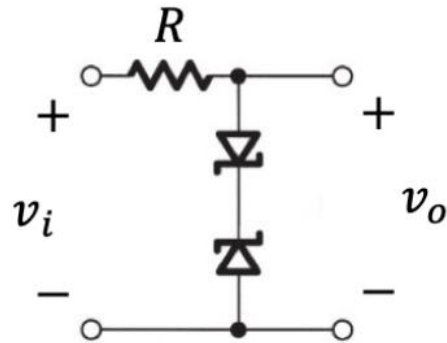


**Problem1:**

(a)

(1)  $V_{D1} = \text{on}, V_{D2} = \text{Zener region}$ (2)  $V_{D1} = \text{Zener region}, V_{D2} = \text{on}$ (3)  $V_{D1} = \text{off}, V_{D2} = \text{off}$ 

(b)

**Case1:  $V_{D1} = \text{on}, V_{D2} = \text{Zener}$** 

$$V_{D1} = V_{D0}, V_{D2} = -V_Z$$

$$V_o = V_{D1} - V_{D2} = V_{D0} + V_Z = 0.7 + 2.3 = 3V$$

$$V_i = V_R + V_o = iR + V_o = iR + 3V$$

$$\rightarrow i = \frac{V_i - 3V}{R} \geq 0$$

$$\rightarrow V_i - 3V \geq 0$$

$$\rightarrow V_i \geq 3V$$

So, when  $V_i \geq 3V$ ,  $V_o = 3V$

**Case2:  $V_{D1} = \text{Zener}, V_{D2} = \text{on}$** 

$$V_{D1} = -V_Z, V_{D2} = V_{D0}$$

$$V_o = V_{D1} - V_{D2} = -V_Z - V_{D0} = -2.3 - 0.7 = -3V$$

$$V_i = V_R + V_o = iR + V_o = iR - 3V$$

$$\rightarrow i = \frac{V_i + 3V}{R} \leq 0$$

$$\rightarrow V_i + 3V \leq 0$$

$$\rightarrow V_i \leq -3V$$

So, when  $V_i \leq -3V$ ,  $V_o = -3V$

**Case3:  $V_{D1} = \text{off}, V_{D2} = \text{off}$** 

$$-2.3V < V_{D1} < 0.7V, -2.3V < V_{D2} < 0.7V$$

$$V_o = V_i - V_R = V_i - iR = V_i \quad \because i = 0 \text{ (no current flows)}$$

