

$i_2 : 12 \text{ A}$

$I_3 : -7 \text{ A}$

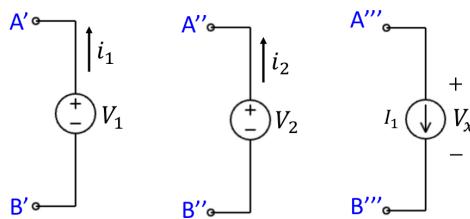
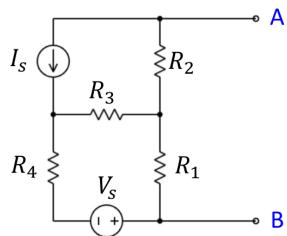
$R_4 : 2 \text{ ohm}$

Calculate the following:

$V_x (\text{V}) :$

Hint: Redraw the circuit on the left as its Thevenin equivalent model

Consider the circuit on the left. You are not given the values of V_S , I_S , R_1 , R_2 or R_3 .



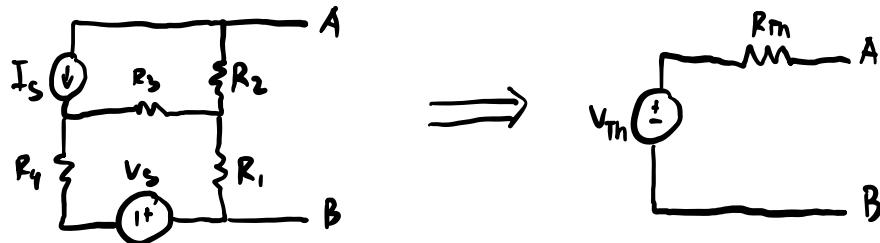
$$\begin{aligned}V_1 &= 1S \text{ V} \\i_1 &= 6A \\V_2 &= 10 \text{ V} \\i_2 &= 5A \\I_1 &= 5A \\R_4 &= 2\Omega\end{aligned}$$

You are told the value of current i_1 if V_1 is attached to this circuit, with A connected to A' and B connected to B'.

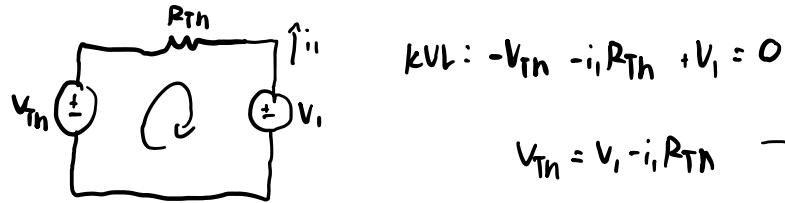
You are also told the value of current i_2 if V_2 is attached, with A connected to A'' and B connected to B''. However, in this case, the independent sources were first turned off (i.e., $V_S = 0$ and $I_S = 0$).

Your task is to find V_x if current source I_1 is connected to the original circuit (i.e., with the independent sources V_S and I_S not turned off), with A connected to A''' and B connected to B'''.

Represent the left circuit as its Thevenin equivalent circuit



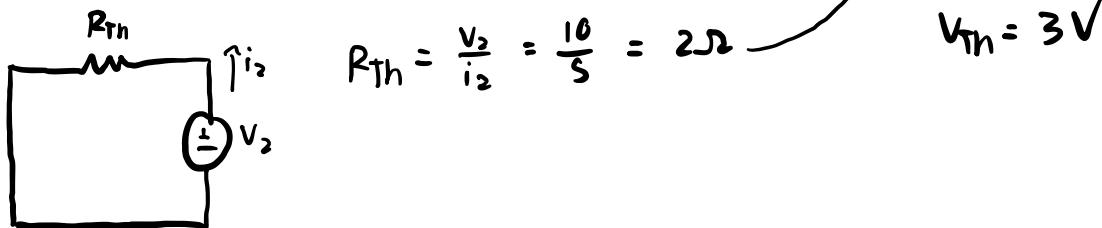
When $A \rightarrow A'$, $B \rightarrow B'$



