Assignment 3

November 29, 2019

This set of assingments will teach you the differences between various fairness measures. Note that this is not a programming assingment.

Assume we have a Binary classifier to promote employees in an organization. The following table presents the Confusion Matrix for female and male employees:

Female	Actual positive	Actual negative
Predicted positve	30	70
Predicted negative	20	105

Male	Actual positive	Actual negative
Predicted positve	100	15
Predicted negative	90	20

- 1- Calculate the overall accuracy of the promotion classifier.
- 2- Calculate the accuracy of the promotion system for female and male employees.
- 3- Evaluate the pormotion system based on three fairness measures: Demographic parity, Equialized odds, and Equiality of opportunity.
- 4- Is this promotion model fair? if not, suggest an approach to make it fair. Justify your answer.

Answer

Please note that I expressed all probability calculations in up to 4 decimal places. The exact values shall be the fraction.

1. Overall Accuracy

$$\frac{\sum_{G} TP + TN}{\sum_{G} TP + FP + TN + FN} = \frac{30 + 105 + 100 + 20}{30 + 70 + 105 + 20 + 100 + 15 + 20 + 90} = \frac{255}{450} = 0.5667$$

2. Accuracies

Female:

$$\frac{TP + TN}{TP + FP + TN + FN} = \frac{30 + 105}{30 + 70 + 105 + 20} = \frac{135}{225} = 0.6$$

Male:

$$\frac{TP + TN}{TP + FP + TN + FN} = \frac{100 + 20}{100 + 15 + 20 + 90} = \frac{135}{225} = 0.5333$$

Female have a higher prediction accuracy than male

3.

Demographic Parity:

Female:

$$P(d=1|G=f) = \frac{30+70}{30+70+105+20} = \frac{100}{225} = 0.4444$$

Male:

$$P(d=1|G=m) = \frac{100+15}{100+15+20+90} = \frac{115}{225} = 0.5111$$

Male's is predicted positive is higher than female's

Equalized Odds:

Female:

$$P(d = 1|Y = 0, G = f) = \frac{70}{70 + 105} = \frac{70}{175} = 0.4$$

$$P(d = 1|Y = 1, G = f) = \frac{30}{30 + 20} = \frac{30}{50} = 0.6$$

Male:

$$P(d = 1|Y = 0, G = m) = \frac{15}{15 + 20} = \frac{15}{35} = 0.4286$$

$$P(d = 1|Y = 1, G = m) = \frac{100}{100 + 90} = \frac{100}{190} = 0.5263$$

When given it's actually negative, male's predicted positive is higher, so that's as if male were given false presumptions; when given it's actually positive, female's predicted positive is higher.

Equality of Opportunity:

Female:

$$P(d = 0|Y = 1, G = f) = \frac{20}{30 + 20} = \frac{20}{50} = 0.4$$
$$P(d = 1|Y = 1, G = f) = \frac{30}{20 + 30} = \frac{30}{50} = 0.6$$

Male:

$$P(d = 0|Y = 1, G = m) = \frac{90}{100 + 90} = \frac{90}{190} = 0.4737$$
$$P(d = 1|Y = 1, G = m) = \frac{100}{100 + 90} = \frac{100}{190} = 0.5263$$

When it's actually positive, we see male's predicted negative is higher, and female's predicted positive is higher.

4. Answer

In a general sense this system is not 100% fair, justified sufficiently by evaluation metrics we calculated above, as none of the metrics provide equal results as it should have been. Although there is no significant one-sided preference/bias towards one gender, male could get more favoured pre-judgement from, for instance, equalized odds.

We can improvise on a system level. One approach could be adding fairness constraints and to make it easy to solve for, making it a regularization parameter. For the problem concerned, when minimizing the loss function, we shall do so such that it's subjected to a certain metric, say demographic parity. Define a small constant (say smaller than 0.01), θ , and have

$$\theta > = |P(d = 1|G = f) - P(d = 1|G = m)|$$

And minimize the new, regularized loss function:

$$f_{\theta}(x, y; \theta) + \lambda \times \theta$$

And we can impose other regularization terms accordingly using the same technique, and in a way such that we achieve balance between being reasonably easy to solve the problem and ensure all the metrics are represented

Natural Language Processing

This set of assignments will give you experience with a text corpus, Python programming, part-of-speech (PoS) tags, sentiment analysis, and machine learning with scikit-learn.

This assignment shows how you can perform sentiment analysis on reviews using Python and <u>Natural Language Toolkit (NLTK) (https://www.nltk.org/)</u>.

Sentiment Analysis means analyzing the sentiment of a given text or document and categorizing the text/document into a specific class or category (like positive and negative). In other words, building a sentiment analysis model classifies any particular text or document as positive or negative. In the simplest form, the classification is done for two classes: positive and negative. However, we can add more classes like neutral, highly positive, highly negative, etc.

Sentiment analysis is an important topic in computational linguistics in which we quantify subjective aspects of language. These aspects can range from biases in social media for marketing, to a spectrum of cognitive behaviours for disease diagnosis.

In this assignment, you learn about labeling data, extracting features, training classifier, and testing the accuracy of the classifier.

