Package 'mcglm'

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Description

The Australian health survey was used by Bonat and Jorgensen (2015) as an example of multivariate count regression model. The data consists of five count response variables concerning health system access measures and nine covariates concerning social conditions in Australian for 1987-88.

- sex Factor with levels male and female.
- age Respondent's age in years divided by 100.
- income Respondent's annual income in Australian dollars divided by 1000.
- levyplus Coded factor. If respondent is covered by private health insurance fund for private patients in public hospital with doctor of choice (1) or otherwise (0).
- freepoor Coded factor. If respondent is covered by government because low income, recent immigrant, unemployed (1) or otherwise (0).
- freerepa Coded factor. If respondent is covered free by government because of old-age or disability pension, or because invalid veteran or family of deceased veteran (1) or otherwise (0)
- illnes Number of illnesses in past 2 weeks, with 5 or illnesses coded as 5.
- actdays Number of days of reduced activity in the past two weeks due to illness or injury.
- hscore Respondent's general health questionnaire score using Goldberg's method. High score indicates poor health.
- chcond Factor with three levels. If respondent has chronic condition(s) and is limited in activity (limited), or if the respondent has chronic condition(s) but is not limited in activity (nonlimited) or otherwise (otherwise, reference level).
- Ndoc Number of consultations with a doctor or specialist (response variable).
- Nndoc Number of consultations with health professionals (response variable).
- Nadm Number of admissions to a hospital, psychiatric hospital, nursing or convalescence home in the past 12 months (response variable).
- Nhosp Number of nights in a hospital during the most recent admission.
- Nmed Total number of prescribed and non prescribed medications used in the past two days.

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Usage

```
data(ahs)
```

Format

a data. frame with 5190 records and 17 variables.

Source

Deb, P. and Trivedi, P. K. (1997). Demand for medical care by the elderly: A finite mixture approach, Journal of Applied Econometrics 12(3):313–336.

Examples

```
library(lattice)
library(latticeExtra)
data(ahs, package="mcglm")
str(ahs)
xt <- xtabs(~age+sex, data=ahs)</pre>
mosaicplot(xt)
xt <- xtabs(~age+chcond, data=ahs)</pre>
mosaicplot(xt)
useOuterStrips(
    combineLimits(
        xyplot(Ndoc+Nndoc+Nadm+Nhosp+Nmed~age|sex,
               outer=TRUE, data=ahs,
               jitter.x=TRUE, amount=0.01,
               type=c("p", "a"),
               scales=list(y=list(relation="free")),
               ylab="Number or occurences",
               xlab="Age (years/100)")
)
useOuterStrips(
    combineLimits(
        xyplot(Ndoc+Nndoc+Nadm+Nhosp+Nmed~income|sex,
               outer=TRUE, data=ahs,
               jitter.x=TRUE, amount=0.01,
               type=c("p", "a"),
               scales=list(y=list(relation="free")),
               ylab="Number or occurences",
               xlab="Age (years/100)")
    )
)
```

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anova.mcglm

ANOVA method for McGLMs.

Description

ANOVA method for object of class McGLMS.

Usage

```
## S3 method for class 'mcglm'
anova(object, ...)
```

Arguments

object an object of class mcglm, usually, a result of a call to mcglm().

additional arguments affecting the summary produced. Note that there is no extra options for mcglm object class.

Value

A data.frame with Chi-square statistic to test the null hypothesis of a parameter, or a set of parameters, be zero. The Wald test based on the observed covariance matrix of the parameters is used.

Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

coef.mcglm

Extract model coefficients for mcglm class

Description

coef.mcglm is a function which extracts model coefficients from objects of mcglm class.

```
## S3 method for class 'mcglm'
coef(object, std.error = FALSE, response = c(NA,
   1:length(object$beta_names)), type = c("beta", "tau", "power",
   "correlation"), ...)
```

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Arguments

object An object of mcglm class.

std.error Logical. If TRUE returns the standard errors of the estimates. Default is FALSE.

response A numeric vector specyfing for which response variables the coefficients should be returned.

type A string vector (can be 1 element length) specyfing which coefficients should be returned. Options are "beta", "tau", "power", "tau" and "correlation".

additional arguments affecting the summary produced. Note that there is no extra options for mcglm object class.

Value

A data. frame with parameters names, estimates, response number and parameters type.

Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

|--|--|

Description

Computes confidence intervals for parameters in a fitted mcglm model.

Usage

```
## S3 method for class 'mcglm'
confint(object, parm, level = 0.95, ...)
```

Arguments

object a fitted mcglm object.

parm a specification of which parameters are to be given confidence intervals, either a

vector of number or a vector of strings. If missing, all parameters are considered.

level the nominal confidence level.

... additional arguments affecting the confidence interval produced. Note that there

is no extra options for mcglm object class.

Value

A data. frame with confidence intervals, parameters names, response number and parameters type.

Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

covprod 7

covprod

Cross variability matrix

Description

Compute the cross-covariance matrix between covariance and regression parameters. Equation (11) of Bonat and Jorgensen (2015).

Usage

```
covprod(A, res, W)
```

Arguments

A A matrix.

res A vector of residuals.

W A matrix of weights.

Author(s)

Wagner Hugo Bonat

ESS

Extract generalized error sum of squares (ESS) for multivariate covariance generalized linear models.

Description

Extract the generalized error sum of squares for a fitted McGLM.

Usage

```
ESS(object, verbose = TRUE)
```

Arguments

object an object or a list of objects representing a model of mcglm class.

verbose Logical

Value

Returns the value of the Gaussian pseudo-loglikelihood.

