

Relational Algebra

- 1) All_Course_aIDs $\sqsubset \pi$ aID (Training_Course)
All_DB_aIDs $\sqsubset \pi$ aID (σ aTitle = 'Databases' (Technology_Area))
All_DB_Course_aIDs \sqsubset All_Course_aIDs * All_DB_aIDs
Result $\sqsubset \pi$ cID, cTitle, cHours (All_DB_Course_aIDs \Join aID = aID (Training_Course))
- 2) All_Course_aIDs $\sqsubset \pi$ aID (Training_Course)
All_DB_aIDs $\sqsubset \pi$ aID (σ aTitle = 'Databases' (Technology_Area))
All_DB_Course_aIDs \sqsubset All_Course_aIDs * All_DB_aIDs
All_DB_Course_cIDs $\sqsubset \pi$ cID (All_DB_Course_aIDs \Join aID = aID (Training_Course))
EIDs_Taken_DB_Course $\sqsubset \pi$ eID (All_DB_Course_cIDs \Join cID = cID (Takes))
Result $\sqsubset \pi$ eID, eFirst, eLast, eTitle (EIDs_Taken_DB_Course \Join eID = eID (Employee))
- 3) All_Course_aIDs $\sqsubset \pi$ aID (Training_Course)
All_DBNW_aIDs $\sqsubset \pi$ aID (σ aTitle = 'Databases' OR aTitle = 'Networks' (Technology_Area))
All_DBNW_Course_aIDs \sqsubset All_Course_aIDs * All_DBNW_aIDs
All_DBNW_Course_cIDs $\sqsubset \pi$ cID (All_DBNW_Course_aIDs \Join aID = aID (Training_Course))
EIDs_Taken_DBNW_Course $\sqsubset \pi$ eID (All_DBNW_Course_cIDs \Join cID = cID (Takes))
Result $\sqsubset \pi$ eID, eFirst, eLast, eTitle (EIDs_Taken_DBNW_Course \Join eID = eID (Employee))
- 4) All_DB_aIDs $\sqsubset \pi$ aID (σ aTitle = 'Databases' (Technology_Area))
All_NW_aIDs $\sqsubset \pi$ aID (σ aTitle = 'Networks' (Technology_Area))
All_DB_Course_cIDs $\sqsubset \pi$ cID (All_DB_Course_aIDs \Join aID = aID (Training_Course))
All_NW_Course_cIDs $\sqsubset \pi$ cID (All_NW_Course_aIDs \Join aID = aID (Training_Course))
EIDs_Taken_DB_Course $\sqsubset \pi$ eID (All_DB_Course_cIDs \Join cID = cID (Takes))
EIDs_Taken_NW_Course $\sqsubset \pi$ eID (All_NW_Course_cIDs \Join cID = cID (Takes))
EIDs_DB_No_NW_Course \sqsubset EIDs_Taken_DB_Course $-$ EIDs_Taken_NW_Course
Result $\sqsubset \pi$ eID, eFirst, eLast, eTitle (EIDs_DB_No_NW_Course \Join eID = eID (Employee))
- 5) All_DB_aIDs $\sqsubset \pi$ aID (σ aTitle = 'Databases' (Technology_Area))
All_NW_aIDs $\sqsubset \pi$ aID (σ aTitle = 'Networks' (Technology_Area))
All_DB_Course_cIDs $\sqsubset \pi$ cID (All_DB_Course_aIDs \Join aID = aID (Training_Course))
All_NW_Course_cIDs $\sqsubset \pi$ cID (All_NW_Course_aIDs \Join aID = aID (Training_Course))
EIDs_Taken_DB_Course $\sqsubset \pi$ eID (All_DB_Course_cIDs \Join cID = cID (Takes))
EIDs_Taken_NW_Course $\sqsubset \pi$ eID (All_NW_Course_cIDs \Join cID = cID (Takes))
EIDs_DB_And_NW_Course \sqsubset EIDs_Taken_DB_Course \cap EIDs_Taken_NW_Course
Result $\sqsubset \pi$ eID, eFirst, eLast, eTitle (EIDs_DB_And_NW_Course \Join eID = eID (Employee))
- 6) All_eIDs $\sqsubset \pi$ eID (Employee)
All_eIDs_Taken_Course $\sqsubset \pi$ eID (Takes)
All_eIDs_Not_Taken_Course \sqsubset All_eIDs $-$ All_eIDs_Taken_Course
Result $\sqsubset \pi$ eID, eFirst, eLast, eTitle (All_eIDs_Not_Taken_Course \Join eID = eID (Employee))
- 7) Takes_Copy $\sqsubset \pi$ eID (eID2), cID (cID2) (Takes)
Takes_Cross_Takes_Copy \sqsubset Takes \times Takes_Copy
EIDs_Diff_Courses $\sqsubset \pi$ eID (σ eID = eID2 AND cID \neq cID2 (Takes_Cross_Takes_Copy))
Result $\sqsubset \pi$ eID, eFirst, eLast, eTitle (EIDs_Diff_Courses \Join eID = eID (Employee))