For this assignment, we use a reviews dataset as our labeled data which is collected from Yelp, Amazon, and IMDB. We attempted to select sentences that have a clearly positive or negative connotaton, the goal was for no neutral sentences to be selected. The review corpus contains reviews with sentiment polarity classification, where score is either 1 (for positive) or 0 (for negative). You can find the assignment data on the website (https://github.com/ift6758/jitf6758.github.io/blob/master/assignments/assignment 3(data).zip).

a) (Data processing): First create a list of all reviews and their categories. You can create a list of tuples where the first item is the review and the second item is the sentiment, i.e., '0' or '1'.

```
train_path = './assignment_3(data)/reviews/train.txt'
test_path = './assignment_3(data)/reviews/test.txt'
# create a list of all reviews and their categories
def createlist(path):
    with open(path, 'r') as fp:
        data = fp.read()
    data = data.split('\n')
    ret = []
    for i,review label in enumerate(data):
        if len(review_label)==0:
            print(i+1,':Blank line')
            continue
        label = int(review label[-1])
        review = ' '.join(review_label[:-1].split(' ')).replace('\t',
'')
        ret.append((review, label),)
    return ret
train original = createlist(train path)
test_original = createlist(test path)
```

669 :Blank line 1418 :Blank line 225 :Blank line

b) (Tokenization): Extract all the words from the reviews. You can either use the string *split()* method directly or use the following method from NLTK.

Calculate the number of occurence of each word in the entire corpus and report the 10 most common tokens. You can use the following method from NLTK.

```
In [0]: from nltk.probability import FreqDist
         fdist = FreqDist()
         # Count the number of words
        for review,_ in train_token+test_token:
             for word in review:
                 fdist[word.lower()] += 1
         print('the 10 most common tokens:')
         for token,n in fdist.most_common(10):
             print(token,'\t',n)
        the 10 most common tokens:
        the
                  1941
        and
                  1134
                  1027
        i
                  886
        a
        it
                  784
                  760
        is
                  667
        to
        this
                  642
                  622
        of
```

c) (Stop words removal): Remove all the stop words from the reviews and re-calculate the number of occurence of each word in the entire corpus.

594

was

```
In [0]: from nltk.corpus import stopwords
        stopwords english = stopwords.words('english')
        # Extract all the words from the reviews(Not included stopwords)
        def extract_words_remove_stop_words(original):
             ret = []
            for review, label in original:
                 tokens = []
                 for token in word_tokenize(review):
                     if token.lower() not in stopwords english:
                         tokens.append(token.lower())
                 ret.append((tokens,label),)
             return ret
        train_token_remove_stopwords = extract_words_remove_stop_words(train_
        original)
        test token remove stopwords = extract words remove stop words(test or
        iginal)
        fdist = FreqDist()
        # Count the number of words
        for tokens,_ in train_token_remove_stopwords+test_token_remove_stopwo
        rds:
            for token in tokens:
                 fdist[token] += 1
        print('the 10 most common tokens:')
        for token,n in fdist.most common(10):
            print(token,'\t',n)
        the 10 most common tokens:
```

```
2639
          1306
          503
          276
n't
's
          244
          225
good
          209
great
          180
movie
phone
          165
          159
film
```

d) (Stemmization): Normalize the reviews by stemming and re-calculate the number of occurence of each word in the entire corpus. You can use the following function from NLTK.

```
In [0]: from nltk.stem import SnowballStemmer
        stemmer spanish = SnowballStemmer('english')
        # Extract all the words from the reviews and stemmization
        def extract_words_remove_stop_words(original):
            ret = []
            for review,label in original:
                 tokens = []
                 for token in word_tokenize(review):
                     if token.lower() not in stopwords english:
                         tokens.append(stemmer_spanish.stem(token.lower()))
                 ret.append((tokens,label),)
             return ret
        train_stemmization = extract_words_remove_stop_words(train_original)
        test stemmization = extract words remove stop words(test original)
        fdist = FreqDist()
        for tokens,_ in train_stemmization+test_stemmization:
            for token in tokens:
                 fdist[token] += 1
        print('the 10 most common tokens:')
        for token,n in fdist.most_common(10):
            print(token,'\t',n)
        the 10 most common tokens:
                 2639
                 1306
                 503
        n't
                 276
        ' S
                 244
                 225
```

e) (BOW): Create 1-hot encoding and represent each review as Bag of Words (BOW).

good

movi film

great

phone

210

210

186

174

```
In [0]:
        # Build vocabulary and generate vectors
        bow = \{\}
        index = 0
        for word in fdist:
            bow[word] = index
            bow[index] = word
            index+=1
        print('number of words:',index)
        # get one-hot
        def get one hot(stemization):
             ret = []
             for review, label in stemization:
                 one hot = [0]*(len(bow)//2)
                 for token in review:
                     one hot[bow[token]]+=1
                 ret.append((one hot,label),)
             return ret
        train one hot = get one hot(train stemmization)
        test one hot = get one hot(test stemmization)
```

number of words: 4140

f) (Train a Classifier): Use reviews in the train folder as "train-set" and use reviews in the test folder as "test-set". Use Naive Bayes Classifer to train your sentiment predictor. You can use the following code for this purpose.

```
In [0]: from nltk import NaiveBayesClassifier,classify
        import collections
        # create unigram dataset
        def getset(stemmization):
            ret = []
            for tokens,label in stemmization:
                 features = collections.defaultdict(int)
                 for feature in tokens:
                     features[feature] += 1
                 ret.append((features, label),)
            return ret
        train unigram set = getset(train stemmization)
        test_unigram_set = getset(test_stemmization)
        classifier = NaiveBayesClassifier.train(train unigram set)
        accuracy = classify.accuracy(classifier, test_unigram_set)
        print(accuracy)
```

g) (N-gram): There are different n-grams like unigram, bigram, trigram, etc. For example, Bigram = Item having two words, such as, very good. BOW and unigram representation as the same.

