International Olympiad in Informatics 2018
September 2–7th, 2018
Tsukuba, Japan
Day 1 Tasks

seats
English (ZAF)

Seats

You are going to hold an international programming contest in a rectangular hall, which has HW seats arranged in H rows and W columns. The rows are numbered from 0 through $H - 1$ and the columns are numbered from 0 through $W - 1$. The seat in row r and column c is denoted by (r, c). You invited HW contestants, numbered from 0 through $HW - 1$. You also made a seating chart, which assigns the contestant i ($0 \leq i \leq HW - 1$) to the seat (R_i, C_i). The chart assigns exactly one contestant to each seat.

A set of seats in the hall S is said to be **rectangular** if there are integers r_1, r_2, c_1, and c_2 satisfying the following conditions:

- $0 \leq r_1 \leq r_2 \leq H - 1$.
- $0 \leq c_1 \leq c_2 \leq W - 1$.
- S is exactly the set of all seats (r, c) such that $r_1 \leq r \leq r_2$ and $c_1 \leq c \leq c_2$.

A rectangular set consisting of k seats ($1 \leq k \leq HW$) is **beautiful** if the contestants whose assigned seats are in the set have numbers from 0 through $k - 1$. The **beauty** of a seating chart is the number of beautiful rectangular sets of seats in the chart.

After preparing your seating chart, you receive several requests to swap two seats assigned to two contestants. More precisely, there are Q such requests numbered from 0 through $Q - 1$ in chronological order. The request j ($0 \leq j \leq Q - 1$) is to swap the seats assigned to contestants A_j and B_j. You accept each request immediately and update the chart. After each update, your goal is to compute the beauty of the current seating chart.

Implementation details

You should implement the following procedure and function:

```
give_initial_chart(int H, int W, int[] R, int[] C)
```

- H, W: the number of rows and the number of columns.
- R, C: arrays of length HW representing the initial seating chart.
- This procedure is called exactly once, and before any call to swap_seats.

```
int swap_seats(int a, int b)
```

- This function describes a request to swap two seats.
- a, b: contestants whose seats are to be swapped.
- This function is called Q times.
- This function should return the beauty of the seating chart after the swap.

Example

Let $H = 2$, $W = 3$, $R = [0, 1, 1, 0, 0, 1]$, $C = [0, 0, 1, 1, 2, 2]$, and $Q = 2$.

The grader first calls `give_initial_chart(2, 3, [0, 1, 1, 0, 0, 1], [0, 0, 1, 1, 2, 2])`.

At first, the seating chart is as follows.

0	3	4
1	2	5

Let's say the grader calls `swap_seats(0, 5)`. After the request 0, the seating chart is as follows.

5	3	4
1	2	0

The sets of seats corresponding to the contestants $\{0\}$, $\{0, 1, 2\}$, and $\{0, 1, 2, 3, 4, 5\}$ are rectangular and beautiful. Thus, the beauty of this seating chart is 3, and `swap_seats` should return 3.

Let's say the grader calls `swap_seats(0, 5)` again. After the request 1, the seating chart goes back to the initial state. The sets of seats corresponding to the contestants $\{0\}$, $\{0, 1\}$, $\{0, 1, 2, 3\}$, and $\{0, 1, 2, 3, 4, 5\}$ are rectangular and beautiful. Hence, the beauty of this seating chart is 4, and `swap_seats` should return 4.

The files `sample-01-in.txt` and `sample-01-out.txt` in the zipped attachment package correspond to this example. Other sample inputs/outputs are also available in the package.

Constraints

- $1 \leq H$
- $1 \leq W$
- $HW \leq 1\,000\,000$
- $0 \leq R_i \leq H - 1$ $(0 \leq i \leq HW - 1)$
- $0 \leq C_i \leq W - 1$ $(0 \leq i \leq HW - 1)$
- $(R_i, C_i) \neq (R_j, C_j)$ $(0 \leq i < j \leq HW - 1)$
- $1 \leq Q \leq 50\,000$
- $0 \leq a \leq HW - 1$ for any call to `swap_seats`
- $0 \leq b \leq HW - 1$ for any call to `swap_seats`
- $a \neq b$ for any call to `swap_seats`

Subtasks

1. (5 points) $HW \leq 100$, $Q \leq 5\,000$
2. (6 points) $HW \leq 10\,000$, $Q \leq 5\,000$
3. (20 points) $H \leq 1\,000$, $W \leq 1\,000$, $Q \leq 5\,000$
4. (6 points) $Q \leq 5\,000$, $|a - b| \leq 10\,000$ for any call to `swap_seats`
5. (33 points) $H = 1$
6. (30 points) No additional constraints

Sample grader

The sample grader reads the input in the following format:

- line 1: H W Q
- line $2 + i$ $(0 \leq i \leq HW - 1)$: R_i C_i
- line $2 + HW + j$ $(0 \leq j \leq Q - 1)$: A_j B_j

Here, A_j and B_j are parameters for the call to `swap_seats` for the request j.

The sample grader prints your answers in the following format:

- line $1 + j$ $(0 \leq j \leq Q - 1)$: the return value of `swap_seats` for the request j