

# Package ‘mcglm’

April 10, 2018

**Type** Package

**Title** Multivariate Covariance Generalized Linear Models

**Version** 0.4.0

**Date** 2018-04-10

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**Description** Fitting multivariate covariance generalized linear models (McGLMs) to data. McGLM is a general framework for non-normal multivariate data analysis, designed to handle multivariate response variables, along with a wide range of temporal and spatial correlation structures defined in terms of a covariance link function combined with a matrix linear predictor involving known matrices. The models take non-normality into account in the conventional way by means of a variance function, and the mean structure is modelled by means of a link function and a linear predictor. The models are fitted using an efficient Newton scoring algorithm based on quasi-likelihood and Pearson estimating functions, using only second-moment assumptions. This provides a unified approach to a wide variety of different types of response variables and covariance structures, including multivariate extensions of repeated measures, time series, longitudinal, spatial and spatio-temporal structures. The package offers a user-friendly interface for fitting McGLMs similar to the `glm()` R function. See Bonat (2018) <doi:10.18637/jss.v084.i04>, for more information and examples.

**Depends** R (>= 3.2.1)

**Suggests** testthat, plyr, lattice, latticeExtra, knitr, rmarkdown,  
MASS, mvtnorm, tweedie, devtools

**Imports** stats, Matrix, assertthat, graphics

**License** GPL-3 | file LICENSE

**LazyData** TRUE

**URL** <https://github.com/wbonat/mcglm>

**BugReports** <https://github.com/wbonat/mcglm/issues>

**Encoding** UTF-8

**VignetteBuilder** knitr

**RoxygenNote** 6.0.1

**NeedsCompilation** no

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ahs	<i>Australian Health Survey</i>
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## Description

The Australian health survey was used by Bonat and Jorgensen (2016) as an example of multivariate count regression model. The data consists of five count response variables concerning health system access measures and nine covariates concerning social conditions in Australian for 1987-88.

- sex - Factor with levels male and female.
- age - Respondent's age in years divided by 100.
- income - Respondent's annual income in Australian dollars divided by 1000.
- levypplus - Coded factor. If respondent is covered by private health insurance fund for private patients in public hospital with doctor of choice (1) or otherwise (0).
- freepoor - Coded factor. If respondent is covered by government because low income, recent immigrant, unemployed (1) or otherwise (0).
- freerepa - Coded factor. If respondent is covered free by government because of old-age or disability pension, or because invalid veteran or family of deceased veteran (1) or otherwise (0).
- illnes - Number of illnesses in past 2 weeks, with 5 or illnesses coded as 5.
- actdays - Number of days of reduced activity in the past two weeks due to illness or injury.
- hscore - Respondent's general health questionnaire score using Goldberg's method. High score indicates poor health.
- chcond - Factor with three levels. If respondent has chronic condition(s) and is limited in activity (limited), or if the respondent has chronic condition(s) but is not limited in activity (nonlimited) or otherwise (otherwise, reference level).
- Ndoc - Number of consultations with a doctor or specialist (response variable).
- Nndoc - Number of consultations with health professionals (response variable).
- Nadm - Number of admissions to a hospital, psychiatric hospital, nursing or convalescence home in the past 12 months (response variable).
- Nhosp - Number of nights in a hospital during the most recent admission.
- Nmed - Total number of prescribed and non prescribed medications used in the past two days.

**Usage**

```
data(ahs)
```

**Format**

a data.frame with 5190 records and 15 variables.

**Source**

Deb, P. and Trivedi, P. K. (1997) Demand for medical care by the elderly: A finite mixture approach. *Journal of Applied Econometrics* 12(3):313–336.

Bonat, W. H. and Jorgensen, B. (2016) Multivariate covariance generalized linear models. *Journal of Royal Statistical Society - Series C* 65:649–675.

**Examples**

```
require(mcglm)
data(ahs, package="mcglm")
form1 <- Ndoc ~ income + age
form2 <- Nndoc ~ income + age
Z0 <- mc_id(ahs)
fit.ahs <- mcglm(linear_pred = c(form1, form2),
                 matrix_pred = list(Z0, Z0), link = c("log", "log"),
                 variance = c("poisson_tweedie", "poisson_tweedie"),
                 data = ahs)
summary(fit.ahs)
```

---

anova.mcglm

*Anova Tables*

---

**Description**

Performs Wald tests of the significance for the linear predictor components by response variables. This function is useful for joint hypothesis tests of regression coefficients associated with categorical covariates with more than two levels. It is not designed for model comparison.

**Usage**

```
## S3 method for class 'mcglm'
anova(object, ...)
```

**Arguments**

object	an object of class mcglm, usually, a result of a call to mcglm() function.
...	additional arguments affecting the summary produced. Note that there is no extra options for mcglm object class.

**Value**

A data.frame with Chi-square statistic to test the null hypothesis of a parameter, or a set of parameters, be zero. Degree of freedom (Df) and p-values. The Wald test based on the observed covariance matrix of the parameters is used.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Examples**

```
x1 <- seq(-1, 1, l = 100)
x2 <- gl(5, 20)
beta <- c(5, 0, -2, -1, 1, 2)
X <- model.matrix(~ x1 + x2)
set.seed(123)
y <- rnorm(100, mean = X%*%beta, sd = 1)
data = data.frame("y" = y, "x1" = x1, "x2" = x2)
fit.anova <- mcglm(c(y ~ x1 + x2), list(mc_id(data)), data = data)
anova(fit.anova)
```

coef.mcglm

*Model Coefficients***Description**

Extract model coefficients for objects of mcglm class.

**Usage**

```
## S3 method for class 'mcglm'
coef(object, std.error = FALSE, response = c(NA,
  1:length(object$beta_names)), type = c("beta", "tau", "power",
  "correlation"), ...)
```

**Arguments**

object	an object of mcglm class.
std.error	logical. If TRUE returns the standard errors for the estimates. Default is FALSE.
response	a numeric vector specifying for which response variable the coefficients should be returned.
type	a string vector (can be 1 element length) specifying which coefficients should be returned. Options are "beta", "tau", "power", "tau" and "correlation".
...	additional arguments affecting the summary produced. Note that there is no extra options for mcglm object class.

**Value**

A `data.frame` with parameters names, estimates, response variable number and parameters type.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

---

confint.mcglm

*Confidence Intervals for Model Parameters*

---

**Description**

Computes confidence intervals for parameters in a fitted `mcglm` model.

**Usage**

```
## S3 method for class 'mcglm'
confint(object, parm, level = 0.95, ...)
```

**Arguments**

<code>object</code>	a fitted <code>mcglm</code> object.
<code>parm</code>	specifies for which parameters are to be given confidence intervals, either a vector of numbers or a vector of strings. If missing, all parameters are considered.
<code>level</code>	the nominal confidence level.
<code>...</code>	additional arguments affecting the confidence interval produced. Note that there is no extra options for <code>mcglm</code> object class.

**Value**

A `data.frame` with confidence intervals, parameters names, response variable number and parameters type.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

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ESS	<i>Generalized Error Sum of Squares</i>
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**Description**

Extract the generalized error sum of squares (ESS) for objects of `mcglm` class.