Extract Bigram features from the reviews and re-train the model with Naive Bayes classifier on the train-set and report accuracy on the test-set. You can use the following method from NLTK to extract bigrams.

```
In [0]:
        from nltk.util import ngrams
        import collections
        fdisk bigram = FreqDist()
        # create bigram dataset
        def get bigram set(stemmization):
            ret = []
            for tokens,label in stemmization:
                 features = collections.defaultdict(int)
                 for feature in ngrams(tokens,2):
                     features[feature[0]+' '+feature[1]] += 1
                     fdisk bigram[feature[0]+' '+feature[1]] += 1
                 ret.append((features, label),)
            return ret
        train bigram set = get bigram set(train stemmization)
        test_bigram_set = get_bigram_set(test_stemmization)
        classifier = NaiveBayesClassifier.train(train bigram set)
        accuracy = classify.accuracy(classifier, test bigram set)
        print(accuracy)
```

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h) (Combined features): Represent each review based on the combination of 2000 most frequent unigram and bi-grams. Re-train the Naive Bayes Classifier and report the accuracy.

```
most frequent unigram = set(map(lambda x:x[0],fdist.most common(2000))
In [0]:
        )))
        most frequent bigram = set(map(lambda x:x[0],fdisk bigram.most common
        (2000)))
        # Combined features from unigram and bigram
        def get combined(uni grams, bi grams):
            ret = []
            for f1,f2 in zip(uni_grams,bi_grams):
                 featuredict = collections.defaultdict(int)
                 for feature in f1[0]:
                     if feature in most_frequent_unigram:
                         featuredict[feature] += 1
                 for feature in f2[0]:
                     if feature in most frequent bigram:
                         featuredict[feature] += 1
                 ret.append((featuredict,f1[1]),)
            return ret
        train com = get combined(train unigram set,train bigram set)
        test_com = get_combined(test_unigram_set,test_bigram_set)
        classifier = NaiveBayesClassifier.train(train com)
        accuracy = classify.accuracy(classifier, test_com)
        print(accuracy)
```

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Dense representation with SVD

i) Generate a co-occurance matrix with window size = 2. Represent each revew with a dense vector extracted from SVD where dimention = 300. Re-train the model and report the accuracy on the test-set.

```
In [0]:
        import numpy as np
        import pandas as pd
        def get co occurrence(stemmization, window size):
            d = collections.defaultdict(int)
            vocab = set()
            for tokens,_ in stemmization:
                 for i in range(len(tokens)):
                     token = tokens[i]
                     vocab.add(token)
                     next_token = tokens[i+1 : i+1+window_size]
                     for t in next token:
                         key = tuple(sorted([t, token]))
                         d[key] += 1
            vocab = sorted(vocab)
            df = pd.DataFrame(data=np.zeros((len(vocab), len(vocab))),index=v
        ocab,columns=vocab)
            for key, value in d.items():
                 df.at[key[0], key[1]] = value
                 df.at[key[1], key[0]] = value
            return df
        df = get co occurrence(train stemmization+test stemmization,2)
In [0]: | from numpy.linalg import svd
        X = df.to numpy()
        u, s, vh = np.linalg.svd(X, full_matrices=True)
        vh
        svd model = \{\}
        for i,word in enumerate(df.index):
             svd model[word] = vh[i,:300]
In [0]: data = []
        for one_hot,_ in (train_one_hot+test_one_hot):
            data.append(one hot)
        data = np.array(data).T
        u, s ,vh = np.linalg.svd(data, full matrices=True)
In [0]:
        data = vh.T[:,:300]
        def get set(data, one hot):
             ret = []
            for features,o in zip(data,one_hot):
                 featuresdict = {}
                 for i,feature in enumerate(features):
                     featuresdict['feature'+str(i)] = feature
                 label = o[1]
                 ret.append((featuresdict, label),)
            return ret
        train set = get set(data[:len(train one hot)],train one hot)
        test set = get set(data[len(train one hot):],test one hot)
```

Word Embeddings

Download pretrained word embeddings from Google News dataset. The model includes embeddings for 3 million words and phrases. Words with frequency below 5 were discarded. Download the model from the link below: https://code.google.com/archive/p/word2vec/ (https://code.google.com/archive/ (https://code.google.com/archive/ (https://code.google.com/archive/ (https://code.google.com/archive/ (https://code.google.com/archive/ (https://code.google.com/archive/ (<a href="ht

You can load the model using gensim:

- j) Represent the 5 most positive informative words with word2vec (dimention = 300) and SVD.
- k) Represent the 5 most negative informative words with word2vec (dimention = 300) and SVD.

You can use the following code to determine which features are most effective in sentiment analysis.

In [0]: classifier.show_most_informative_features(20)
positive excel, perfect, great, hippy, love
negative bad, terribl, worst, money, aw

Most Informati	ve Features excel = 1	1 : 0		34.3
: 1.0			=	
: 1.0	bad = 1	0 : 1	=	21.5
: 1.0	terribl = 1	0 : 1	=	20.6
	worst = 1	0 : 1	=	20.6
: 1.0	perfect = 1	1 : 0	=	19.4
: 1.0	great = 1	1 : 0	=	18.6
1.0	money = 1	0 : 1	=	17.3
: 1.0	·			
1.0	happi = 1	1 : 0	=	16.0
: 1.0	love = 1	1 : 0	=	16.0
: 1.0	aw = 1	0 : 1	=	13.4
	work great = 1	1 : 0	=	13.2
: 1.0	fine = 1	1 : 0	=	13.2
: 1.0	great . = 1	1 : 0	=	12.6
: 1.0	nice = 1	1 : 0	=	12.1
1.0				
: 1.0	start = 1	0 : 1	=	11.5
: 1.0	famili = 1	1 : 0	=	11.2
: 1.0	bore = 1	0 : 1	=	9.5
	comfort = 1	1 : 0	=	8.8
: 1.0	amaz = 1	1 : 0	=	8.6
: 1.0	write = 1	0 : 1	_	8.2
: 1.0	-	- -		- -

