# Package 'mcglm'

June 9, 2016

Type Package

Title Multivariate Covariance Generalized Linear Models

**Version** 0.3.0

Date 2016-06-06

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Description Fitting multivariate covariance generalized linear models (McGLMs) to data. McGLMs is a general framework for non-normal multivariate data analysis, designed to handle multivariate response variables, along with a wide range of temporal and spatial correlation structures defined in terms of a covariance link function combined with a matrix linear predictor involving known matrices.

The models take non-normality into account in the conventional way by means of a variance function, and the mean structure is modelled by means of a link function and a linear predictor.

The models are fitted using an efficient Newton scoring algorithm based on quasi-likelihood and Pearson estimating functions, using only second-moment assumptions. This provides a unified approach to a wide variety of different types of response variables and covariance structures, including multivariate extensions of repeated measures, time series, longitudinal, spatial and spatio-temporal structures. The package offers a user-friendly interface for fitting McGLMs similar to the glm() R function.

**Depends** R (>= 3.2.1)

**Suggests** testthat, plyr, lattice, latticeExtra, knitr, rmarkdown, MASS, mytnorm, tweedie, devtools

**Imports** stats, Matrix, assertthat, graphics

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LazyData TRUE

URL https://github.com/wbonat/mcglm

BugReports https://github.com/wbonat/mcglm/issues
Encoding UTF-8
VignetteBuilder knitr
RoxygenNote 5.0.1
NeedsCompilation no

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ahs

Australian Health Survey

#### **Description**

The Australian health survey was used by Bonat and Jorgensen (2016) as an example of multivariate count regression model. The data consists of five count response variables concerning health system access measures and nine covariates concerning social conditions in Australian for 1987-88.

- sex Factor with levels male and female.
- age Respondent's age in years divided by 100.
- income Respondent's annual income in Australian dollars divided by 1000.
- levyplus Coded factor. If respondent is covered by private health insurance fund for private patients in public hospital with doctor of choice (1) or otherwise (0).
- freepoor Coded factor. If respondent is covered by government because low income, recent immigrant, unemployed (1) or otherwise (0).
- freerepa Coded factor. If respondent is covered free by government because of old-age or disability pension, or because invalid veteran or family of deceased veteran (1) or otherwise (0).
- illnes Number of illnesses in past 2 weeks, with 5 or illnesses coded as 5.
- actdays Number of days of reduced activity in the past two weeks due to illness or injury.
- hscore Respondent's general health questionnaire score using Goldberg's method. High score indicates poor health.
- choond Factor with three levels. If respondent has chronic condition(s) and is limited in activity (limited), or if the respondent has chronic condition(s) but is not limited in activity (nonlimited) or otherwise (otherwise, reference level).
- Ndoc Number of consultations with a doctor or specialist (response variable).
- Nndoc Number of consultations with health professionals (response variable).
- Nadm Number of admissions to a hospital, psychiatric hospital, nursing or convalescence home in the past 12 months (response variable).
- Nhosp Number of nights in a hospital during the most recent admission.
- Nmed Total number of prescribed and non prescribed medications used in the past two days.

## Usage

data(ahs)

#### Format

a data. frame with 5190 records and 15 variables.

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#### **Source**

Deb, P. and Trivedi, P. K. (1997) Demand for medical care by the elderly: A finite mixture approach. Journal of Applied Econometrics 12(3):313–336.

Bonat, W. H. and Jorgensen, B. (2016) Multivariate covariance generalized linear models. Journal of Royal Statistical Society - Series C X(X):XX–XX.

#### **Examples**

anova.mcglm

Anova Tables

## **Description**

Performs Wald tests of the significance for the linear predictor components by response variables. This function is useful for joint hypothesis tests of regression coefficients associated with categorical covariates with more than two levels. It is not designed for model comparison.

#### Usage

```
## S3 method for class 'mcglm'
anova(object, ...)
```

#### **Arguments**

object an object of class mcglm, usually, a result of a call to mcglm() function.

additional arguments affecting the summary produced. Note that there is no extra options for mcglm object class.

#### Value

A data frame with Chi-square statistic to test the null hypothesis of a parameter, or a set of parameters, be zero. Degree of freedom (Df) and p-values. The Wald test based on the observed covariance matrix of the parameters is used.

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

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#### **Examples**

```
x1 <- seq(-1, 1, 1 = 100)
x2 <- gl(5, 20)
beta <- c(5, 0, -2, -1, 1, 2)
X <- model.matrix(~ x1 + x2)
set.seed(123)
y <- rnorm(100, mean = X%*%beta, sd = 1)
data = data.frame("y" = y, "x1" = x1, "x2" = x2)
fit.anova <- mcglm(c(y ~ x1 + x2), list(mc_id(data)), data = data)
anova(fit.anova)</pre>
```

coef.mcglm

Model Coefficients

#### **Description**

Extract model coefficients for objects of mcglm class.

## Usage

```
## S3 method for class 'mcglm'
coef(object, std.error = FALSE, response = c(NA,
    1:length(object$beta_names)), type = c("beta", "tau", "power",
    "correlation"), ...)
```

## Arguments

object an object of mcglm class.

std.error logical. If TRUE returns the standard errors for the estimates. Default is FALSE.

response a numeric vector specifyng for which response variable the coefficients should be returned.

type a string vector (can be 1 element length) specifying which coefficients should be returned.

Options are "beta", "tau", "power", "tau" and "correlation".

additional arguments affecting the summary produced. Note that there is no extra options for mcglm object class.

