

JAWABAN:

$$1. \quad a. \quad f(x) = \frac{1}{2} x^{\frac{3}{2}}$$

$$f'(x) = 3\sqrt{x}$$

$$b. \quad f(x) = 6x^{\frac{3}{2}}$$

$$f'(x) = 9\sqrt{x}$$

$$c. \quad f(x) = 6\sqrt{x^3}$$

$$f'(x) = 9x^{\frac{1}{2}}$$

$$d. \quad f(x) = 12\sqrt[3]{x^4}$$

$$f'(x) = 24x^{\frac{1}{3}}$$

$$e. \quad f(x) = 5(2x^2 + 4x^2)$$

$$f'(x) = 20x^2 + 20$$

$$f. \quad f(x) = 3x^4 + 2x^2 - 5$$

$$f'(x) = 12x^3 + 4x - 5$$

$$g. \quad 1. \quad f(x) = \frac{x}{x+2}$$

$$f'(x) = \frac{(x+2) - (x+2)}{(x+2)^2}$$

$$= \frac{x+2-x}{(x+2)^2} = \frac{2}{x^2+4x+4}$$

$$2. \quad f(x) = \frac{1}{x^2+1}$$

$$f'(x) = \frac{0 \cdot (x^2+1) - (1) \cdot (2x)}{(x^2+1)^2}$$

$$= \frac{-2x}{x^4+2x^2+1}$$

$$2. \quad a. \quad f(x) = \frac{1}{(x^3+2)^4}$$

$$f'(x) = -4 \cdot (x^3 - 2)^{-4-1} \cdot (3x^2)$$

$$= -12x^2 \cdot (x^3 - 2)^{-5}$$

$$= \frac{-12x^2}{(x^3+2)^5}$$

$$b. \quad f(x) = (x^4 - 6x^3 + 10x)^{68}$$

$$f'(x) = 68 \cdot (x^4 - 6x^3 + 10x)^{67} \cdot (4x^3 - 18x^2 + 10)$$

$$\begin{aligned} \text{c. } f(x) &= (x+10)^9 \\ &= 9(x+10)^8 \end{aligned}$$

$$3. F(x) = 9x^2 + 6x^3 + 8$$

$$\text{Turunan 1} \quad 15x^4 - 18x^2 + 8$$

$$\text{Turunan 2} \quad 60x^3 - 36x$$

$$\text{Turunan 3} \quad 180x^2 - 36$$

$$\text{Turunan 4} \quad 360x$$

$$4. y = \left(\frac{3x^2 - 2}{x + 3} \right)^3$$

$$d(y)/dx = \frac{d\left(\frac{3x^2 - 2}{x + 3}\right)^3}{dx}$$

$$dy/dx = 3 \left(\frac{3x^2 - 2}{x + 3} \right)^2 \cdot \left(\frac{6x^2 + 18x - 3x^2 + 2}{(x + 3)^2} \right)$$

$$dy/dx = 2 \left(\frac{3x^2 - 2}{(x + 3)^2} \right)^2 \cdot \frac{3x^2 + 18 + 2}{(x + 3)^2}$$

$$dy/dx = \left(\frac{(9x^4 - 12x^2 + 4)(9x^2 + 54 + 6)}{(x + 3)^4} \right)$$

$$5. \text{ a. } g(x) = 13x^3 - 32x^2 + 2x - 6 \text{ ditanya nilai } g'(0) = ?$$

$$g'(x) = 39x^2 - 64x + 2$$

$$g'(2) = 39(0)^2 - 64(0) + 2 = 0$$

$$g'(x) = 0$$

$$\text{b. } f(x) = \left(\frac{3x+1}{x^2+2} \right)^3 \text{ ditanya } f'(3) = ?$$

$$f'(x) = 3 \left(\frac{3x+1}{x^2+2} \right)^2 \left(\frac{(3x^2+6) - (6x^2+2x)}{(x^2+2)^2} \right)$$

$$f'(3) = 3 \left(\frac{3(3)+1}{(3)^2+2} \right)^2 \left(\frac{(3(3)^2+6) - (6(3)^2+2(3))}{((3)^2+2)^2} \right)$$