**Usage**

```
ESS(object, verbose = TRUE)
```

**Arguments**

<code>object</code>	an object or a list of objects representing a model of <code>mcglm</code> class.
<code>verbose</code>	logical. Print or not the ESS value.

**Value**

Returns the value of the generalized error sum of squares (ESS).

**Author(s)**

Wagner Hugo Bonat, <[wbonat@ufpr.br](mailto:wbonat@ufpr.br)>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The `mcglm` Package. *Journal of Statistical Software*, 84(4):1–30.

Wang, M. (2014). Generalized Estimating Equations in Longitudinal Data Analysis: A Review and Recent Developments. *Advances in Statistics*, 1(1)1–13.

**See Also**

`gof`, `plogLik`, `pAIC`, `pKLIC`, `GOSH0` and `RJC`.

---

<code>fitted.mcglm</code>	<i>Fitted Values</i>
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**Description**

Extract fitted values for objects of `mcglm` class.

**Usage**

```
## S3 method for class 'mcglm'  
fitted(object, ...)
```

**Arguments**

object            an object of mcglm class.

...               additional arguments affecting the summary produced. Note that there is no extra options for mcglm object class.

**Value**

A matrix with fitted values.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

---

fit\_mcglm

*Chaser and Reciprocal Likelihood Algorithms*


---

**Description**

This function implements the two main algorithms used for fitting multivariate covariance generalized linear models. The chaser and the reciprocal likelihood algorithms.

**Usage**

```
fit_mcglm(list_initial, list_link, list_variance,
          list_covariance, list_X, list_Z, list_offset,
          list_Ntrial, list_power_fixed, list_sparse,
          y_vec, correct, max_iter, tol, method,
          tuning, verbose)
```

**Arguments**

list\_initial    a list of initial values for regression and covariance parameters.

list\_link       a list specifying the link function names.  
Options are: "logit", "probit", "cauchit", "cloglog", "loglog", "identity",  
"log", "sqrt", "1/mu^2" and "inverse".  
See [mc\\_link\\_function](#) for details. Default link = "identity".

list\_variance   a list specifying the variance function names. Options are: "constant", "tweedie",  
"poisson\_tweedie", "binomialP" and "binomialPQ". See [mc\\_variance\\_function](#)  
for details. Default variance = "constant".

list\_covariance   a list of covariance function names. Options are: "identity", "inverse" and  
"expm". Default covariance = "identity".

list\_X           a list of design matrices. See [model.matrix](#) for details.

list\_Z           a list of known matrices to compose the matrix linear predictor.

list\_offset     a list of offset values. Default NULL.



<code>list_Ntrial</code>	a list of number of trials, useful only when analysing binomial data. Default 1.
<code>list_power_fixed</code>	a list of logicals indicating if the power parameters should be estimated or not. Default <code>power_fixed = TRUE</code> .
<code>list_sparse</code>	a list of logicals indicating if the matrices should be set up as sparse matrices. This argument is useful only when using exponential-matrix covariance link function. In the other cases the algorithm detects automatically if the matrix should be sparse or not.
<code>y_vec</code>	a vector of the stacked response variables.
<code>correct</code>	a logical indicating if the algorithm will use the correction term or not. Default <code>correct = TRUE</code> .
<code>max_iter</code>	maximum number of iterations. Default <code>max_iter = 20</code> .
<code>tol</code>	a numeric specifying the tolerance. Default <code>tol = 1e-04</code> .
<code>method</code>	a string specifying the method used to fit the models ("chaser" or "rc"). Default <code>method = "chaser"</code> .
<code>tuning</code>	a numeric value in general close to zero for the rc method and close to 1 for the chaser method. This argument control the step-length. Default <code>tuning = 1</code> .
<code>verbose</code>	a logical if TRUE print the values of the covariance parameters used on each iteration. Default <code>verbose = FALSE</code>

### Value

A list with estimated regression and covariance parameters. Details about the estimation procedures as iterations, sensitivity, variability are also provided. In general the users do not need to use this function directly. The `mcglm` provides GLM interface for fitting `mcglm`.

### Author(s)

Wagner Hugo Bonat, <[wbonat@ufpr.br](mailto:wbonat@ufpr.br)>

### Source

Bonat, W. H. and Jorgensen, B. (2016) Multivariate covariance generalized linear models. *Journal of Royal Statistical Society - Series C* 65:649–675.

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The `mcglm` Package. *Journal of Statistical Software*, 84(4):1–30.

### See Also

`mcglm`, `mc_matrix_linear_predictor`, `mc_link_function` and `mc_variance_function`.

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gof	<i>Measures of Goodness-of-Fit</i>
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**Description**

Extract the pseudo Gaussian log-likelihood (plogLik), pseudo Akaike Information Criterion (pAIC), pseudo Kullback-Leibler Information Criterion (pKLIC) and pseudo Bayesian Information Criterion (pBIC) for objects of `mcglm` class.

**Usage**

```
gof(object)
```

**Arguments**

`object`                    an object or a list of objects representing a model of `mcglm` class.

**Value**

Returns a data frame containing goodness-of-fit measures.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The `mcglm` Package. *Journal of Statistical Software*, 84(4):1–30.

Wang, M. (2014). Generalized Estimating Equations in Longitudinal Data Analysis: A Review and Recent Developments. *Advances in Statistics*, 1(1)1–13.

**See Also**

plogLik, pAIC, pKLIC and pBIC.

---

GOSHO*Gosho Information Criterion*

---

**Description**

Extract the Gosho Information Criterion (GOSHO) for an object of `mcglm` class. **WARNING:** This function is limited to models with ONE response variable. This function is general useful only for longitudinal data analysis.

**Usage**

```
GOSHO(object, id, verbose = TRUE)
```

**Arguments**

<code>object</code>	an object of <code>mcglm</code> class.
<code>id</code>	a vector which identifies the clusters or groups. The length and order of <code>id</code> should be the same as the number of observations. Data are assumed to be sorted so that observations on a cluster are contiguous rows for all entities in the formula.
<code>verbose</code>	logical. Print or not the GOSHO value.

**Value**

The value of the GOSHO criterion. Note that the function assumes that the data are in the correct order.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Wang, M. (2014). Generalized Estimating Equations in Longitudinal Data Analysis: A Review and Recent Developments. *Advances in Statistics*, 1(1)1–13.

**See Also**

`gof`, `plogLik`, `pAIC`, `pKLIC`, `ESS` and `RJC`.

Hunting

*Hunting in Pico Basile, Bioko Island, Equatorial Guinea.***Description**

Case study analysed in Bonat et. al. (2016) concernings on data of animals hunted in the village of Basile Fang, Bioko Norte Province, Bioko Island, Equatorial Guinea. Monthly number of blue duikers and other small animals shot or snared was collected for a random sample of 52 commercial hunters from August 2010 to September 2013. For each animal caught, the species, sex, method of capture and altitude were documented. The data set has 1216 observations.

- ALT - Factor five levels indicating the Altitude where the animal was caught.
- SEX - Factor two levels Female and Male.
- METHOD - Factor two levels Escopeta and Trampa.
- OT - Monthly number of other small animals hunted.
- BD - Monthly number of blue duikers hunted.
- OFFSET - Monthly number of hunter days.
- HUNTER - Hunter index.
- MONTH - Month index.
- MONTHCALENDAR - Month using calendar numbers (1-January, ..., 12-December).
- YEAR - Year calendar (2010–2013).
- HUNTER.MONTH - Index indicating observations taken at the same HUNTER and MONTH.