#### Value

A data. frame with parameters names, estimates, response variable number and parameters type.

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

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cont	1nt	.mcg]	m

Confidence Intervals for Model Parameters

#### Description

Computes confidence intervals for parameters in a fitted mcglm model.

## Usage

```
## S3 method for class 'mcglm'
confint(object, parm, level = 0.95, ...)
```

## Arguments

object a fitted mcglm object.

parm specifies for which parameters are to be given confidence intervals, either a vec-

tor of numbers or a vector of strings. If missing, all parameters are considered.

level the nominal confidence level.

.. additional arguments affecting the confidence interval produced. Note that there

is no extra options for mcglm object class.

#### Value

A data.frame with confidence intervals, parameters names, response variable number and parameters type.

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

**ESS** 

Generalized Error Sum of Squares

## Description

Extract the generalized error sum of squares (ESS) for objects of mcglm class.

#### Usage

```
ESS(object, verbose = TRUE)
```

## Arguments

object an object or a list of objects representing a model of mcglm class.

verbose logical. Print or not the ESS value.

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#### Value

Returns the value of the generalized error sum of squares (ESS).

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### **Source**

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

Wang, M. (2014). Generalized Estimating Equations in Longitudinal Data Analysis: A Review and Recent Developments. Advances in Statistics, 1(1)1–13.

#### See Also

```
gof, plogLik, pAIC, pKLIC, GOSHO and RJC.
```

fitted.mcglm

Fitted Values

## Description

Extract fitted values for objects of mcglm class.

## Usage

```
## S3 method for class 'mcglm'
fitted(object, ...)
```

## **Arguments**

object an object of mcglm class.

additional arguments affecting the summary produced. Note that there is no extra options for mcglm object class.

#### Value

A matrix with fitted values.

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

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fit_mcglm	Chaser and Reciprocal Likelihood Algorithms

## Description

This function implements the two main algorithms used for fitting multivariate covariance generalized linear models. The chaser and the reciprocal likelihood algorithms.

## Usage

a numeric specyfing the tolerance.

## Arguments

tol

_	
list_initial	a list of initial values for regression and covariance parameters.
list_link	a list specifying the link function names.  Options are: "logit", "probit", "cauchit", "cloglog", "loglog", "identity", "log", "sqrt", "1/mu^2" and "inverse".  See mc_link_function for details.
list_variance	a list specifying the variance function names. Options are: "constant", "tweedie", "poisson_tweedie", "binomialP" and "binomialPQ". See mc_variance_function for details.
list_covarianc	e
	a list of covariance function names. Options are: "identity", "inverse" and "expm".
list_X	a list of design matrices. See model.matrix for details.
list_Z	a list of knowm matrices to compose the matrix linear predictor.
list_offset	a list of offset values.
list_Ntrial	a list of number of trials, useful only when analysing binomial data.
list_power_fix	ed
	a list of logicals indicating if the power parameters should be estimated or not.
list_sparse	a list of logicals indicating if the matrices should be set up as sparse matrices. This argument is useful only when using exponential-matrix covariance link function. In the other cases the algorithm detects automatically if the matrix should be sparse or not.
y_vec	a vector of the stacked response variables.
correct	a logical indicating if the algorithm will use the correction term or not.
max_iter	maximum number of iterations.

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method a string specyfing the method used to fit the models ("chaser" or "rc").

tunning a numeric value in general close to zero for the rc method and close to 1 for the

chaser method. This argument control the step-length.

verbose a logical if TRUE print the values of the covariance parameters used on each

iteration.

#### Value

A list with estimated regression and covariance parameters. Details about the estimation procedures as iterations, sensitivity, variability are also provided. In general the users do not need to use this function directly. The mcglm provides GLM interface for fitting mcglm.

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### Source

Bonat, W. H. and Jorgensen, B. (2016) Multivariate covariance generalized linear models. Journal of Royal Statistical Society - Series C X(X):XX–XX.

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

#### See Also

```
mcglm, mc_matrix_linear_predictor, mc_link_function and
mc_variance_function.
```

gof

Measures of Goodness-of-Fit

## **Description**

Extract the pseudo Gaussian log-likelihood (plogLik), pseudo Akaike Information Criterion (pAIC), pseudo Kullback-Leibler Information Criterion (pKLIC) and Error Sum of Squares (ESS) for objects of mcglm class.

## Usage

gof(object)

#### **Arguments**

object

an object or a list of objects representing a model of mcglm class.

#### Value

Returns a data frame containing goodness-of-fit measures.

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#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### Source

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

Wang, M. (2014). Generalized Estimating Equations in Longitudinal Data Analysis: A Review and Recent Developments. Advances in Statistics, 1(1)1–13.

#### See Also

```
plogLik, pAIC, pKLIC, ESS.
```

**GOSHO** 

Gosho Information Criterion

## Description

Extract the Gosho Information Criterion (GOSHO) for an object of mcglm class. WARNING: This function is limited to models with ONE response variable. This function is general useful only for longitudinal data analysis.

## Usage

```
GOSHO(object, id, verbose = TRUE)
```

#### **Arguments**

object an object of mcglm class.

id a vector which identifies the clusters or groups. The length and order of id should

be the same as the number of observations. Data are assumed to be sorted so that observations on a cluster are contiguous rows for all entities in the formula.

verbose logical. Print or not the GOSHO value.

#### Value

The value of the GOSHO criterion. Note that the function assumes that the data are in the correct order.

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### Source

Wang, M. (2014). Generalized Estimating Equations in Longitudinal Data Analysis: A Review and Recent Developments. Advances in Statistics, 1(1)1–13.

