International Olympiad in Informatics 2016



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aliens
Country: LKA

Aliens

Our satellite has just discovered an alien civilization (පිටසක්වල ශිෂ්ඨාචාරය) on a remote planet

(දුරස්ථ ග්රහලෝකය). We have already obtained a low-resolution photo of a square area of the planet. The photo shows many signs of intelligent life (බුද්ධිමත් ජීවිතය ගැන සංඥ). Our experts have identified n points of interest (උනන්දුව දනවන ලක්ෂ්යන්) in the photo. The points are numbered from 0 to n-1. We now want to take high-resolution photos that contain all of those n points.

Internally, the satellite has divided the area of the low-resolution photo into an m by m grid of unit square cells (කොටු). Both rows and columns of the grid are consecutively numbered from 0 to m-1 (from the top and left, respectively). We use (s,t) to denote the cell in row s and column t. The point number i is located in the cell (r_i,c_i) . Each cell may contain an arbitrary (ඔනෑම සංඛ්යාවක්) number of these points.

Our satellite is on a stable orbit (ස්ථාවර කක්ෂයක) that passes directly over the *main* diagonal (විකර්ණය) of the grid. The main diagonal is the line segment that connects the top left corner and the bottom right corner of the grid. The satellite can take a high-resolution photo of any area that satisfies the following constraints (පීමාවන්):

- the shape of the area is a square,
- two opposite corners of the square both lie on the main diagonal of the grid,
- each cell of the grid is either completely inside or completely outside the photographed area.

The satellite is able to take at most k high-resolution photos.

Once the satellite is done taking photos, it will transmit (ಲಿಕೆಂಟಿಕ್ಕು) the high-resolution photo of each photographed cell to our home base (regardless of whether that cell contains some points of interest). The data for each photographed cell will only be transmitted *once*, even if the cell was photographed several times.

Thus, we have to choose at most k square areas that will be photographed, assuring that (පහත සදහන් සීමාවන් අනුගමනය කරමින්):

- each cell containing at least one point of interest is photographed at least once,
 and
- the number of cells that are photographed at least once is minimized.

Your task is to find the smallest possible total number of photographed cells.

Implementation details

You should implement the following function (method):

- o int64 take photos(int n, int m, int k, int[] r, int[] c)
 - n: the number of points of interest,
 - m: the number of rows (and also columns) in the grid,
 - k: the maximum number of photos the satellite can take,
 - r and c: two arrays of length n describing the coordinates (asia) as) of the grid cells that contain points of interest. For $0 \le i \le n-1$, the i-th point of interest is located in the cell (r[i], c[i]),
 - the function should return the smallest possible total number of cells that are photographed at least once (given that the photos must cover all points of interest).

Please use the provided template files for details of implementation in your programming language.

Examples

Example 1

```
take photos(5, 7, 2, [0, 4, 4, 4, 4], [3, 4, 6, 5, 6])
```

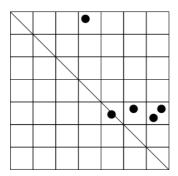
In this example we have a 7×7 grid with 5 points of interest. The points of interest are located in four different cells: (0,3), (4,4), (4,5) and (4,6). You may take at most 2 high-resolution photos.

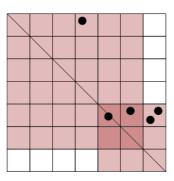
One way to capture all five points of interest is to make two photos: a photo of the 6×6 square containing the cells (0,0) and (5,5), and a photo of the 3×3 square containing the cells (4,4) and (6,6). If the satellite takes these two photos, it will transmit the data about 41 cells. This amount is not ((5,5)).

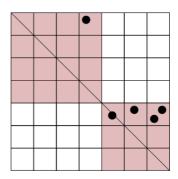
The optimal solution uses one photo to capture the 4×4 square containing cells (0,0) and (3,3) and another photo to capture the 3×3 square containing cells (4,4) and (6,6). This results in only 25 photographed cells, which is optimal, so take photos should return 25.

Note that it is sufficient (ප්රමාණවත්) to photograph the cell (4,6) once, even though it contains two points of interest.

This example is shown in the figures below. The leftmost figure shows the grid that corresponds to this example. The middle figure (ర్మల టెల్లిల్లా) shows the suboptimal solution in which 41 cells were photographed. The rightmost figure shows the optimal solution.



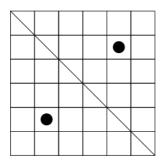


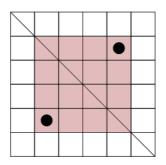


Example 2

Here we have 2 points of interest located symmetrically (සම්මිතිකව): in the cells (1,4) and (4,1). Any valid photo that contains one of them contains the other one as well. Therefore, it is sufficient to use a single photo.

The figures below show this example and its optimal solution. In this solution the satellite captures a single photo of 16 cells.





Subtasks

For all subtasks, $1 \le k \le n$.

- 1. (4 points) $1 \leq n \leq 50$, $1 \leq m \leq 100$, k=n ,
- 2. (12 points) $1 \leq n \leq 500$, $1 \leq m \leq 1000$, for all i such that $0 \leq i \leq n-1$, $r_i = c_i$,
- 3. (9 points) $1 \le n \le 500$, $1 \le m \le 1000$,
- 4. (16 points) $1 \leq n \leq 4000$, $1 \leq m \leq 1000000$,
- 5. (19 points) $1 \leq n \leq 50\,000$, $1 \leq k \leq 100$, $1 \leq m \leq 1\,000\,000$,
- 6. (40 points) $1 \le n \le 100\,000$, $1 \le m \le 1\,000\,000$.

Sample grader

The sample grader reads the input in the following format:

- \circ line 1: integers n, m and k,
- line 2 + i ($0 \le i \le n-1$): integers r_i and c_i .