Answer

positive: excel, perfect, great, hippy, love

negative: bad, terribl, worst, money, aw

```
In [0]: # positive excel, perfect, great, happi, love
    positive_words = ['excel', 'perfect', 'great', 'happi', 'love']
    for word in positive_words:
        print('word2vec: ',word)
        print(model[word])
        print('SVD: ' + word)
        print(svd_model[word])
```

```
word2vec: excel
                  1.02050781e-01 -1.83593750e-01 -5.44433594e-02
[-1.86523438e-01
  6.93359375e-02
                  9.66796875e-02
                                 1.79687500e-01
                                                 2.18200684e-03
 -2.32421875e-01
                  1.58691406e-02
                                 1.26953125e-01 -4.15802002e-04
  1.20605469e-01
                  3.95507812e-02 -3.14941406e-02
                                                 1.57226562e-01
 -5.46875000e-02
                  3.53515625e-01 9.13085938e-02 -1.02539062e-01
 -2.84423828e-02
                  3.02734375e-02 -1.08886719e-01
                                                 1.71875000e-01
  7.22656250e-02 -1.66015625e-01
                                 5.07812500e-02 -2.91015625e-01
 -7.91015625e-02 -4.80957031e-02
                                 4.02832031e-02 1.25122070e-02
  1.27929688e-01 -3.07617188e-02
                                 1.72851562e-01
                                                 1.04492188e-01
  5.98144531e-02
                  3.85742188e-02
                                 9.42382812e-02 -5.07812500e-02
  4.37500000e-01
                  2.33398438e-01 -4.61425781e-02
                                                 1.69921875e-01
 -1.31835938e-01
                  6.20117188e-02 -2.98828125e-01 -1.30859375e-01
                  1.53320312e-01 -2.07031250e-01 6.34765625e-02
 -1.31835938e-01
 -4.63867188e-02 -6.39648438e-02 -5.98144531e-02 -1.66992188e-01
  2.16796875e-01 -2.45117188e-01 -1.07910156e-01 -9.76562500e-02
 -5.17578125e-02 -8.00781250e-02 -1.63085938e-01 -1.22070312e-01
 -2.55126953e-02
                 2.80761719e-02 -8.93554688e-02 5.54199219e-02
                  3.47656250e-01 -9.03320312e-03 -1.84570312e-01
  2.80761719e-02
  1.75781250e-01
                  5.83496094e-02 -1.36718750e-01 -3.12500000e-01
 -1.49414062e-01 -1.24023438e-01 8.25195312e-02 9.52148438e-03
 -9.52148438e-02
                 2.44140625e-01 -5.56640625e-02
                                                 1.96289062e-01
  1.58203125e-01
                  1.23046875e-01 5.44433594e-02
                                                 1.31835938e-01
  2.84423828e-02
                  2.94189453e-02
                                 4.76074219e-02 -2.16796875e-01
  1.90429688e-02 -2.53906250e-01
                                 3.39843750e-01
                                                 1.91497803e-03
                 3.80859375e-01
  4.78515625e-01
                                 1.06811523e-02 -2.22656250e-01
 -3.86718750e-01 -6.71386719e-03
                                 3.61328125e-02
                                                 3.75976562e-02
 -2.69531250e-01 -1.40625000e-01 -2.30468750e-01 -5.67626953e-03
  3.32031250e-01
                 4.39453125e-03 -9.37500000e-02
                                                  8.25195312e-02
 -2.85156250e-01
                 1.12792969e-01 2.83203125e-01
                                                 2.67333984e-02
  2.24609375e-02 -3.90625000e-01
                                 7.86132812e-02 -2.04101562e-01
 -1.69921875e-01 -1.11816406e-01
                                 1.26953125e-01
                                                 1.82617188e-01
 -2.85644531e-02 -2.37304688e-01 -3.63769531e-02 -4.66308594e-02
 -2.12890625e-01 3.06640625e-01 -8.88671875e-02
                                                 4.88281250e-02
  5.15136719e-02 -1.08398438e-01 2.48046875e-01
                                                  7.95898438e-02
  2.09960938e-01 -5.05371094e-02 -2.00195312e-01
                                                 1.12304688e-01
 -1.54296875e-01 -3.26171875e-01
                                 5.15136719e-02 -1.34765625e-01
 -2.24609375e-01 -1.04980469e-01
                                 1.99218750e-01
                                                  2.29492188e-02
  1.12792969e-01 -1.53320312e-01
                                 7.17773438e-02
                                                 3.75000000e-01
 -1.43554688e-01 2.08007812e-01 -4.47265625e-01 2.34375000e-01
                                 3.66210938e-02 -2.51953125e-01
 -1.93786621e-03 -1.92382812e-01
  9.86328125e-02 6.73828125e-02 -1.54296875e-01 -1.00097656e-01
                                 9.66796875e-02 -1.52343750e-01
  1.13769531e-01 -1.20117188e-01
 -1.99218750e-01 -1.44042969e-02 -2.59765625e-01 -1.88476562e-01
 -1.03027344e-01 -1.93359375e-01 3.61328125e-02 2.55859375e-01
  1.72851562e-01 - 2.73437500e-01 - 1.10351562e-01 - 1.56250000e-01
 -2.22656250e-01 -1.26953125e-01 -2.30712891e-02 -5.54199219e-02
 -2.83203125e-01 -2.63671875e-02 4.49218750e-02 -5.39550781e-02
 -9.13085938e-02 -5.66406250e-02 1.65039062e-01 -3.32031250e-02
  6.34765625e-02 -1.25976562e-01
                                 9.66796875e-02 -5.71289062e-02
  3.39843750e-01 -2.05078125e-01 -1.57226562e-01 -8.20312500e-02
 -8.20312500e-02 -5.20019531e-02 -2.52685547e-02 -1.98242188e-01
 -1.96289062e-01 -3.04687500e-01 4.57763672e-03 -2.85156250e-01
  8.10546875e-02 -1.40380859e-02 1.38671875e-01 1.73339844e-02
 -1.88476562e-01 -1.42822266e-02 -2.11914062e-01 -1.05468750e-01
  2.43164062e-01 -6.03027344e-02 -1.86523438e-01 -3.59375000e-01
 -2.81250000e-01 -1.85546875e-01 -1.30859375e-01 1.11816406e-01
```

```
3.95507812e-02
                  2.71484375e-01
                                  1.29882812e-01 -7.47070312e-02
 -1.31835938e-01
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```