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#### See Also

gof, plogLik, pAIC, pKLIC, ESS and RJC.

Hunting

Hunting in Pico Basile, Bioko Island, Equatorial Guinea.

#### **Description**

Case study analysed in Bonat et. al. (2016) concernings on data of animals hunted in the village of Basile Fang, Bioko Norte Province, Bioko Island, Equatorial Guinea. Monthly number of blue duikers and other small animals shot or snared was collected for a random sample of 52 commercial hunters from August 2010 to September 2013. For each animal caught, the species, sex, method of capture and altitude were documented. The data set has 1216 observations.

- ALT Factor five levels indicating the Altitude where the animal was caught.
- SEX Factor two levels Female and Male.
- METHOD Factor two levels Escopeta and Trampa.
- OT Monthly number of other small animals hunted.
- BD Monthly number of blue duikers hunted.
- OFFSET Monthly number of hunter days.
- HUNTER Hunter index.
- MONTH Month index.
- MONTHCALENDAR Month using calendar numbers (1-January, ..., 12-December).
- YEAR Year calendar (2010–2013).
- HUNTER. MONTH Index indicating observations taken at the same HUNTER and MONTH.

## Usage

data(Hunting)

#### **Format**

a data, frame with 1216 records and 11 variables.

#### Source

Bonat, et. al. (2016). Modelling the covariance structure in marginal multivariate count models: Hunting in Bioko Island. Environmetrics, submitted.

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

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#### **Examples**

mcglm

Fitting Multivariate Covariance Generalized Linear Models

#### **Description**

The function mcglm is used to fit multivariate covariance generalized linear models. The models are specified by a set of lists giving a symbolic description of the linear and matrix linear predictors. The user can choose between a list of link, variance and covariance functions. The models are fitted using an estimating function approach, combining quasi-score functions for regression parameters and Pearson estimating function for covariance parameters. For details see Bonat and Jorgensen (2016).

## Usage

## **Arguments**

mc\_bias\_corrected\_std

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covariance a list of covariance link functions names. Options are: "identity", "inverse"

and exponential-matrix "expm".

offset a list of offset values if any.

Ntrial a list of number of trials on Bernoulli experiments. It is useful only for binomialP

and binomialPQ variance functions.

power\_fixed a list of logicals indicating if the values of the power parameter should be esti-

mated or not.

data a data frame.

control\_initial

a list of initial values for the fitting algorithm. If no values are supplied automatic

initial values will be provided by the function mc\_initial\_values.

contrasts extra arguments to passed to model.matrix.

control\_algorithm

a list of arguments to be passed for the fitting algorithm. See fit\_mcglm for

details.

#### Value

mcglm returns an object of class 'mcglm'.

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### Source

Bonat, W. H. and Jorgensen, B. (2016) Multivariate covariance generalized linear models. Journal of Royal Statistical Society - Series C X(X):XX–XX.

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

#### See Also

fit\_mcglm, mc\_link\_function and mc\_variance\_function.

mc\_bias\_corrected\_std Bias-corrected Standard Error for Regression Parameters

#### **Description**

Compute bias-corrected standard error for regression parameters in the context of clustered observations for an object of mcglm class. It is also robust and has improved finite sample properties.

#### Usage

```
mc_bias_corrected_std(object, id)
```

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## Arguments

object an object of mcglm class.

id a vector which identifies the clusters. The length and order of id should be the

same as the number of observations. The data set are assumed to be sorted so

that observations on a cluster are contiguous rows for all entities.

#### Value

A variance-covariance matrix. Note that the function assumes that the data are in the correct order.

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### **Source**

Nuamah, I. F. and Qu, Y. and Aminu, S. B. (1996). A SAS macro for stepwise correlated binary regression. Computer Methods and Programs in Biomedicine 49, 199–210.

#### See Also

 $mc\_robust\_std.$ 

mc\_car

Conditional Autoregressive Model Structure

#### **Description**

The function mc\_car helps to build the components of the matrix linear predictor used for fitting conditional autoregressive models. This function is used in general for fitting spatial areal data using the well known conditional autoregressive models (CAR). This function depends on a list of neighboors, such a list can be constructed, for example using the tri2nb function from the spdep package based on spatial coordinates. This way to specify the matrix linear predictor can also be applied for spatial continuous data, as an approximation.

#### Usage

```
mc_car(list_neigh, intrinsic = FALSE)
```

#### **Arguments**

list\_neigh list of neighboors.

intrinsic logical.

#### Value

A list of a matrix (intrinsic = TRUE) or two matrices (intrinsic = FALSE).

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#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### **Source**

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

#### See Also

```
\mbox{mc\_id}, \mbox{mc\_compute\_rho}, \mbox{mc\_conditional\_test}, \mbox{mc\_dist}, \mbox{mc\_ma}, \mbox{mc\_rw} and \mbox{mc\_mixed}.
```

mc\_compute\_rho

Autocorrelation Estimates

## Description

Compute autocorrelation estimates based on a fitted model using the mc\_car structure. The mcglm approach fits models using a linear covariance structure, but in general in this parametrization for spatial models the parameters have no simple interpretation in terms of spatial autocorrelation. The function mc\_compute\_rho computes the autocorrelation based on a fitted model.

#### Usage

```
mc_compute_rho(object, level = 0.975)
```

#### **Arguments**

object an object or a list of objects representing a model of mcglm class.

level the confidence level required.

## Value

Returns estimate, standard error and confidential interval for the spatial autocorrelation parameter.

