



$$I_1 = I_s - I_x$$

$$|I_s|^2 = 4$$

$$\text{KVL: } I_x (10 - 2j) = 10 I_x + (2 + 4j) I_1$$

$$= 10 I_x + (2 + 4j)(I_s - I_x)$$

$$I_x (\cancel{10} - 2j - \cancel{10} + 2 + 4j) = (2 + 4j) I_s$$

$$I_x (2 + 2j) = I_s (2 + 4j) \Rightarrow I_x = I_s \frac{(1 + 2j)}{(1 + j)} = I_s \frac{(3 + j)}{2}$$

$$(1) \quad V_1 = I_x (10 - 2j) = I_s \frac{(3 + j)(10 - 2j)}{2} = I_s (16 + 2j)$$

NOTE  
DIRECTION  
OPPOSITE

PASSIVE  
SIGN  
CONVENTION

$$S_1 = \frac{1}{2} V_1 \cdot I_s^* = \frac{1}{2} I_s (16 + 2j) I_s^* = |I_s|^2 (8 + j) \Rightarrow \boxed{S_1 = 32 + 4j}$$

$$S_2 = \frac{1}{2} \cdot Z_{10\Omega} \cdot |I_x|^2 = \frac{1}{2} \cdot 10 \cdot |I_s|^2 \cdot \frac{10}{4} \Rightarrow \boxed{S_2 = 50 + 0j}$$

AS  
EXPECTED

$$(3) \quad I_1 = I_s - I_x = I_s \left(1 - \frac{3 + j}{2}\right) = I_s \frac{(-1 - j)}{2}$$

$$S_3 = \frac{1}{2} Z_{2\Omega} |I_1|^2 = \frac{1}{2} \cdot 2 \cdot |I_s|^2 \cdot \frac{|-1 - j|^2}{4} = \frac{|I_s|^2}{4} \cdot 2 \Rightarrow \boxed{S_3 = 2 + 0j}$$

$$(4) \quad S_4 = \frac{1}{2} V_2 I_1^* = \frac{1}{2} \cdot 10 I_x \cdot I_1^* = 5 \cdot I_s \frac{(3 + j)}{2} \cdot I_s^* \frac{(-1 - j)}{2} = |I_s|^2 \cdot \frac{5}{4} (-4 + 2j)$$

$$\Rightarrow \boxed{S_4 = -20 + 10j}$$

RECEIVED SINCE WE  
USED PASSIVE SIGN CONVENTION

$$(5) \quad S_5 = \frac{1}{2} Z_L \cdot |I_1|^2 = \frac{1}{2} \cdot 4j \cdot |I_s|^2 \cdot \frac{|-1 - j|^2}{4} = 2j \cdot 4 \cdot \frac{2}{4} \Rightarrow \boxed{S_5 = 0 + 4j}$$

AS EXPECTED

$$(6) \quad S_6 = \frac{1}{2} Z_C |I_x|^2 = \frac{1}{2} (-2j) |I_s|^2 \frac{|3 + j|^2}{4} = -j \cdot 4 \cdot \frac{10}{4} \Rightarrow \boxed{S_6 = 0 - 10j}$$

$$\text{CHECK: } \sum P_{\text{REC}} = \sum P_{\text{SUPPL}} \Rightarrow 50 + 2 - 20 = 32 \quad \text{OK}$$

$$\sum Q_{\text{REC}} = \sum Q_{\text{SUPPL}} \Rightarrow 10 + 4 - 10 = 4 \quad \text{OK}$$