TAD Graph

Graph = {nodes: < Node₁, Node₂, Node₃, ..., Node_n>}

• Where:

Node = {key: <key>, value: <value>, edges: <Edge₁, Edge₂, Edge₃, ..., Edge_n>}

• Where:

 $Edge_m = \{weight: < weight_m >, to: < key_k > \}$

{ invariant: Node_a.key \neq Node_h.key \wedge Edge.to \neq NULL \wedge Edge.weight \geq 0 }

Primitive functions:

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addNode: Graph X Value X Key

addEdge: Graph X Key₁ X Key₂ X Integer

removeNode: Graph X Key

• removeEdge: Graph X Key₁ X Key₂

getNeighbors: Graph X Key

getEdge: Graph X Key₁ X Key₂

DFS Graph X Key

BFS Graph X Key

Dijkstra Graph X Key

→ Graph

→ Graph

→ Graph

→ Graph

→ Graph

→ List<Edge>

→ Edge

→ List<Key>

→ List<Key>

→ List<List<Key>>

CreateGraph()

"Creates a new Graph object with 0 elements"

{ pre: TRUE}

{ post: graph = {nodes: []}}

addNode(graph, value, key)

"Adds a new node with the given key and value to the graph"

{ pre: key ∉ {n.key | n ∈ graph.nodes} }

{ post: graph = {nodes: graph.nodes U {Node(key, value, [])}} }

addEdge(graph, key₁, key₂, weight)

"Adds a new edge between the nodes with keys key₁ and key₂ in the graph with the given weight"

{ pre: $key_1 \in \{n.key \mid n \in graph.nodes\} \land key_2 \in \{n.key \mid n \in graph.nodes\} \land weight \ge 0 \land key_1 \ne key_2 \}$

{ post: $\{n_1, n_2, e \mid n_1. \text{key} = \text{key}_1 \land n_2. \text{key} = \text{key}_2 \land e. \text{weight} = \text{weight} \land e. \text{to} = n_2. \text{key} \land e \in n_1. \text{edges} \} \}$

removeNode(graph, key)

"Removes the node with the given key from the graph"

{ pre: key \in {n.key | n \in graph.nodes} }

{ post: \exists n {n ∈ graph.nodes \land n.key \neq key \exists e { e ∈ n.edges \land e.to \neq key } } }

removeEdge(graph, key₁, key₂)

"Removes the edge between the nodes with keys key₁ and key₂ from the graph"

{ pre: $key_1 \in \{n.key \mid n \in graph.nodes\} \land key_2 \in \{n.key \mid n \in graph.nodes\} \}$

{ post: \exists n, e { n \in graph.nodes \land n.key = key₁ \land e \in n.edges \land e.to \neq key₂}}

getEdge(graph, key₁, key₂)

"Returns the edge between the nodes with keys key₁ and key₂ in the graph"

{ pre: $key_1 \in \{n.key \mid n \in graph.nodes\} \land key_2 \in \{n.key \mid n \in graph.nodes\} \}$

{ post: $e = \{e \mid (n_1, e, n_2) \in \text{graph } \land n_1.\text{key} = \text{key}_1 \land n_2.\text{key} = \text{key}_2\} \}$

BFS(graph, key)

"Returns a list of nodes representing the result of a breadth-first search starting from the node with the given key in the graph"

{ pre: key \in {n.key | n \in graph.nodes} }

{ post: result = $[n \mid n \in \text{graph.nodes } \land \text{ there exists a path from the node with key to n in the graph}] }$

getNeighbors(graph, key)

"Returns a list of edges representing the neighbors of the node with the given key in the graph"

{ pre: key \in {n.key | n \in graph.nodes} }

{ post: neighbors = {e | $(n_1, e, n_2) \in \text{graph } \land n_1.\text{key} = \text{key}}$ }

DFS(graph, key)

"Returns a list of nodes representing the result of a depth-first search starting from the node with the given key in the graph"

{ pre: key \in {n.key | n \in graph.nodes} }

{ post: result = $[n \mid n \in \text{graph.nodes } \land \text{ there exists a path from the node with key to n in the graph}] }$

Dijkstra(graph, key)

"Calculates the shortest paths from the node with the given key to all other nodes in the graph using Dijkstra's algorithm"

{ pre: key \in {node.key | node \in graph.nodes} }

{ post: shortest_paths = $\{n: path \mid n \in graph.nodes \land path is the shortest path from the start node to n} \}$