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

## Source

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

#### See Also

```
mc_car and mc_conditional_test.
```

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## **Description**

Compute conditional hypotheses tests for fitted mcglm model class. When fitting models with extra power parameters, the standard errors associated with the dispersion parameters can be large. In that cases, we suggest to conduct conditional hypotheses test instead of the orthodox marginal test for the dispersion parameters. The function mc\_conditional\_test offers an ease way to conduct such conditional test. Furthermore, the function is quite flexible and can be used for any other conditional hypotheses test.

## Usage

```
mc_conditional_test(object, parameters, test, fixed)
```

## **Arguments**

object an object representing a model of mcglm class.

parameters which parameters will be included in the conditional test.

test index indicating which parameters will be tested given the values of the other

parameters.

fixed index indicating which parameters should be fixed on the conditional test.

## Value

Returns estimates, conditional standard errors and Z-statistics.

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

## Source

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

mc\_dist

mc_dist	Distance Models Structure	

## Description

The function mc\_dist helps to build the components of the matrix linear predictor using matrices based on distances. This function is generally used for the analysis of longitudinal and spatial data. The idea is to use the inverse of some measure of distance as for example the Euclidean distance to model the covariance structure within response variables. The model can also use the inverse of distance squared or high order power.

## Usage

```
mc_dist(id, time, data, method = "euclidean")
```

## **Arguments**

id	name of the column (string) containing the subject index. For spatial data use the same id for all observations (one unit sample).
time	name of the column (string) containing the index indicating the time. For spatial data use the same index for all observations.
data	data set.
method	distance measure to be used.

#### **Details**

The distance measure must be one of "euclidean", "maximum", "manhattan", "canberra", "binary" or "minkowski". This function is a customize call of the dist function.

#### Value

A matrix of dgCMatrix class.

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### **Source**

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

#### See Also

```
dist, mc_id, mc_conditional_test, mc_car, mc_ma, mc_rw and mc_mixed.
```

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## **Examples**

```
id <- rep(1:2, each = 4)
time <- rep(1:4, 2)
data <- data.frame("id" = id, "time" = time)
mc_dist(id = "id", time = "time", data = data)
mc_dist(id = "id", time = "time", data = data, method = "canberra")</pre>
```

 $mc\_id$ 

Independent Model Structure

## Description

Builds an identity matrix to be used as a component of the matrix linear predictor. It is in general the first component of the matrix linear predictor, a kind of intercept matrix.

## Usage

```
mc_id(data)
```

## **Arguments**

data

the data set to be used.

#### Value

A list of matrix.

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

## Source

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

## See Also

```
mc_dist, mc_ma, mc_rw and mc_mixed.
```

19 mc\_initial\_values

<pre>mc_initial_values</pre>	Automatic Initial Values	

## **Description**

This function provides initial values to be used when fitting multivariate covariance generalized linear models by using the function mcglm. In general the users do not need to use this function, since it is already employed when setting the argument control\_initial = "automatic" in the mcglm function. However, if the users want to change some of the initial values, this function can be useful.

## Usage

```
mc_initial_values(linear_pred, matrix_pred, link, variance,
                  covariance, offset, Ntrial, contrasts, data)
```

#### **Arguments**

a list of formula see formula for details. linear\_pred matrix\_pred

a list of known matrices to be used on the matrix linear predictor.

See mc\_matrix\_linear\_predictor for details.

link a list of link functions names, see mcglm for details.

a list of variance functions names, see mcglm for details. variance

covariance a list of covariance link functions names, see mcglm for details.

offset a list of offset values if any.

a list of the number of trials on Bernoulli experiments. It is useful only for Ntrial

"binomialP" and "binomialPO" variance functions.

list of contrasts to be used in the model.matrix. contrasts

data data frame.

#### **Details**

To obtain initial values for multivariate covariance generalized linear models the function mc\_initial\_values fits a generalized linear model (GLM) using the function glm with the specified linear predictor and link function for each response variables considering independent observations. The family argument is always specified as quasi. The link function depends on the specification of the argument link. The variance function is always specified as "mu" the only excession appears when using variance = "constant" then the family argument in the glm function is specified as quasi(link = link, variance = "constant"). The estimated value of the dispersion parameter from the glm function is used as initial value for the first component of the matrix linear predictor, for all other components the value zero is used.

For the cases covariance = "inverse" and covariance = "expm" the inverse and the logarithm of the estimated dispersion parameter is used as initial value for the first component of the matrix linear predictor. The value of the power parameter is always started at 1. In the cases of multivariate models the correlation between response variables is always started at 0.

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#### Value

Return a list of initial values to be used while fitting in the mcglm function.

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

mc\_link\_function

Link Functions

## **Description**

The mc\_link\_function is a customized call of the make.link function.

Given the name of a link function, it returns a list with two elements. The first element is the inverse of the link function applied on the linear predictor  $\mu = g^{-1}(X\beta)$ . The second element is the derivative of  $\mu$  with respect to the regression parameters  $\beta$ . It will be useful when computing the quasi-score function.

