$$y(x) - \frac{1}{2} \int_a^b x e^s y(s) ds = e^{-x}$$

$$y(x) = e^{-x} + Cx$$

$$C = \frac{a - b}{e^b(b-1) - e^a(a-1) - 2}$$