$$V_i = V_R + V_o = iR + V_{D1} - V_{D2} = 0 + V_{D1} - V_{D2}$$

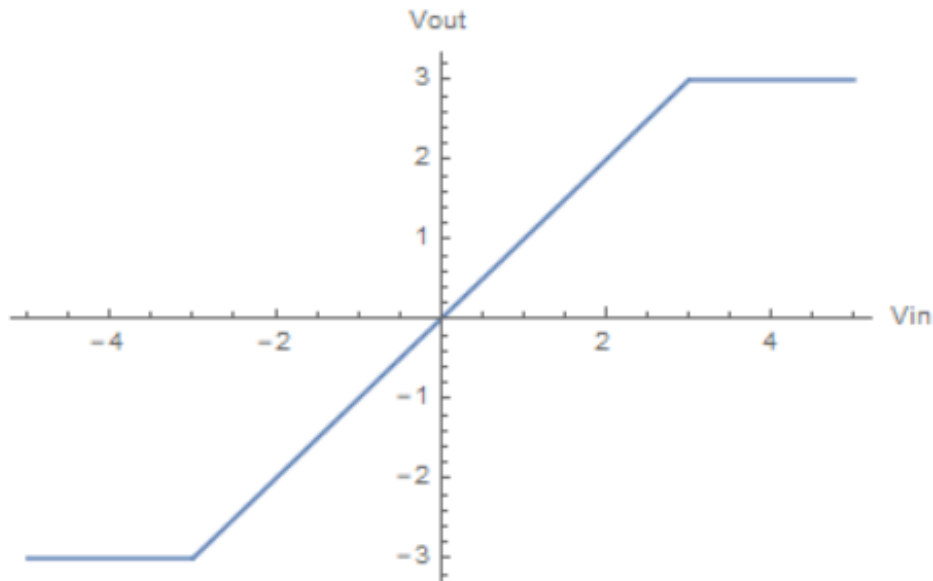
$$\therefore -2.3V < V_{D1} < 0.7V,$$

$$\text{and } -0.7V < -V_{D2} < 2.3V$$

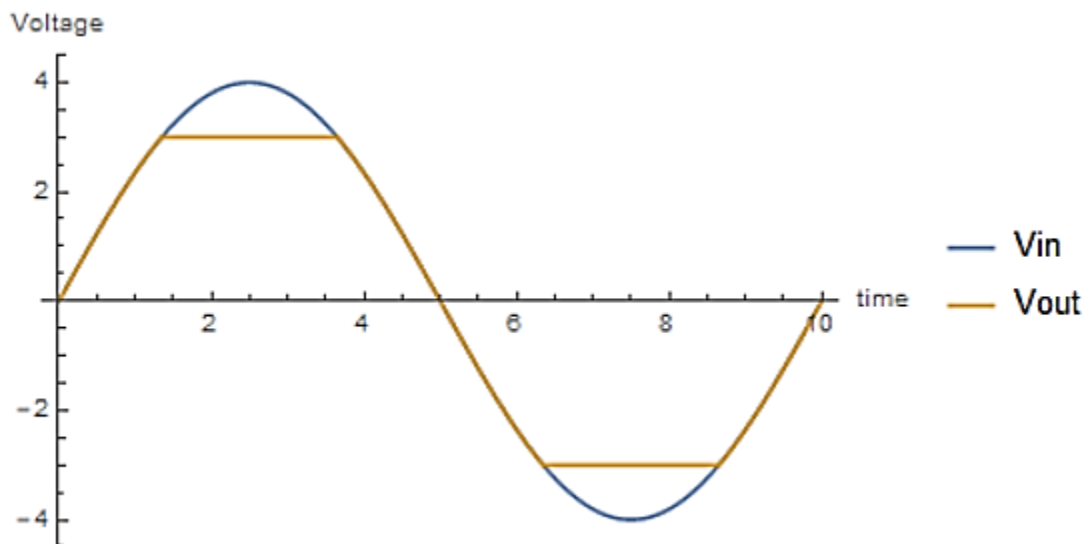
$$\therefore -3V < V_{D1} - V_{D2} < 3V$$

$$\rightarrow -3V < V_i < 3V$$

So, when  $-3V < V_i < 3V$ ,  $V_o = V_i$

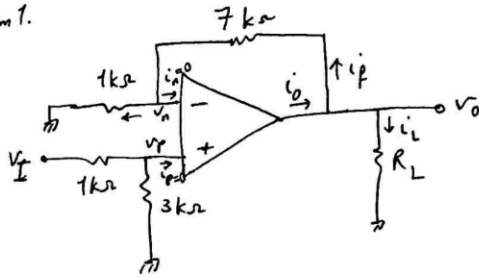


(c)



**Problem2:**

Problem 1.



a) ideal op-amp :  $i_n = i_p = 0$  , negative feedback is present  $\Rightarrow v_n = v_p$

KCL at the inverting node:

$$\frac{v_n}{1k} + \frac{v_n - v_o}{7k} = 0 \quad \rightarrow \quad \frac{v_o}{7k\Omega} = \left( \frac{1}{1k} + \frac{1}{7k} \right) v_n$$

$$\rightarrow v_o = \left( 1 + \frac{7k\Omega}{1k\Omega} \right) v_n$$

$$\Rightarrow v_n = v_p$$

$$v_o = \frac{3}{4} (1 + 7) v_I = 6 v_I$$

$$v_p = \frac{3k\Omega}{3k\Omega + 1k\Omega} \times v_I$$

$$\rightarrow \boxed{v_o = 6 v_I}$$

b) checking the positive peak of  $v_I = 2V$  :

@  $v_I = 2V$  :  $v_o = 6 \times 2 = 12V < V_{sat} \Rightarrow$  We are not limited by the saturation voltage for the max positive  $v_I$ .

