International Olympiad in Informatics 2016



12-19th August 2016 Kazan, Russia day1 1

molecules
Country: AZE

Molekulların aşkarlanması

Pyotr molekulları aşkarlayan maşın düzəltmiş şirkətdə çalışır. Hər bir molekul tam ədədlə ölçülən çəkiyə malikdir. Maşın [l,u] aşkarlama aralığına malikdir, burada l və u tam ədədlərdir. Maşın molekullar çoxluğunu yalnız o zaman aşkarlaya bilər ki, həmin çoxluğun elə altçoxluğu var ki, ora daxil olan molekulların çəkiləri cəmi maşının aşkarlama aralığında yerləşsin.

Formal olaraq, müsbət tam w_0,\ldots,w_{n-1} çəkiləri olan n molekula baxaq. Aşkarlama o zaman uğurlu olur ki, elə fərqli $I=i_1,\ldots,i_m$ indeksləri var ki, $l\leq w_{i_1}+\ldots w_{i_m}\leq u$.

Maşının özəlliyi sayəsində l və u arasındakı intervalın ən ağır və an yüngül molukulun çəkiləri arasındakı intervaldan böyük və ya bərabər olmasına zəmanət verilir. Formal olaraq, $u-l \geq w_{max}-w_{min}$, burada $w_{max}=\max(w_0,\ldots,w_{n-1})$ və $w_{min}=\min(w_0,\ldots,w_{n-1})$.

Siz elə proqram yazmalısınız ki, toplam çəkiləri aşkarlama aralığında olan molekullar altçoxluğunu tapsın və ya belə altçoxluğun olmadığını müəyyənləşdirsin.

Implementation details

You should implement one function (method):

- int[] solve(int I, int u, int[] w)
 - I and u: the endpoints of the detection range,
 - w: weights of the molecules.
 - if the required subset exists, the function should return an array of indices of molecules that form any one such subset. If there are several correct answers, return any of them.
 - if the required subset does not exist, the function should return an empty array.

For the C language the function signature is slightly different:

- int solve(int I, int u, int[] w, int n, int[] result)
 - n: the number of elements in w (i.e., the number of molecules),
 - the other parameters are the same as above.
 - \circ instead of returning an array of m indices (as above), the function should write the indices to the first m cells of array result and then return m.
 - \circ if the required subset does not exist, the function should not write anything to the result array and it should return 0.

Please use the provided template files for details of implementation in your programming language.

Examples

Example 1

```
solve(15, 17, [6, 8, 8, 7])
```

In this example we have four molecules with weights 6, 8, 8 and 7. The machine can detect subsets of molecules with total weight between 15 and 17, inclusive. Note, that $17-15 \geq 8-6$. The total weight of molecules 1 and 3 is $w_1+w_3=8+7=15$, so the function can return [1, 3]. Other possible correct answers are [1, 2]($w_1+w_2=8+8=16$) and [2, 3]($w_2+w_3=8+7=15$).

Example 2

```
solve(14, 15, [5, 5, 6, 6])
```

In this example we have four molecules with weights 5, 5, 6 and 6, and we are looking for a subset of them with total weight between 14 and 15, inclusive. Again, note that $15-14 \geq 6-5$. There is no subset of molecules with total weight between 14 and 15 so the function should return an empty array.

Example 3

```
solve(10, 20, [15, 17, 16, 18])
```

In this example we have four molecules with weights 15, 17, 16 and 18, and we are looking for a subset of them with total weight between 10 and 20, inclusive. Again, note that $20 - 10 \ge 18 - 15$. Any subset consisting of exactly one element satisfies the requirement, so correct answers are: [0], [1], [2] and [3].

Subtasks

- 1. (9 points): $n \leq 100$, $w_i \leq 100$, all w_i are equal.
- 2. (10 points): $n \leq 100, w_i \leq 1000$, and $max(w_0,\ldots,w_{n-1})-min(w_0,\ldots,w_{n-1}) \leq 1$.
- 3. (12 points): $n \leq 100$ and $w_i, u, l \leq 1000$.
- 4. (15 points): $n \leq 10\,000$ and $w_i, u, l \leq 10\,000$.
- 5. (23 points): $n \leq 10\,000$ and $w_i, u, l \leq 500\,000$
- 6. (31 points): $n \leq 200\,000$ and $w_i, u, l < 2^{31}$.

Sample grader

The sample grader reads the input in the following format:

- line 1: integers n, l, u.
- \circ line 2: n integers: w_0, \ldots, w_{n-1} .