

Three S's

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Using R Markdown

Using R Markdown allows us to write both text and code in the same document. Use R code chunks to insert code:

```
```{r}
Some code
x <- 1:10
```
```

Use inline R to write answers inline using the following format: ``r R_CODE``. For example, to compute the mean of the values 1, 3, 5, and 7, one might can use ``r mean(c(1, 3, 5, 7))``. The mean of 1, 3, 5, and 7 is 4.

Using packages

To use functions in packages such as `psych`, one must either specify the package by prepending the function with the package name and two colons or load the package using the command `library(PackageName)`.

Consider using the function `describe` on the `mtcars` data set.

```
describe(mtcars) # psych has not been loaded!
```

```
Error in describe(mtcars): could not find function "describe"
```

```
psych::describe(mtcars)
```

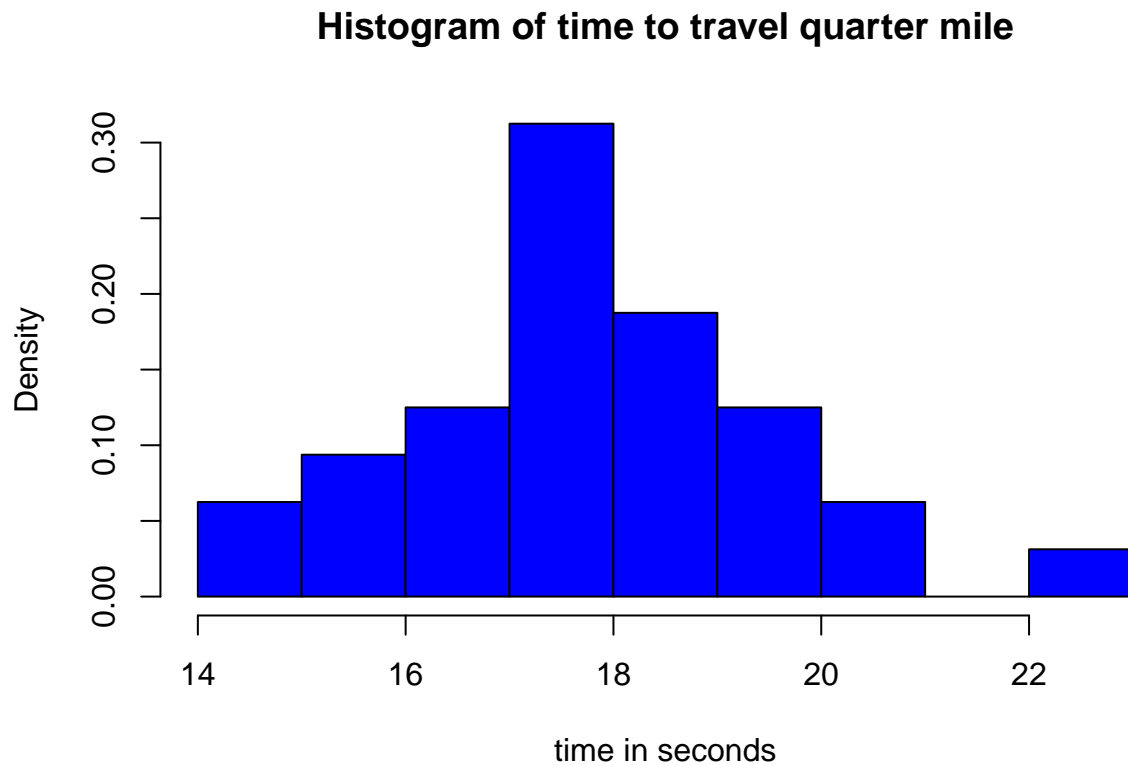
| | vars | n | mean | sd | median | trimmed | mad | min | max | range | skew |
|------|----------|-------|--------|--------|--------|---------|--------|-------|--------|--------|-------|
| mpg | 1 | 32 | 20.09 | 6.03 | 19.20 | 19.70 | 5.41 | 10.40 | 33.90 | 23.50 | 0.61 |
| cyl | 2 | 32 | 6.19 | 1.79 | 6.00 | 6.23 | 2.97 | 4.00 | 8.00 | 4.00 | -0.17 |
| disp | 3 | 32 | 230.72 | 123.94 | 196.30 | 222.52 | 140.48 | 71.10 | 472.00 | 400.90 | 0.38 |
| hp | 4 | 32 | 146.69 | 68.56 | 123.00 | 141.19 | 77.10 | 52.00 | 335.00 | 283.00 | 0.73 |
| drat | 5 | 32 | 3.60 | 0.53 | 3.70 | 3.58 | 0.70 | 2.76 | 4.93 | 2.17 | 0.27 |
| wt | 6 | 32 | 3.22 | 0.98 | 3.33 | 3.15 | 0.77 | 1.51 | 5.42 | 3.91 | 0.42 |
| qsec | 7 | 32 | 17.85 | 1.79 | 17.71 | 17.83 | 1.42 | 14.50 | 22.90 | 8.40 | 0.37 |
| vs | 8 | 32 | 0.44 | 0.50 | 0.00 | 0.42 | 0.00 | 0.00 | 1.00 | 1.00 | 0.24 |
| am | 9 | 32 | 0.41 | 0.50 | 0.00 | 0.38 | 0.00 | 0.00 | 1.00 | 1.00 | 0.36 |
| gear | 10 | 32 | 3.69 | 0.74 | 4.00 | 3.62 | 1.48 | 3.00 | 5.00 | 2.00 | 0.53 |
| carb | 11 | 32 | 2.81 | 1.62 | 2.00 | 2.65 | 1.48 | 1.00 | 8.00 | 7.00 | 1.05 |
| | kurtosis | | se | | | | | | | | |
| mpg | | -0.37 | 1.07 | | | | | | | | |
| cyl | | -1.76 | 0.32 | | | | | | | | |
| disp | | -1.21 | 21.91 | | | | | | | | |
| hp | | -0.14 | 12.12 | | | | | | | | |
| drat | | -0.71 | 0.09 | | | | | | | | |
| wt | | -0.02 | 0.17 | | | | | | | | |
| qsec | | 0.34 | 0.32 | | | | | | | | |
| vs | | -2.00 | 0.09 | | | | | | | | |
| am | | -1.92 | 0.09 | | | | | | | | |

```
gear    -1.07  0.13
carb     1.26  0.29
```