$$KVL: -V_{Th} - i_1 R_{Th} + V_1 = 0$$

$$V_{Th} = V_1 - i_1 R_{Th}$$

when $A \rightarrow A''$, $B \rightarrow B''$ and $V_S = 0$, $I_S = 0$

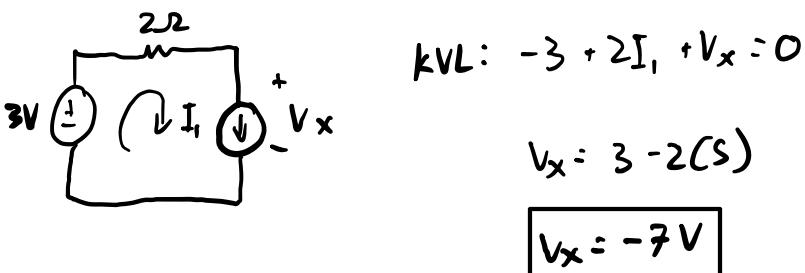


$$R_{Th} = \frac{V_2}{i_2} = \frac{10}{5} = 2\Omega$$

$$V_{Th} = 1S - 6(2)$$

$$V_{Th} = 3V$$

when $A \rightarrow A'''$, $B \rightarrow B'''$



$$KVL: -3 + 2I_1 + V_x = 0$$

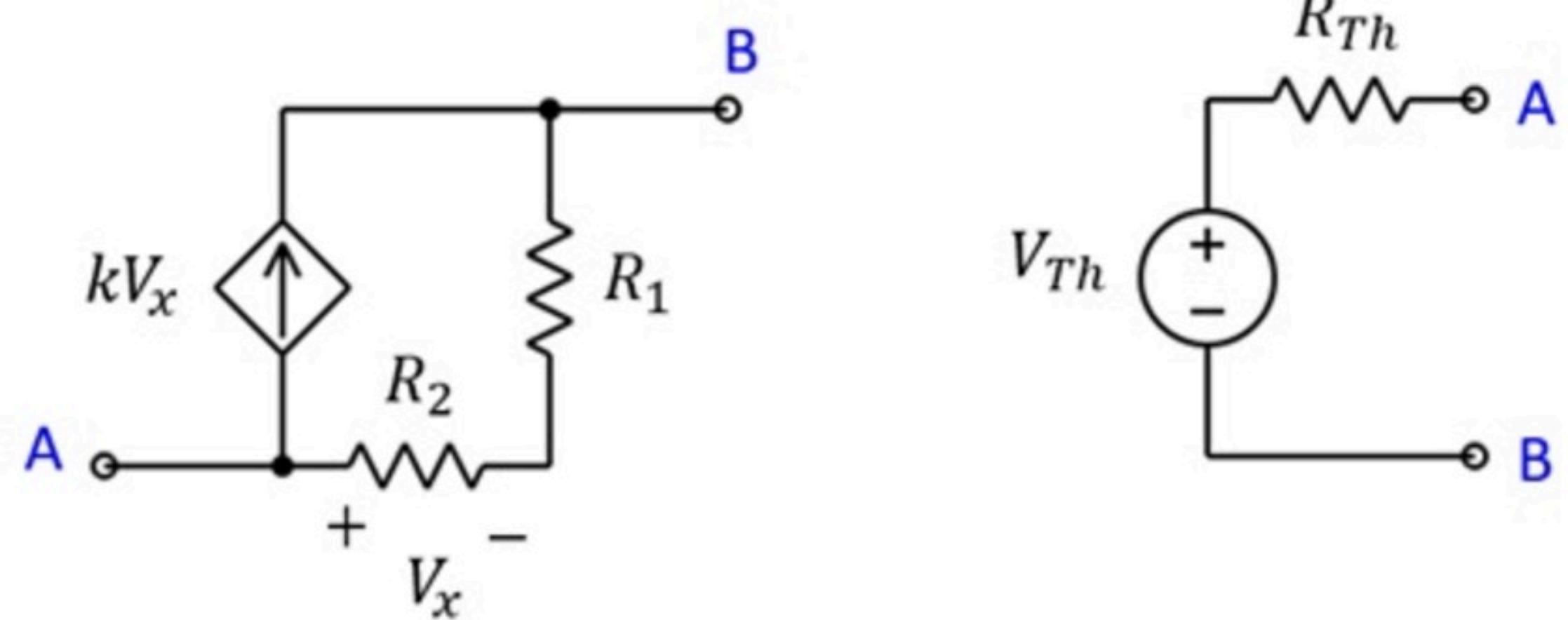
$$V_x = 3 - 2(S)$$

$$V_x = -7V$$

Circuit theorems 014

Problem has been graded.

The circuit on the right represent the Thevenin model of the circuit on the left. Find the value of V_{Th} and R_{Th} .