## Usage

```
mc_link_function(beta, X, offset, link)
mc_logit(beta, X, offset)
mc_probit(beta, X, offset)
mc_cauchit(beta, X, offset)
mc_cloglog(beta, X, offset)
mc_loglog(beta, X, offset)
mc_identity(beta, X, offset)
mc_log(beta, X, offset)
mc_log(beta, X, offset)
mc_sqrt(beta, X, offset)
mc_invmu2(beta, X, offset)
mc_inverse(beta, X, offset)
```

## Arguments

```
beta a numeric vector of regression parameters.

X a design matrix, see model.matrix for details.
```

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offset a numeric vector of offset values. It will be sum up on the linear predictor as a covariate with known regression parameter equals one  $(\mu = g^{-1}(X\beta +$ 

of f set)). If no offset is present in the model, set offset = NULL.

link a string specifying the name of the link function. Options are: "logit", "probit",

"cauchit", "cloglog", "loglog", "identity", "log", "sqrt", "1/mu^2"

and inverse. A user defined link function can be used (see Details).

#### **Details**

The link function is an important component of the multivariate covariance generalized linear models, since it links the expectation of the response variable with the covariates. Let  $\beta$  be a (p x 1) regression parameter vector and X be an (n x p) design matrix. The expected value of the response variable Y is given by

$$E(Y) = g^{-1}(X\beta),$$

where g is the link function and  $\eta = X\beta$  is the linear predictor. Let D be a (n x p) matrix whose entries are given by the derivatives of  $\mu$  with respect to  $\beta$ . Such a matrix will be required for the fitting algorithm. The function mc\_link\_function returns a list where the first element is  $\mu$  (n x 1) vector and the second is the D (n x p) matrix. A user defined function can also be used. It must be a function with arguments beta, X and offset (set to NULL if non needed). The function must return a length 2 named list with mu and D elements as a vector and a matrix of proper dimensions.

#### Value

A list with two elements: mu and D (see Details).

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### See Also

```
model.matrix, make.link.
```

## **Examples**

22 mc\_ma

mc_ma	Moving Average Models Structure	

## **Description**

The function mc\_ma helps to build the components of the matrix linear predictor associated with moving average models. This function is generally used for the analysis of longitudinal and times series data. The user can specify the order of the moving average process.

#### Usage

```
mc_ma(id, time, data, order = 1)
```

## Arguments

id	name of the column (string) containing the subject index. Note that this structure was designed to deal with longitudinal data. For times series data use the same id for all observations (one unit sample).
time	name of the column (string) containing the index indicating the time.
data	data set.
order	order of the moving average process.

## **Details**

This function was designed mainly to deal with longitudinal data, but can also be used for times series analysis. In that case, the id argument should contain only one index. It pretends a longitudinal data taken just for one individual or unit sample. This function is a simple call of the bandSparse function from the Matrix package.

#### Value

A matrix of dgCMatrix class.

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### **Source**

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

#### See Also

```
mc_id, mc_dist, mc_car, mc_rw and mc_mixed.
```

#### **Examples**

```
id <- rep(1:2, each = 4)
time <- rep(1:4, 2)
data <- data.frame("id" = id, "time" = time)
mc_ma(id = "id", time = "time", data = data, order = 1)
mc_ma(id = "id", time = "time", data = data, order = 2)</pre>
```

```
mc_matrix_linear_predictor
```

Matrix Linear Predictor

## **Description**

Compute the matrix linear predictor. It is an internal function, however, since the concept of matrix linear predictor was proposed recently. I decided let this function visible to the interested reader gets some feeling about how it works.

#### Usage

```
mc_matrix_linear_predictor(tau, Z)
```

## **Arguments**

tau a numeric vector of dispersion parameters.

Z a list of known matrices.

#### **Details**

```
Given a list with a set of known matrices (Z_0,...,Z_D) the function mc_matrix_linear_predictor returns U=\tau_0Z_0+...+\tau_DZ_D.
```

#### Value

A matrix.

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

## Source

Bonat, W. H. and Jorgensen, B. (2016) Multivariate covariance generalized linear models. Journal of Royal Statistical Society - Series C X(X):XX–XX.

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

24 mc\_mixed

#### See Also

```
mc_id, mc_dist, mc_ma, mc_rw, mc_mixed and mc_car.
```

#### **Examples**

```
require(Matrix)
Z0 <- Diagonal(5, 1)
Z1 <- Matrix(rep(1,5)%*%t(rep(1,5)))
Z <- list(Z0, Z1)
mc_matrix_linear_predictor(tau = c(1,0.8), Z = Z)</pre>
```

mc\_mixed

Mixed Models Structure

#### **Description**

The function mc\_mixed helps to build the components of the matrix linear predictor associated with mixed models. It is useful to model the covariance structure as a function of known covariates in a linear mixed model fashion (Bonat, et. al. 2016). The mc\_mixed function was designed to analyse repeated measures and longitudinal data, where in general the observations are taken at a fixed number of groups, subjects or unit samples.

#### Usage

```
mc_mixed(formula, data)
```

#### **Arguments**

formula a formula model to build the matrix linear predictor. See details.

data data set.

#### Details

The formula argument should be specified similar to the linear predictor for the mean structure, however the first component should be 0 and the second component should always indicate the name of the column containing the subject or unit sample index. It should be a factor. The other covariates are specified after a slash "\" in the usual way. For example,  $\sim 0$  + SUBJECT/(x1 + x2) means that the column SUBJECT contains the subject or unit sample index, while the covariates that can be continuous or factors are given in the columns x1 and x2. Be careful the parenthesis after the "\" are mandatory, when including more than one covariate. The special case where only the SUBJECT effect is requested the formula takes the form  $\sim 0$  + SUBJECT without any extra covariate. This structure corresponds to the well known compound symmetry structure. By default the function mc\_mixed include all interaction terms, the users can ignore the interactions terms removing them from the matrix linear predictor.

