# MATHFUN Lecture FP4 Strings, Tuples and Lists

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2014/15

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- In the following lecture we look at how to write list-processing functions using recursion.

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- An example function definition that processes such tuples is:

• For example,

```
ghci> betterStu ("Jim",45) ("Fred",87)
"Fred"
```

It's often a good idea to define a type synonym:
 type StudentMark = (String, Int)
 and use StudentMark in place of (String, Int).

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 Tuples can be used in the result type of a function to enable it to return more than one value; e.g.:

#### Lists

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- For example:

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[12, 64, -92, 85, 12]
is a list of integers, and
   ["This", "is", "a", "list"]
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is a list of strings.
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 For any type t, we denote the type of lists of elements from t by [t]. For example:

```
ghci> :type [True, False, False]
[True, False, False] :: [Bool]
```

• The empty list [] is an element of any list type.

# Strings as lists of Chars

• Strings in Haskell are simply lists of characters: the type String is declared as:

```
type String = [Char]
```

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• The list operations that we see later (e.g. for concatenating lists) thus also apply to strings.

```
ghci> :type ["This", "is", "a", "sentence"]
```

• What are the types of the following expressions?

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["This","is","a","sentence"] :: [[Char]]
ghci>
```

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## Lists from ranges

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• For example:

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[3 .. 9] = [3,4,5,6,7,8,9]
[3.1 .. 9] = [3.1,4.1,5.1,6.1,7.1,8.1,9.1]
['a' .. 'z'] = "abcdefghijklmnopqrstuvwxyz"
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 $['a' ... 'z']$  = "abcdefghijklmnopqrstuvwxyz"

• We can also add an argument to give steps different from 1:

$$[3, 5 \dots 15]$$
 =  $[3,5,7,9,11,13,15]$   $[0, 0.1 \dots 0.5]$  =  $[0.0,0.1,0.2,0.3,0.4,0.5]$ 

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- We read this as: "take all 2\*i where i comes from aList."
- (The <- is meant to resemble the set member symbol  $\in$ .)
- List comprehensions are a powerful feature (almost) unique to functional programming languages.
- (A few imperative languages (e.g. Python) have some functional programming facilities including list comprehensions.)

 Let's look at some further examples; suppose here that the list aList is defined as:

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We can add a test at the end of the generator i <- aList:</li>

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• Here, the generator/test has given all the values in aList that are less than 5; i.e. 2, 3, 4.

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- For example, consider the definition:

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addPairs :: [(Int,Int)] -> [Int]
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• For some final examples, recall the type synonym:

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An example of the type [StudentMark] of name/mark lists is:

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[("Sam", 67), ("Kate", 35), ("Jill", 75)]
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• The following definition will generate a list of just the marks:

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- We call a function that has many types a **polymorphic** function.
- The actual type of length is given as:

```
length :: [a] -> Int
```

 Here a is a type variable that stands for an arbitrary type (i.e. its possible values are types).

- (By convention, a, b, c, ... are used as type variables.)
- Types [String] -> Int and [Bool] -> Int are instances of type [a] -> Int (they are found by replacing a with a type).
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square :: Num a => a -> a says that the type is a -> a where a can be any numeric type.
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5
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8