Given Variables:

$R1 : 4 \text{ ohm}$

$R2 : 2 \text{ ohm}$

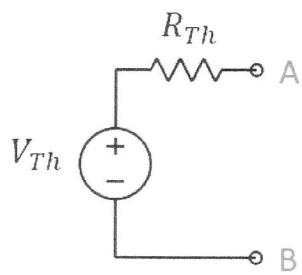
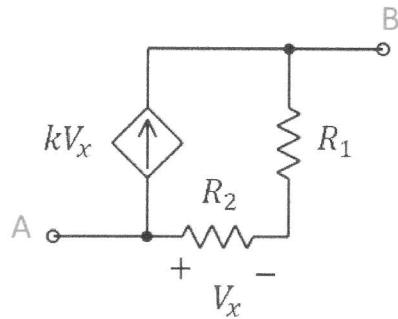
$k : -2 \text{ A/V}$

Calculate the following:

$V_{Th} (\text{V}) :$

$R_{Th} (\text{ohm}) :$

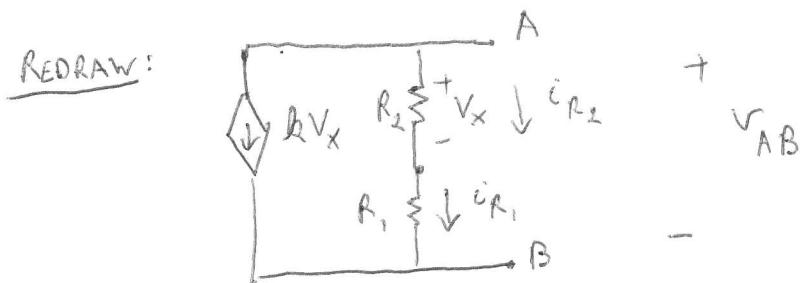
The circuit on the right represent the Thevenin model of the circuit on the left. Find the value of V_{Th} and R_{Th} .



$$R_1 = 4 \Omega$$

$$R_2 = 2 \Omega$$

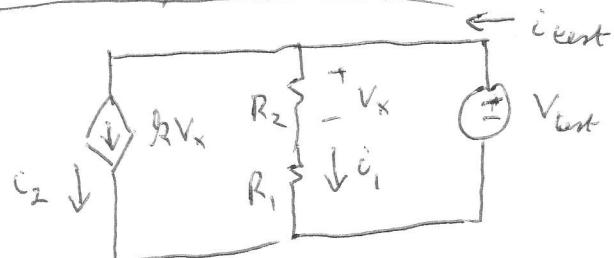
$$k = -2 \text{ A/V}$$



(i) LEAVE A-B OPEN: KCL: $kV_x + \frac{V_x}{R_2} = 0 \Rightarrow (k + \frac{1}{R_2})V_x = 0 \Rightarrow V_x = 0$

$$\Rightarrow i_{R_2} = i_{R_1} = 0 \text{ A} \Rightarrow V_{AB} = 0 \Rightarrow \boxed{V_{TH} = 0 \text{ V}}$$

(ii) FOR R_{TH} , APPLY TEST VOLTAGE



$$i_{test} = i_1 + i_2 = V_{test} \frac{(1+kR_2)}{R_1+R_2}$$

$$\Rightarrow R_{TH} = \frac{V_{test}}{i_{test}} = \frac{R_1+R_2}{1+kR_2} = \frac{4+2}{1+(-2)2} = \frac{6}{-3}$$