#### Value

A list of matrices.

mc\_robust\_std 25

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### Source

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

Bonat, et. al. (2016). Modelling the covariance structure in marginal multivariate count models: Hunting in Bioko Island. Environmetrics, submitted.

#### See Also

```
mc_id, mc_conditional_test, mc_dist, mc_ma, mc_rw and mc_car.
```

#### **Examples**

```
SUBJECT <- gl(2, 6)
x1 <- rep(1:6, 2)
x2 <- rep(gl(2,3),2)
data <- data.frame(SUBJECT, x1 , x2)
# Compound symmetry structure
mc_mixed(~0 + SUBJECT, data = data)
# Compound symmetry + random slope for x1 and interaction or correlation
mc_mixed(~0 + SUBJECT/x1, data = data)
# Compound symmetry + random slope for x1 and x2 plus interactions
mc_mixed(~0 + SUBJECT/(x1 + x2), data = data)
```

 $mc\_robust\_std$ 

Robust Standard Error for Regression Parameters

#### **Description**

Compute robust standard error for regression parameters in the context of clustered observations for an object of mcglm class.

## Usage

```
mc_robust_std(object, id)
```

#### **Arguments**

object

an object of mcglm class.

id

a vector which identifies the clusters or subject indexes. The length and order of id should be the same as the number of observations. Data are assumed to be sorted so that observations on a cluster are contiguous rows for all entities in the formula.

26 mc\_rw

#### Value

A variance-covariance matrix. Note that the function assumes that the data are in the correct order.

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

### Source

Nuamah, I. F. and Qu, Y. and Aminu, S. B. (1996). A SAS macro for stepwise correlated binary regression. Computer Methods and Programs in Biomedicine 49, 199–210.

#### See Also

```
mc_bias_correct_std.
```

mc	P L
mc	rw

Random Walk Models Structure

## **Description**

The function mc\_rw builds the components of the matrix linear predictor associated with random walk models. This function is generaly used for the analysis of longitudinal and times series data. The user can specify the order of the random walk process.

#### Usage

```
mc_rw(id, time, data, order = 1, proper = FALSE)
```

## **Arguments**

id	name of the column (string) containing the subject index. Note that this structure was designed to deal with longitudinal data. For times series data use the same id for all observations (one unit sample).
time	name of the column (string) containing the index indicating the time.

data data set.

order order of the random walk model.

proper logical.

#### Value

If proper = FALSE a matrix of dgCMatrix class. If proper = TRUE a list with two matrices of dgCMatrix class.

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

mc\_sic 27

#### Source

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

#### See Also

```
mc_id, mc_dist, mc_car, mc_ma, mc_mixed and mc_compute_rho.
```

## **Examples**

```
id <- rep(1:2, each = 4)
time <- rep(1:4, 2)
data <- data.frame("id" = id, "time" = time)
mc_rw(id = "id", time = "time", data = data, order = 1, proper = FALSE)
mc_rw(id = "id", time = "time", data = data, order = 1, proper = TRUE)
mc_rw(id = "id", time = "time", data = data, order = 2, proper = TRUE)</pre>
```

mc\_sic

Score Information Criterion - Regression

## **Description**

Compute the score information criterion (SIC) for an object of mcglm class. The SIC is useful for selecting the components of the linear predictor. It can be used to construct an stepwise covariate selection.

#### Usage

```
mc_sic(object, scope, data, response, penalty = 2)
```

## **Arguments**

object an object of mcglm class.

scope a vector of covariate names to be tested.

data data set containing all variables involved in the model.

response index indicating for which response variable the SIC should be computed.

penalty penalty term (default = 2).

## Value

A data frame containing SIC values, degree of freedom, Tu-statistics and chi-squared reference values.

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

28 mc\_sic\_covariance

#### **Source**

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

Bonat, et. al. (2016). Modelling the covariance structure in marginal multivariate count models: Hunting in Bioko Island. Environmetrics, submitted.

#### See Also

mc\_sic\_covariance.

## **Examples**

```
set.seed(123)
x1 <- runif(100, -1, 1)
x2 <- gl(2,50)
beta = c(5, 0, 3)
X <- model.matrix(~ x1 + x2)
y <- rnorm(100, mean = X%*%beta , sd = 1)
data <- data.frame(y, x1, x2)
# Reference model
fit0 <- mcglm(c(y ~ 1), list(mc_id(data)), data = data)
# Computing SIC
mc_sic(fit0, scope = c("x1","x2"), data = data, response = 1)</pre>
```

mc\_sic\_covariance

Score Information Criterion - Covariance

#### **Description**

Compute the score information criterion (SIC) for an object of mcglm class. The SIC-covariance is useful for selecting the components of the matrix linear predictor. It can be used to construct an stepwise procedure to select the components of the matrix linear predictor.

## Usage

```
mc_sic_covariance(object, scope, idx, data, penalty = 2, response)
```

## **Arguments**

object	an object of mcglm class.
scope	a list of matrices to be tested.
idx	indicator of matrices belong to the same effect. It is useful for the case where more than one matrix represents the same effect.
data	data set containing all variables involved in the model.
penalty	penalty term (default = $2$ ).
response	index indicating for which response variable SIC-covariance should be computed.

mc\_variance\_function 29

#### Value

A data frame containing SIC-covariance values, degree of freedom, Tu-statistics and chi-squared reference values for each matrix in the scope argument.

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### Source

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

Bonat, et. al. (2016). Modelling the covariance structure in marginal multivariate count models: Hunting in Bioko Island. Environmetrics, submitted.

#### See Also

mc\_sic.