@  $V_I = 2V$  :  $i_o = i_L + i_f$

$$i_L = \frac{V_o}{R_L} = \frac{12V}{1k\Omega} = 12mA, \quad i_f = \frac{V_o}{8k\Omega} = \frac{12V}{8k\Omega} = 1.5mA$$

$$i_o = 12mA + 1.5mA = 13.5mA < 25mA \rightarrow \text{we are not limited by the max output current for the max positive } V_I.$$

checking the negative peak of  $V_I = -3V$ :

@

$$@ V_I = -3V \rightarrow V_o = 6 \times (-3) = -18V \text{ and } |-18V| > |V_{sat}|$$

$\Rightarrow$  we are limited by the saturation voltage for the max negative  $V_I$ .

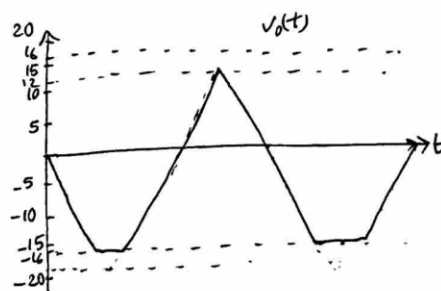
ch  $\Rightarrow V_{out}$  cannot go below  $V_{sat} = -16V$

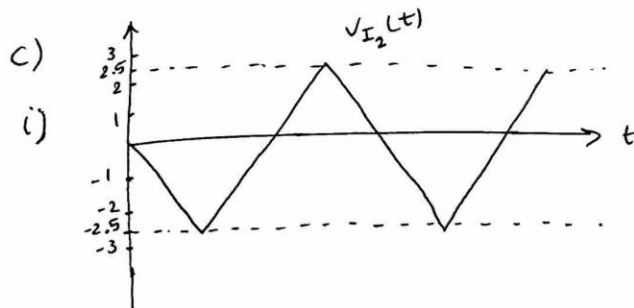
checking for the max output current at  $V_{out} = -16V$ :

$$i_o = i_L + i_f, \quad i_L = \frac{V_o}{R_L} = \frac{-16V}{1k\Omega} = -16mA$$

$$i_f = \frac{-16V}{8k\Omega} = -2mA \rightarrow i_o = -16mA - 2mA = -18mA$$

$$|i_o| < |i_{o,max}|$$





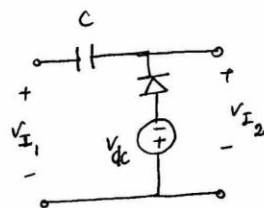
ii) The max positive and negative values of  $v_I$  are  $2.5V$  and  $-2.5V$

$$\text{For } |v_I| = 2.5V \rightarrow |v_o| = 2.5 \times 6 = 15V$$

$$|i_{o,max}| = \frac{|v_{o,max}|}{R_{Lmin}} + \frac{|v_{o,max}|}{8k\Omega} = \frac{15V}{R_{Lmin}} + \frac{15V}{8k\Omega} = \frac{15V}{R_{Lmin}} + 1.875 \text{ (mA)} = 2.5 \text{ mA}$$

$$\frac{15V}{R_{Lmin}} = 23.125 \text{ mA} \rightarrow R_{Lmin} \approx 649 \Omega$$

iii)



Assume using a diode with  $v_{D0} = 0.7V$

$$v_{I2} = v_{I1} + (V_P - V_{DC} - V_{D0})$$

$$v_{I2} = v_{I1} + 0.5V$$

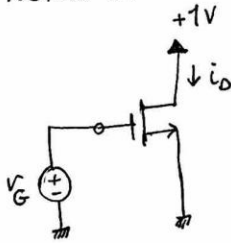
$$\rightarrow V_P - V_{DC} - V_{D0} = 0.5V$$

$$3V - V_{DC} - 0.7V = 0.5V$$

$$\boxed{V_{DC} = 1.8V}$$

## Problem3:

Problem 3.