voltage divider

$$i_1 = \frac{V_{test}}{R_1+R_2}$$

$$i_2 = kV_x = k V_{test} \frac{R_2}{R_1+R_2}$$

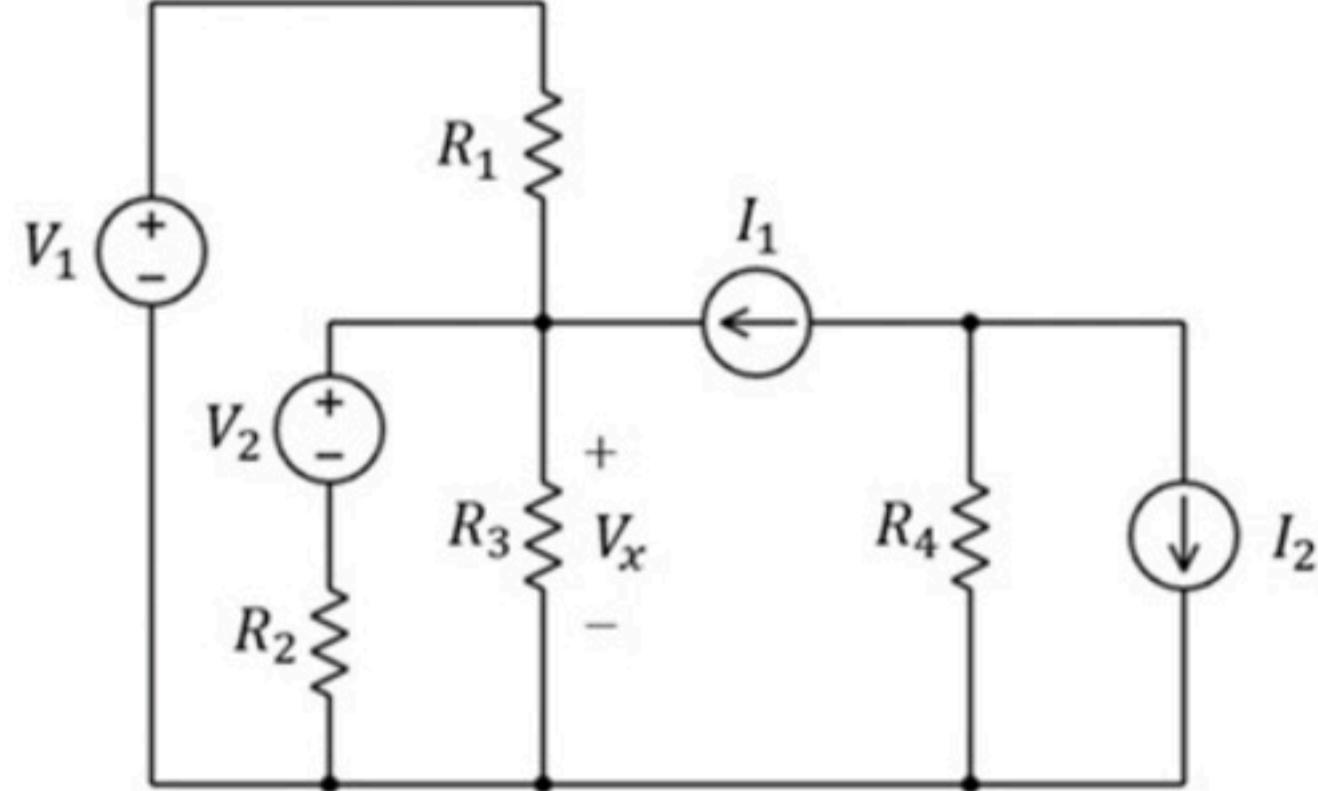
$$\boxed{R_{TH} = -2 \Omega}$$

Circuit theorems 015

Problem has been graded.

Consider the circuit below. You are not given the values of V_1 , V_2 and I_2 . However, you are told the values of the other components and that of V_x .

- What is the new value of V_x when all the source values (i.e., V_1 , V_2 , I_1 and I_2) are doubled? We will call this new value V_{x1} .
- What is the new value of V_x when only I_1 is doubled and the other sources are what they were originally? We will call this new value V_{x2} .



Given Variables:

R1 : 10 ohm

R2 : 10 ohm

R3 : 5 ohm

R4 : 7 ohm

I1 : 2 A

Vx : 16 V

Calculate the following:

Vx1 (V) :

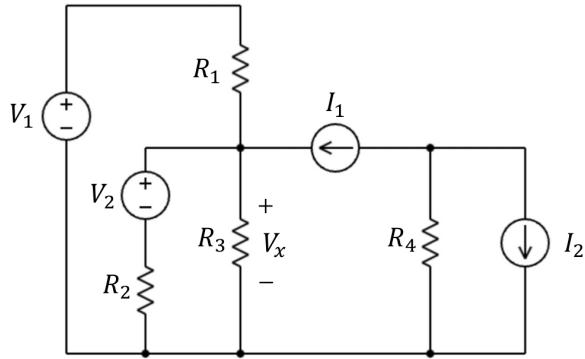
Vx2 (V) :

Hint: Use linearity and superposition to express V_x as a linear combination of all sources

Consider the circuit below. You are not given the values of V_1 , V_2 and I_2 . However, you are told the values of the other components and that of V_x .

(a) What is the new value of V_x when all the source values (i.e., V_1 , V_2 , I_1 and I_2) are doubled? We will call this new value V_{x1} .

