

Astronomer

Problem ID: astronomer

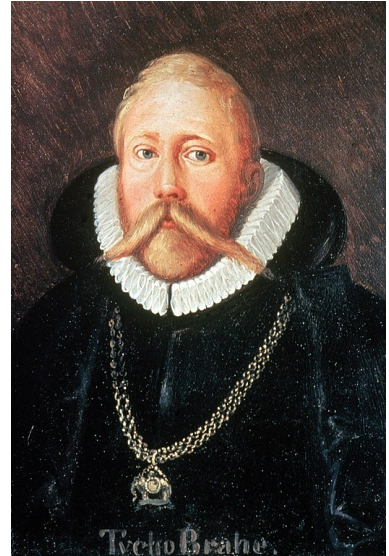
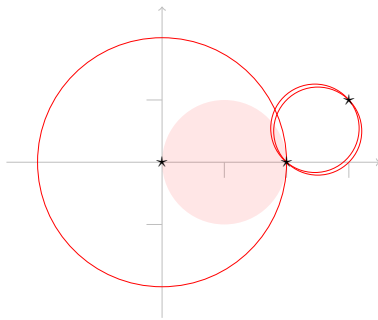
The astronomer has a passion for stargazing. In particular, he gets immense pleasure out of gazing at k stars simultaneously through his telescope. Building a telescope with radius r costs $t \cdot r$ kroner. The radius can be any nonnegative real number. A newly built telescope will point exactly at the origin $(0, 0)$. Moving it to point somewhere else also takes effort; shifting the telescope a distance of d units incurs a cost of $s \cdot d$ kroner. The astronomer can observe all stars at distance at most r from where the telescope points.

How much does it cost to build and move a telescope that allows at least k stars to be observed at once?

All coordinates and distances are given in the Euclidean plane.

Example

Here is an example with $n = 3$ stars at positions $(0, 0)$, $(2, 0)$, and $(3, 1)$. The shaded area shows a telescope of radius 1 pointing at $(1, 0)$ covering two stars; this costs $s + t$ kroner and is an optimal solution to sample input 3. The image also shows optimal solutions to sample inputs 1, 2, and 4.



Input

The first line consists of four integers: the number k of stars the astronomer wants to observe, the number n of stars in tonight's sky, the shifting cost s , and the telescope building cost t . Then follow n lines, where the i th line contains the integer coordinates x_i and y_i of the i th star. The coordinates of all stars are unique.

Output

A single real number: the minimum number of kroner that the astronomer needs to spend.

Constraints and Scoring

You can assume

1. $1 \leq k \leq n \leq 700$.
2. $x_i, y_i \in \{-10^9, \dots, 10^9\}$ for all $i \in \{1, \dots, n\}$.
3. $s, t \in \{0, \dots, 10^9\}$.
4. Your output is accepted if it is within a relative or absolute tolerance of $\epsilon = 10^{-6}$ of the correct answer.

Your solution will be tested on a set of test groups, each worth a number of points. Each test group contains a set of test cases. To get the points for a test group you need to solve all test cases in the test group. Your final score will be the maximum score of a single submission.

Group	Points	Constraints
1	8	$t \leq s$
2	9	$n \leq 50$ og $s = 0$
3	18	$s = 0$
4	13	$n \leq 50$
5	14	$n \leq 350$
6	15	$\epsilon = 1/10$
7	23	<i>No further constraints</i>

Sample Input 1

```
2 3 1000 500
0 0
2 0
3 1
```

Sample Output 1

```
1000.0
```

Sample Input 2

```
2 3 500 3000
0 0
2 0
3 1
```

Sample Output 2

```
3387.277541898787
```

Sample Input 3

```
2 3 250 750
0 0
2 0
3 1
```

Sample Output 3

```
1000.0
```

Sample Input 4

```
2 3 0 500
0 0
2 0
3 1
```

Sample Output 4

```
353.55339059327395
```

Sample Input 5

```
3 4 0 10
0 0
10 0
5 10
5 5
```

Sample Output 5

```
50.0
```