Author(s)

8 fit_mcglm

fitted.mcglm

Extract Model Fitted Values of McGLM

Description

Extract fitted values for objects of mcglm class.

Usage

```
## S3 method for class 'mcglm'
fitted(object, ...)
```

Arguments

object An object of mcglm class.

additional arguments affecting the summary produced. Note that there is no extra options for mcglm object class.

Value

Depending on the number of response variable, the function fitted.mcglm returns a vector (univariate models) or a matrix (multivariate models) of fitted values.

Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

fit_mcglm

Chaser and reciprocal likelihood algorithms.

Description

This function implements the two manin algorithms used to fitting McGLMs. The chaser and the reciprocal likelihood algorithms. In general the chaser algorithm is faster than the reciprocal likelihood and should be preferred.

```
fit_mcglm(list_initial, list_link, list_variance, list_covariance, list_X,
   list_Z, list_offset, list_Ntrial, list_power_fixed, list_sparse, y_vec,
   correct = TRUE, max_iter, tol = 0.001, method = "rc", tunning = 0,
   verbose)
```

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Arguments

list_initial A list of initial values for regression and covariance parameters.

list_link A list of link function names.

list_variance A list of variance function names.

list_covariance

A list of covariance function names.

list_X A list of design matrices.

list_Z A list of knowm matrices to used on the matrix linear predictor.

list_offset A list of offset values.

list_Ntrial A list of number of trials, useful only when analysis binomial data.

list_power_fixed

A list of logicals indicating if the power parameters should be estimated or not.

list_sparse A list of logicals indicating if the matrices should be set up as sparse matrices.

This argument is useful only when using exponential-matrix covariance link function. In the other cases the algorithm detects automatically if the matrix

should be sparse or not.

y_vec A vector of the response variables stacked.

correct A logical indicating if the algorithm will use the correction term or not.

max_iter Maximum number of iterations.
tol A numeric spcyfing the tolerance.

method A string specyfing the method used to fit the models (chaser or rc).

tunning A numeric value in general near zero for the rc method and near 1 for the chaser

method. This argument control the step-length.

verbose A logical if TRUE print the values of the covariance parameters used on each

iteration.

Value

A list with estimated regression and covariance parameters.

GOSHO NA

Description

Compute the Gosho's information criterion for multivariate covariance generalized linear models. WARNINGS: This function is limited to models with ONE response variable.

Usage

GOSHO(object, id, verbose = TRUE)

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Arguments

object An object of mcglm class.

id a vector which identifies the clusters. The length and order of id should be

the same as the number of observations. Data are assumed to be sorted so that observations on a cluster are contiguous rows for all entities in the formula.

verbose Logical.

Value

A matrix. Note that the function assumes that the data are in the correct order.

Author(s)

Wagner Hugo Bonat

Hunting

Hunting in Pico Basile, Bioko Island, Equatorial Guinea.

Description

Case study analysed in Bonat et. al. (2016) concernings on data of animals hunted in the village of Basile Fang, Bioko Norte Province, Bioko Island, Equatorial Guinea. Monthly number of blue duikers and other small animals shot or snared was collected for a random sample of 52 commercial hunters from August 2010 to September 2013. For each animal caught, the species, sex, method of capture and altitude were documented. The data set has 1216 observations.

- Alt Factor five levels indicating the Altitude where the animal was caught.
- Sex Factor two levels Female and Male.
- Method Factor two levels Escopeta and Trampa.
- OT Monthly number of other small animals hunted.
- BD Monthly number of blue duikers hunted.
- Offset Monthly number of hunter days.
- Hunter Hunter index.
- Month Month index.
- MonthCalendar Month using calendar numbers (1-January, ..., 12-December).
- Year Year calendar (2010–2013).

Usage

data(Hunting)

Format

a data. frame with 1216 records and 10 variables.

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Source

Bonat, et. al. (2016). Modelling the covariance structure in marginal multivariate count models: Hunting in Bioko island. The annals of Applied Statatistics, to appear.

Examples

mcglm

Fitting Multivariate Covariance Generalized Linear Models (McGLM)

Description

mcglm is used to fit multivariate covariance generalized linear models. The models are specified by a set of lists giving a symbolic description of the linear predictor. The user can choose between a list of link, variance and covariance functions. The models are fitted using an estimating function approach, combining quasi-score functions for regression parameters and Pearson estimating function for covariance parameters. For details see Bonat and Jorgensen (2015).

Fits a multivariate covariance generalized linear models (McGLMs) to data. McGLM is a general framework for non-normal multivariate data analysis, designed to handle multivariate response variables, along with a wide range of temporal and spatial correlation structures defined in terms of a covariance link function combined with a matrix linear predictor involving known matrices. The models take non-normality into account in the conventional way by means of a variance function, and the mean structure is modelled by means of a link function and a linear predictor. The models are fitted using an efficient Newton scoring algorithm based on quasi-likelihood and Pearson estimating functions, using only second-moment assumptions. This provides a unified approach to a wide variety of different types of response variables and covariance structures, including multivariate extensions of repeated measures, time series, longitudinal, spatial and spatio-temporal structures.

```
mcglm(linear_pred, matrix_pred, link, variance, covariance, offset, Ntrial,
   power_fixed, data, control_initial = "automatic", contrasts = NULL,
   control_algorithm = list())
```

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Arguments

linear_pred A list of formula see formula for details.

matrix_pred A list of known matrices to be used on the matrix linear predictor. Details can

be obtained on mc_matrix_linear_predictor.

link A list of link functions names, see mc_link_function for details.

variance A list of variance functions names, see mc_variance_function for details.

covariance A list of covariance link functions names, current options are: identity, inverse

and exponential-matrix (expm).

offset A list with values of offset values if any.