Characterizing qsec

- Shape

```
hist(mtcars$qsec, col = "blue", freq = FALSE,
     main = "Histogram of time to travel quarter mile",
     xlab = "time in seconds")
```



- Center

```
Mean <- mean(mtcars$qsec)
Mean
```

```
[1] 17.84875
```

- Spread

```
SD <- sd(mtcars$qsec)
SD
```

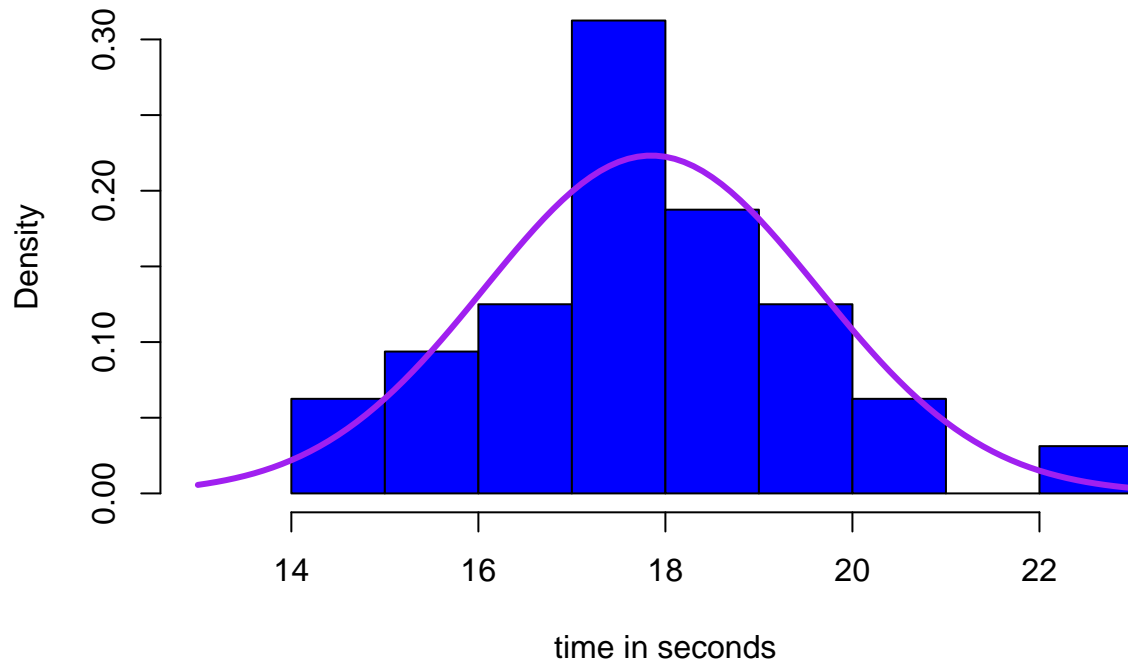
```
[1] 1.786943
```

