

First order circuits 008

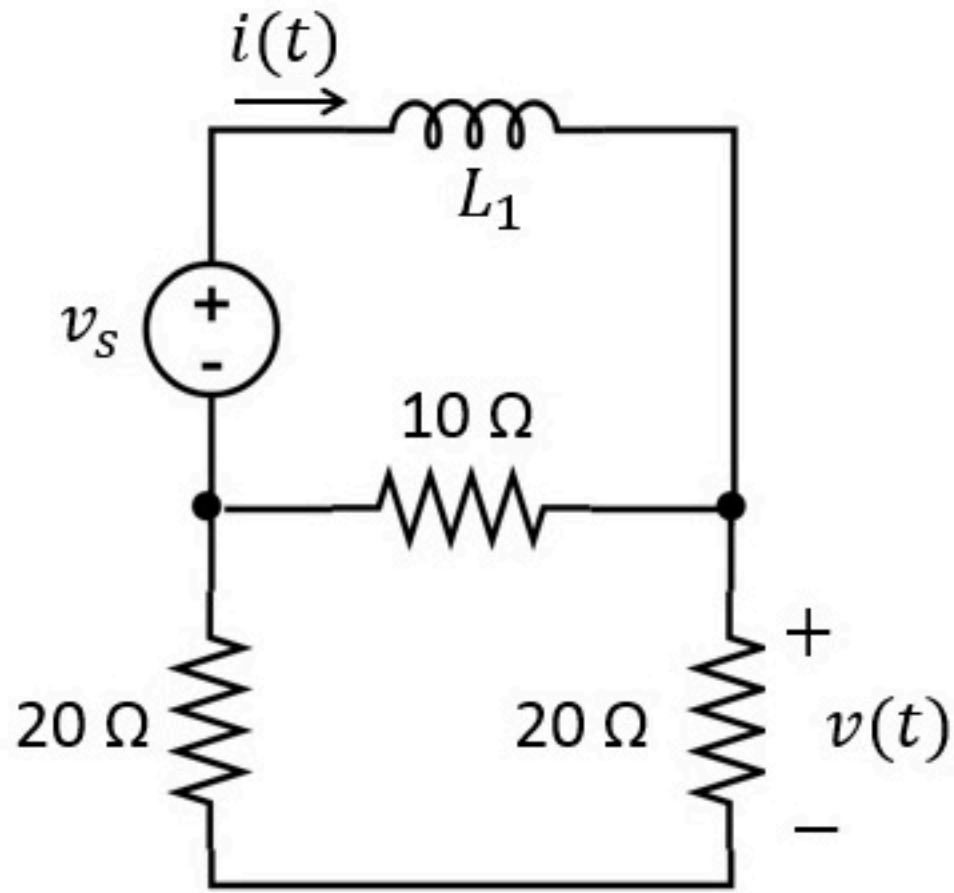
Unlimited Attempts.

When $t < 0$, $v_s = V_0$

When $t > 0$, $v_s = V_1$

Find $i(t) = A_1 + B_1 \cdot e^{-t/\tau_1}$ for $t > 0$

and $v(t) = A_2 + B_2 \cdot e^{-t/\tau_2}$ for $t > 0$



Given Variables:

$V_0 : 24\text{ V}$

$V_1 : 32\text{ V}$

$L_1 : 4\text{ mH}$

Calculate the following:

$A_1\text{ (A)} :$

4

✓

$B_1\text{ (A)} :$

-1

✓

$\tau_1\text{ (ms)} :$

0.5

✓

$A_2\text{ (V)} :$

16

✓

$B_2\text{ (V)} :$

-4

✓

$\tau_2\text{ (ms)} :$

0.5

✓

Hint: What is the current i_L for $t < 0$? Note where A and B are.

When $t < 0$, $v_s = V_0$

When $t > 0$, $v_s = V_1$

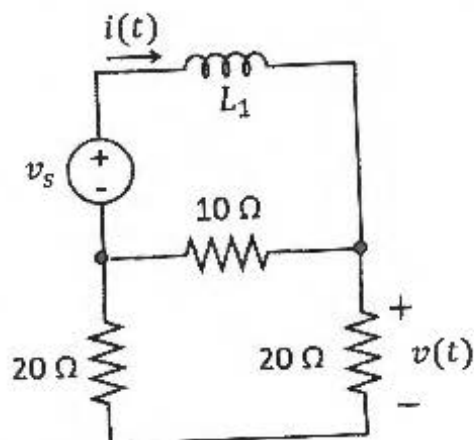
Find $i(t) = A_1 + B_1 \cdot e^{-t/\tau_1}$ for $t > 0$

and $v(t) = A_2 + B_2 \cdot e^{-t/\tau_2}$ for $t > 0$

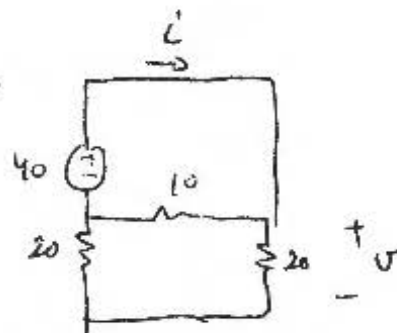
$V_0 = 40 \text{ V}$

$V_1 = 64 \text{ V}$

$L_1 = 2 \text{ mH}$



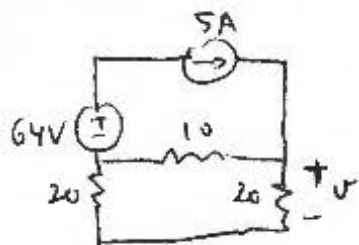
(a) $t = 0^-$



$$i(0^-) = \frac{40}{10 \parallel 20} = \frac{40}{8} = 5 \text{ A}$$

$$v(0^-) = 40 \cdot \frac{20}{20+20} = 20 \text{ V}$$

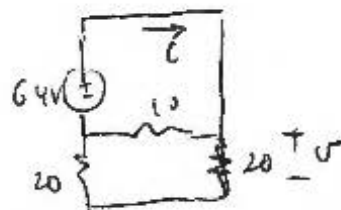
(b) $t = 0^+$



$$i(0^+) = 5 \text{ A}$$

$$v(0^+) = (5 \text{ A}) \cdot (10 \parallel 20) \cdot \frac{20}{20+20} = 20 \text{ V}$$

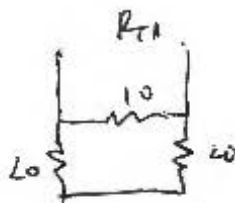
(c) $t = \infty$



$$i(\infty) = \frac{64}{10 \parallel 20} = 8 \text{ A}$$

$$v(\infty) = 64 \cdot \frac{20}{20+20} = 32 \text{ V}$$

(d)



$$R_{TH} = 10 \parallel 20 = 8 \Omega$$

$$\tau = \frac{L_1}{R_{TH}} = \frac{2 \cdot 10^{-3}}{8} = 0.25 \cdot 10^{-3}$$

$$A_1 = i(\infty) \Rightarrow \boxed{A_1 = 8 \text{ A}}$$

$$A_2 = v(\infty) \Rightarrow \boxed{A_2 = 32 \text{ V}}$$

$$B_1 + A_1 = i(0^+) \Rightarrow \boxed{B_1 = -3 \text{ A}}$$

$$B_2 + A_2 = v(0^+) \Rightarrow \boxed{B_2 = -12 \text{ V}}$$

$$\boxed{\tau_1 = \tau_2 = 0.25 \text{ ms}}$$