Ntrial A list with values of the number of trials on Bernoulli experiments. It is useful

only for binomialP and binomialPQ variance functions.

power_fixed A list of logicals indicating if the values of the power parameter should be esti-

mated or not.

data A dta frame.

control_initial

A list of initial values for the fitting algorithm. See details below.

contrasts Extra arguments to passed to model.matrix.

control_algorithm

A list of arguments to be passed for the fitting algorithm. See fit_mcglm for

details.

Value

mcglm returns an object of class 'mcglm'.

Author(s)

Wagner Hugo Bonat

mc_bias_corrected_std Bias-corrected standard error for regression parameters

Description

Compute bias-corrected standard error for regression parameters in the context of clustered observations. It is also robust and has improved finite sample properties.

```
mc_bias_corrected_std(object, id)
```

mc_build_bdiag

Arguments

object An object of mcglm class.

id a vector which identifies the clusters. The length and order of id should be

the same as the number of observations. Data are assumed to be sorted so that observations on a cluster are contiguous rows for all entities in the formula.

Value

A matrix. Note that the function assumes that the data are in the correct order.

Author(s)

Wagner Hugo Bonat

mc_build_bdiag Build a block-diagonal matrix of zeros.

Description

Build a block-diagonal matrix of zeros. Such functions is used when computing the derivatives of the Cholesky decomposition of C.

Usage

```
mc_build_bdiag(n_resp, n_obs)
```

Arguments

n_resp A numeric specifying the number of response variables.

n_obs A numeric specifying the number of observations in the data set.

Details

It is an internal function.

Value

A list of zero matrices.

Author(s)

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mc_build_C	Build the joint covariance matrix

Description

This function builds the joint variance-covariance matrix using the Generalized Kronecker product and its derivatives with respect to rho, power and tau parameters.

Usage

```
mc_build_C(list_mu, list_Ntrial, rho, list_tau, list_power, list_Z, list_sparse,
  list_variance, list_covariance, list_power_fixed, compute_C = FALSE,
  compute_derivative_beta = FALSE, compute_derivative_cov = TRUE)
```

Arguments

list_mu A list with values of the mean.

list_Ntrial A list with the number of trials. Usefull only for binomial responses.

Vector of correlation parameters. rho

A list with values for the tau parameters. list_tau A list with values for the power parameters. list_power

A list of matrix to be used in the matrix linear predictor. list_Z

list_sparse A list with Logical.

list_variance A list specifying the variance function to be used for each response variable.

list_covariance

A list specifying the covariance function to be used for each response variable.

list_power_fixed

A list of Logical specifying if the power parameters are fixed or not.

compute_C Logical. Compute or not the C matrix.

compute_derivative_beta

Logical. Compute or not the derivative of C with respect to regression parameters.

compute_derivative_cov

Logical. Compute or not the derivative of C with respect the covariance parameters.

Value

A list with the inverse of the C matrix and the derivatives of the C matrix with respect to rho, power and tau parameters.

Author(s)

mc_build_omega 15

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IIIC_	_build_	_omega	

Build omega matrix

Description

This function build Ω matrix according the covariance link function.

Usage

```
mc_build_omega(tau, Z, covariance_link, sparse = FALSE)
```

Arguments

tau A vector

Z A list of matrices.

covariance_link

String specifing the covariance link function: identity, inverse, expm.

sparse Logical force to use sparse matrix representation 'dsCMatrix'.

Value

A list with the Ω matrix its inverse and derivatives with respect to τ .

Author(s)

Wagner Hugo Bonat

mc_build_sigma

Build variance-covariance matrix

Description

This function builds a variance-covariance matrix, based on the variance function and omega matrix.

```
mc_build_sigma(mu, Ntrial = 1, tau, power, Z, sparse, variance, covariance, power_fixed, compute_derivative_beta = FALSE)
```

Arguments

mu A numeric vector. In general the output from mc_link_function.

Ntrial A numeric vector, or NULL or a numeric specifing the number of trials in the

binomial experiment. It is usefull only when using variance = binomialP or

binomialPQ. In the other cases it will be ignored.

tau A numeric vector.

power A numeric or numeric vector. It should be one number for all variance functions

except binomialPQ, in that case the argument specifies both p and q.

Z A list of matrices.

sparse Logical.

variance String specifing the variance function: constant, tweedie, poisson_tweedie, bi-

nomialP or binomialPQ.

covariance String specifing the covariance function: identity, inverse or expm.

power_fixed Logical if the power parameter is fixed at initial value (TRUE). In the case

power_fixed = FALSE the power parameter will be estimated.

compute_derivative_beta

Logical. Compute or not the derivative with respect to regression parameters.

Value

A list with the Cholesky decomposition of Σ , Σ^{-1} and the derivative of Σ with respect to the power and tau parameters.

Author(s)

Wagner Hugo Bonat

See Also

```
mc_link_function, mc_variance_function, mc_build_omega.
```

```
mc_build_sigma_between
```

Build the correlation matrix between response variables

Description

This function builds the correlation matrix between response variable, its inverse and derivatives.

```
mc_build_sigma_between(rho, n_resp, inverse = FALSE)
mc_derivative_sigma_between(n_resp)
```

mc_core_pearson 17

Arguments

rho A numeric vector.

n_resp A numeric. inverse Logical.

Value

A list with sigmab and its derivatives with respect to rho.

Author(s)

Wagner Hugo Bonat

mc_core_pearson

Core of the Pearson estimating function.

