Assignment 1

Your Full Name Your Student ID

February 27, 2025

Abstract

Course: SOEN 331

Instructor: Dr. Constantinos Constantinides **Due Date:** Tuesday, 4 March 2025 (23:59)

Weight: 10% of the overall grade

General information

Introduction and ground rules

- 1 Problem 1: Propositional Logic (7 pts)
- 1.1 Statement by Sophia the robot (3 pts)
- 1.2 Argument from "Computing Machinery and Intelligence" $(4~\mathrm{pts})$

2 Problem 2: Predicate Logic (8 pts)

2.1 Interpreting given formalizations (4 pts)

- (a) $\forall x : \mathbb{R} : \text{number}(x) \to \neg \text{rational}(x)$
- (b) $\exists x : \mathbb{R} : \text{number}(x) \land \text{rational}(x)$

2.2 Formalizing statements (4 pts)

- \bullet (a) "There are no irrational real numbers."
- (b) "Some real numbers are irrational."

3 Problem 3: Linear Temporal Logic 1 (15 pts)

- 3.1 (3 pts)
- 3.2 (3 pts)
- 3.3 (3 pts)
- 3.4 (3 pts)
- 3.5 (3 pts)

- 4 Problem 4: Linear Temporal Logic 2 (15 pts)
- 4.1 Visualizing all models of behavior (9 pts)
- 4.2 Mathematical structures (4 pts)
- 4.3 Observations on termination, non-termination, consistency (2 pts)

5 Problem 5: Unordered Structures (10 pts)

- 6 Problem 6: Ordered Structures (10 pts)
- 6.1 Implementing a Queue using two lists (4 pts)
- 6.2 Defining Enqueue and Dequeue (6 pts)

7 Problem 7: Binary Relations, Functions, and Orderings (15 pts)

7.1 Poset proofs and Hasse diagrams

- (a) $(\{2,3,4,6,24,36,72\},/)$ is a poset (2 pts) Hasse diagram, maximal/minimal elements
- (b) $(\mathcal{P}\{1,2,3\},\subseteq)$ is a poset (1 pt) Hasse diagram, maximal/minimal elements
- 7.2 Analyzing variable map (12 pts)

- 8 Problem 8: Binary Relations, Functions, and Orderings 2 (10 pts)
- 8.1 Is map2 a function, domain/codomain (2 pts)
- 8.2 Properties (8 pts)

9 Problem 9: Construction Techniques (10 pts)

9.1 Function map (f, Λ) (5 pts)

- (a) Transform into computable function
- (b) Define function recursively

9.2 Function insert (x, Λ) (5 pts)

- $\bullet \,$ (a) Transform into computable function
- ullet (b) Define function recursively
- (c) Unfold example: $insert(5, \langle 1, 3, 5, 7 \rangle)$

What to submit