**Usage**

```
data(Hunting)
```

**Format**

a `data.frame` with 1216 records and 11 variables.

**Source**

Bonat, et. al. (2017). Modelling the covariance structure in marginal multivariate count models: Hunting in Bioko Island. *Journal of Agricultural Biological and Environmental Statistics*, 22(4):446–464.

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The `mcglm` Package. *Journal of Statistical Software*, 84(4):1–30.

## Examples

```
library(mcglm)
library(Matrix)
data(Hunting, package="mcglm")
formu <- OT ~ METHOD*ALT + SEX + ALT*poly(MONTH, 4)
Z0 <- mc_id(Hunting)
Z1 <- mc_mixed(~0 + HUNTER.MONTH, data = Hunting)
fit <- mcglm(linear_pred = c(formu), matrix_pred = list(c(Z0, Z1)),
             link = c("log"), variance = c("poisson_tweedie"),
             power_fixed = c(FALSE),
             control_algorithm = list(max_iter = 100),
             offset = list(log(Hunting$OFFSET)), data = Hunting)
summary(fit)
anova(fit)
```

mcglm

*Fitting Multivariate Covariance Generalized Linear Models*

## Description

The function `mcglm` is used to fit multivariate covariance generalized linear models. The models are specified by a set of lists giving a symbolic description of the linear and matrix linear predictors. The user can choose between a list of link, variance and covariance functions. The models are fitted using an estimating function approach, combining quasi-score functions for regression parameters and Pearson estimating function for covariance parameters. For details see Bonat and Jorgensen (2016).

## Usage

```
mcglm(linear_pred, matrix_pred, link, variance, covariance,
      offset, Ntrial, power_fixed, data, control_initial,
      contrasts, control_algorithm)
```

## Arguments

<code>linear_pred</code>	a list of formula see <a href="#">formula</a> for details.
<code>matrix_pred</code>	a list of known matrices to be used on the matrix linear predictor. For details see <a href="#">mc_matrix_linear_predictor</a> .
<code>link</code>	a list of link functions names. Options are: "logit", "probit", "cauchit", "cloglog", "loglog", "identity", "log", "sqrt", "1/mu^2" and "inverse". See <a href="#">mc_link_function</a> for details.
<code>variance</code>	a list of variance functions names. Options are: "constant", "tweedie", "poisson_tweedie", "binomialP" and "binomialPQ". See <a href="#">mc_variance_function</a> for details.

covariance	a list of covariance link functions names. Options are: "identity", "inverse" and exponential-matrix "expm".
offset	a list of offset values if any.
Ntrial	a list of number of trials on Bernoulli experiments. It is useful only for binomialP and binomialPQ variance functions.
power_fixed	a list of logicals indicating if the values of the power parameter should be estimated or not.
data	a data frame.
control_initial	a list of initial values for the fitting algorithm. If no values are supplied automatic initial values will be provided by the function <code>mc_initial_values</code> .
contrasts	extra arguments to be passed to <code>model.matrix</code> .
control_algorithm	a list of arguments to be passed for the fitting algorithm. See <code>fit_mcglm</code> for details.

**Value**

`mcglm` returns an object of class 'mcglm'.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. and Jorgensen, B. (2016) Multivariate covariance generalized linear models. *Journal of Royal Statistical Society - Series C* 65:649–675.

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The `mcglm` Package. *Journal of Statistical Software*, 84(4):1–30.

**See Also**

`fit_mcglm`, `mc_link_function` and `mc_variance_function`.

---

`mc_bias_corrected_std` *Bias-corrected Standard Error for Regression Parameters*

---

**Description**

Compute bias-corrected standard error for regression parameters in the context of clustered observations for an object of `mcglm` class. It is also robust and has improved finite sample properties.

**Usage**

```
mc_bias_corrected_std(object, id)
```

**Arguments**

object	an object of mcglm class.
id	a vector which identifies the clusters. The length and order of id should be the same as the number of observations. The data set are assumed to be sorted so that observations on a cluster are contiguous rows for all entities.

**Value**

A variance-covariance matrix. Note that the function assumes that the data are in the correct order.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Nuamah, I. F. and Qu, Y. and Aminu, S. B. (1996). A SAS macro for stepwise correlated binary regression. *Computer Methods and Programs in Biomedicine* 49, 199–210.

**See Also**

mc\_robust\_std.

---

mc\_car

---

*Conditional Autoregressive Model Structure*


---

**Description**

The function mc\_car helps to build the components of the matrix linear predictor used for fitting conditional autoregressive models. This function is used in general for fitting spatial areal data using the well known conditional autoregressive models (CAR). This function depends on a list of neighbors, such a list can be constructed, for example using the tri2nb function from the spdep package based on spatial coordinates. This way to specify the matrix linear predictor can also be applied for spatial continuous data, as an approximation.

**Usage**

```
mc_car(list_neigh, intrinsic = FALSE)
```

**Arguments**

list_neigh	list of neighbors.
intrinsic	logical.

**Value**

A list of a matrix (intrinsic = TRUE) or two matrices (intrinsic = FALSE).

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, 84(4):1–30.

**See Also**

mc\_id, mc\_compute\_rho, mc\_conditional\_test, mc\_dist, mc\_ma, mc\_rw and mc\_mixed.

---

mc_complete_data	<i>Complete Data Set with NA</i>
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---

**Description**

The function `mc_complete_data` completes a data set with NA values for helping to construct the components of the matrix linear predictor in models that require equal number of observations by subjects (`id`).

**Usage**

```
mc_complete_data(data, id, index, id.exp)
```

**Arguments**

<code>data</code>	a data.frame to be completed with NA.
<code>id</code>	name of the column (string) containing the subject id.
<code>index</code>	name of the column (string) containing the index to be completed.
<code>id.exp</code>	how the index is expected to be for all subjects.

**Value**

A data.frame with the same number of observations by subject.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, 84(4):1–30.

**See Also**

mc\_dglm, mc\_ns, mc\_ma and mc\_rw.



---

mc_compute_rho	<i>Autocorrelation Estimates</i>
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---

**Description**

Compute autocorrelation estimates based on a fitted model using the `mc_car` structure. The `mcglm` approach fits models using a linear covariance structure, but in general in this parametrization for spatial models the parameters have no simple interpretation in terms of spatial autocorrelation. The function `mc_compute_rho` computes the autocorrelation based on a fitted model.

**Usage**

```
mc_compute_rho(object, level = 0.975)
```

**Arguments**

<code>object</code>	an object or a list of objects representing a model of <code>mcglm</code> class.
<code>level</code>	the confidence level required.

**Value**

Returns estimate, standard error and confidential interval for the spatial autocorrelation parameter.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The `mcglm` Package. *Journal of Statistical Software*, 84(4):1–30.

**See Also**

`mc_car` and `mc_conditional_test`.