(b) What is the new value of V_x when only I_1 is doubled and the other sources are what they were originally? We will call this new value V_{x2} .



$$R_1 = 15\Omega$$

$$R_2 = 5\Omega$$

$$R_3 = 15\Omega$$

$$R_4 = 7\Omega$$

$$I_1 = 2A$$

$$V_x = 15$$

a. Generally,

$$V_x = aV_1 + bV_2 + cI_1 + dI_2 \quad \text{from linearity and superposition}$$

If all sources are doubled,

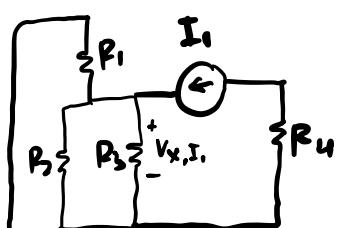
$$\begin{aligned} V_{x1} &= a(2V_1) + b(2V_2) + c(2I_1) + d(2I_2) = 2(aV_1 + bV_2 + cI_1 + dI_2) \\ &= 2V_x \\ &= 2 \cdot 15 \\ V_{x1} &= 30V \end{aligned}$$

b. If only I_1 is doubled

$$\begin{aligned} V_{x2} &= aV_1 + bV_2 + c(I_1) + dI_2 = (aV_1 + bV_2 + cI_1 + dI_2) + cI_1 \\ &= V_x + cI_1 \end{aligned}$$

find the contribution of I_1 using superposition

when only I_1 is on,



$$V_{x,I1} = I_1 \left(\frac{R_1/R_2}{R_1/R_2 + R_3} \right) R_3$$

$$\begin{aligned} V_{x,I1} &= 2 \left(\frac{\frac{15}{5}}{\frac{15}{5} + 15} \right) 15 \\ &= 2 \left(\frac{15}{15+60} \right) 15 \\ &= 2 \cdot \frac{1}{5} \cdot 15 \\ &= 6V \Rightarrow cI_1 \end{aligned}$$