```
In [0]: # negative bad, terribl, worst, money, aw
negative_words = ['bad', 'terribl', 'worst', 'money', 'aw']
for word in positive_words:
    print('word2vec: ',word)
    print(model[word])
    print('SVD: ' + word)
    print(svd_model[word])
```

```
word2vec: excel
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  6.93359375e-02
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             0.07421875 - 0.14746094 - 0.08642578  0.16113281 - 0.07128
 -0.2109375
906
  0.109375
             0.17675781
                         0.18554688 -0.15820312 -0.2265625
                                                             0.15039
062
 -0.08544922 0.09130859 -0.03198242 0.13476562 -0.15136719 -0.42773
438
 -0.03442383 -0.27929688
                         0.125
                                    -0.19824219 -0.12304688
                                                             0.06494
1411
SVD: love
[ 1.34480893e-03
                 5.83306532e-03
                                 2.30172537e-03
                                                 1.19278924e-03
  1.44154856e-03
                 5.61566487e-03 -1.05948719e-03
                                                 2.17648721e-02
  3.12789532e-04
                 2.30293158e-03
                                 1.85801735e-03 -2.42070560e-03
  7.90212033e-03 -1.49276382e-02
                                 2.44326608e-03 -5.30343879e-03
                 4.24725036e-03
                                 4.09080512e-03 -7.42327343e-03
 -1.81488578e-04
  5.22325965e-03
                 2.09243834e-02
                                2.81938944e-02 -2.24417185e-04
                 1.43038210e-02 -2.42987661e-03
 -9.93457093e-04
                                                 4.88476552e-03
  1.10331428e-02 -4.89373660e-02 -9.55302891e-03
                                                 1.00897642e-02
 -2.75989077e-02 3.69453479e-03 -4.97324715e-03 -3.25497188e-03
  2.46833629e-02
                 2.28991584e-02
                                 2.06448982e-02
                                                 4.45552966e-03
 -6.46621173e-03
                 9.44919151e-03 -4.09205675e-03 -3.83368425e-03
 9.71304360e-03 -7.23742678e-03 -5.51650693e-04 -5.43831355e-03
  1.62593387e-02 -8.39301863e-03 -2.06820207e-02
                                                 2.07954663e-03
 -5.87554449e-03
                 1.47323242e-02 -1.55779063e-02
                                                 3.33641222e-02
  8.32499468e-03 -1.81958029e-02 -7.48928754e-03
                                                 2.10946583e-02
  2.46612153e-04 -9.45632343e-03
                                 1.26745353e-02
                                                 9.73411866e-03
 9.17434153e-03 -2.61894524e-02 -1.49905434e-02 -1.93238619e-02
 -2.97484695e-03
                 3.60527629e-03
                                 4.41474553e-04 -8.64804976e-03
 -8.53692289e-03
                 5.07192792e-03 -1.66286058e-03
                                                 9.49601723e-03
  3.13856980e-03 -5.34776330e-03
                                 4.42137781e-03
                                                 1.21159573e-02
 -2.66931888e-03 -1.48004445e-03 -3.83612497e-03 -9.86412735e-03
                                 1.46051898e-03 -6.01270742e-03
 -1.34188857e-02
                 2.46768728e-02
 -1.88771723e-02
                 2.80091610e-02
                                 4.03919241e-03 -8.53530971e-03
 -1.62172657e-03
                 7.03108578e-03
                                 4.92119775e-02 -9.14361804e-03
 -3.87088600e-04 -1.41811576e-02 -6.57888831e-03
                                                 9.75226975e-03
  5.77258514e-04 -2.42277340e-02 -4.38698101e-04 -3.56178664e-02
 -2.95084868e-03
                 1.11860788e-03
                                 1.19592632e-02 -6.02899320e-04
                                 6.39948262e-03 -7.47945415e-04
  6.50620265e-03 -1.28262853e-02
  2.92960897e-02
                 3.00364921e-03
                                 9.60578485e-03 -6.56662580e-03
  1.72430568e-02 -1.06022388e-02 -2.48892436e-02
                                                 2.13897949e-02
                 2.07712381e-04 -2.07496670e-02
  1.41483301e-03
                                                 7.65549207e-04
```