The distribution of `qsec` is unimodal and symmetric with a mean of 17.85 seconds and a standard deviation of 1.79 seconds.

Superimposing a Normal Distribution

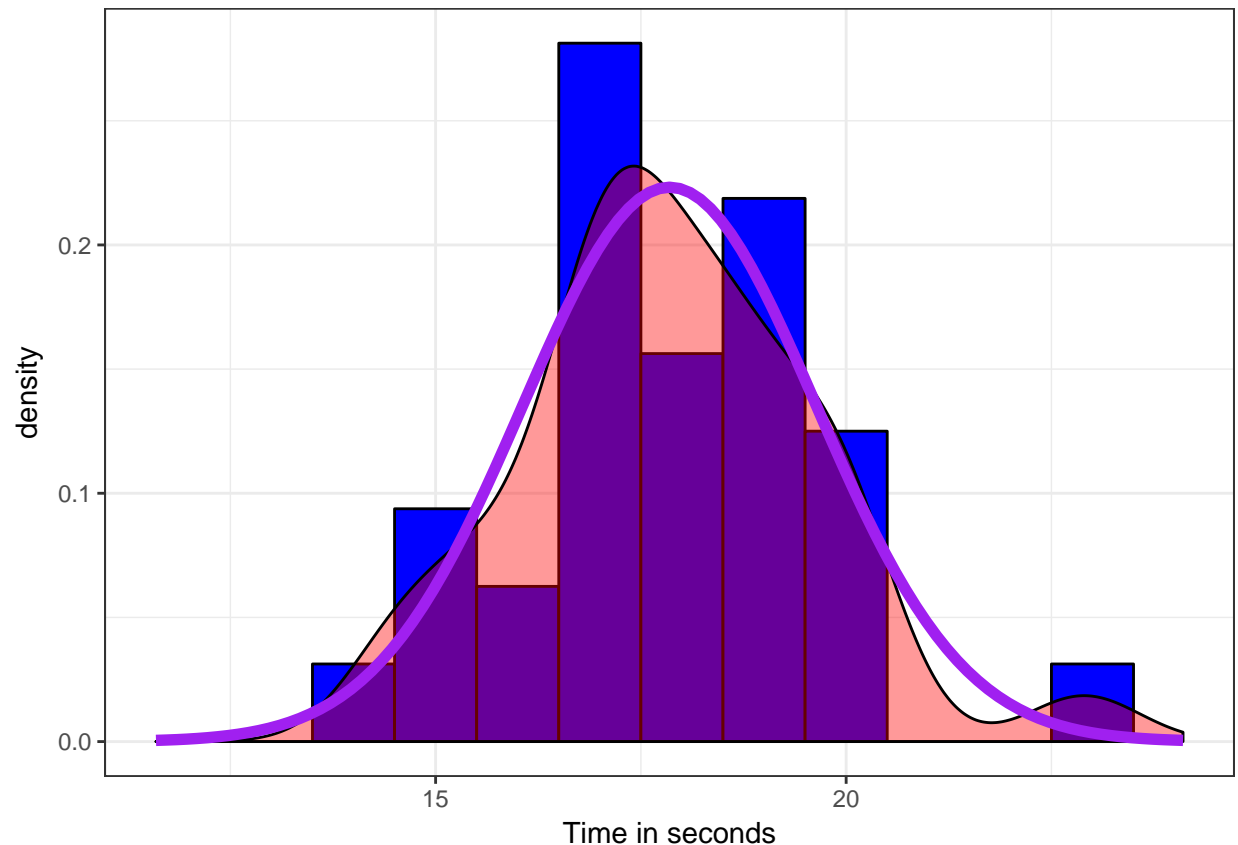
```
hist(mtcars$qsec, col = "blue", freq = FALSE,
     main = "Histogram of time to travel quarter mile",
     xlab = "time in seconds", xlim = c(13, 23))
curve(dnorm(x, Mean, SD), 13, 23, col = "purple", add = TRUE, lwd = 3)
```