$$V_{x2} = V_x + cI_1$$

$$= 15 + 6$$

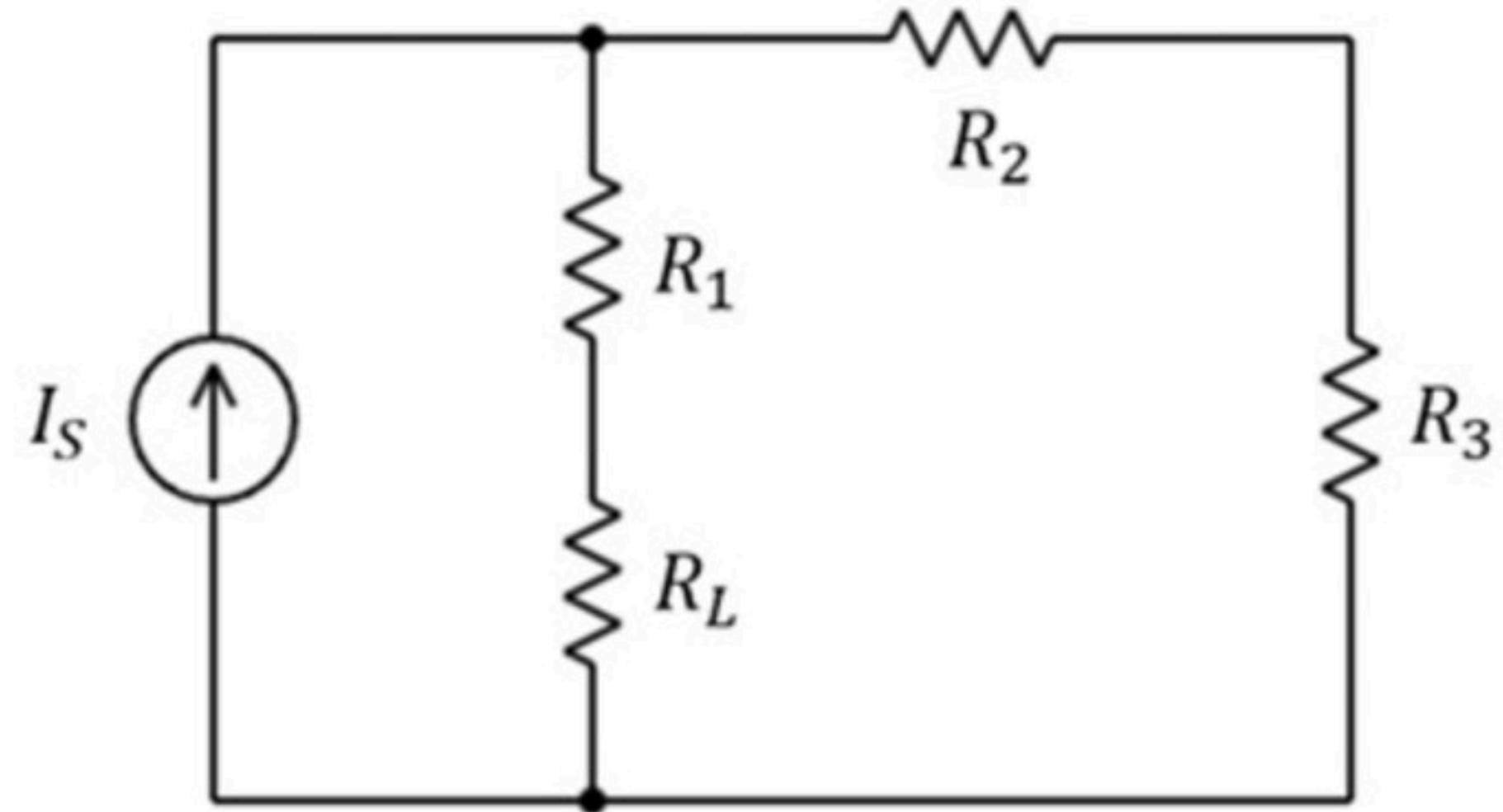
$$V_{x2} = 21V$$

Circuit theorems 016

Problem has been graded.

Find the value of R_L such that the power received by R_L is maximized.

Find the corresponding max power received by R_L .



Given Variables:

$I_s : 2 \text{ A}$

$R_1 : 2 \text{ ohm}$

$R_2 : 1 \text{ ohm}$

$R_3 : 1 \text{ ohm}$

Calculate the following:

$R_L (\text{ohm}) :$

$P_{\max} (\text{W}) :$

Hint: Find the Thevenin equivalent model of the circuit after taking out R_L

Find the value of R_L such that the power received by R_L is maximized.

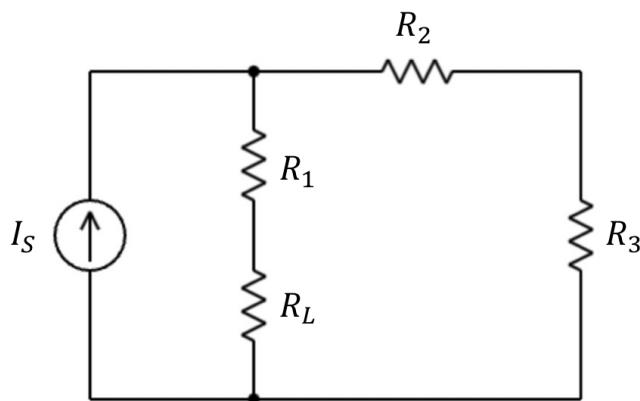
Find the corresponding max power received by R_L .

$$I_S = 2A$$

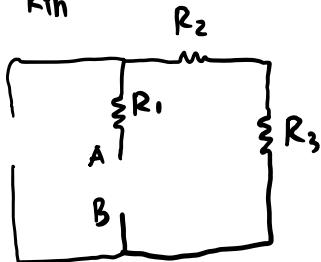
$$R_1 = 12\Omega$$

$$R_2 = 2\Omega$$

$$R_3 = 2\Omega$$



find R_{Th}

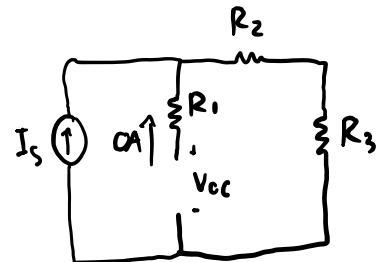


R_1, R_2, R_3 are in series

$$\begin{aligned} R_{Th} &= R_1 + R_2 + R_3 \\ &= 12 + 2 + 2 \end{aligned}$$

$$R_{Th} = 16\Omega$$

find V_{Th}



$$\begin{aligned} V_{OC} &= I_S \cdot (R_2 + R_3) \\ &= 2 \cdot (2 + 2) \end{aligned}$$