Description

Core of the Pearson estimating function.

Usage

```
mc_core_pearson(product, inv_C, res)
```

Arguments

product A matrix.
inv_C A matrix.

res A vector of residuals.

Details

It is an internal function.

Value

A vector

Author(s)

18 mc_cross_sensitivity

Description

Compute the correction term associated with the Pearson estimating function.

Usage

```
mc_correction(D_C, inv_J_beta, D, inv_C)
```

Arguments

D_C A list of matrices.

inv_J_beta A matrix. In general it is computed based on the output of the [mcglm]{mc_quasi_score}.

D A matrix. In general it is the output of the mc_link_function.

inv_C A matrix. In general the output of the mc_build_C.

Details

It is an internal function useful inside the fitting algorithm.

Value

A vector with the correction terms to be used on the Pearson estimating function.

Author(s)

Wagner Hugo Bonat

```
mc_cross_sensitivity Cross-sensitivity
```

Description

Compute the cross-sensitivity matrix between regression and covariance parameters. Equation 10 of Bonat and Jorgensen (2015).

```
mc_cross_sensitivity(Product_cov, Product_beta,
    n_beta_effective = length(Product_beta))
```

mc_cross_variability 19

Arguments

```
Product_cov A list of matrices.

Product_beta A list of matrices.

n_beta_effective
```

Numeric. Effective number of regression parameters.

Value

The cross-sensitivity matrix. Equation (10) of Bonat and Jorgensen (2015).

Author(s)

Wagner Hugo Bonat

```
mc_cross_variability Compute the cross-variability matrix
```

Description

Compute the cross-variability matrix between covariance and regression parameters.

Usage

```
mc_cross_variability(Product_cov, inv_C, res, D)
```

Arguments

Product_cov A list of matrices.

inv_C A matrix.

res A vector.

D A matrix.

Value

The cross-variability matrix between regression and covariance parameters.

Author(s)

20 mc_derivative_C_rho

```
mc_derivative_cholesky
```

Derivatives of the Cholesky decomposition

Description

This function compute the derivative of the Cholesky decomposition.

Usage

```
mc_derivative_cholesky(derivada, inv_chol_Sigma, chol_Sigma)
```

Arguments

```
derivada A matrix.
inv_chol_Sigma A matrix.
chol_Sigma A matrix.
```

Details

It is an internal function.

Value

A list of matrix.

Author(s)

Wagner Hugo Bonat

Description

Compute the derivative of the C matrix with respect to the correlation parameters rho.

```
mc_derivative_C_rho(D_Sigmab, Bdiag_chol_Sigma_within,
   t_Bdiag_chol_Sigma_within, II)
```

mc_derivative_expm 21

Arguments

```
D_Sigmab A matrix. Bdiag_chol_Sigma_within
```

A block-diagonal matrix.

 $t_Bdiag_chol_Sigma_within$

A block-diagonal matrix.

II A diagonal matrix.

Details

It is an internal function used to build the derivatives of the C matrix.

Value

A matrix.

Author(s)

Wagner Hugo Bonat

mc_derivative_expm

Derivative of exponential-matrix function

Description

Compute the derivative of the exponential-matrix covariance link function.

Usage

```
mc_derivative_expm(dU, UU, inv_UU, Q, n = dim(UU)[1], sparse = FALSE)
```

Arguments

dU A matrix.
UU A matrix.
inv_UU A matrix.

Q A numeric vector.

n A numeric. sparse Logical.

Details

Many arguments required by this function are provide by the link[mcglm]{mc_dexpm}. The argument dU is the derivative of the U matrix with respect to the models parameters. It should be computed by the user.

Value

A matrix.

Author(s)

Wagner Hugo Bonat

See Also

```
expm, link[mcglm]{mc_dexp_gold} and link[mcglm]{mc_dexpm}.
```

```
mc_derivative_sigma_beta
```

Derivatives of V^1/2 with respect to beta.

Description

Compute the derivatives of $V^{1/2}$ matrix with respect to the regression parameters beta.

Usage

```
mc_derivative_sigma_beta(D, D_V_sqrt_mu, Omega, V_sqrt, variance)
```

Arguments

 $\begin{array}{lll} \textbf{D} & \textbf{A matrix.} \\ \textbf{D}_{-}\textbf{V}_{-}\textbf{sqrt}_{-}\textbf{mu} & \textbf{A matrix.} \\ \textbf{Omega} & \textbf{A matrix.} \\ \textbf{V}_{-}\textbf{sqrt} & \textbf{A matrix.} \end{array}$

variance A string specifying the variance function name.

Value

A list of matrices, containg the derivatives of $V^{1/2}$ with respect to the regression parameters.

Author(s)

mc_dexp_gold 23

mc_dexp_gold

Exponential-matrix and its derivatives

Description

Given a matrix M and its derivative dM the function dexp_gold returns the exponential-matrix expm(M) and its derivative. This function is based on the expm function. It is not really used in the package, but I keep this function to test my own implementation based on eigen values decomposition.

Usage

```
mc_dexp_gold(M, dM)
```

Arguments

M A matrix.

dM A matrix.

Value

A list with two elements: expm(M) and its derivatives.

Author(s)

Wagner Hugo Bonat

See Also

```
expm, eigen.
```

Examples

```
M <- matrix(c(1,0.8,0.8,1), 2,2)
dM <- matrix(c(0,1,1,0),2,2)
mcglm::mc_dexp_gold(M = M, dM = dM)</pre>
```

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mc_dist	Distances models
---------	------------------

Description

Builds distances model matrix.