## **Examples**

```
set.seed(123)
SUBJECT <- gl(10, 10)
y <- rnorm(100)
data <- data.frame(y, SUBJECT)
Z0 <- mc_id(data)
Z1 <- mc_mixed(~0+SUBJECT, data = data)
# Reference model
fit0 <- mcglm(c(y ~ 1), list(Z0), data = data)
# Testing the effect of the matrix Z1
mc_sic_covariance(fit0, scope = Z1, idx = 1,
data = data, response = 1)
# As expected Tu < Chisq indicating non-significance of Z1 matrix</pre>
```

mc\_variance\_function Variance Functions

## **Description**

Compute the variance function and its derivatives with respect to regression, dispersion and power parameters.

30 mc\_variance\_function

#### Usage

#### **Arguments**

mu a numeric vector. In general the output from mc\_link\_function.

power a numeric value (power and binomialP) or a vector (binomialPQ) of the power

parameters.

Ntrial number of trials, useful only when dealing with binomial response variables.

variance a string specifying the name (power, binomialP or binomialPQ) of the vari-

ance function.

inverse logical. Compute the inverse or not.

derivative\_power

logical if compute (TRUE) or not (FALSE) the derivatives with respect to the

power parameter.

derivative\_mu logical if compute (TRUE) or not (FALSE) the derivative with respect to the mu

parameter.

#### **Details**

The function mc\_variance\_function computes three features related with the variance function. Depending on the logical arguments, the function returns  $V^{1/2}$  and its derivatives with respect to the parameters power and mu, respectivelly. The output is a named list, completely informative about what the function has been computed. For example, if inverse = FALSE, derivative\_power = TRUE and derivative\_mu = TRUE. The output will be a list, with three elements:  $V_{sqrt}, D_{v_{sqrt}}$  power and  $D_{v_{sqrt}}$ .

## Value

A list with from one to four elements depends on the arguments.

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### Source

Bonat, W. H. and Jorgensen, B. (2016) Multivariate covariance generalized linear models. Journal of Royal Statistical Society - Series C X(X):XX–XX.

NewBorn 31

#### See Also

```
mc_link_function.
```

## Examples

NewBorn

Respiratory Physiotherapy on Premature Newborns.

## Description

The NewBorn dataset consists of a prospective study to assess the effect of respiratory physiotherapy on the cardiopulmonary function of ventilated preterm newborn infants with birth weight lower than 1500 g. The data set was collected and kindly made available by the nursing team of the Waldemar Monastier hospital, Campo Largo, PR, Brazil. The NewBorn dataset was analysed in Bonat and Jorgensen (2016) as an example of mixed outcomes regression model.

- Sex Factor two levels Female and Male.
- GA Gestational age (weeks).
- BW Birth weight (mm).
- APGAR1M APGAR index in the first minute of life.
- APGAR5M APGAR index in the fifth minute of life.
- PRE Factor, two levels (Premature: YES; NO).
- HD Factor, two levels (Hansen's disease, YES; NO).
- SUR Factor, two levels (Surfactant, YES; NO).
- JAU Factor, two levels (Jaundice, YES; NO).
- PNE Factor, two levels (Pneumonia, YES; NO).
- PDA Factor, two levels (Persistence of ductus arteriosus, YES; NO).
- PPI Factor, two levels (Primary pulmonary infection, YES; NO).
- OTHERS Factor, two levels (Other diseases, YES; NO).
- DAYS Age (days).
- AUX Factor, two levels (Type of respiratory auxiliary, HOOD; OTHERS).
- RR Respiratory rate (continuous).
- HR Heart rate (continuous).

pAIC pAIC

- SP02 Oxygen saturation (bounded).
- TREAT Factor, three levels (Respiratory physiotherapy, Evaluation 1; Evaluation 2; Evaluation 3).
- NBI Newborn index.
- TIME Days of treatment.

## Usage

```
data(NewBorn)
```

#### **Format**

a data. frame with 270 records and 21 variables.

#### **Source**

Bonat, W. H. and Jorgensen, B. (2016) Multivariate covariance generalized linear models. Journal of Royal Statistical Society - Series C X(X):XX–XX.

## **Examples**

pAIC

Pseudo Akaike Information Criterion

## Description

Extract the pseudo Akaike information criterion (pAIC) for objects of mcglm class.

#### Usage

```
pAIC(object, verbose = TRUE)
```

## Arguments

object an object or a list of objects representing a model of mcglm class.

verbose logical. Print or not the pAIC value.

pKLIC 33

#### Value

Returns the value of the pseudo Akaike information criterion (pAIC).

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### Source

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

#### See Also

```
gof, plogLik, ESS, pKLIC, GOSHO and RJC.
```

pKLIC

Pseudo Kullback-Leibler Information Criterion

## **Description**

Extract the pseudo Kullback-Leibler information criterion (pKLIC) for objects of mcglm class.

#### Usage

```
pKLIC(object, verbose = TRUE)
```

## **Arguments**

object an object or a list of objects representing a model of mcglm class.

verbose logical. Print or not the pKLIC value.

#### Value

Returns the value of the pseudo Kullback-Leibler information criterion.

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### **Source**

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

## See Also

```
gof, plogLik, ESS, pAIC, GOSHO and RJC.
```

34 plot.mcglm

plogLik

Gaussian Pseudo-loglikelihood

## **Description**

Extract the Gaussian pseudo-loglikelihood (plogLik) value for objects of mcglm class.