$$V_{OC} = 8V$$

$$P_{max} = \frac{V_{Th}^2}{4R_{Th}}$$

$$= \frac{8^2}{4(16)}$$

$P_{max} = 1W$

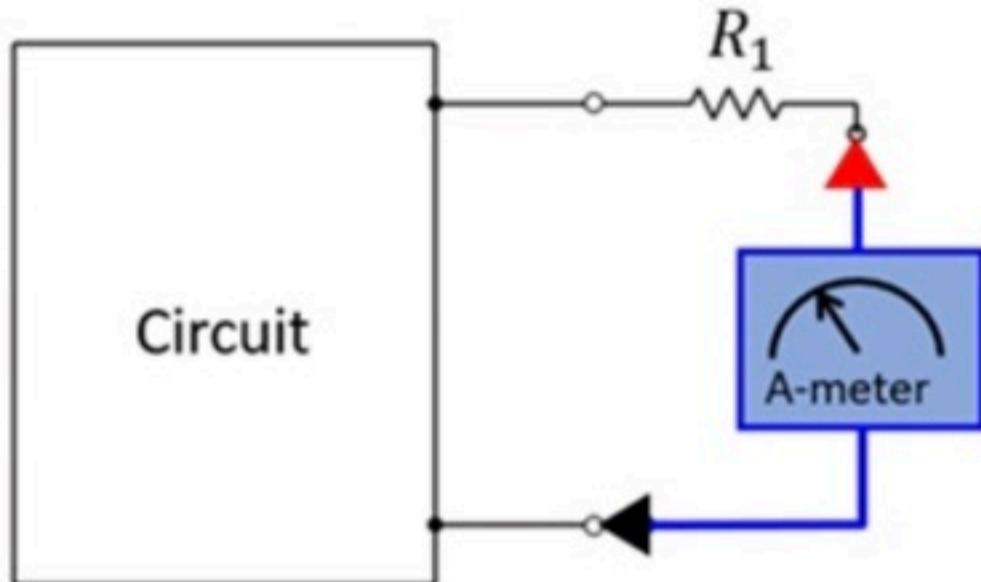
Circuit theorems 017

No more attempts left.

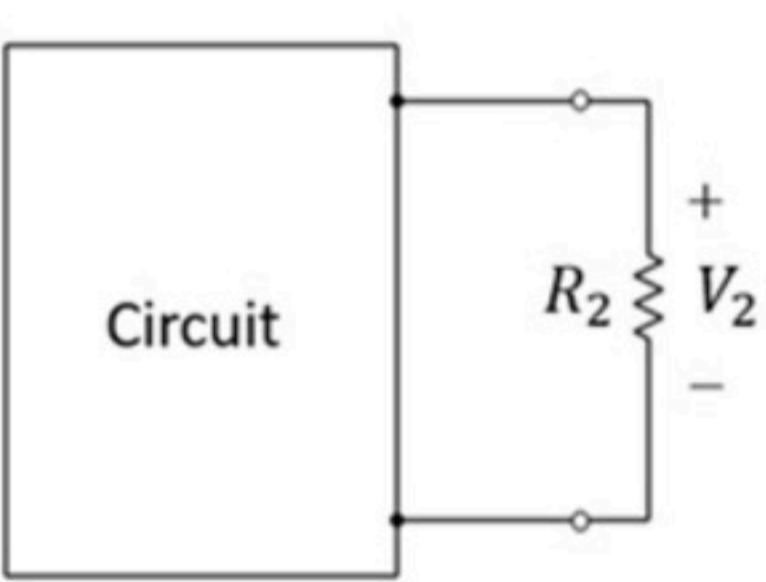
The box contains a linear circuit. This same circuit is placed into the three configurations shown below.

The reading of the ammeter in configuration 1 is given as X.

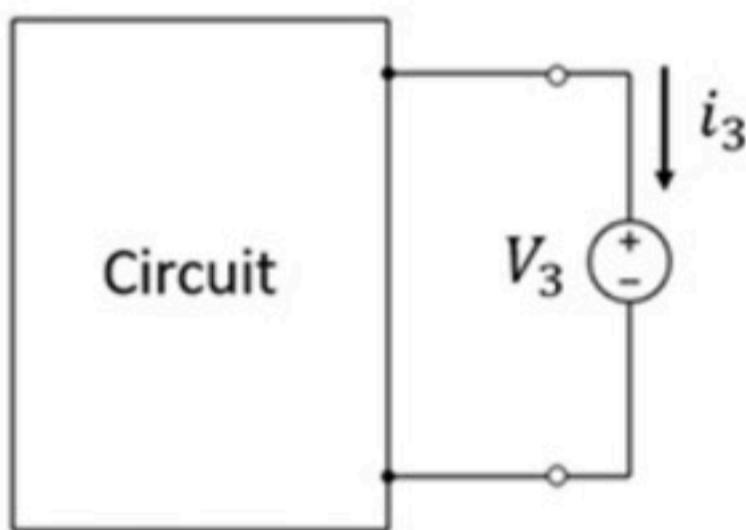
Find the current i_3 in configuration 3.



