





Day 1, Wednesday 31st August, 2022

### **Problem AB**

Input data stdin
Output data stdout

Alice has decided to impress her little brother, Bob, with her mathematical deduction abilities. She places, in a matrix with N rows and M columns, all the numbers  $1, 2, ..., N \times M$ , such that each line, and each column, respectively, is sorted in a strictly increasing order. We call a matrix with these properties an AB matrix.

Alice then asks Bob to take out *K* values from the matrix, such that no two such values are adjacent horizontally or vertically. She will then try to place those *K* numbers back into the matrix, such that it remains an *AB matrix*. After several tries, Alice realises that, in some cases, there can be multiple ways of placing back the *K* numbers on the empty positions.

Write a program that, given the initial *AB matrix* and *Q* queries, each consisting of a list of numbers that are taken out from the matrix, determines, for each query, whether a unique way of placing those numbers exists such that the resulting matrix is an *AB matrix*.

#### **Input Data**

The first line of the input contains three space separated positive integers N, M, and Q, with the respective meanings from the statement above. The next N lines contain M space separated values each, representing the initial AB matrix as built by Alice. Then, Q queries follow, each consisting of two lines. The first line of a query contains the positive integer K, representing the number of values that Bob takes out for this query. Then second line contains K space separated integers, representing the numbers that are taken out.

## **Output Data**

Output Q lines, each containing an integer. On the  $i^{th}$  line, output the answer for the  $i^{th}$  query: the answer will be 1 if there is a unique way of placing back the numbers such that the resulting matrix is an AB matrix, or 0 otherwise.

#### **Restrictions**

- $1 \le N, M \le 2000$
- 1 ≤ *Q* ≤ 25
- *K* ≥ 1
- For any query, we guarantee that no two numbers that Bob takes out are equal, and also that they are not horizontally or vertically adjacent.
- The total number of numbers that Bob takes out over all queries does not exceed 4 000 000.
- You will get points for a test only if all queries are answered correctly.

#	Points	Restrictions	
1	21	$1 \le N, M \le 10$	
2	18	$1 \le N, M \le 100$	
3	55	$1 \le N, M \le 400$	
4	6	No further constraints.	







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# **Examples**

Input data	Output data	Explanations
3 3 2	1	In the first query Bob takes out
1 2 4	0	numbers 1, 5 and 9. The matrix, after
3 5 8		this operation, looks like this:
6 7 9		? 2 4
3		3 ? 8
1 5 9		6 7 ?
3		We observe that there is a unique way
5 4 6		of placing the numbers back, as we
		can only obtain the initial matrix.
		In the second query Bob takes out
		numbers 5, 4 and 6:
		1 2 ?
		3 ? 8
		? 7 9
		Placing back the numbers is not
		unique, as, besides the original
		matrix, we can also obtain:
		1 2 5
		3 6 8
		4 7 9