Name:	
GitHub Username:	
Purdue Username:	
Instructor:	
Section:	
Problem 1	
Part A	
Given the probability density function:	
$f_X(x) = \begin{cases} \frac{3x^2}{2} & when \ x \in [-1,1] \\ 0 & otherwise \end{cases}$	
Use Python to plot the probability density function from -1 to 1. When looking at the plot determine by inspection what is the mean of the distribution.	
Mean of the distribution:	
From this distribution we grab 100 i.i.d samples X_1 , X_2 , X_{100} .	
The sample mean random variable is defined as	
$\bar{X}_n = \frac{1}{n} \sum_{i=1}^n X_i$	
We know that the variance of each X_i is $\frac{3}{5}$.	
What is the shape of the probability density function of the sample mean?	
What is the mean of the probability density function of the sample mean?	
Explain how you know the shape and mean.	

Part B

of the random variable Y = -X (Give you	ur answer with the shape, mean and variance).
What is the shape of the distribution?	
What is the mean?	
What is the variance?	

Let X be a normally distributed random variable with mean = 0 and variance = 1. What is the distribution

Problem 2

Yes

A student exploring making a car maintenance subscription service an "uber for oil changes" is pretty confident that the average age of used cars on campus (the vehicle_survey_1.txt population) is 8 years old.

1. Formulate null and alternative hypotheses for a statistical test that seeks to challenge this

belief. What are the null and alternative hypotheses? **Null Hypothesis:** Alternative Hypothesis: What type of test should be used and why? 2. Carry out this statistical test using the vehicle_survey_1 sample. Report the sample size, the sample mean, the standard error, the standard score (z or t, depending on what was used), and the p-value. *****ROUND ALL DECIMAL VALUES TO 4 DECIMAL PLACES**** Sample size Sample mean Standard error Standard score p - value(if less than 0.01 use scientific notation) (For the following fill the box next to your selected answer) Are the results statistically significant at a level of 0.05?

No

	What (if anything) can we conclude about the	e hypothesis at the confidence level of 0.05?	
	(For the following fill the box next to your se Are the results statistically significant at a lev		
	Yes	No	
	What (if anything) can we conclude about the	e hypothesis at the confidence level of 0.10?	
3.	3. What is the largest standard error for which the test will be significant at a level of 0.05?		
	What is the corresponding minimum sample variance and mean does not change.)	size? (You may assume that the population	
	******ROUND ALL DECIMAL VALUES	S TO 4 DECIMAL PLACES****	
	Largest standard error		
	corresponding minimum sample size		
4.	Suppose the student is also convinced that the whose owners regularly change their own oil those who do not (the vehicle_survey_3 popularly potheses that seek to validate this belief. We and what type of test can be used?	(the vehicle_survey_2 population) and lation). Formulate null and alternative	
ll Hy	rpothesis:		
	•		
erna	ative Hypothesis:		
l 4 4	hung af kant ah sulal ha wasad an dunku 2		
nat t	type of test should be used and why?		

	Report the sample sizes, the sample means, the standard e value. Are the results significant at levels 0.05 or 0.10? W	rror, the z-score, and the p-			
conclude about the hypothesis at the two different confidence levels? *****ROUND ALL DECIMAL VALUES TO 4 DECIMAL PLACES***					
	Sample size of vehicle_survey_2 (non oil changers)				
	Sample size of vehicle_survey_3 (oil changers)				
	Sample mean of vehicle_survey_2 (non oil changers)				
	Sample mean of vehicle_survey_3 (non oil changers)				
	Standard error				
	Standard score				
	p – value (if less than 0.01 use scientific notation)				
(For the	e following, fill the box next to your selected answer) results statistically significant at a level of 0.05?				
Yes	No				
Are the	results statistically significant at a level of 0.10?				
Yes	No				
What (if	anything) can we conclude (i.e., what is the interpretation of	the result)?			

Problem 3

Wider

	standard error, the standard stati	Il use a z-test or t-test and report the sample mean, the stic (t or z value), and the interval. (Think, which if very few datapoints are available?)
	l you use a t-test or z-test (Hint: Thi nts are available)? Justify your ansv	nk which distribution should you use here if very few data ver.
	*****ROUND ALL DECIM	AL VALUES TO 4 DECIMAL PLACES****
	Sample mean	
	Standard error	
	Standard score (t or z score)	
	90% confidence interval	
2.	Repeat Q1 for a 95% confidence ******ROUND ALL DECIM	e interval. AL VALUES TO 4 DECIMAL PLACES****
	Standard error	
	Standard score (t or z score)	
	95% confidence interval	

Is your interval wider or narrower compared to using the 90% confidence interval in Q1?

Narrower

(For the following, fill the box next to your selected answer)

1. Use the sample to construct a 90% confidence interval for the weight of the robots on

Will you use a t-test or z-test (Hint: Think which distribution should you use here now that you have the true population standard deviation)? Justify your answer.				
******ROUND ALL DECIMAL VALUES TO 4 DECIMAL PLACES****				
Standard error				
Standard score (t or z score)				
95% confidence interval				

Is your interval wider or narrower than the interval computed in Q2? $(Fill\ Box\ to\ select\ your\ answer)$

Narrower

3. Repeat Q2 if you are told that the population standard deviation is 10.

Wider