International Olympiad in Informatics 2016



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messy Country: LKA

Unscrambling a Messy Bug

Ilshat is a software engineer working on efficient (කාර්යක්ෂම) data structures. One day he invented (නිපදවන) a new data structure. This data structure can store a set of *nonnegative* n-bit integers, where n is a power of two. That is, $n=2^b$ for some nonnegative integer b.

The data structure is initially (මුලින්) empty. A program using the data structure has to follow the following rules:

- one at a time (වරකට එක බැගින්), by using the function $add_element(x)$. If the program tries to add an element that is already present (මේ වන විටත් පවතින) in the data structure, nothing happens.
- After adding the last element the program should call the function compile_set() exactly once.
- Finally, the program may call the function $check_element(x)$ to check whether the element x is present in the data structure. This function may be used multiple times.

When Ilshat first implemented this data structure, he made a bug in the function compile_set(). The bug reorders (order වෙනස් කර) the binary digits of each element in the set in the same manner (එම ආකාරයෙන්ම). Ilshat wants you to find the exact reordering of digits caused by the bug.

Formally, consider a sequence $p=[p_0,\ldots,p_{n-1}]$ in which every number from 0 to n-1 appears exactly once. We call such a sequence a *permutation*. Consider an element of the set, whose digits in binary are a_0,\ldots,a_{n-1} (with a_0 being the most significant bit). When the function <code>compile_set()</code> is called, this element is replaced by the element $a_{p_0},a_{p_1},\ldots,a_{p_{n-1}}$.

The same permutation p is used to reorder the digits of every element. Any permutation is possible, including the possibility that $p_i=i$ for each $0 \le i \le n-1$.

For example, suppose that n=4, p=[2,1,3,0], and you have inserted into the set integers whose binary representations are 0000, 1100 and 0111. Calling the function compile_set changes these elements to 0000, 0101 and 1110, respectively (පිළිවෙලින්).

Your task is to write a program that finds the *permutation* p by interacting with the data structure. It should (in the following order):

1. choose a set of n-bit integers,

- 2. insert those integers into the data structure,
- 3. call the function compile set to trigger the bug,
- 4. check the presence of some elements in the modified set,
- 5. use that information to determine and return the *permutation* p.

Note that your program may call the function compile_set only once (එක් වරක් පමණක්).

In addition, there is a limit on the number of times (වාර සංඛ්යාව) your program calls the library functions. Namely, it may

- call add element at most w times (w is for "writes"),
- call check_element at most r times (r is for "reads").

Implementation details

You should implement one function (method):

- int[] restore permutation(int n, int w, int r)
 - n: the number of bits in the binary representation of each element of the set (and also the length of p).
 - w: the maximum number of add_element operations your program can perform.
 - r: the maximum number of check_element operations your program can perform.
 - the function should return the restored *permutation* p.

In the C language, the function prototype is a bit different:

- void restore permutation(int n, int w, int r, int* result)
 - n, w and r have the same meaning as above.
 - the function should return the restored permutation p by storing it into the provided array result: for each i, it should store the value p_i into result[i].

Library functions

In order to interact with the data structure, your program should use the following three functions (methods):

- void add element(string x)
 - This function adds the element described by x to the set.
 - x: a string of '0' and '1' characters giving the binary representation of an integer that should be added to the set. The length of x must be n.
- void compile set()
 - This function must be called exactly once. Your program cannot call add_element() after this call. Your program cannot call check_element() before this call.
- boolean check_element(string x)

This function checks whether the element x is in the modified set.

- x: a string of '0' and '1' characters giving the binary representation of the element that should be checked. The length of x must be n.
- returns true if element x is in the modified set, and false otherwise.

Note that if your program violates (උල්ලංසනය) any of the above restrictions (සීමා), its grading outcome will be "Wrong Answer".

For all the strings, the first character gives the most significant bit of the corresponding integer.

The grader fixes the permutation p before the function restore_permutation is called.

Please use the provided template files for details of implementation in your programming language.

Example

The grader makes the following function call:

• restore_permutation(4, 16, 16). We have n=4 and the program can do at most 16 "writes" and 16 "reads".

The program makes the following function calls:

```
add_element("0001")
add_element("0100")
add_element("0100")
compile_set()
check_element("0001") returns false
check_element("0010") returns true
check_element("1000") returns false
check_element("1000") returns false
check_element("0011") returns false
check_element("0101") returns false
check_element("1001") returns false
check_element("1010") returns false
check_element("1010") returns false
check_element("1010") returns false
```

Only one permutation is consistent (වලංහු වන) with these values returned by $check_element()$: the permutation p=[2,1,3,0]. Thus, $restore_permutation$ should return [2, 1, 3, 0].

Subtasks

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1. (20 points) n=8, w=256, r=256, p_i\neq i for at most 2 indices i ( 0\leq i\leq n-1),
2. (18 points) n=32, w=320, r=1024,
3. (11 points) n=32, w=1024, r=320,
4. (21 points) n=128, w=1792, r=1792,
5. (30 points) n=128, w=896, r=896.
```

Sample grader

The sample grader reads the input in the following format:

```
\circ line 1: integers n, w, r,
```

 $\circ \:$ line 2: n integers giving the elements of p .