Usage

```
mc_dist(id, time, data, method = "euclidean")
```

Arguments

id Subject index. Note that this structure was designed to deal with longitudinal

data.

time Index indicating the time.

data Data set

method The distance measure to be used. This must be one of "euclidean", "maxi-

mum", "manhattan", "canberra", "binary" or "minkowski".

Value

A matrix of dgCMatrix class.

mc_expm	Exponential-matrix covariance link function	

Description

Given a matrix U the function mc_{expm} returns the exponential-matrix expm(U) and some auxiliares matrices to compute its derivatives. This function is based on the eigen-value decomposition it means that it is very slow.

Usage

```
mc_{expm}(U, n = dim(U)[1], sparse = FALSE, inverse = FALSE)
```

Arguments

U	A matrix.
•	

n A number specifing the dimension of the matrix U. Default n = dim(U)[1].

sparse Logical defining the class of the output matrix. If sparse = TRUE the output

class will be 'dgCMatrix' if sparse = FALSE the class will be 'dgMatrix'.

inverse Logical defining if the inverse will be computed or not.

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Value

A list with $\Omega = expm(U)$ its inverse (if inverse = TRUE) and auxiliares matrices to compute the derivatives.

Author(s)

Wagner Hugo Bonat

See Also

```
expm, eigen, link[mcglm]{mc_dexp_gold}.
```

mc_getInformation

Getting information about model parameters

Description

This computes all information required about the number of model parameters.

Usage

```
mc_getInformation(list_initial, list_power_fixed, n_resp)
```

Arguments

```
list_initial A list of initial values.
```

list_power_fixed

A list of logical specyfing if the power parameters should be estimated or not.

n_resp

A number specyfing the nmber of response variables.

Value

The number of β 's, τ 's, power and correlation parameters.

Author(s)

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mc_id	Independent model structure	

Description

Builds a identity matrix to be used as a component of the matrix linear predictor.

Usage

```
mc_id(data)
```

Arguments

data The data set to be used.

Value

A list of matrix.

|--|--|--|--|

Description

This function provides o list of initial values to be used while fitting McGLMs.

Usage

```
mc_initial_values(linear_pred, matrix_pred, link, variance, covariance, offset,
   Ntrial, contrasts = NULL, data)
```

Arguments

linear_pred	A list of formula see formula for details.
matrix_pred	A list of known matrices to be used on the matrix linear predictor. Details can be obtained on mc_matrix_linear_predictor.
link	A list of link functions names, see mc_link_function for details.
variance	A list of variance functions names, see mc_variance_function for details.
covariance	A list of covariance link functions names, current options are: identity, inverse and exponential-matrix (expm).
offset	A list with values of offset values if any.
Ntrial	A list with values of the number of trials on Bernoulli experiments. It is useful only for binomialP and binomialPQ variance functions.
contrasts	List of contrasts to be used in the model.matrix.
data	A data frame.

mc_link_function 27

Value

Return a list of initial values to be used while fitting McGLMs.

Author(s)

Wagner Hugo Bonat

mc_link_function

Link functions

Description

The mc_link_function is a customized call of the make.link function.

Given the name of a link function, it returns a list with two elements. The first element is the inverse of the link function applied on the linear predictor $\mu = g^{-1}(X\beta)$. The second element is the derivative of mu with respect to the regression parameters β . It will be useful when computing the quasi-score function.

Usage

```
mc_link_function(beta, X, offset, link)
mc_logit(beta, X, offset)
mc_probit(beta, X, offset)
mc_cauchit(beta, X, offset)
mc_cloglog(beta, X, offset)
mc_loglog(beta, X, offset)
mc_identity(beta, X, offset)
mc_log(beta, X, offset)
mc_log(beta, X, offset)
mc_log(beta, X, offset)
mc_sqrt(beta, X, offset)
mc_invmu2(beta, X, offset)
mc_inverse(beta, X, offset)
```

Arguments

beta A numeric vector of regression parameters.

X A design matrix, see model.matrix for details.

28 mc_link_function

offset A numeric vector of offset values. It will be sum up on the linear predictor

as a covariate with known regression parameter equals one $(\mu = g^{-1}(X\beta +$

offset)). If no offset is present in the model, set offset = NULL.

link A string specifing the name of the link function. mcglm implements the following link functions: logit, probit, cauchit, cloglog, loglog, identity, log, sqrt,

1/mu² and inverse. A user defined link function can be used (see Details).

Details

The link function is an important component of the multivariate covariance generalized linear model, since it link the expectation of the response variable with the covariates. Let β a px1 regression parameter vector and X an nxp design matrix. The expected value of a response variable Y is given by

$$E(Y) = g^{-1}(X\beta),$$

where g is the link function and $\eta=X\beta$ is the linear predictor. Let D be a $n\times p$ matrix whose entries are given by the derivatives of mu with respect to β . Such matrix will be required by the fitting algorithm. The function mc_link_function returns a list where the first element is mu (n x 1) vector and the second D (n x p) matrix. A user defined function can be used. It must be a function with arguments beta, X and offset (set to NULL if non needed). The function must return a length 2 named list with mu and D elements as a vector and a matrix of proper dimensions dimensions.

Value

A list with two elements: mu and D.

Author(s)

Wagner Hugo Bonat

See Also

```
model.matrix, make.link.
```

Examples

mc_list2vec 29

mc_list2vec

Auxiliar function transforms list to a vector.

Description

This function takes a list of parameters and tranforms to a vector.

