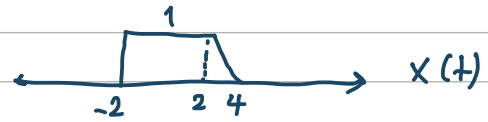


## Discussion Session 4:

① plot the following signals



a)  $x(2t+4)$

b)  $x\left(\frac{-t}{2}+1\right)$

c)  $3x(-t+1)+2$

d)  $-x(t)u(t-1)$

Answers:

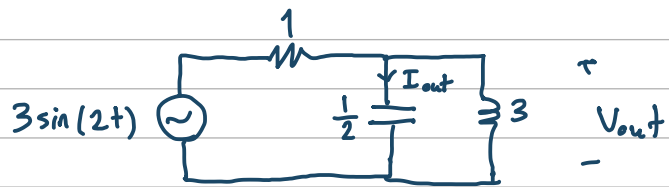
② Find  $x(t) * h(t)$

$$x(t) = \text{rect}\left(\frac{t}{2} - 3\right) \quad h(t) = \text{rect}(t + 2)$$

~



③ Find  $V_{out}$  and  $I_{out}$  with phasor method



Answer

#### ④ LTI checking

$$a) \quad y(t) = \int_{-\infty}^{\infty} x(\tau) h(2t-\tau) d\tau$$

$$b) \quad y(t) = \begin{cases} x(t) & t \geq 0 \\ 0 & t < 0 \end{cases}$$

$t-t_0$ )

Transfer Function: Laplace transform of the impulse response.

$$H(s) = \int_{-\infty}^{\infty} h(\tau) e^{-s\tau} d\tau$$

$$x(t) = e^{st} \longrightarrow \boxed{\text{LTI}} \longrightarrow y(t) = H(s) e^{st} \quad \text{Eigenfunction of a LTI system}$$

Some properties of Laplace:  $\{x(t) : a \text{ cos}\}$

$$L\{a f(t) + b g(t)\} = a F(s) + b G(s) \quad \text{Linearity}$$

$$L\{f(t-T) u(t-T)\} = e^{-Ts} F(s) \quad \text{Time Shifting}$$

$$L\{e^{at} f(t)\} = F(s-a) \quad \text{Frequency Shifting}$$

$$L\{f'(t)\} = s F(s) - f(0^+) \quad \text{Differentiation in time domain}$$

$$L\{f''(t)\} = s L\{f'(t)\} - f'(0^+) = s^2 F(s) - s F(0^+) - f'(0^+)$$

$$L\left\{\int_0^t f(\tau) d\tau\right\} = \frac{F(s)}{s} \quad \text{Integration in time domain}$$

$$L\{f(t) * g(t)\} = F(s) G(s) \quad \text{Convolution Theorem}$$

$$L\{t f(t)\} = -\frac{d}{ds} F(s) \quad \text{Differentiation in } s \text{ domain}$$

$$L\{t^n f(t)\} = (-1)^n \frac{d^n}{ds^n} F(s) \quad \left\{ \begin{array}{l} L^{-1}\left\{\frac{1}{s+a}\right\} = e^{-at} u(t) \\ L^{-1}\left\{\frac{1}{(s+a)^2}\right\} = t e^{-at} u(t) \end{array} \right.$$

$$\text{Partial Fraction: } \frac{N(s)}{D(s)} \quad (\text{degree of } N(s) \text{ is less than degree of } D(s))$$

$$\begin{aligned} \text{Example: } y(s) &= \frac{3}{s(s+2)} \quad (\text{no repeated factor, no irreducible quadratic factor}) \\ &= \frac{A}{s} + \frac{B}{s+2} \end{aligned}$$

Example #2:  $y(s) = \frac{5s+7}{(s+1)^2}$  (Repeated linear factor)

$$= \frac{A}{s+1} + \frac{B}{(s+1)^2}$$

Example #3: what is  $y(t)$  in example #2?