



## Xp Orbs

In Minecraft, for every task completed, the player is rewarded with a certain number of experience points in the form of some green orbs, each orb rewarding the player with different amounts of experience based on its size.

An orb of size  $i$  rewards the player with  $xp_i$  experience points. Where  $xp$  is defined as follows:

- $xp_1 = 1$ ;
- $xp_i = \text{prev\_prime}(2 \cdot xp_{i-1})$ , where  $\text{prev\_prime}(a)$  is the largest prime number that is smaller than or equal to  $a$ . For example,  $\text{prev\_prime}(16) = 13$  and  $\text{prev\_prime}(23) = 23$ .

For instance, the first 8 sizes of orbs reward the player with: 1, 2, 3, 5, 7, 13, 23 and 43 experience points, respectively.

Notch, the creator of Minecraft, made it so that any non-negative integer number of experience points can be broken down as a sum of experience rewarded by orbs in the following way (here  $\oplus$  represents array concatenation):

- Let  $\text{dec}(a)$  be an array representing the decomposition of  $a$  experience points as a sum of experience rewarded by orbs;
- $\text{dec}(0) = []$  (the empty array)
- $\text{dec}(a) = [xp_{\max}] \oplus \text{dec}(a - xp_{\max})$ , where  $xp_{\max}$  is the largest element in  $xp$  such that  $xp_{\max} \leq a$ . For example, the decomposition of 11 is  $\text{dec}(11) = [7, 3, 1]$  and the decomposition of 15 is  $\text{dec}(15) = [13, 2]$ . He also defined  $\text{cnt}(a)$  to be the length of the array  $\text{dec}(a)$ , therefore  $\text{cnt}(11) = 3, \text{cnt}(15) = 2$ .

Notch wants to know the answer to  $q$  queries of the following form:

- $l, r$  – find the sum  $\frac{l}{\text{cnt}(l)} + \frac{l+1}{\text{cnt}(l+1)} + \dots + \frac{r-1}{\text{cnt}(r-1)} + \frac{r}{\text{cnt}(r)}$

## Input

The first line contains a single integer representing the number of queries  $q$ . Each of the next  $q$  lines contains a pair of integers. The  $i^{\text{th}}$  of these lines describes the  $i^{\text{th}}$  query:  $l_i$  and  $r_i$ .

## Output

The output contains  $q$  lines. The  $i^{th}$  of these lines contains a single integer representing the answer to the  $i^{th}$  query.

**Note regarding printing the output.** Let the fraction  $\frac{x}{y}$  be the answer for a query. In order to output it, you should print a single integer representing the product  $x \cdot \text{mod\_inv}(y) \bmod 998\,244\,353$ , where  $\text{mod\_inv}(y)$  is defined as  $\text{mod\_inv}(y) = y^{998\,244\,351} \bmod 998\,244\,353$ .

**Note regarding modular arithmetic.** Additionally, keep in mind the following:

- Given two fractions  $\frac{a}{b}$  and  $\frac{c}{d}$ , their modular sum can be easily computed as:  $(a \cdot \text{mod\_inv}(b) + c \cdot \text{mod\_inv}(d)) \bmod 998\,244\,353$ ;
- If two fractions  $\frac{a}{b}$  and  $\frac{c}{d}$  are equal, then  $a \cdot \text{mod\_inv}(b) \bmod 998\,244\,353 = c \cdot \text{mod\_inv}(d) \bmod 998\,244\,353$ .

## Constraints

- $1 \leq q \leq 5 \cdot 10^4$
- $1 \leq l_i \leq r_i \leq 10^{12}$

## Subtasks

#	Points	Restrictions
1	18	$0 \leq r_i - l_i < 100$
2	65	$1 \leq l_i \leq r_i \leq 10^8$
3	17	No further constraints.

## Examples

### Input Example #1

```
2
5 12
1 1000000
```

### Output Example #1

```
166374097
439931963
```

## Input Example #2

```
5
11 15
5 14
3 10
12 20
7 19
```

## Output Example #2

```
166374096
166374117
499122210
499122249
665496322
```

## Explanation

For the first query in the first example, the answer, starting with  $ans = 0$ , can be computed as follows:

- $dec(5) = [5] \rightarrow ans += \frac{5}{1}$
- $dec(6) = [5, 1] \rightarrow ans += \frac{6}{2}$
- $dec(7) = [7] \rightarrow ans += \frac{7}{1}$
- $dec(8) = [7, 1] \rightarrow ans += \frac{8}{2}$
- $dec(9) = [7, 2] \rightarrow ans += \frac{9}{2}$
- $dec(10) = [7, 3] \rightarrow ans += \frac{10}{2}$
- $dec(11) = [7, 3, 1] \rightarrow ans += \frac{11}{3}$
- $dec(12) = [7, 5] \rightarrow ans += \frac{12}{2}$

The total sum is  $ans = \frac{229}{6}$  and the output is:  
 $229 \cdot mod\_inv(6) \bmod 998\,244\,353 = 229 \cdot 166\,374\,059 \bmod 998\,244\,353 = 166\,374\,097.$