```
2.07093040e-02
                8.48321693e-03 -2.71536073e-02
                                                 4.03150665e-05
-3.71512412e-03 -1.37458820e-03
                                 1.30095087e-02
                                                 3.62385495e-03
-8.08740258e-03 -1.13704562e-03
                                 3.13990131e-03 -1.42539412e-02
-3.08997201e-04 -2.18703502e-03 -4.03167240e-03 -2.08646422e-02
2.43404852e-02 -5.61416898e-04
                                3.98425182e-03 -4.18902145e-03
5.59369698e-03
                2.05349518e-03 -1.07065529e-02
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                 5.73019322e-02 -7.86731919e-03 -1.10177151e-04
-5.94289083e-03
5.74805684e-03 -7.94853309e-03 -5.36130889e-04 -5.83296393e-03
1.36980133e-02
                8.00228704e-03 -3.13296510e-03 -2.35720293e-02
4.85731138e-02
                                2.05024267e-02 -8.03062427e-03
                5.00315203e-03
2.05484342e-02
                8.99377258e-04 -1.84215865e-02 -2.39200788e-02
-1.52580319e-02
                 3.31355381e-02
                                 2.18732875e-03
                                                 1.82750822e-02
2.01773067e-02 -1.08664170e-02
                                 2.71564459e-03
                                                 2.56135303e-02
3.05266252e-03 -9.87369390e-03
                                 1.43638874e-03
                                                 2.56913237e-03
7.08723883e-03 -2.49616039e-03
                                 1.37893269e-02
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-6.81607561e-04
                9.40258997e-03
                                 4.71735926e-03 -2.38361388e-03
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                                 8.51229624e-04
                                                 1.04594889e-02
7.08567073e-03 -9.69170948e-04 -8.91047002e-03 -9.30386333e-04
-5.18904058e-03 -1.37150278e-02
                                 1.35726319e-02 -1.12198341e-01
-9.41719643e-04 -1.45748881e-02
                                 3.10666076e-02
                                                 1.48988298e-02
-3.33994151e-03
                 5.36431260e-03
                                 2.64428383e-02
                                                 2.06228241e-03
6.47501274e-02
                 6.91454109e-03
                                 1.48658985e-02
                                                -1.28479739e-03
-3.47360505e-03
                 1.44134819e-02
                                 9.92363128e-02
                                                 1.08017430e-02
9.29799298e-03 -4.29142764e-04 -7.02232749e-03
                                                 1.18147987e-02
-1.78663465e-03
                9.01868467e-04
                                 1.19627372e-02
                                                 2.51272561e-02
-5.95973687e-05
                 4.09543454e-03 -5.87458091e-03 -5.08602047e-03
-3.71917958e-03
                 6.86404083e-03 -1.28272001e-02
                                                 6.62272944e-03
-3.65449183e-02
                 7.02743507e-03
                                 1.43041263e-02
                                                 5.95245070e-03
                1.45907131e-04
                                 1.25160101e-03 -1.73368945e-02
2.54347939e-03
1.92365751e-03 -2.54671651e-04
                                 3.01744412e-03
                                                 5.26365210e-03
                                 9.20549389e-04 -5.52915037e-03
-1.16151940e-03 -1.49004894e-02
1.43478576e-03 -3.18397947e-02 -1.33651161e-03
                                                 7.42157131e-03
1.43893107e-02 -8.97047001e-04
                                 5.17946440e-04
                                                 3.10734926e-02
-3.90056473e-03 -3.85243679e-03 -3.87202345e-02
                                                 1.67213072e-02
 1.21556588e-02
                3.97906025e-02
                                7.16375318e-04 -1.13245799e-02
-2.79293554e-04
                 5.08270448e-03 -1.80641092e-03 -1.00952026e-02
2.75617391e-02 -5.95187289e-03
                                 4.04165429e-03
                                                 8.09786638e-03
-3.68580932e-03
                5.14082116e-03
                                 7.04208365e-03
                                                 3.89430260e-03
-7.23938968e-03 -1.38129099e-02
                                 4.88102697e-03 -2.96114451e-03
-1.33727227e-02 -3.64038455e-03 -5.84665148e-03
                                                 2.15449030e-03
-1.38086324e-02
                1.24782494e-02 -3.48533631e-03
                                                 2.24454107e-02
-9.30412585e-03 -1.94824225e-02
                                2.24997534e-02
                                                 3.84908508e-05
 1.02826903e-03 -6.86625986e-03 -4.74564224e-02
                                                 9.78703702e-03
-5.83331581e-03 -8.26898665e-03 3.62650777e-03 -1.63410606e-02]
```

- I) Calculate the dot product between the most frequent positive word and the most frequent negative word represented with SVD and word2Vec. Compare the results.
- m) Can one use word2vec for sentiment analysis on the review dataset? Justify your answer.