- 8) CIDs_With_Titles $\sqsubset \pi$ cID, aTitle (Training_Course **J** areaID = aID (Technology_Area))
 EIDs_Takes_Course $\sqsubset \pi$ eID, aTitle (CIDs_With_Titles * Takes)
 EIDs_Takes_Course_Copy $\sqsubset \pi$ eID (eID2), aTitle (aTitle2) (EIDs_Takes_Course)
 EIDs_Takes_Cross \sqsubset EIDs_Takes_Course x EIDs_Takes_Course_Copy
 EIDs_1+_Area $\sqsubset \pi$ eID (σ eID = eID2, aTitle \neq aTitle2 (EIDs_Takes_Cross))
 Result $\sqsubset \pi$ eID, eFirst, eLast, eTitle (EIDs_1+_Area)
- 9) Lowest_Salary $\sqsubset f$ Min(Salary) (Employee)
 Result \sqsubset Lowest_Salary **J** MIN_Salary = Salary (Employee)
- 10) All_Internet_aIDs $\sqsubset \pi$ aID (σ aTitle = 'Internet' (Technology_Area))
 All_Internet_cIDs $\sqsubset \pi$ cID (All_Internet_aIDs **J** aID = aID (Training_Course))
 EIDs_Takes_CIDs $\sqsubset \pi$ eID, cID (Takes)
 EIDs_Taken_All_Internet \sqsubset EIDs_Takes_CIDs \div All_Internet_cIDs
 Result $\sqsubset \pi$ eID, eFirst, eLast, eTitle (EIDs_Taken_All_Internet **J** eID = eID (Employee))
- 11) All_EIDs $\sqsubset \pi$ eID (Employee)
 All_Internet_aIDs $\sqsubset \pi$ aID (σ aTitle = 'Internet' (Technology_Area))
 All_Internet_cIDs $\sqsubset \pi$ cID (All_Internet_aIDs **J** aID = aID (Training_Course))
 All_Combos \sqsubset All_EIDs x All_Internet_cIDs
 EIDs_Takes_CIDs $\sqsubset \pi$ eID, cID (Takes)
 Diff \sqsubset All_Combos – EIDs_Takes_CIDs
 Matches $\sqsubset \pi$ eID (EIDs_Takes_CIDs – Diff)
 Result $\sqsubset \pi$ eID, eFirst, eLast, eTitle (Matches **J** eID = eID (Employee))
- 12) All_EIDs_All_CIDs $\sqsubset \pi$ eID, cID (Takes)
 EIDs_Join_Course $\sqsubset \pi$ eID, areaID (All_EIDs_All_CIDs **J** cID = cID (Training_Course))
 Tech_Area_Join_EIDs $\sqsubset \pi$ eID, aID, aTitle (EIDs_Join_Course **J** areaID = aID (Technology_Area))
 Count_EIDs_Per_Area \sqsubset (aTitle f Count(eID) (Tech_Area_Join_EIDs)
 COUNT_RESULT $\sqsubset \pi$ aID (TechAreaID), aTitle (Title), COUNT_eID (Total_Enrollees) (Count_EIDs_Per_Area)
- 13) All_Leaders $\sqsubset \pi$ eID, aID (Employee **J** eID = aLeadID (Technology_Area))
 All_Course_Title $\sqsubset \pi$ aID, aTitle, cID (Technology_Area **J** aID = areaID (Training_Course))
 EIDs_Taken_Courses_Titles $\sqsubset \pi$ eID, aTitle (Takes **LOJ** cID = cID (All_Course_Title))
 Result $\sqsubset \pi$ eFirst, eLast, aTitle (EIDs_Taken_Courses_Titles **J** eID = eID (Employee))

Relational Calculus

$\exists \forall$

- 1) { c.cID, c.cTitle, c.cHours | **TRAINING_COURSE**(c) and ($\exists a$)(**TRAINING_AREA**(a) and c.areaID = a.aID) }
- 2) { e.eID, e.eFirst, e.eLast, e.eTitle | **EMPLOYEE**(e) and (($\exists c$)(**TAKES**(c) and c.eID = e.eID) and ($\exists c$)**TRAINING_COURSE**(c) c.areaID = a.aID) and ($\exists a$)(**TRAINING_AREA**(a) and aTitle = 'Databases')) }
- 3) { e.eID, e.eFirst, e.eLast, e.eTitle | **EMPLOYEE**(e) and (($\exists c$)(**TAKES**(c) and c.eID = e.eID) and ($\exists c$)**TRAINING_COURSE**(c) c.areaID = a.aID) and ($\exists a$)(**TRAINING_AREA**(a) and a.aTitle = 'Databases' or a.aTitle = 'Networks')) }
- 4)
- 5)

- 6)
- 7)
- 8)
- 9)
- 10)
- 11)
- 12)