Usage

```
mc_list2vec(list_initial, list_power_fixed)
```

Arguments

```
list_initial A list specifying initial values.
```

list_power_fixed

A list of logical operators specyfing if the power parameter should be estimated or not.

Details

It is an internal function, in general the users never will use this function. It will be useful, only if the user wants to implement a different variance-covariance matrix.

Value

A vector of model parameters.

Author(s)

Wagner Hugo Bonat

mc_ma

Moving average models

Description

Builds moving average model matrix of order k.

```
mc_ma(id, time, data, order = 1)
```

Arguments

id Subject index. Note that this structure was designed to deal with longitudinal

data.

time Index indicating the time.

data Data set.

order Order of the random walk model.

Value

A matrix of dgCMatrix class.

```
mc_matrix_linear_predictor
```

Matrix linear predictor

Description

Compute the matrix linear predictor.

Usage

```
mc_matrix_linear_predictor(tau, Z)
```

Arguments

tau A numeric vector.

Z A list of known matrices.

Details

Given a list with a set of known matrices $(Z_0,...,Z_D)$ the function mc_matrix_linear_predictor returns $U=\tau_0Z_0+...+\tau_DZ_D$.

Value

A matrix.

Author(s)

Wagner Hugo Bonat

Examples

```
require(Matrix)
Z0 <- Diagonal(5, 1)
Z1 <- Matrix(rep(1,5)%*%t(rep(1,5)))
Z <- list(Z0, Z1)
mc_matrix_linear_predictor(tau = c(1,0.8), Z = Z)</pre>
```

mc_mixed 31

 mc_mixed

Mixed model structure

Description

Builds a mixed model structure

Usage

```
mc_mixed(formula, data)
```

Arguments

formula A formula model to build the matrix linear predictor (see Details).

data The data set to be used.

Value

A list matrices.

mc_pearson

Pearson estimating function

Description

Compute the Pearson estimating function its sensitivity and variability matrices.

Usage

```
mc_pearson(y_vec, mu_vec, Cfeatures, inv_J_beta = NULL, D = NULL,
    correct = FALSE, compute_variability = FALSE)
```

Arguments

 $\begin{array}{ll} \mbox{y_vec} & \mbox{A vector.} \\ \mbox{mu_vec} & \mbox{A vector.} \end{array}$

Cfeatures A list of matrices.

32 mc_quasi_score

Details

Compute the Pearson estimating function its sensitivity and variability matrices. For more details see Bonat and Jorgensen (2015) equations 6, 7 and 8.

Value

A list with three components: (i) a vector of quasi-score values, (ii) the sensitivity and (iii) variability matrices associated with the Pearson estimating function.

Author(s)

Wagner Hugo Bonat

mc_quasi_score

Quasi-score function

Description

Compute the quasi-score function, its sensitivy and variability matrix.

Usage

```
mc_quasi_score(D, inv_C, y_vec, mu_vec)
```

Arguments

D A matrix. In general the output from mc_link_function.

inv_C A matrix. In general the output from mc_build_C.

 y_{vec} A vector. M_{vec} A vector.

Value

The quasi-score vector, the Sensivity and variability matrices.

Author(s)

mc_robust_std 33

mc_robust_std	Robust standard error for regression parameters	

Description

Compute robust standard error for regression parameters in the context of clustered observations.

Usage

```
mc_robust_std(object, id)
```

Arguments

object An object of mcglm class.

id a vector which identifies the clusters. The length and order of id should be

the same as the number of observations. Data are assumed to be sorted so that observations on a cluster are contiguous rows for all entities in the formula.

Value

A matrix. Note that the function assumes that the data are in the correct order.

Author(s)

Wagner Hugo Bonat

mc_rw	Random walk models

Description

Builds a random walk model matrix of order k.

Usage

```
mc_rw(id, time, data, order = 1, proper = FALSE)
```

Arguments

id	Subject index. Note that this structure was designed to deal with longitudinal data.
time	Index indicating the time.
data	Data set.
order	Order of the random walk model.
proper	Logical.

34 mc_sandwich

Value

A matrix of dgCMatrix class.

mc_sandwich

Matrix product in sandwich form

Description

The function mc_sandwich is just an auxiliar function to compute product matrix in the sandwich form bord1 * middle * bord2. An special case appears when computing the derivative of the covariance matrix with respect to the power parameter. Always the bord1 and bord2 should be diagonal matrix. If it is not true, this product is too slow.

Usage

```
mc_sandwich(middle, bord1, bord2)
mc_sandwich_negative(middle, bord1, bord2)
mc_sandwich_power(middle, bord1, bord2)
mc_sandwich_cholesky(bord1, middle, bord2)
mc_multiply(bord1, bord2)
mc_multiply2(bord1, bord2)
```

Arguments

middle A matrix.
bord1 A matrix.
bord2 A matrix.

Value

The matrix product bord1 * middle * bord2.

Author(s)

mc_sensitivity 35

<pre>mc_sensitivity</pre>	Sensitivity matri
---------------------------	-------------------

Description

Compute the sensitivity matrix associated with the Pearson estimating function.

Usage

```
mc_sensitivity(product)
```

Arguments

product

A list of matrix.

Details

This function implements the equation 7 of Bonat and Jorgensen (2015).

Value

The sensitivity matrix associated with the Pearson estimating function.

Author(s)

Wagner Hugo Bonat

mc_sic	Compute the score information criterion (SIC) for multivariate covari-
	ance generalized linear models.

Description

Compute the SIC for McGLMS.

Usage

```
mc_sic(object, scope, data, response, penalty = 2)
```

Arguments

an object representing a model of mcglm class.
a vector containing all covariate names to be tested.
data frame containing the all variables envolved
Indicate for which response variable SIC is computed.

penalty penalty term (default = 2).