---

mc_conditional_test	<i>Conditional Hypotheses Tests</i>
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---

## Description

Compute conditional hypotheses tests for fitted mcglm model class. When fitting models with extra power parameters, the standard errors associated with the dispersion parameters can be large. In that cases, we suggest to conduct conditional hypotheses test instead of the orthodox marginal test for the dispersion parameters. The function `mc_conditional_test` offers an ease way to conduct such conditional test. Furthermore, the function is quite flexible and can be used for any other conditional hypotheses test.

## Usage

```
mc_conditional_test(object, parameters, test, fixed)
```

## Arguments

<code>object</code>	an object representing a model of mcglm class.
<code>parameters</code>	which parameters will be included in the conditional test.
<code>test</code>	index indicating which parameters will be tested given the values of the other parameters.
<code>fixed</code>	index indicating which parameters should be fixed on the conditional test.

## Value

Returns estimates, conditional standard errors and Z-statistics.

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

## Source

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, 84(4):1–30.

---

`mc_dglm`*Double Generalized Linear Models Structure*

---

**Description**

The function `mc_dglm` builds the components of the matrix linear predictor used for fitting double generalized linear models.

**Usage**

```
mc_dglm(formula, id, data)
```

**Arguments**

<code>formula</code>	a formula spefying the components of the covariance structure.
<code>id</code>	name of the column (string) containing the subject index. (If ts is not repeated measures, use <code>id = 1</code> for all observations).
<code>data</code>	data set.

**Value**

A list of a diagonal matrices, whose values are given by the covariates assumed to describe the covariance structure.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The `mcglm` Package. *Journal of Statistical Software*, 84(4):1–30.

**See Also**

`mc_id`, `mc_dist`, `mc_ma`, `mc_rw`  
and `mc_mixed`.

mc\_dist

*Distance Models Structure***Description**

The function `mc_dist` helps to build the components of the matrix linear predictor using matrices based on distances. This function is generally used for the analysis of longitudinal and spatial data. The idea is to use the inverse of some measure of distance as for example the Euclidean distance to model the covariance structure within response variables. The model can also use the inverse of distance squared or high order power.

**Usage**

```
mc_dist(id, time, data, method = "euclidean")
```

**Arguments**

<code>id</code>	name of the column (string) containing the subject index. For spatial data use the same <code>id</code> for all observations (one unit sample).
<code>time</code>	name of the column (string) containing the index indicating the time. For spatial data use the same index for all observations.
<code>data</code>	data set.
<code>method</code>	distance measure to be used.

**Details**

The distance measure must be one of "euclidean", "maximum", "manhattan", "canberra", "binary" or "minkowski". This function is a customize call of the `dist` function.

**Value**

A matrix of `dgCMatrix` class.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The `mcglm` Package. *Journal of Statistical Software*, 84(4):1–30.

**See Also**

`dist`, `mc_id`, `mc_conditional_test`, `mc_car`, `mc_ma`, `mc_rw` and `mc_mixed`.

**Examples**

```
id <- rep(1:2, each = 4)
time <- rep(1:4, 2)
data <- data.frame("id" = id, "time" = time)
mc_dist(id = "id", time = "time", data = data)
mc_dist(id = "id", time = "time", data = data, method = "canberra")
```

---

mc\_id

*Independent Model Structure*

---

**Description**

Builds an identity matrix to be used as a component of the matrix linear predictor. It is in general the first component of the matrix linear predictor, a kind of intercept matrix.

**Usage**

```
mc_id(data)
```

**Arguments**

data                      the data set to be used.

**Value**

A list of matrix.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, 84(4):1–30.

**See Also**

mc\_dist, mc\_ma, mc\_rw and mc\_mixed.

---

mc_initial_values	<i>Automatic Initial Values</i>
-------------------	---------------------------------

---

## Description

This function provides initial values to be used when fitting multivariate covariance generalized linear models by using the function `mcglm`. In general the users do not need to use this function, since it is already employed when setting the argument `control_initial = "automatic"` in the `mcglm` function. However, if the users want to change some of the initial values, this function can be useful.

## Usage

```
mc_initial_values(linear_pred, matrix_pred, link, variance,
                  covariance, offset, Ntrial, contrasts, data)
```

## Arguments

<code>linear_pred</code>	a list of formula see <a href="#">formula</a> for details.
<code>matrix_pred</code>	a list of known matrices to be used on the matrix linear predictor. See <a href="#">mc_matrix_linear_predictor</a> for details.
<code>link</code>	a list of link functions names, see <a href="#">mcglm</a> for details.
<code>variance</code>	a list of variance functions names, see <a href="#">mcglm</a> for details.
<code>covariance</code>	a list of covariance link functions names, see <a href="#">mcglm</a> for details.
<code>offset</code>	a list of offset values if any.
<code>Ntrial</code>	a list of the number of trials on Bernoulli experiments. It is useful only for "binomialP" and "binomialPQ" variance functions.
<code>contrasts</code>	list of contrasts to be used in the <a href="#">model.matrix</a> .
<code>data</code>	data frame.

## Details

To obtain initial values for multivariate covariance generalized linear models the function `mc_initial_values` fits a generalized linear model (GLM) using the function `glm` with the specified linear predictor and link function for each response variables considering independent observations. The family argument is always specified as `quasi`. The link function depends on the specification of the argument `link`. The variance function is always specified as `"mu"` the only exception appears when using `variance = "constant"` then the family argument in the `glm` function is specified as `quasi(link = link, variance = "constant")`. The estimated value of the dispersion parameter from the `glm` function is used as initial value for the first component of the matrix linear predictor, for all other components the value zero is used.

For the cases `covariance = "inverse"` and `covariance = "expm"` the inverse and the logarithm of the estimated dispersion parameter is used as initial value for the first component of the matrix linear predictor. The value of the power parameter is always started at 1. In the cases of multivariate models the correlation between response variables is always started at 0.

**Value**

Return a list of initial values to be used while fitting in the `mcglm` function.

**Author(s)**

Wagner Hugo Bonat, <[wbonat@ufpr.br](mailto:wbonat@ufpr.br)>

---

mc_link_function	<i>Link Functions</i>
------------------	-----------------------

---

**Description**

The `mc_link_function` is a customized call of the [make.link](#) function.

Given the name of a link function, it returns a list with two elements. The first element is the inverse of the link function applied on the linear predictor  $\mu = g^{-1}(X\beta)$ . The second element is the derivative of  $\mu$  with respect to the regression parameters  $\beta$ . It will be useful when computing the quasi-score function.

**Usage**

```
mc_link_function(beta, X, offset, link)
```

```
mc_logit(beta, X, offset)
```

```
mc_probit(beta, X, offset)
```

```
mc_cauchit(beta, X, offset)
```

```
mc_cloglog(beta, X, offset)
```

```
mc_loglog(beta, X, offset)
```

```
mc_identity(beta, X, offset)
```

```
mc_log(beta, X, offset)
```

```
mc_sqrt(beta, X, offset)
```

```
mc_invmu2(beta, X, offset)
```

```
mc_inverse(beta, X, offset)
```

**Arguments**

`beta` a numeric vector of regression parameters.