Histogram of time to travel quarter mile



Using ggplot2

```
library(ggplot2)
ggplot(data = mtcars, aes(x = qsec, ..density..)) +
  geom_histogram(binwidth = 1, fill = "blue", color = "black") +
  xlim(Mean - 3.5*SD, Mean + 3.5*SD) +
  labs(x = "Time in seconds") +
  geom_density(fill = "red", alpha = 0.4) +
  stat_function(fun = dnorm, args = list(mean = Mean, sd = SD),
               inherit.aes = FALSE, size = 2, color = "purple") +
  theme_bw()
```



Tests of Significance

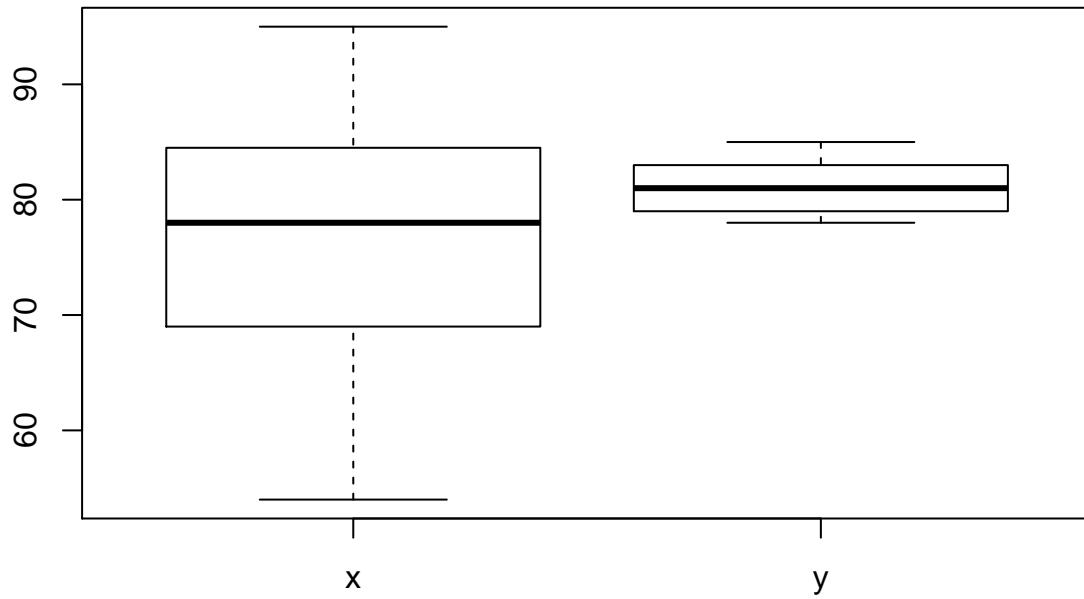
1. Hypotheses — State the null and alternative hypotheses.
2. Test Statistic
3. Rejection Region Calculations
4. Statistical Conclusion
5. English Conclusion