36 mc_sic_covariance

Value

A data frame with SIC values for each covariate in the scope argument.

Author(s)

Wagner Hugo Bonat

mc_sic_covariance Compute the score information criterion (SIC) for multivariate covariance generalized linear models.

Description

Compute SIC for covariance parameters in McGLMS.

Usage

```
mc_sic_covariance(object, scope, idx, data, penalty = 2, response)
```

Arguments

object an object representing a model of mcglm class.

scope a list of matrices to be tested in the matrix linear predictor.

idx Indicator of matrices belong to the same effect.

data frame containing all variables envolved in the model.

penalty penalty term (default = 2).

response Indicate for which response variable SIC is computed.

Value

A data frame with SIC values for each matrix in the scope argument.

Author(s)

```
mc_transform_list_bdiag
```

Auxiliar function to compute the derivatives of the C matrix.

Description

This function take a list of matrices and return a list of block-diagonal matrices, where the original matrices are one block non-zero of the matrix.

Usage

```
mc_transform_list_bdiag(list_mat, mat_zero, response_number)
```

Arguments

list_mat A list of matrices.

mat_zero A list of zero matrices. In general the output of link[mcglm]{mc_build_bdiag}.

response_number

A numeric specifying the response variable number.

Value

A list of block-diagonal matrices.

Author(s)

Wagner Hugo Bonat

<pre>mc_updateBeta</pre>	Updated regression parameters	

Description

This function update a list of regression parameters. It will be useful only inside the fitting algorithm.

Usage

```
mc_updateBeta(list_initial, betas, information, n_resp)
```

Arguments

list_initial A list of initial values.

betas A vector with actual regression parameters values.

information A list with information about the number of parameters in the model. In general

the output from mc_getInformation.

n_resp A numeric specyfing the number of response variables.

38 mc_updateCov

Value

A list with updated values of the regression parameters.

Author(s)

Wagner Hugo Bonat

mc_updateCov

Updated covariance parameters

Description

This function update a list of covariance parameters. It will be useful only inside the fitting algorithm.

Usage

```
mc_updateCov(list_initial, covariance, list_power_fixed, information, n_resp)
```

Arguments

list_initial A list of initial values.

covariance A vector with actual covariance parameters values.

list_power_fixed

A list of logicals indicating if the power parameter should be estimated or not.

information A list with information about the number of parameters in the model. In general

the output from mc_getInformation.

n_resp A numeric specyfing the number of response variables.

Value

A list with updated values of the covariance parameters.

Author(s)

Wagner Hugo Bonat

39 mc_variability

	mc_variability	Variability matrix		
--	----------------	--------------------	--	--

Description

Compute the variability matrix associated with the Pearson estimating function.

Usage

```
mc_variability(sensitivity, product, inv_C, C, res)
```

Arguments

A matrix. In general the output from mc_sensitivity. sensitivity product A list of matrix. inv_C A matrix. In general the output from mc_build_C. С A matrix. In general the output from mc_build_C. A vector. The residuals vector, i.e. (y_vec - mu_vec).

Details

res

This function implements the equation 8 of Bonat and Jorgensen (2015).

Value

The variability matrix associated with the Pearson estimating function.

Author(s)

Wagner Hugo Bonat

```
mc_variance_function
                        Variance function
```

Description

Compute features related with variance functions.

Usage

```
mc_variance_function(mu, power, Ntrial, variance, inverse, derivative_power,
  derivative_mu)
mc_power(mu, power, inverse, derivative_power, derivative_mu)
mc_binomialP(mu, power, inverse, Ntrial, derivative_power, derivative_mu)
mc_binomialPQ(mu, power, inverse, Ntrial, derivative_power, derivative_mu)
```

40 mc_variance_function

Arguments

mu A numeric vector. In general the output from mc_link_function.

power A numeric value (power and binomialP) or vector (binomialPQ) of the power

parameters.

Ntrial Number of trials, useful only when dealing with binomial response variables.

variance A string specifing the name (power, binomialP or binomialPQ) of the vari-

ance function.

inverse Logical.

derivative_power

Logical if compute (TRUE) or not (FALSE) the derivatives with respect to the

power parameter.

derivative_mu Logical if compute (TRUE) or not (FALSE) the derivative with respect to the

mu parameter.

Details

The function mc_variance_function computing three features related with the variance function. Depending on the Logical arguments, the function returns $V^{1/2}$ and its derivatives with respect to the parameters power and mu, respectivelly. The output is a named list, completely informative about what the function has been computed. For example, if inverse = FALSE, derivative_power = TRUE and derivative_mu = TRUE. The output will be a list, with three elements: V_{sqrt} , D_{sqrt} power and D_{sqrt} mu.

Value

A list with from one to four elements depends on the arguments.

Author(s)

Wagner Hugo Bonat

See Also

```
mc_link_function.
```

Examples

NewBorn 41

NewBorn

Respiratory physiotherapy on premature newborns.

Description

The NewBorn dataset consist of a prospective study to assess the effect of respiratory physiotherapy on the cardiopulmonary function of ventilated preterm newborn infants with birth weight lower than 1500 g. The data set was collected and kindly made available by the nursing team of the Waldemar Monastier hospital, Campo Largo, PR, Brazil. The NewBorn dataset was analysed in Bonat and Jorgensen (2016) as an example of mixed outcomes regression model.