`X` a design matrix, see [model.matrix](#) for details.

offset	a numeric vector of offset values. It will be sum up on the linear predictor as a covariate with known regression parameter equals one ( $\mu = g^{-1}(X\beta + offset)$ ). If no offset is present in the model, set offset = NULL.
link	a string specifying the name of the link function. Options are: "logit", "probit", "cauchit", "cloglog", "loglog", "identity", "log", "sqrt", "1/mu^2" and inverse. A user defined link function can be used (see Details).

## Details

The link function is an important component of the multivariate covariance generalized linear models, since it links the expectation of the response variable with the covariates. Let  $\beta$  be a (p x 1) regression parameter vector and  $X$  be an (n x p) design matrix. The expected value of the response variable  $Y$  is given by

$$E(Y) = g^{-1}(X\beta),$$

where  $g$  is the link function and  $\eta = X\beta$  is the linear predictor. Let  $D$  be a (n x p) matrix whose entries are given by the derivatives of  $\mu$  with respect to  $\beta$ . Such a matrix will be required for the fitting algorithm. The function `mc_link_function` returns a list where the first element is  $\mu$  (n x 1) vector and the second is the  $D$  (n x p) matrix. A user defined function can also be used. It must be a function with arguments `beta`, `X` and `offset` (set to NULL if non needed). The function must return a length 2 named list with `mu` and `D` elements as a vector and a matrix of proper dimensions.

## Value

A list with two elements: `mu` and `D` (see Details).

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

## See Also

[model.matrix](#), [make.link](#).

## Examples

```
x1 <- seq(-1, 1, l = 5)
X <- model.matrix(~ x1)
mc_link_function(beta = c(1,0.5), X = X,
                 offset = NULL, link = 'log')
mc_link_function(beta = c(1,0.5), X = X,
                 offset = rep(10,5), link = 'identity')
```



**Description**

The function `mc_ma` helps to build the components of the matrix linear predictor associated with moving average models. This function is generally used for the analysis of longitudinal and times series data. The user can specify the order of the moving average process.

**Usage**

```
mc_ma(id, time, data, order = 1)
```

**Arguments**

<code>id</code>	name of the column (string) containing the subject index. Note that this structure was designed to deal with longitudinal data. For times series data use the same <code>id</code> for all observations (one unit sample).
<code>time</code>	name of the column (string) containing the index indicating the time.
<code>data</code>	data set.
<code>order</code>	order of the moving average process.

**Details**

This function was designed mainly to deal with longitudinal data, but can also be used for times series analysis. In that case, the `id` argument should contain only one index. It pretends a longitudinal data taken just for one individual or unit sample. This function is a simple call of the [bandSparse](#) function from the `Matrix` package.

**Value**

A matrix of `dgCMatrix` class.

**Author(s)**

Wagner Hugo Bonat, <[wbonat@ufpr.br](mailto:wbonat@ufpr.br)>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The `mcglm` Package. *Journal of Statistical Software*, 84(4):1–30.

**See Also**

`mc_id`, `mc_dist`, `mc_car`, `mc_rw` and `mc_mixed`.

**Examples**

```
id <- rep(1:2, each = 4)
time <- rep(1:4, 2)
data <- data.frame("id" = id, "time" = time)
mc_ma(id = "id", time = "time", data = data, order = 1)
mc_ma(id = "id", time = "time", data = data, order = 2)
```

---

mc\_matrix\_linear\_predictor

*Matrix Linear Predictor*


---

**Description**

Compute the matrix linear predictor. It is an internal function, however, since the concept of matrix linear predictor was proposed recently. I decided let this function visible to the interested reader gets some feeling about how it works.

**Usage**

```
mc_matrix_linear_predictor(tau, Z)
```

**Arguments**

tau	a numeric vector of dispersion parameters.
Z	a list of known matrices.

**Details**

Given a list with a set of known matrices  $(Z_0, \dots, Z_D)$  the function `mc_matrix_linear_predictor` returns  $U = \tau_0 Z_0 + \dots + \tau_D Z_D$ .

**Value**

A matrix.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, 84(4):1–30.

Bonat, W. H. and Jorgensen, B. (2016) Multivariate covariance generalized linear models. Journal of Royal Statistical Society - Series C 65:649–675.

**See Also**

mc\_id, mc\_dist, mc\_ma, mc\_rw, mc\_mixed and mc\_car.

**Examples**

```
require(Matrix)
Z0 <- Diagonal(5, 1)
Z1 <- Matrix(rep(1,5)%*%t(rep(1,5)))
Z <- list(Z0, Z1)
mc_matrix_linear_predictor(tau = c(1,0.8), Z = Z)
```

---

mc\_mixed

Mixed Models Structure

---

**Description**

The function `mc_mixed` helps to build the components of the matrix linear predictor associated with mixed models. It is useful to model the covariance structure as a function of known covariates in a linear mixed model fashion (Bonat, et. al. 2016). The `mc_mixed` function was designed to analyse repeated measures and longitudinal data, where in general the observations are taken at a fixed number of groups, subjects or unit samples.

**Usage**

```
mc_mixed(formula, data)
```

**Arguments**

formula	a formula model to build the matrix linear predictor. See details.
data	data set.

**Details**

The formula argument should be specified similar to the linear predictor for the mean structure, however the first component should be 0 and the second component should always indicate the name of the column containing the subject or unit sample index. It should be a factor. The other covariates are specified after a slash "/" in the usual way. For example, `~0 + SUBJECT/(x1 + x2)` means that the column SUBJECT contains the subject or unit sample index, while the covariates that can be continuous or factors are given in the columns x1 and x2. Be careful the parenthesis after the "/" are mandatory, when including more than one covariate. The special case where only the SUBJECT effect is requested the formula takes the form `~ 0 + SUBJECT` without any extra covariate. This structure corresponds to the well known compound symmetry structure. By default the function `mc_mixed` include all interaction terms, the users can ignore the interactions terms removing them from the matrix linear predictor.

**Value**

A list of matrices.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The mcglm Package. *Journal of Statistical Software*, 84(4):1–30.

Bonat, et. al. (2016). Modelling the covariance structure in marginal multivariate count models: Hunting in Bioko Island. *Journal of Agricultural Biological and Environmental Statistics*, 22(4):446–464.

**See Also**

mc\_id, mc\_conditional\_test, mc\_dist, mc\_ma, mc\_rw and mc\_car.

**Examples**

```
SUBJECT <- gl(2, 6)
x1 <- rep(1:6, 2)
x2 <- rep(gl(2,3),2)
data <- data.frame(SUBJECT, x1 , x2)
# Compound symmetry structure
mc_mixed(~0 + SUBJECT, data = data)
# Compound symmetry + random slope for x1 and interaction or correlation
mc_mixed(~0 + SUBJECT/x1, data = data)
# Compound symmetry + random slope for x1 and x2 plus interactions
mc_mixed(~0 + SUBJECT/(x1 + x2), data = data)
```

---

mc\_ns

---

*Non-structure Model Structure*


---

**Description**

The function mc\_non builds the components of the matrix linear predictor used for fitting non-structured covariance matrix. In general this model is hard to fit due to the large number of parameters.

**Usage**

```
mc_ns(id, data, group = NULL, marca = NULL)
```

**Arguments**

id	name of the column (string) containing the subject index. Note this structure was designed to deal with longitudinal data. For times series or spatial data use the same id for all observations (one unit sample).
data	data set.
group	name of the column (string) containing a group specific for which the covariance should change.
marca	level (string) of the column group for which the covariance should change.