a) b) when  $V_G < V_t \rightarrow$  Mos is off  $i_D = 0$

$$V_G = V_{GS}, \quad V_D = V_{DS} = 1V$$

when

$$V_{GS} - V_t \leq V_{DS} \rightarrow \text{Mos is in saturation}$$

$$0.5V \leq V_G \leq 1V + 0.5V \rightarrow 0.5V \leq V_G \leq 1.5V \quad \text{Mos is in saturation}$$

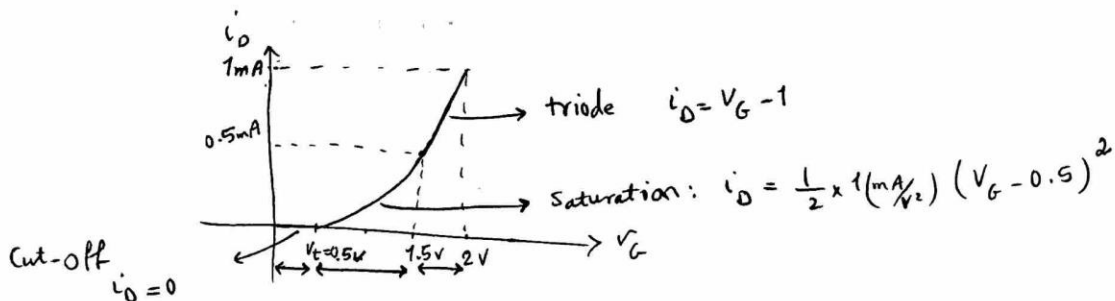
$$i_D = \frac{1}{2} k_n (V_{GS} - V_t)^2 = \frac{1}{2} \times 1 \left( \frac{\text{mA}}{\text{V}^2} \right) \times (V_G - 0.5)^2$$

when

$$V_G > 1.5V \rightarrow \text{Mos is in triode:}$$

$$i_D = \frac{1}{2} k_n (2V_{OV}V_{DS} - V_{DS}^2) = \frac{1}{2} \times 1 \frac{\text{mA}}{\text{V}^2} (2 \times (V_G - 0.5) - 1)$$

$$i_D = V_G - 1$$



**Problem4:**

Both MOS are in saturation since  $V_{DG1} = V_{DG2} = 0 < |V_t|$ .

Here,  $V_{G1} = V_{D1} = V_{S2}$ ,  $V_{G2} = V_{D2}$  and  $I_{D1} = I_{D2} = I_D = 1\text{mA}$ .

Then,

$$V_{OV1} = V_{OV2} \Rightarrow 4 - V_{S2} = V_{S2} - V_{D2} - 1 = \sqrt{\frac{2I_D}{\mu C_{ox} \frac{W}{L}}} = 1\text{ V}$$

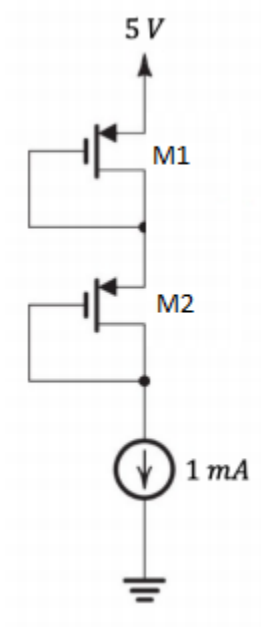
(a)

$$V_{G1} = V_{D1} = V_{S2} = 3\text{V}$$

$$V_{G2} = V_{D2} = 1\text{V}$$

(b) As same current is flowing through the MOSs',  $V_{S2}$  remains same. Then

$$R = \frac{V_{S2}}{I_D} = 1\text{k}\Omega$$



**Problem5:**

$$\beta = 100, V_{D0} = 0.7 \text{ V}, V_T = 25 \text{ mV}$$

(a) Due to current source,  $I_E = 0.1 \text{ mA}$

Assuming BJT is in active mode.

