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Compilation Principle 编译原理

第17讲：中间代码(2)

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DCS290, 5/13/2021



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Review Questions (1)

- What are the main tasks of compilation backend?

Intermediate code generation, optimizations, target code generation

- What is IR (specifically, the low-level IR)?

Intermediate Representation. A machine- and language-independent version of the original source code.

- Why do we use IR?

Clean separation of front- and back-end; easy to optimize and extend

- What is three-address code (TAC)?

A type of IR, with at most three operands. (High-level assembly)

- TAC of $x + y * z + 5$?

$t_1 = y * z; t_2 = x + t_1; t_3 = t_2 + 5;$

Review Questions (2)

- Possible ways to implement TAC?

Quadruples: op arg1, arg2, result

Triples: op arg1 arg2

Indirect triples: op arg1 arg2

- What is Single Static Assignment?

An IR that facilitates certain code optimization.

Give variable different version name on every assignment.

- In code generation, how to layout variables in memory?

Calculate the location using base address and type width.

- What is address alignment?

Enforce $\text{addr}(x) \% \text{sizeof}(x.\text{type}) == 0$, to respect the hardware constraints to avoid unexpected performance degradation.

Code Generation[代码生成]

- To generate three-address codes (TACs)
 - By now, we have
 - an AST, annotated with scope and type information
 - Do another round of tree traversal
 - Lay out variables in memory
 - Generate TAC for any subexpressions or substatements
 - Using the result, generate TAC for the overall expression
- We will use the syntax-directed formalisms to specify translation
 - Variable definitions [变量定义]
 - Assignment [赋值]
 - Array references [数组引用]
 - Boolean expressions [布尔表达式]
 - Control-flow statements [控制流语句]

Type Expressions[类型表达式]

- A **type expression** is either a basic type or is formed by applying an operator called a *type constructor* [类型构造符] to a type expression
 - Basic type: *integer, float, char, Boolean, void*
 - Array: *array(l, T)* is a type expression, if *T* is
 - $\text{int}[3] \leftrightarrow \text{array}(3, \text{int})$
 - $\text{int}[2][3] \leftrightarrow \text{array}(2, \text{array}(3, \text{int}))$
 - Pointer: *pointer(T)* is a type expression, if *T* is
 - $\text{int}^* \text{val} \leftrightarrow \text{pointer}(\text{int})$

$$\begin{aligned}P &\rightarrow D \\D &\rightarrow T \text{ id}; D_1 \mid \epsilon \\T &\rightarrow B C \mid *T_1 \\B &\rightarrow \text{int} \mid \text{real} \\C &\rightarrow [\text{num}]C_1 \mid \epsilon\end{aligned}$$

CodeGen: Variable Definitions

- Translating variable definitions

- *enter(name, type, offset)*

- Save the type and relative address in the symbol-table entry for the name

① $P \rightarrow \{ \text{offset} = 0 \} D$

② $D \rightarrow T \text{ id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset});$
 $\text{offset} = \text{offset} + T.\text{width}; \} D_1$

③ $D \rightarrow \varepsilon$

④ $T \rightarrow B \{ t = B.\text{type}; w = B.\text{width}; \}$
 $C \{ T.\text{type} = C.\text{type}; T.\text{width} = C.\text{width}; \}$

⑤ $T \rightarrow *T_1 \{ T.\text{type} = \text{pointer}(T_1.\text{type}); T.\text{width} = 4; \}$

⑥ $B \rightarrow \text{int} \{ B.\text{type} = \text{int}; B.\text{width} = 4; \}$

⑦ $B \rightarrow \text{real} \{ B.\text{type} = \text{real}; B.\text{width} = 8; \}$

⑧ $C \rightarrow \varepsilon \{ C.\text{type} = t; C.\text{width} = w; \}$

⑨ $C \rightarrow [\text{num}]C_1 \{ C.\text{type} = \text{array}(\text{num.val}, C_1.\text{type});$
 $C.\text{width} = \text{num.val} * C_1.\text{width}; \}$

- Examples:

- *real x; int i;*

- *int[2][3];*

- *type, width*

- Syn attributes

- *t, w*

- Vars to pass type and width from B node to the node for $C \rightarrow \varepsilon$