**Value**

A list of a  $n*(n-1)/2$  matrices.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, 84(4):1–30.

**See Also**

mc\_id, mc\_dglm, mc\_dist, mc\_ma, mc\_rw  
and mc\_mixed.

---

mc_remove_na	<i>Remove NA from Matrix Linear Predictor</i>
--------------	---

---

**Description**

The function mc\_remove\_na removes NA from each component of the matrix linear predictor. It is in general used after the function mc\_complete\_data.

**Usage**

```
mc_remove_na(matrix_pred, cod)
```

**Arguments**

matrix_pred	a list of known matrices.
cod	index indicating the columns should be removed.

**Value**

A list of matrices.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, 84(4):1–30.

**See Also**

mc\_dglm, mc\_ns, mc\_ma and mc\_rw.

---

mc\_robust\_std

---

*Robust Standard Error for Regression Parameters*


---

**Description**

Compute robust standard error for regression parameters in the context of clustered observations for an object of mcglm class.

**Usage**

```
mc_robust_std(object, id)
```

**Arguments**

object	an object of mcglm class.
id	a vector which identifies the clusters or subject indexes. The length and order of id should be the same as the number of observations. Data are assumed to be sorted so that observations on a cluster are contiguous rows for all entities in the formula.

**Value**

A variance-covariance matrix. Note that the function assumes that the data are in the correct order.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Nuamah, I. F. and Qu, Y. and Aminu, S. B. (1996). A SAS macro for stepwise correlated binary regression. Computer Methods and Programs in Biomedicine 49, 199–210.

**See Also**

mc\_bias\_correct\_std.

## Description

The function `mc_rw` builds the components of the matrix linear predictor associated with random walk models. This function is generally used for the analysis of longitudinal and times series data. The user can specify the order of the random walk process.

## Usage

```
mc_rw(id, time, data, order = 1, proper = FALSE)
```

## Arguments

<code>id</code>	name of the column (string) containing the subject index. Note that this structure was designed to deal with longitudinal data. For times series data use the same <code>id</code> for all observations (one unit sample).
<code>time</code>	name of the column (string) containing the index indicating the time.
<code>data</code>	data set.
<code>order</code>	order of the random walk model.
<code>proper</code>	logical.

## Value

If `proper = FALSE` a matrix of `dgCMatrix` class. If `proper = TRUE` a list with two matrices of `dgCMatrix` class.

## Author(s)

Wagner Hugo Bonat, <[wbonat@ufpr.br](mailto:wbonat@ufpr.br)>

## Source

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The `mcglm` Package. *Journal of Statistical Software*, 84(4):1–30.

## See Also

`mc_id`, `mc_dist`, `mc_car`, `mc_ma`, `mc_mixed` and `mc_compute_rho`.

### Examples

```
id <- rep(1:2, each = 4)
time <- rep(1:4, 2)
data <- data.frame("id" = id, "time" = time)
mc_rw(id = "id", time = "time", data = data, order = 1, proper = FALSE)
mc_rw(id = "id", time = "time", data = data, order = 1, proper = TRUE)
mc_rw(id = "id", time = "time", data = data, order = 2, proper = TRUE)
```

---

mc\_sic

---

*Score Information Criterion - Regression*


---

### Description

Compute the score information criterion (SIC) for an object of `mcglm` class. The SIC is useful for selecting the components of the linear predictor. It can be used to construct an stepwise covariate selection.

### Usage

```
mc_sic(object, scope, data, response, penalty = 2)
```

### Arguments

<code>object</code>	an object of <code>mcglm</code> class.
<code>scope</code>	a vector of covariate names to be tested.
<code>data</code>	data set containing all variables involved in the model.
<code>response</code>	index indicating for which response variable the SIC should be computed.
<code>penalty</code>	penalty term (default = 2).

### Value

A data frame containing SIC values, degree of freedom, Tu-statistics and chi-squared reference values.

### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

### Source

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The `mcglm` Package. *Journal of Statistical Software*, 84(4):1–30.

Bonat, et. al. (2016). Modelling the covariance structure in marginal multivariate count models: Hunting in Bioko Island. *Journal of Agricultural Biological and Environmental Statistics*, 22(4):446–464.



**See Also**

mc\_sic\_covariance.

**Examples**

```
set.seed(123)
x1 <- runif(100, -1, 1)
x2 <- gl(2,50)
beta = c(5, 0, 3)
X <- model.matrix(~ x1 + x2)
y <- rnorm(100, mean = X%%beta , sd = 1)
data <- data.frame(y, x1, x2)
# Reference model
fit0 <- mcglm(c(y ~ 1), list(mc_id(data)), data = data)
# Computing SIC
mc_sic(fit0, scope = c("x1","x2"), data = data, response = 1)
```

---

mc_sic_covariance	<i>Score Information Criterion - Covariance</i>
-------------------	---

---

**Description**

Compute the score information criterion (SIC) for an object of mcglm class. The SIC-covariance is useful for selecting the components of the matrix linear predictor. It can be used to construct an stepwise procedure to select the components of the matrix linear predictor.

**Usage**

```
mc_sic_covariance(object, scope, idx, data, penalty = 2, response)
```

**Arguments**

object	an object of mcglm class.
scope	a list of matrices to be tested.
idx	indicator of matrices belong to the same effect. It is useful for the case where more than one matrix represents the same effect.
data	data set containing all variables involved in the model.
penalty	penalty term (default = 2).
response	index indicating for which response variable SIC-covariance should be computed.

**Value**

A data frame containing SIC-covariance values, degree of freedom, Tu-statistics and chi-squared reference values for each matrix in the scope argument.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, et. al. (2016). Modelling the covariance structure in marginal multivariate count models: Hunting in Bioko Island. *Journal of Agricultural Biological and Environmental Statistics*, 22(4):446–464.

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The mcglm Package. *Journal of Statistical Software*, 84(4):1–30.

**See Also**

mc\_sic.

**Examples**

```
set.seed(123)
SUBJECT <- gl(10, 10)
y <- rnorm(100)
data <- data.frame(y, SUBJECT)
Z0 <- mc_id(data)
Z1 <- mc_mixed(~0+SUBJECT, data = data)
# Reference model
fit0 <- mcglm(c(y ~ 1), list(Z0), data = data)
# Testing the effect of the matrix Z1
mc_sic_covariance(fit0, scope = Z1, idx = 1,
data = data, response = 1)
# As expected Tu < Chisq indicating non-significance of Z1 matrix
```

---

mc\_twin

---

*Twin Models Structure*


---

**Description**

The function `mc_twin` helps to build the components of the matrix linear predictor associated with ACDE models for analysis of twin data.

