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CS 210

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## Assignment #2

- 1)  $\langle \text{pattern} \rangle ::= \langle \text{name} \rangle \mid \_ \mid \langle \text{constant} \rangle \mid \langle \text{tuple} \rangle \mid \langle \text{list} \rangle \mid \langle \text{cons} \rangle$   
 $\langle \text{more patterns} \rangle ::= \langle \text{pattern} \rangle \langle \text{more patterns} \rangle \mid \langle \text{empty} \rangle$   
 $\langle \text{tuple} \rangle ::= (\langle \text{pattern} \rangle, \langle \text{pattern} \rangle \langle \text{more patterns} \rangle)$   
 $\langle \text{list} \rangle ::= [] \mid [\langle \text{list element} \rangle \langle \text{more list elements} \rangle]$   
 $\langle \text{cons} \rangle ::= \langle \text{list element} \rangle :: \langle \text{list} \rangle$   
 $\langle \text{more list elements} \rangle ::= \langle \text{list element} \rangle \langle \text{more list elements} \rangle \mid \langle \text{empty} \rangle$

2)b) 

Step	Action
1	$x = 3k$ ; $k$ is an integer
2	$y = 24m$ ; $m$ is an integer
3	$y = 24m$ $= 3(8m)$ $x = 3k$ ; $k$ is an integer because $(8m)$ is an integer $\therefore x := y$ is safe

c) Counter example: 7 is a prime integer greater than 3  
and is not divisible by 3  
 $\therefore Z := X$  is unsafe

Back Side



e) Step Action

- 1  $y = 24k$ ;  $k$  is an integer
- 2  $z$  is a prime integer  $> 3$
- 3 This must mean  $z$  is odd
- 4  $z^2 - 1 = (z-1)(z+1)$
- 5  $(z-1) \div (z+1)$  are both even integers  
 $\div$  because they are both consecutive even integers,  
 either  $(z-1)$  is a multiple of 4  $\div$   $(z+1)$  is a  
 multiple of 2 or  $(z-1)$  is a multiple of 2  
 $\div$   $(z+1)$  is a multiple of 4
- 6  $(z-1)$  or  $(z+1)$  must also be a multiple of 3  
 because  $(z-1)$ ,  $z$ ,  $\div$   $(z+1)$  are 3 consecutive integers;  
 $z$  can't be divisible by 3 because it is prime
- 7  $y = 2 \cdot 2 \cdot 2 \cdot 3 \cdot k = 24k$   
 $\therefore Y := (z * z) - 1$  is safe

Work:  $x$  is prime integer  $> 3$

$$x^2 - 1 = (x-1)(x+1)$$

$$\begin{array}{ccccc} (x-1) & \times & (x+1) \\ \uparrow & & \uparrow & & \uparrow \\ \text{even} & & \text{odd} & & \text{even} \end{array}$$

3)