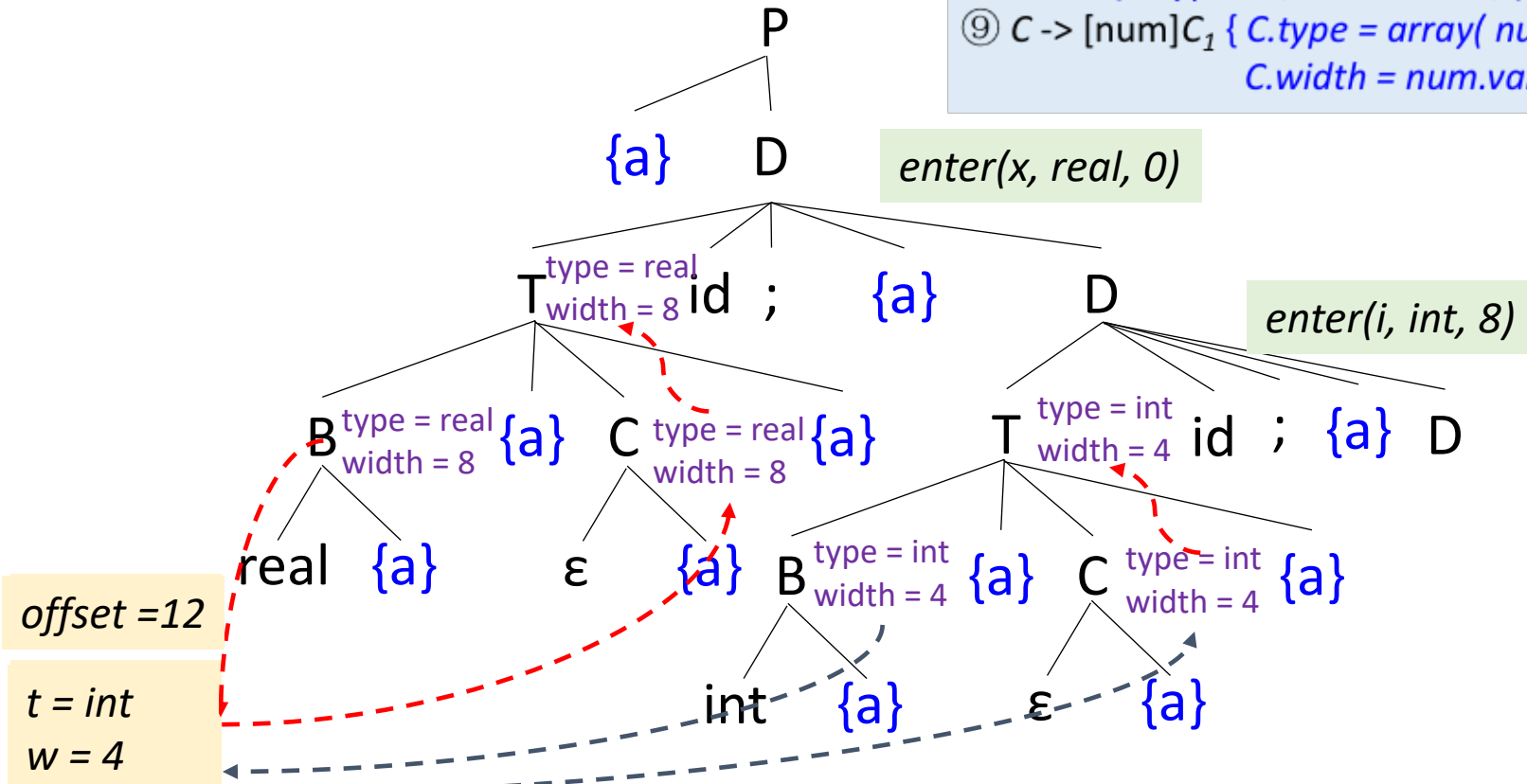
- *offset*

- The next relative address

Example

- Input: `real x; int i;`


- ① $P \rightarrow \{ \text{offset} = 0 \} D$
- ② $D \rightarrow T \text{ id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset});$
 $\text{offset} = \text{offset} + T.\text{width}; \} D_1$
- ③ $D \rightarrow \epsilon$
- ④ $T \rightarrow B \{ t = B.\text{type}; w = B.\text{width}; \}$
 $C \{ T.\text{type} = C.\text{type}; T.\text{width} = C.\text{width}; \}$
- ⑤ $T \rightarrow *T_1 \{ T.\text{type} = \text{pointer}(T_1.\text{type}); T.\text{width} = 4; \}$
- ⑥ $B \rightarrow \text{int} \{ B.\text{type} = \text{int}; B.\text{width} = 4; \}$
- ⑦ $B \rightarrow \text{real} \{ B.\text{type} = \text{real}; B.\text{width} = 8; \}$
- ⑧ $C \rightarrow \epsilon \{ C.\text{type} = t; C.\text{width} = w; \}$
- ⑨ $C \rightarrow [\text{num}]C_1 \{ C.\text{type} = \text{array}(\text{num.val}, C_1.\text{type});$
 $C.\text{width} = \text{num.val} * C_1.\text{width}; \}$



CodeGen: Assignment Statement

- Translate into three-address code [赋值语句]
 - An expression with more than one operator will be translated into instructions with at most one operator per instruction
- Helper functions in translation
 - *lookup(id)*: search *id* in symbol table, return null if none
 - *emit()/gen()*: generate three-address IR
 - *newtemp()*: get a new temporary location

- ① $S \rightarrow id = E;$
- ② $E \rightarrow E_1 + E_2;$
- ③ $E \rightarrow - E_1$
- ④ $E \rightarrow (E_1)$
- ⑤ $E \rightarrow id$

Assignment statement:

$a = b + (-c)$

Three-address code:

$t_1 = \text{minus } c$

$t_2 = b + t_1$

$a = t_2$

SDT Translation of Assignment

- Attributes **code** and **addr**

- *S.code* and *E.code* denote the TAC for *S* and *E*, respectively
- *E.addr* denotes the address that will hold the value of *E* (can be a name, constant, or a compiler-generated temporary)

