

Find  $P$  and  $Q$ .

Note: We've used bold capital letters to denote complex variables. The  $*$  operator stands for complex conjugate. The  $\text{Re}[]$  and  $\text{Im}[]$  operators stand for taking the real part and imaginary part respectively.

a: 2.

b: 4.

$$\mathbf{V}_1 = be^{j\frac{\pi}{3}} \quad \mathbf{Z}_1 = a - aj \quad \mathbf{I}_1 = \frac{\mathbf{V}_1}{\mathbf{Z}_1}$$

$$\mathbf{S} = \frac{1}{2} \cdot \mathbf{V}_1 \cdot \mathbf{I}_1^* \quad P = \text{Re}[\mathbf{S}] \quad Q = \text{Im}[\mathbf{S}]$$

$$\mathbf{S} = \frac{1}{2} \mathbf{V}_1 \mathbf{I}_1^* = \frac{1}{2} \mathbf{V}_1 \frac{\mathbf{V}_1^*}{\mathbf{Z}_1^*} = \frac{1}{2} \frac{|\mathbf{V}_1|^2}{\mathbf{Z}_1^*}$$

$$\mathbf{S} = \frac{1}{2} \cdot \frac{4^2}{2+2j} = \frac{4^2}{2 \cdot 2} \frac{1}{1+j} \frac{1-j}{1-j} = 4 \frac{(1-j)}{1+1} = 2(1-j)$$

$$\boxed{P = 2}$$

$$\boxed{Q = -2}$$