## Usage

```
plogLik(object, verbose = TRUE)
```

## Arguments

object an object or a list of objects representing a model of mcglm class.

verbose logical. Print or not the plogLik value.

#### Value

Returns the value of the Gaussian pseudo-loglikelihood.

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

plot.mcglm

Residuals and algorithm check plots

## Description

Residual and algorithm check analysis for objects of mcglm class.

#### Usage

```
## S3 method for class 'mcglm'
plot(x, type = "residuals", ...)
```

#### **Arguments**

x a fitted mcglm object.

type specify which graphical analysis will be performed. Options are: "residuals"

and "algorithm".

... additional arguments affecting the plot produced. Note that there is no extra

options for mcglm object class.

print.mcglm 35

## Value

The function plot.mcglm was designed to offer a fast residuals analysis based on the Pearson residuals. Current version offers a simple Pearson residuals versus fitted values and a quantile plot. When using algorithm = TRUE the function will plot a summary of the fitting algorithm shows the trajectory or iterations of the fitting algorithm. The iterations are shown in terms of values of the model parameters and also the actually value of the quasi-score and Pearson estimating functions. Hence, a quickly check of the algorithm convergence is obtained.

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### See Also

residuals and fitted.

print.mcglm

Print

## Description

The default print method for an object of mcglm class.

## Usage

```
## S3 method for class 'mcglm'
print(x, ...)
```

## **Arguments**

x fitted model objects of class mcglm as produced by mcglm().

... further arguments passed to or from other methods.

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

## See Also

summary.

36 RJC

residuals.mcglm

Residuals

## Description

Compute residuals for an object of mcglm class.

#### Usage

```
## S3 method for class 'mcglm'
residuals(object, type = "raw", ...)
```

## Arguments

object an object of mcglm class.

type the type of residuals which should be returned. Options are: "raw" (default),

"pearson" and "standardized".

... additional arguments affecting the residuals produced. Note that there is no extra

options for mcglm object class.

#### Value

The function residuals.mcglm returns a matrix of residuals values.

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

## See Also

fitted.

RJC

Rotnitzky-Jewell Information Criterion

## **Description**

Compute the Rotnitzky-Jewell information criterion for an object of mcglm class. WARNINGS: This function is limited to models with ONE response variable.

## Usage

```
RJC(object, id, verbose = TRUE)
```

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#### **Arguments**

object an object of mcglm class.

id a vector which identifies the clusters. The length and order of id should be

the same as the number of observations. Data are assumed to be sorted so that observations on a cluster are contiguous rows for all entities in the formula.

verbose logical. Print or not the RJC value.

#### Value

The value of the Rotnitzky-Jewell information criterion. Note that the function assumes that the data are in the correct order.

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### **Source**

Wang, M. (2014). Generalized Estimating Equations in Longitudinal Data Analysis: A Review and Recent Developments. Advances in Statistics, 1(1)1–13.

#### See Also

gof, plogLik, pAIC, pKLIC, ESS and GOSHO.

soil

Soil Chemistry Properties Data

## **Description**

Soil chemistry properties measured on a regular grid with 10 x 25 points spaced by 5 meters.

- COORD. X X coordinate.
- COORD.Y Y coordinate.
- SAND Sand portion of the sample.
- SILT Silt portion of the sample.
- CLAY Clay portion of the sample.
- PHWATER Soil pH at water.
- CA Calcium content.
- MG Magnesium content.
- K Potassio content.

#### Usage

data(soil)

38 soya

#### **Format**

a data. frame with 250 records and 9 variables.

#### Source

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

## **Examples**

soya

Soybeans

## Description

Experiment carried out in a vegetation house with soybeans. The experiment has two plants by plot with three levels of the factor amount of water in the soil (water) and five levels of potassium fertilization (pot). The plots were arranged in five blocks (block). Three response variables are of the interest, namely, grain yield, number of seeds and number of viable peas per plant. The data set has 75 observations of 7 variables.

- pot Factor five levels of potassium fertilization.
- water Factor three levels of amount of water in the soil.
- block Factor five levels.
- grain Continuous Grain yield per plant.
- seeds Count Number of seeds per plant.
- viablepeas Binomial Number of viable peas per plant.
- totalpeas Binomial Total number of peas per plant.

summary.mcglm 39

#### Usage

```
data(soya)
```

#### **Format**

a data. frame with 75 records and 7 variables.

#### **Source**

Bonat, W. H. (2016). Multiple Response Variables Regression Models in R: The mcglm Package. Journal of Statistical Software, submitted.

## **Examples**

summary.mcglm

Summarizing

## **Description**

The default summary method for an object of mcglm class.

#### Usage

```
## S3 method for class 'mcglm'
summary(object, verbose = TRUE, print = c("Regression",
   "power", "Dispersion", "Correlation"), ...)
```

## Arguments

object an object of mcglm class.

verbose logical. Print or not the model summary.

print print only part of the model summary, options are Regression, power, Dispersion

and Correlation.

.. additional arguments affecting the summary produced. Note the there is no extra

options for mcglm object class.

#### Value

Print a mcglm object.

40 vcov.mcglm

#### Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

#### See Also

print.

vcov.mcglm

Variance-Covariance Matrix

## Description

Returns the variance-covariance matrix for an object of mcglm class.

## Usage

```
## S3 method for class 'mcglm'
vcov(object, ...)
```

## Arguments

object an object of mcglm class.

... additional arguments affecting the summary produced. Note that there is no

extra options for mcglm object class.

#### Value

A variance-covariance matrix.

## Author(s)

Wagner Hugo Bonat, <wbonat@ufpr.br>

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