Then,  $V_{BE} = V_{D0} = 0.7 \text{ V}$  and

$$I_C = \frac{\beta}{\beta + 1} I_E = I_E - I_B = 99.01 \mu\text{A}$$

$$I_B = \frac{I_C}{\beta} = \frac{I_E}{\beta + 1} = I_E - I_C = 0.99 \mu\text{A}$$

$$V_B = -I_B \times 200k = -0.198 \text{ V} \approx -0.2 \text{ V}$$

$$V_E = V_B - V_{BE} = -0.898 \text{ V} \approx -0.9 \text{ V}$$

$$V_C = 3 - I_C \times 20k = 1.0198 \text{ V} \approx 1.02 \text{ V}$$

Now,

$$V_{CE} = 1.92 \text{ V} \Rightarrow \text{Correct assumption}$$

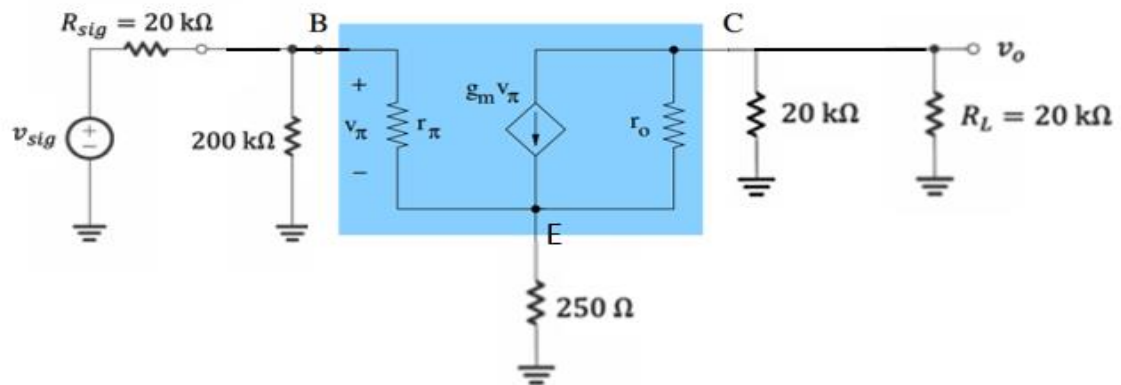
(b) Small signal parameters:

$$g_m = \frac{I_C}{V_T} = 3.9604 \frac{\text{mA}}{\text{V}} \approx 3.96 \frac{\text{mA}}{\text{V}}$$

$$r_\pi = \frac{\beta}{g_m} = 25.25 \text{ k}\Omega$$

$$r_o = \frac{|V_A|}{I_C} = \frac{\infty}{I_C} = \infty \Omega$$

(c) Small signal equivalent circuit:



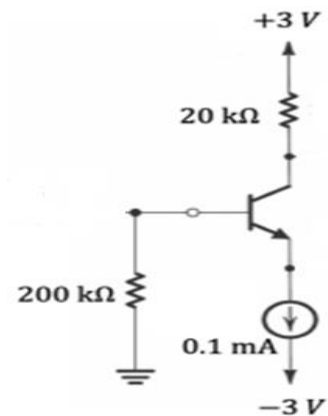
(d) CE with  $R_E$  amplifier.

$$R_i = R_B \parallel \left[ R_E + r_\pi + \frac{\beta R_E}{1 + \frac{[R_E + R_C \parallel R_L]}{r_o}} \right] = 200k \parallel [101 \times 0.25k + 25.25k] = 40.32 \text{ k}\Omega$$

$$R_o = R_C \parallel [r_o(1 + g_m(r_\pi \parallel R_E))] = 20 \text{ k}\Omega$$

$$A_{vo} = \frac{-R_C}{R_E + \left(1 + \frac{R_C}{r_o}\right) \frac{R_E + r_\pi}{\beta}} = \frac{-20k}{0.25k + \frac{0.25k + 25.25k}{100}} = -39.6 \text{ V/V}$$

$$A_v = A_{vo} \times \frac{R_L}{R_o + R_L} = -19.8$$





$$A = A_v \times \frac{R_i}{R_i + R_{sig}} = -13.235$$

(e)  $v_{b,max} = 10 \text{ mV}$

$$v_{sig,max} = v_{b,max} \times \frac{R_i + R_{sig}}{R_i} = v_{b,max} \times \frac{A_v}{A} = 14.96 \text{ mV}$$

$$v_{o,max} = v_{sig,max} \times |A| = v_{b,max} \times |A_v| = 198 \text{ mV}$$