**Usage**

```
mc_twin(id, twin.id, type, replicate = NULL, structure, data)

mc_twin_bio(id, twin.id, type, replicate = NULL, structure, data)

mc_twin_full(id, twin.id, type, replicate, formula, data)
```

**Arguments**

id	name of the column (string) containing the twin index. It should be the same index (number) for both twins.
twin.id	name of the column (string) containing the twin index inside the pair. In general 1 for the first twin and 2 for the second twin.
type	name of the column (string) containing the indication of the twin as mz or dz. It should be a factor with only two levels mz and dz. Be sure that the reference level is mz.
replicate	name of the column (string) containing the index for more than one observation taken at the same twin pair. It is used for example in twin longitudinal studies. In that case, the replication column should contain the time index.
structure	model type options are full, flex, uns, ACE, ADE, AE, CE and E. See example for details.
data	data set.
formula	internal.

**Value**

A list of matrices of dgCMatrix class.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, 84(4):1–30.

**See Also**

mc\_id, mc\_dist, mc\_car, mc\_rw, mc\_ns, mc\_dglm and mc\_mixed.

**Examples**

```
id <- rep(1:5, each = 4)
id.twin <- rep(1:2, 10)
```

---

mc\_variance\_function    *Variance Functions*


---

## Description

Compute the variance function and its derivatives with respect to regression, dispersion and power parameters.

## Usage

```
mc_variance_function(mu, power, Ntrial, variance, inverse,
                    derivative_power, derivative_mu)
```

```
mc_power(mu, power, inverse, derivative_power, derivative_mu)
```

```
mc_binomialP(mu, power, inverse, Ntrial,
             derivative_power, derivative_mu)
```

```
mc_binomialPQ(mu, power, inverse, Ntrial,
              derivative_power, derivative_mu)
```

## Arguments

mu	a numeric vector. In general the output from <a href="#">mc_link_function</a> .
power	a numeric value (power and binomialP) or a vector (binomialPQ) of the power parameters.
Ntrial	number of trials, useful only when dealing with binomial response variables.
variance	a string specifying the name (power, binomialP or binomialPQ) of the variance function.
inverse	logical. Compute the inverse or not.
derivative_power	logical if compute (TRUE) or not (FALSE) the derivatives with respect to the power parameter.
derivative_mu	logical if compute (TRUE) or not (FALSE) the derivative with respect to the mu parameter.

## Details

The function `mc_variance_function` computes three features related with the variance function. Depending on the logical arguments, the function returns  $V^{1/2}$  and its derivatives with respect to the parameters power and mu, respectively. The output is a named list, completely informative about what the function has been computed. For example, if `inverse = FALSE`, `derivative_power = TRUE` and `derivative_mu = TRUE`. The output will be a list, with three elements: `V_sqrt`, `D_V_sqrt_power` and `D_V_sqrt_mu`.

**Value**

A list with from one to four elements depends on the arguments.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. and Jorgensen, B. (2016) Multivariate covariance generalized linear models. Journal of Royal Statistical Society - Series C X(X):XX–XX.

**See Also**

[mc\\_link\\_function](#).

**Examples**

```
x1 <- seq(-1, 1, l = 5)
X <- model.matrix(~x1)
mu <- mc_link_function(beta = c(1, 0.5), X = X, offset = NULL,
  link = "logit")
mc_variance_function(mu = mu$mu, power = c(2, 1), Ntrial = 1,
  variance = "binomialPQ", inverse = FALSE,
  derivative_power = TRUE, derivative_mu = TRUE)
```

---

NewBorn

*Respiratory Physiotherapy on Premature Newborns.*

---

**Description**

The NewBorn dataset consists of a prospective study to assess the effect of respiratory physiotherapy on the cardiopulmonary function of ventilated preterm newborn infants with birth weight lower than 1500 g. The data set was collected and kindly made available by the nursing team of the Waldemar Monastier hospital, Campo Largo, PR, Brazil. The NewBorn dataset was analysed in Bonat and Jorgensen (2016) as an example of mixed outcomes regression model.

- Sex - Factor two levels Female and Male.
- GA - Gestational age (weeks).
- BW - Birth weight (mm).
- APGAR1M - APGAR index in the first minute of life.
- APGAR5M - APGAR index in the fifth minute of life.
- PRE - Factor, two levels (Premature: YES; NO).
- HD - Factor, two levels (Hansen's disease, YES; NO).
- SUR - Factor, two levels (Surfactant, YES; NO).

- JAU - Factor, two levels (Jaundice, YES; NO).
- PNE - Factor, two levels (Pneumonia, YES; NO).
- PDA - Factor, two levels (Persistence of ductus arteriosus, YES; NO).
- PPI - Factor, two levels (Primary pulmonary infection, YES; NO).
- OTHERS - Factor, two levels (Other diseases, YES; NO).
- DAYS - Age (days).
- AUX - Factor, two levels (Type of respiratory auxiliary, HOOD; OTHERS).
- RR - Respiratory rate (continuous).
- HR - Heart rate (continuous).
- SP02 - Oxygen saturation (bounded).
- TREAT - Factor, three levels (Respiratory physiotherapy, Evaluation 1; Evaluation 2; Evaluation 3).
- NBI - Newborn index.
- TIME - Days of treatment.

### Usage

```
data(NewBorn)
```

### Format

a `data.frame` with 270 records and 21 variables.

### Source

Bonat, W. H. and Jorgensen, B. (2016) Multivariate covariance generalized linear models. *Journal of Royal Statistical Society - Series C* 65:649–675.

### Examples

```
library(mcglm)
library(Matrix)
data(NewBorn, package="mcglm")
formu <- SP02 ~ Sex + APGAR1M + APGAR5M + PRE + HD + SUR
Z0 <- mc_id(NewBorn)
fit <- mcglm(linear_pred = c(formu), matrix_pred = list(Z0),
             link = c("logit"), variance = c("binomialP"),
             power_fixed = c(TRUE),
             data = NewBorn,
             control_algorithm = list(verbose = FALSE, tuning = 0.5))
summary(fit)
```

---

pAIC

*Pseudo Akaike Information Criterion*

---

**Description**

Extract the pseudo Akaike information criterion (pAIC) for objects of mcglm class.

**Usage**

```
pAIC(object, verbose = TRUE)
```

**Arguments**

object            an object or a list of objects representing a model of mcglm class.  
verbose           logical. Print or not the pAIC value.

**Value**

Returns the value of the pseudo Akaike information criterion (pAIC).

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, 84(4):1–30.

**See Also**

gof, plogLik, ESS, pKLIC, GOSH0 and RJC.

---

pBIC

*Pseudo Bayesian Information Criterion*

---

**Description**

Extract the pseudo Bayesian information criterion (pBIC) for objects of mcglm class.

**Usage**

```
pBIC(object, verbose = TRUE)
```

**Arguments**

object            an object or a list of objects representing a model of `mcglm` class.  
 verbose          logical. Print or not the pBIC value.

**Value**

Returns the value of the pseudo Bayesian information criterion (pBIC).

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The `mcglm` Package. *Journal of Statistical Software*, 84(4):1–30.

**See Also**

`gof`, `plogLik`, `ESS`, `pKLIC`, `GOSH0` and `RJC`.

---

pKLIC

*Pseudo Kullback-Leibler Information Criterion*

---

**Description**

Extract the pseudo Kullback-Leibler information criterion (pKLIC) for objects of `mcglm` class.

**Usage**

```
pKLIC(object, verbose = TRUE)
```

**Arguments**

object            an object or a list of objects representing a model of `mcglm` class.  
 verbose          logical. Print or not the pKLIC value.