Example 9.12 from PASWR2

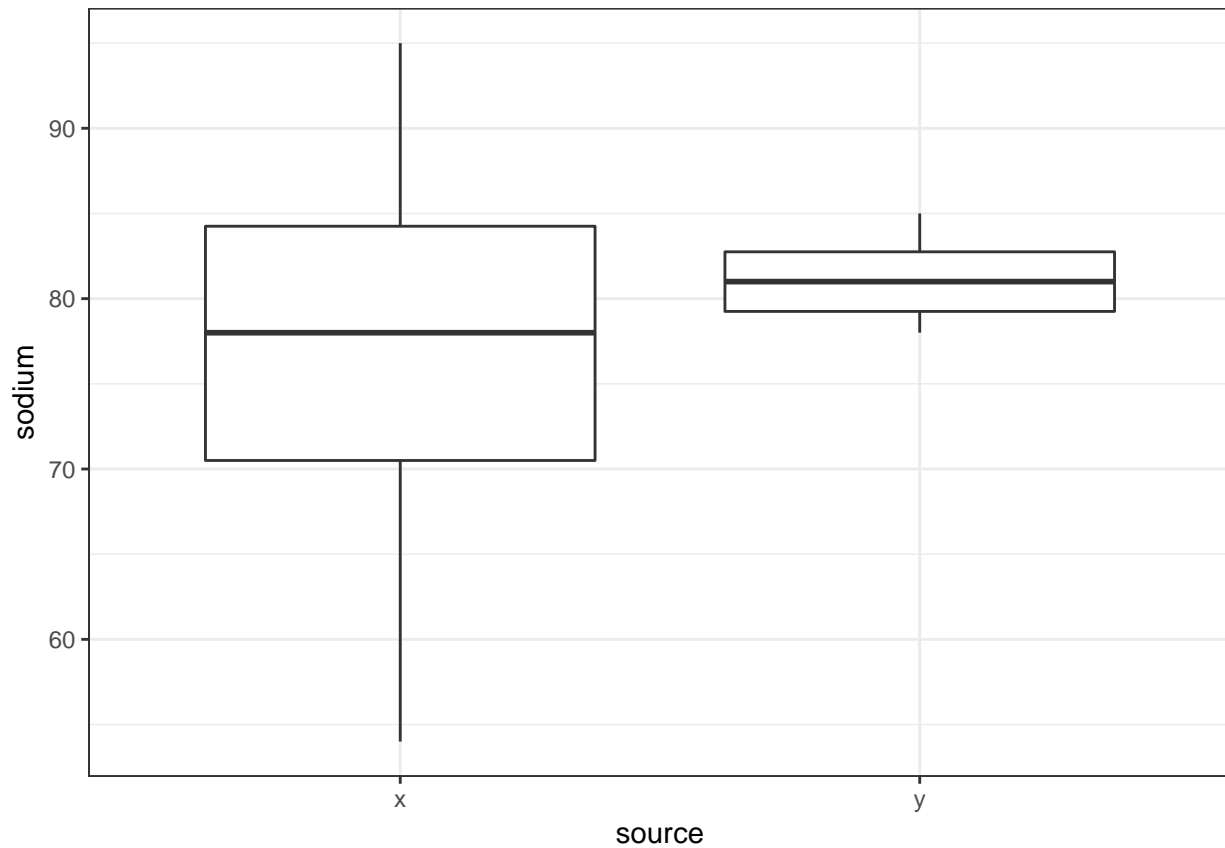
A bottled water company acquires its water from two independent sources, X and Y. The company suspects that the sodium content in the water from source X is less than the sodium content from source Y. An independent agency measures the sodium content in 20 samples from source X and 10 samples from source Y and stores them in data frame `WATER` of the `PASWR2` package. Is there statistical evidence to suggest the average sodium content in the water from source X is less than the average sodium content in Y?

Solution: To solve this problem, start by verifying the reasonableness of the normality assumption.

```
library(PASWR2)      # load the PASWR2 package
library(ggplot2)     # load the ggplot2 package
library(lsr)         # load the lsr package
library(DescTools)   # load the DescTools package
boxplot(sodium ~ source, data = WATER)
```



```
ggplot(data = WATER, aes(x = source, y = sodium)) +  
geom_boxplot() +  
theme_bw()
```



```
LeveneTest(sodium ~ source, data = WATER)
```

Levene's Test for Homogeneity of Variance (center = median)

