highway English (HKG)

# **Highway Tolls**

In Japan, cities are connected by a network of highways. This network consists of N cities and M highways. Each highway connects a pair of distinct cities. No two highways connect the same pair of cities. Cities are numbered from 0 through N-1, and highways are numbered from 0 through M-1. You can drive on any highway in both directions. You can travel from any city to any other city by using the highways.

A toll is charged for driving on each highway. The toll for a highway depends on the **traffic** condition on the highway. The traffic is either **light** or **heavy**. When the traffic is light, the toll is A yen (Japanese currency). When the traffic is heavy, the toll is B yen. It's guaranteed that A < B. Note that you know the values of A and B.

You have a machine which, given the traffic conditions of all highways, computes the smallest total toll that one has to pay to travel between the pair of cities S and T ( $S \neq T$ ), under specified traffic conditions.

However, the machine is just a prototype. The values of S and T are fixed (i.e., hardcoded in the machine) and not known to you. You would like to determine S and T. In order to do so, you plan to specify several traffic conditions to the machine, and use the toll values that it outputs to deduce S and T. Since specifying the traffic conditions is costly, you don't want to use the machine many times.

## 實現細節

你需要實現下面的程序:

### find pair(int N, int[] U, int[] V, int A, int B)

- N: 城市的數目。
- U 及 V: 長度為 M 的陣列, 其中 M 為連接城市的高速公路。 對於每個 i ( $0 \le i \le M-1$ ), 高速公路 i 連接城市 U[i] 及 V[i]。
- A: 交通順暢時高速公路的收費。
- B: 文通擠塞時高速公路的收費。
- 在每個測試用例中,這程序只會被調用一次。
- 請留意 M 的值為陣列的長度,並能如實現注意事項所示般獲取。

程序 find pair 能調用以下函數:

### int64 ask(int[] w)

- $\bullet$  w 的長度一定為 M。 陣列 w 描述高速公路的交通狀況。
- 對於每個 i ( $0 \le i \le M-1$ ), w[i] 描述高速公路 i 的交通狀況。 w[i] 的值一定為 0 或 1。
  - 。 w[i] = 0 表示高速公路 i 交通順暢。
  - w[i] = 1 表示高速公路 i 交通擠塞。
- 該函數的返回值是在 w 所註明的交通狀況下,來往城市 S 及 T 每一單程所需的最少收費。
- 該函數最多只能被調用 100 次 (對於每個測試用例)。

find pair 應調用以下程序以報告答案:

### answer(int s, int t)

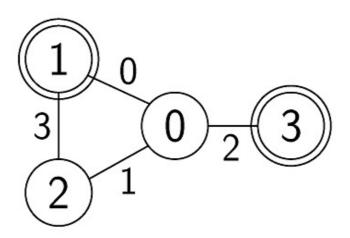
- $\mathsf{s}$  及  $\mathsf{t}$  一定為該對城市 S 及 T (兩者的先後次序並不重要)。
- 該程序一定會被調用及只會被調用一次。

如果不滿足上面的條件,你的程式將被判視 Wrong Answer。否則,你的程式將被判為 Accepted,而你的得分將根據 ask 的調用次數來計算(參見子任務)。

## Example

Let 
$$N=4$$
,  $M=4$ ,  $U=[0,0,0,1]$ ,  $V=[1,2,3,2]$ ,  $A=1$ ,  $B=3$ ,  $S=1$ , and  $T=3$ .

The grader calls find pair(4, [0, 0, 0, 1], [1, 2, 3, 2], 1, 3).



Some possible calls to ask and the corresponding return values are listed below:

Call				Return
ask([0,	0,	0,	0])	2
ask([0,	1,	1,	0])	4
ask([1,	Θ,	1,	0])	5
ask([1,	1,	1,	1])	6

For the function call ask([0, 0, 0, 0]), the traffic of every highway is light and the toll for it is 1. The cheapest route from S=1 to T=3 is  $1\to 0\to 3$ . The total toll for this path is 2. Thus, this function returns 2.

For a correct answer, the procedure find\_pair should call answer(1, 3) or answer(3, 1).

The file sample-01-in.txt in the zipped attachment package corresponds to this example. Other sample inputs are also available in the package.

### Constraints

- $2 \le N \le 90\,000$
- $1 \le M \le 130\,000$
- $1 \le A < B \le 1\,000\,000\,000$
- For each  $0 \le i \le M-1$ 
  - $\circ \ 0 \leq U[i] \leq N-1$
  - $\circ \ 0 \leq V[i] \leq N-1$
  - $\circ U[i] \neq V[i]$
- $(U[i], V[i]) \neq (U[j], V[j])$  and  $(U[i], V[i]) \neq (V[j], U[j])$   $(0 \leq i < j \leq M-1)$
- You can travel from any city to any other city by using the highways.
- 0 < S < N 1
- $0 \le T \le N 1$
- $S \neq T$

In this problem, the grader is NOT adaptive. This means that S and T are fixed at the beginning of the running of the grader and they do not depend on the queries asked by your solution.

### Subtasks

- 1. (5 points) one of S or T is 0,  $N \leq 100$ , M = N 1
- 2. (7 points) one of S or T is 0, M = N 1
- 3. (6 points) M=N-1, U[i]=i, V[i]=i+1 ( $0 \le i \le M-1$ )
- 4. (33 points) M = N 1
- 5. (18 points) A = 1, B = 2

#### 6. (31 points) No additional constraints

Assume your program is judged as **Accepted**, and make X calls to ask. Then your score P for the test case, depending on its subtask number, is calculated as follows:

- Subtask 1. P = 5.
- Subtask 2. If  $X \leq 60$ , P = 7. Otherwise P = 0.
- Subtask 3. If  $X \leq 60$ , P = 6. Otherwise P = 0.
- Subtask 4. If  $X \leq 60$ , P = 33. Otherwise P = 0.
- Subtask 5. If  $X \le 52$ , P = 18. Otherwise P = 0.
- Subtask 6.
  - If  $X \le 50$ , P = 31.
  - If  $51 \le X \le 52$ , P = 21.
  - If  $53 \le X$ , P = 0.

Note that your score for each subtask is the minimum of the scores for the test cases in the subtask.

## Sample grader

The sample grader reads the input in the following format:

- line 1: N M A B S T
- line 2 + i ( $0 \le i \le M 1$ ): U[i] V[i]

If your program is judged as **Accepted**, the sample grader prints Accepted: q, with q the number of calls to ask.

If your program is judged as **Wrong Answer**, it prints Wrong Answer: MSG, where MSG is one of:

- answered not exactly once: The procedure answer was not called exactly once.
- w is invalid: The length of w given to ask is not M or w[i] is neither 0 nor 1 for some i (0  $\leq i \leq M-1$ ).
- more than 100 calls to ask: The function ask is called more than 100 times.
- {s, t} is wrong: The procedure answer is called with an incorrect pair s and t.