```
In [0]: # 'excel', 'bad'
    print((svd_model['excel']*svd_model['bad']).sum())
    print((model['excel']*model['bad']).sum())
    0.003902033146915265
    0.67587197
```

Answer

- I) Dot product: SVD: 0.003902033146915265 word2vec: 0.67587197
- m) Theoretically, we could take a mean of words to get embeddings for a sentence and conduct the analysis. So this is feasible. But, in practice, sentiment information in word2vec represent only the relationship between words, and could be lacking of emotional information, which might pose some limitations.

Computer Vision

This assignment will give you experience with an image corpus. For most of the questions in this assingment, you need to write a python script.

1- *Read image*: Write a python code to read the image. You can find the image of this assingment on the webpage (https://github.com/ift6758/ift6758.github.io/blob/master/assignments/assignment 3(data).zip).

Answer

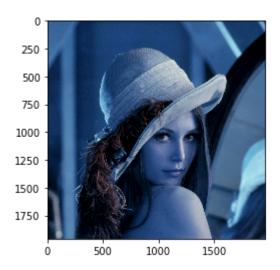
```
In [3]: import cv2
import matplotlib.pyplot as plt
import numpy as np

#write a function to read an image
img = cv2.imread('lena.jpg', -1)

# This line is just a proof that I've read the image
print("This is the BGR version of the image, for the RGB version, ple
ase refer to part 3: \n")
plt.imshow(img)
```

This is the BGR version of the image, for the RGB version, please ref er to part 3:

Out[3]: <matplotlib.image.AxesImage at 0x7f298d827ac8>



2- *Pre-processing*: data augmentation: Write a python code to resize the image and make it 20% smaller, and save the image as greyscale image.

Answer

Here I interpreted this as having the image's 2D area to be 80% of that of the original image. So the width and height shall shrink accordingly. That means either of them will shrink to sqrt(0.8) of the original.

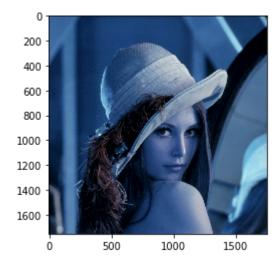
Of course, we could alternatively shrink both width and height by 20% respectively, and that way the area of image would be 64% of the original.

```
In [4]: # re-size an image
    scale = 0.8 # of original size area
    # shrink the sides accordingly and define new dimension
    width = int(img.shape[1] * (scale ** 0.5))
    height = int(img.shape[0] * (scale ** 0.5))
    dim = (width, height)
    # resizing
    img_resized = cv2.resize(img, dim, interpolation = cv2.INTER_AREA) #
    resized image

# This line is just a proof that I've resized the image
    print("Here is the resized BGR image: \n")
    plt.imshow(img_resized)
```

Here is the resized BGR image:

Out[4]: <matplotlib.image.AxesImage at 0x7f298b2f1470>

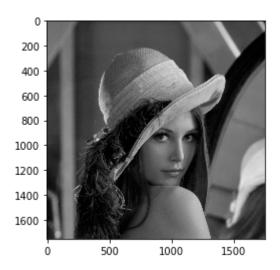


```
In [5]: # save the processed image in grayscale
   img_resized_gray = cv2.cvtColor(img_resized, cv2.COLOR_BGR2GRAY)

# This line is just a proof that I've converted the resized image
   print("Here is the resized BGR image in gray scale: \n")
   plt.imshow(img_resized_gray,cmap='gray')
```

Here is the resized BGR image in gray scale:

Out[5]: <matplotlib.image.AxesImage at 0x7f298b2d2978>



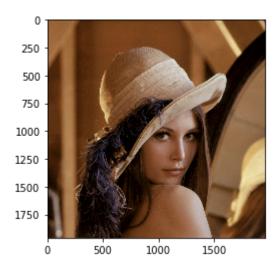
3- *Filter*: Write a python code that load the image in RGB and generate three images where in each one the colors of one channel is inversed. Show the generated images.

```
In [6]: # load image in RGB
    img_rgb = cv2.cvtColor(cv2.imread('lena.jpg', -1) , cv2.COLOR_BGR2RGB
)

# This line is just a proof that I've load the image in RGB format
    print("This is the RGB version of the image: \n")
    plt.imshow(img_rgb)
```

This is the RGB version of the image:

Out[6]: <matplotlib.image.AxesImage at 0x7f298b23a0b8>



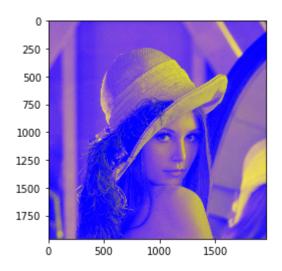
```
In [0]: # Generate 3 images where each the color of one channel in each image
    is inverted
    # Reverse B/G/R separately
    r,g,b = cv2.split(img_rgb)

def inverse(img):
    height, width = img.shape
    dst = np.zeros((height,width), np.uint8)
    for i in range(0, height):
        for j in range(0, width):
            dst[i, j] = 255-img[i,j]
    return dst

inversed_r = inverse(r)
    inversed_g = inverse(g)
    inversed_b = inverse(b)
```

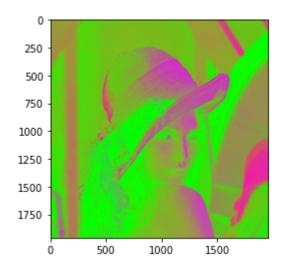
```
In [8]: # show the processed images
plt.imshow(cv2.merge([r,g,inversed_b]))
```

Out[8]: <matplotlib.image.AxesImage at 0x7f298b21a0b8>



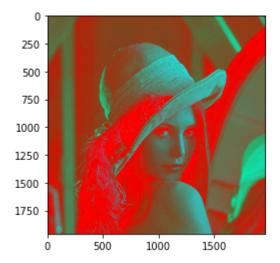
In [9]: plt.imshow(cv2.merge([r,inversed_g,b]))

Out[9]: <matplotlib.image.AxesImage at 0x7f298b174208>



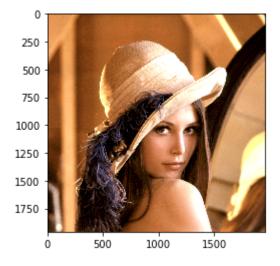
```
In [10]: plt.imshow(cv2.merge([inversed_r,g,b]))
```

Out[10]: <matplotlib.image.AxesImage at 0x7f298b152358>



4- Suggest a filter that make the image 50% lighter and 50% darker. Write a python function that applies the filter on the image.

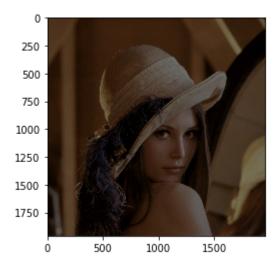
Out[11]: <matplotlib.image.AxesImage at 0x7f298b0b3630>