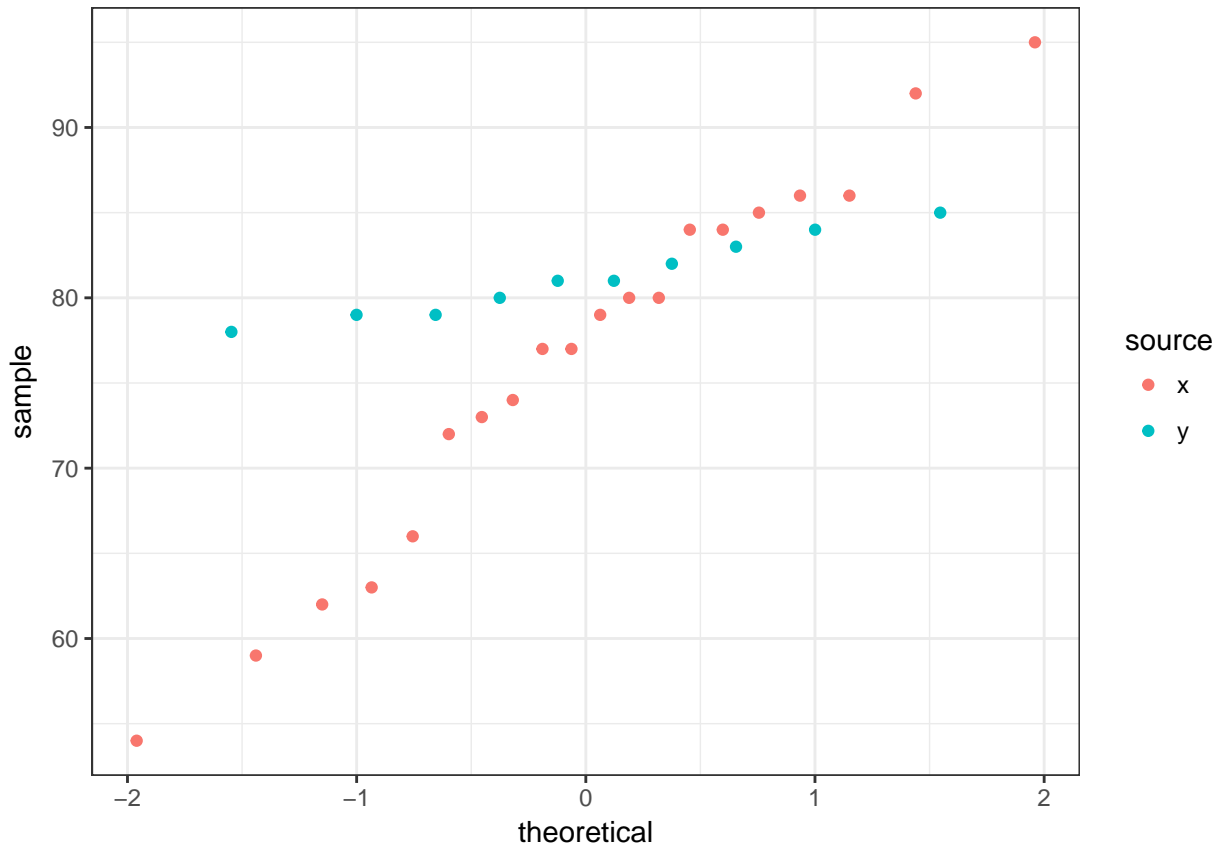
| Df | F value | Pr(>F) |
|----|---------|--------|
| 1 | 1.1 | 0.30 |

```
group 1 10.033 0.003697 **
28
```

```
---
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
ggplot(data = WATER, aes(sample = sodium, color = source)) +
  stat_qq() +
  theme_bw()
```



```
CohenD(WATER$x, WATER$y, na.rm = TRUE)
```

```
[1] -0.5205894
attr("magnitude")
[1] "medium"
```

```
cohensD(formula = sodium ~ source, data = WATER)
```

```
[1] 0.5205894
```

1. **Hypotheses** — $H_0 : \mu_X - \mu_Y = 0$ versus $H_1 : \mu_X - \mu_Y < 0$
2. **Test Statistic** — The test statistic is $\bar{X} - \bar{Y}$. The standardized test statistic under the assumption that H_0 is true and its approximate distribution are

$$\frac{[(\bar{X} - \bar{Y} - \delta_0)]}{\sqrt{\frac{S_X^2}{n_x} + \frac{S_Y^2}{n_Y}}} \sim t_\nu$$

3. **Rejection Region Calculations** — $P(t_{obs} < t_{0.05, 22.069}) = -1.7169086$.

```
TR <- t.test(sodium ~ source, data = WATER, alternative = "less")
TR
```

Welch Two Sample t-test

```
data: sodium by source
t = -1.8589, df = 22.069, p-value = 0.03822
alternative hypothesis: true difference in means is less than 0
95 percent confidence interval:
    -Inf -0.3665724
sample estimates:
mean in group x mean in group y
      76.4         81.2
```

4. **Statistical Conclusion** — Since the p-value is 0.0382165, reject the null hypothesis.
5. **English Conclusion** — There is evidence to suggest the average sodium content for source X is less than the average sodium content for source Y.