- Sex Factor two levels Female and Male.
- GA Gestational age (weeks).
- BW Birth weight (mm).
- APGAR1M APGAR index in the first minute of life.
- APGAR5M APGAR index in the fifth minute of life.
- PRE Factor, two levels (Premature: YES; NO).
- HD Factor, two levels (Hansen's disease, YES; NO).
- SUR Factor, two levels (Surfactant, YES; NO).
- JAU Factor, two levels (Jaundice, YES; NO).
- PNE Factor, two levels (Pneumonia, YES; NO).
- PDA Factor, two levels (Persistence of ductus arteriosus, YES; NO).
- PPI Factor, two levels (Primary pulmonary infection, YES; NO).
- OTHERS Factor, two levels (Other diseases, YES; NO).
- DAYS Age (days).
- AUX Factor, two levels (Type of respiratory auxiliary, HOOD; OTHERS).
- RR Respiratory rate (continuous).
- HR Heart rate (continuous).
- SP02 Oxygen saturation (bounded).
- TREAT Factor, three levels (Respiratory physiotherapy, Evaluation 1; Evaluation 2; Evaluation 3).
- NBI Newborn index.
- TIME Days of treatment.

Usage

data(NewBorn)

Format

a data. frame with 270 records and 21 variables.

pAIC

Source

Bonat, et. al. (2016). Multivariate covariance generalized linear models. Journal of Royal Statistical Society - Series C, to appear.

Examples

pAIC

Extract pseudo Akaike Information Criterion (pAIC) for multivariate covariance generalized linear models.

Description

Extract the pAIC for a fitted McGLM.

Usage

```
pAIC(object, verbose = TRUE)
```

Arguments

object an object or a list of objects representing a model of mcglm class.

verbose Logical

Value

Returns the value of the pAIC.

Author(s)

Wagner Hugo Bonat

pKLIC 43

pKLIC

Extract pseudo Kullback-Leibler Information Criterion for multivariate covariance generalized linear models.

Description

Extract the pKLIC for a fitted McGLM.

Usage

```
pKLIC(object, verbose = TRUE)
```

Arguments

object

an object or a list of objects representing a model of mcglm class.

verbose

Logical

Value

Returns the value of the pKLIC.

Author(s)

Wagner Hugo Bonat

plogLik

Extract Gaussian pseudo-loglikelihood (plogLik) for multivariate covariance generalized linear models.

Description

Extract the Gaussian pseudo-loglikelihood for a fitted McGLM.

Usage

```
plogLik(object, verbose = TRUE)
```

Arguments

object

an object or a list of objects representing a model of mcglm class.

verbose

Logical

Value

Returns the value of the Gaussian pseudo-loglikelihood.

print.mcglm

Author(s)

Wagner Hugo Bonat

plot.mcglm

Default Multivariate Covariance Generalized Linear models plotting

Description

takes a fitted mcglm object and do plots based on residuals, influence diagnostic measures and algorithm check.

Usage

```
## S3 method for class 'mcglm'
plot(x, type = "residuals", ...)
```

Arguments

x a fitted mcglm object.

type Specify which graphical analysis will be performed. Options are: "residuals",

"influence" and "algorithm".

... additional arguments affecting the plot produced. Note that there is no extra

options for mcglm object class.

Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

print.mcglm

Print method for Multivariate Covariance Generalized Linear Model

Description

The default print method for a mcglm object.

Usage

```
## S3 method for class 'mcglm'
print(x, ...)
```

Arguments

x fitted model objects of class mcglm as produced by mcglm().

... further arguments passed to or from other methods.

Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

residuals.mcglm 45

residuals.mcglm	Residuals for Multivariate Covariance Generalized Linear Models (McGLM)

Description

Compute residuals based on fitting mcglm models.

Usage

```
## S3 method for class 'mcglm'
residuals(object, type = "raw", ...)
```

Arguments

object An of class mcglm, typically the result of a call to mcglm.

type the type of residuals which should be returned. The alternatives are: "raw"

(default), "pearson" and "standardized".

... additional arguments affecting the residuals produced. Note that there is no extra

options for mcglm object class.

Value

Depending on the number of response variable the function residuals.mcglm returns a vector (univariate models) or a matrix (multivariate models) of residuals values.

Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

RJC NA

Description

Compute the Rotnitzky-Jewell's information criterion for multivariate covariance generalized linear models. WARNINGS: This function is limited to models with ONE response variable.

Usage

```
RJC(object, id, verbose = TRUE)
```

46 summary.mcglm

Arguments

object An object of mcglm class.

id a vector which identifies the clusters. The length and order of id should be

the same as the number of observations. Data are assumed to be sorted so that

observations on a cluster are contiguous rows for all entities in the formula.

verbose Logical.

Value

A matrix. Note that the function assumes that the data are in the correct order.

Author(s)

Wagner Hugo Bonat

summary.mcglm Summarizing Multivariate Covariance Generalized Linear Models

fits.

Description

Summary for McGLMs objects.

Usage

```
## S3 method for class 'mcglm'
summary(object, ...)
```

Arguments

object an object of class mcglm, usually, a result of a call to mcglm.

... additional arguments affecting the summary produced. Note the there is no extra

options for mcglm object class.

Value

Print an mcglm object.

Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

vcov.mcglm 47

VCOV	mcg	l m

Calculate Variance-Covariance matrix for a fitted McGLM object.

Description

Returns the variance-covariance matrix for all parameters of a mcglm fitted model object.

Usage

```
## S3 method for class 'mcglm'
vcov(object, ...)
```

Arguments

object a fitted model mcglm object.

... additional arguments affecting the summary produced. Note that there is no

extra options for mcglm object class.

Value

A variance-covariance matrix.

Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

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