**Value**

Returns the value of the pseudo Kullback-Leibler information criterion.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>



**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, 84(4):1–30.

**See Also**

gof, plogLik, ESS, pAIC, GOSH0 and RJC.

---

plogLik	<i>Gaussian Pseudo-loglikelihood</i>
---------	--------------------------------------

---

**Description**

Extract the Gaussian pseudo-loglikelihood (plogLik) value for objects of mcglm class.

**Usage**

```
plogLik(object, verbose = TRUE)
```

**Arguments**

object	an object or a list of objects representing a model of mcglm class.
verbose	logical. Print or not the plogLik value.

**Value**

Returns the value of the Gaussian pseudo-loglikelihood.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

---

plot.mcglm	<i>Residuals and algorithm check plots</i>
------------	--

---

**Description**

Residual and algorithm check analysis for objects of mcglm class.

**Usage**

```
## S3 method for class 'mcglm'
plot(x, type = "residuals", ...)
```

**Arguments**

x	a fitted mcglm object.
type	specify which graphical analysis will be performed. Options are: "residuals" and "algorithm".
...	additional arguments affecting the plot produced. Note that there is no extra options for mcglm object class.

**Value**

The function plot.mcglm was designed to offer a fast residuals analysis based on the Pearson residuals. Current version offers a simple Pearson residuals versus fitted values and a quantile plot. When using algorithm = TRUE the function will plot a summary of the fitting algorithm shows the trajectory or iterations of the fitting algorithm. The iterations are shown in terms of values of the model parameters and also the actually value of the quasi-score and Pearson estimating functions. Hence, a quickly check of the algorithm convergence is obtained.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**See Also**

residuals and fitted.

---

print.mcglm

*Print*


---

**Description**

The default print method for an object of mcglm class.

**Usage**

```
## S3 method for class 'mcglm'
print(x, ...)
```

**Arguments**

x	fitted model objects of class mcglm as produced by mcglm().
...	further arguments passed to or from other methods.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**See Also**

summary.

---

residuals.mcglm	<i>Residuals</i>
-----------------	------------------

---

**Description**

Compute residuals for an object of mcglm class.

**Usage**

```
## S3 method for class 'mcglm'
residuals(object, type = "raw", ...)
```

**Arguments**

object	an object of mcglm class.
type	the type of residuals which should be returned. Options are: "raw" (default), "pearson" and "standardized".
...	additional arguments affecting the residuals produced. Note that there is no extra options for mcglm object class.

**Value**

The function residuals.mcglm returns a matrix of residuals values.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**See Also**

fitted.

---

RJC	<i>Rotnitzky-Jewell Information Criterion</i>
-----	---

---

**Description**

Compute the Rotnitzky-Jewell information criterion for an object of mcglm class. **WARNINGS:** This function is limited to models with ONE response variable.

**Usage**

```
RJC(object, id, verbose = TRUE)
```

**Arguments**

object	an object of mcglm class.
id	a vector which identifies the clusters. The length and order of id should be the same as the number of observations. Data are assumed to be sorted so that observations on a cluster are contiguous rows for all entities in the formula.
verbose	logical. Print or not the RJC value.

**Value**

The value of the Rotnitzky-Jewell information criterion. Note that the function assumes that the data are in the correct order.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**Source**

Wang, M. (2014). Generalized Estimating Equations in Longitudinal Data Analysis: A Review and Recent Developments. *Advances in Statistics*, 1(1)1–13.

**See Also**

gof, plogLik, pAIC, pKLIC, ESS and GOSH0.

---

soil

---

*Soil Chemistry Properties Data*


---

**Description**

Soil chemistry properties measured on a regular grid with 10 x 25 points spaced by 5 meters.

- COORD.X - X coordinate.
- COORD.Y - Y coordinate.
- SAND - Sand portion of the sample.
- SILT - Silt portion of the sample.
- CLAY - Clay portion of the sample.
- PHWATER - Soil pH at water.
- CA - Calcium content.
- MG - Magnesium content.
- K - Potassio content.

**Usage**

```
data(soil)
```

**Format**

a data.frame with 250 records and 9 variables.

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, 84(4):1–30.

**Examples**

```
data(soil, package="mcglm")
neigh <- tri2nb(soil[,1:2])
Z1 <- mc_car(neigh)
# Linear predictor
form.ca <- CA ~ COORD.X*COORD.Y + SAND + SILT + CLAY + PHWATER
fit.ca <- mcglm(linear_pred = c(form.ca), matrix_pred = list(Z1),
               link = "log", variance = "tweedie", covariance = "inverse",
               power_fixed = FALSE, data = soil,
               control_algorithm = list(max_iter = 500, tuning = 0.1))
summary(fit.ca)
# Conditional hypothesis test
mc_conditional_test(fit.ca, parameters = c("power11", "tau11", "tau12"),
                   test = 2:3, fixed = 1)
# Spatial autocorrelation
mc_compute_rho(fit.ca)
```

---

soya

*Soybeans*


---

**Description**

Experiment carried out in a vegetation house with soybeans. The experiment has two plants by plot with three levels of the factor amount of water in the soil (water) and five levels of potassium fertilization (pot). The plots were arranged in five blocks (block). Three response variables are of the interest, namely, grain yield, number of seeds and number of viable peas per plant. The data set has 75 observations of 7 variables.

- pot - Factor five levels of potassium fertilization.
- water - Factor three levels of amount of water in the soil.
- block - Factor five levels.
- grain - Continuous - Grain yield per plant.
- seeds - Count - Number of seeds per plant.
- viablepeas - Binomial - Number of viable peas per plant.
- totalpeas - Binomial - Total number of peas per plant.

**Usage**

```
data(soya)
```

**Format**

a data.frame with 75 records and 7 variables.

**Source**

Bonat, W. H. (2018). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, 84(4):1–30.

**Examples**

```
library(mcglm)
library(Matrix)
data(soya, package="mcglm")
formu <- grain ~ block + factor(water) * factor(pot)
Z0 <- mc_id(soya)
fit <- mcglm(linear_pred = c(formu), matrix_pred = list(Z0),
             data = soya)
anova(fit)
```

---

summary.mcglm

*Summarizing*


---

**Description**

The default summary method for an object of mcglm class.

**Usage**

```
## S3 method for class 'mcglm'
summary(object, verbose = TRUE, print = c("Regression",
     "power", "Dispersion", "Correlation"), ...)
```

**Arguments**

object	an object of mcglm class.
verbose	logical. Print or not the model summary.
print	print only part of the model summary, options are Regression, power, Dispersion and Correlation.
...	additional arguments affecting the summary produced. Note the there is no extra options for mcglm object class.

**Value**

Print a mcglm object.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

**See Also**

print.

---

vcov.mcglm

*Variance-Covariance Matrix*

---

**Description**

Returns the variance-covariance matrix for an object of mcglm class.

**Usage**

```
## S3 method for class 'mcglm'  
vcov(object, ...)
```

**Arguments**

object	an object of mcglm class.
...	additional arguments affecting the summary produced. Note that there is no extra options for mcglm object class.

**Value**

A variance-covariance matrix.

**Author(s)**

Wagner Hugo Bonat, <wbonat@ufpr.br>

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