```
In [12]: def darkening_filter(img):
    height, width, deep = img.shape
    dst = np.zeros((height,width,deep), np.uint8)
    for i in range(0, height):
        for j in range(0, width):
            for d in range(0,deep):
                dst[i, j, d] = int(img[i,j,d]*0.5)
    return dst

darker_img = darkening_filter(img)
    plt.imshow(cv2.cvtColor(darker_img, cv2.C0LOR_BGR2RGB))
```

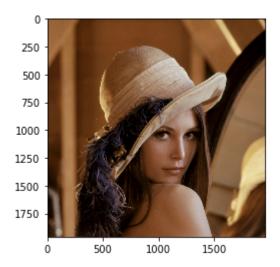
Out[12]: <matplotlib.image.AxesImage at 0x7f298b091518>



5- Write two python functions that apply a 3 x 3 median and 3 x 3 mean filter on the image. Mean filter is a simple sliding window that replace the center value with the average of all pixel values in the window. While median filter is a simple sliding window that replace the center value with the Median of all pixel values in the window. Note that the border pixels remain unchanged.

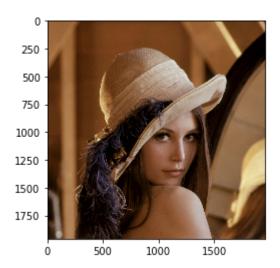
```
In [13]: | def mean_filter(img):
             # apply 3 x 3 mean filter
             def get mean(height, width, single c):
                 dst = np.zeros((height, width, 1), np.uint8)
                  for i in range(height):
                      for j in range(width):
                          if i<1 or i>height-2 or j<1 or j>width-2:
                              dst[i,j] = single c[i,j]
                              continue
                          sum = 0
                          for m in [-1,0,1]:
                              for n in [-1,0,1]:
                                  sum+=single_c[i+m,j+n]
                          dst[i,j] = sum/9
                  return dst
             height, width, deep = img.shape
             b,g,r = cv2.split(img)
             mean b = get mean(height, width,b)
             mean_g = get_mean(height, width,g)
             mean_r = get_mean(height, width,r)
             res = cv2.merge([mean b,mean g,mean r])
              return res
         img mean = mean filter(img)
         plt.imshow(cv2.cvtColor(img mean, cv2.COLOR BGR2RGB))
```

Out[13]: <matplotlib.image.AxesImage at 0x7f298aff3b70>



```
In [14]: def median filter(img):
             # apply 3 x 3 median filter
             def get median(height, width, single c):
                 dst = np.zeros((height, width, 1), np.uint8)
                  for i in range(height):
                      for j in range(width):
                          if i<1 or i>height-2 or j<1 or j>width-2:
                              dst[i,j] = single c[i,j]
                              continue
                          temp = []
                          for m in [-1,0,1]:
                              for n in [-1,0,1]:
                                  temp.append(single_c[i+m,j+n])
                          dst[i,j] = np.median(temp)
                  return dst
             height, width, deep = img.shape
             b,g,r = cv2.split(img)
             median b = get median(height, width,b)
             median g = get median(height, width,g)
             median_r = get_median(height, width,r)
             res = cv2.merge([median b,median g,median r])
              return res
         img median = median filter(img)
         plt.imshow(cv2.cvtColor(img median, cv2.COLOR BGR2RGB))
```

Out[14]: <matplotlib.image.AxesImage at 0x7f298afd6dd8>



6- A mean filter is a linear filter, but a median filter is not. Why?

In order to be linear, a function must satisfy the following condition:

$$f(x_1 + x_2) = f(x_1) + f(x_2)$$

Which is called the Additivity. Together with Homogenity, the two forms principle of superposition. Linear function must satisfy this principle.

For mean filter, say we are filtering using a sliding window of size n, and that the sum of the window is X. For instance, in the code we did for the previous question, the filtering matrix is (n = 9):

$$X = rac{1}{n} egin{bmatrix} 1 & 1 & 1 \ 1 & 1 & 1 \ 1 & 1 & 1 \end{bmatrix}$$

Whereby the mean is then:

$$mean(X) = rac{X}{n} = rac{\sum x_{i,j}}{n}$$

And we can say that for the function *mean*:

$$mean(F_n) = rac{F_n}{n}$$

So when applied, the part of the original photo being filtered has a sum of **Y**, then:

$$mean(X) + mean(Y) = rac{X}{n} + rac{Y}{n} = rac{X+Y}{n} = mean(X+Y)$$

Which is exactly the Additivity we defined at the beginning. Therefore mean filter is linear.

For median filter, the median of each sequence cannot be computed with a definitive arithmetic formulation, as we do for the mean. Since it is just the 'middle' value, there is no guarantee that the sum of two medians DOES NOT equal to the median of the sum, formally,

$$median(X + Y) \neq median(X) + median(Y)$$

For example: Say we have 2 sequences X = [1, 2, 3], Y = [1, 3, 0]. The medians are 2 and 4 respectively. X + Y = [2, 5, 3], and the median is now 3. This obviously does not equal to the sum of the two medians.