

Find  $P$  and  $Q$ .

a: 2.

b: 1.

Note: We've used bold capital letters to denote complex variables. The  $*$  operator stands for complex conjugate. The  $\text{Re}[]$  and  $\text{Im}[]$  operators stand for taking the real part and imaginary part respectively.

$$\mathbf{V}_0 = ae^{j\frac{\pi}{6}} \quad \mathbf{Z}_1 = 2 + j \quad \mathbf{Z}_2 = bj$$

$$\mathbf{I}_1 = \frac{\mathbf{V}_0}{\mathbf{Z}_1} \quad \mathbf{V}_1 = \mathbf{Z}_2 \cdot \mathbf{I}_1 \quad \mathbf{S} = \frac{1}{2} \cdot \mathbf{V}_1 \cdot \mathbf{I}_1^*$$

$$P = \text{Re}[\mathbf{S}] \quad Q = \text{Im}[\mathbf{S}]$$

$$S = \frac{1}{2} V_1 I_1^* = \frac{1}{2} Z_2 I_1 \cdot I_1^* = \frac{1}{2} \cdot j \cdot |I_1|^2$$

$$I_1 = \frac{V_0}{Z_1} \Rightarrow |I_1|^2 = \frac{|V_0|^2}{|Z_1|^2} = \frac{a^2}{4+1} = \frac{4}{5}$$

$$\Rightarrow S = \frac{1}{2} \cdot j \cdot \frac{4}{5} = j \cdot \frac{4}{10}$$

$$\boxed{P = 0}$$

$$\boxed{Q = 0.4}$$