Configuration 1



Configuration 2



Configuration 3

Given Variables:

X : 8 A

R1 : 1 ohm

V2 : 20 V

R2 : 10 ohm

V3 : 2 V

Calculate the following:

i3 (A) :

Hint: Replace the circuit in the box as its Thevenin equivalent model

The box contains a linear circuit. This same circuit is placed into the three configurations shown below.

The reading of the ammeter in configuration 1 is given as X.

Find the current i_3 in configuration 3.

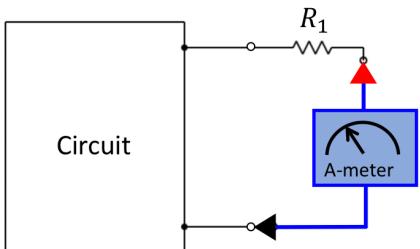
$$X = 8A$$

$$R_1 = 1\Omega$$

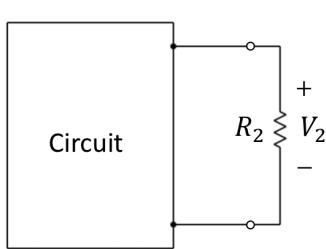
$$V_2 = 16V$$

$$R_2 = 4\Omega$$

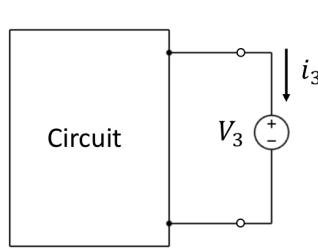
$$V_3 = 8V$$



Configuration 1

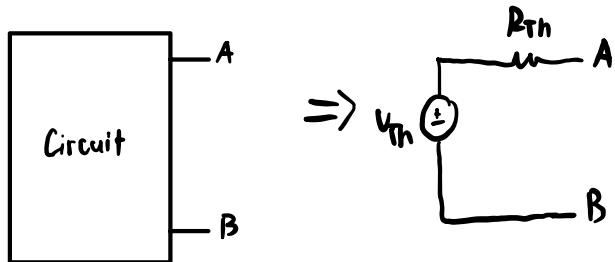


Configuration 2



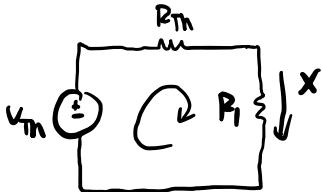
Configuration 3

Replace the box by its Thevenin equivalent model



Configuration 1

$$KVL 1: -V_{Th} + X R_{Th} + X R_1 = 0$$



Solve system of equations

$$-V_{Th} + 8R_{Th} + 8 \cdot 1 = 0$$

$$-V_{Th} + 8R_{Th} = -8$$

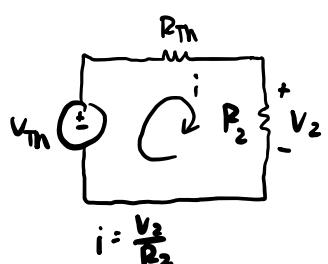
①

$$\textcircled{1}: -V_{Th} = -8 - 8R_{Th}$$

$$V_{Th} = 8 + 8R_{Th}$$

Configuration 2

$$KVL 2: -V_{Th} + i R_{Th} + V_2 = 0$$



$$-V_{Th} + \frac{V_2}{R_2} R_{Th} = -V_2$$

$$-V_{Th} + \frac{16}{4} R_{Th} = -16$$

$$-V_{Th} + 4R_{Th} = -16 \quad \textcircled{2}$$

$$\textcircled{1} \rightarrow \textcircled{2}: -(8 + 8R_{Th}) + 4R_{Th} = -16$$

$$-8 - 8R_{Th} + 4R_{Th} = -16$$

$$-4R_{Th} = -8$$

$$R_{Th} = 2\Omega$$

$$R_{Th} \rightarrow \textcircled{1}: V_{Th} = 8 + 8(2)$$

$$V_{Th} = 24V$$

Configuration 3

$$KVL 3: -24 + 2i_3 + 8 = 0$$

$$2i_3 = 16$$

$$\boxed{i_3 = 8A}$$