- ① $S \rightarrow id = E; \{ p = \text{lookup}(id.lexeme); \text{if } !p \text{ then error};$
 $\quad S.code = E.code \parallel$
 $\quad \text{gen}(p '=' E.addr); \}$
- ② $E \rightarrow E_1 + E_2; \{ E.addr = \text{newtemp}();$
 $\quad E.code = E_1.code \parallel E_2.code \parallel$
 $\quad \text{gen}(E.addr '=' E_1.addr '+' E_2.addr); \}$
- ③ $E \rightarrow - E_1 \{ E.addr = \text{newtemp}();$
 $\quad E.code = E_1.code \parallel$
 $\quad \text{gen}(E.addr '=' \text{'minus'} E_1.addr); \}$
- ④ $E \rightarrow (E_1) \{ E.addr = E_1.addr;$
 $\quad E.code = E_1.code; \}$
- ⑤ $E \rightarrow id \{ E.addr = \text{lookup}(id.lexeme); \text{if } !E.addr \text{ then error};$
 $\quad E.code = ''; \}$

Incremental Translation[增量翻译]

- Generate only the new three-address instructions
 - *gen()* not only constructs a three-address inst, it appends the inst to the sequence of insts generated so far

① $S \rightarrow id = E; \{ p = lookup(id.lexeme); \text{ if } !p \text{ then error};$

$\text{ gen}(p \text{ '=' } E.addr); \}$

② $E \rightarrow E_1 + E_2; \{ E.addr = newtemp();$

$\text{ gen}(E.addr \text{ '=' } E_1.addr \text{ '+' } E_2.addr); \}$

③ $E \rightarrow - E_1 \{ E.addr = newtemp();$

$\text{ gen}(E.addr \text{ '=' 'minus' } E_1.addr); \}$

④ $E \rightarrow (E_1) \{ E.addr = E_1.addr;$
 $\}$

⑤ $E \rightarrow id \{ E.addr = lookup(id.lexeme); \text{ if } !E.addr \text{ then error};$
 $\}$

Code attributes can
be long strings

Example

- ① $S \rightarrow id = E; \{ p = \text{lookup}(id.\text{lexeme}); \text{if } !p \text{ then error; } \\ \text{gen}(p = 'E.\text{addr}'); \}$
- ② $E \rightarrow E_1 + E_2; \{ E.\text{addr} = \text{newtemp}(); \\ \text{gen}(E.\text{addr} = 'E_1.\text{addr} + 'E_2.\text{addr}); \}$
- ③ $E \rightarrow - E_1 \{ E.\text{addr} = \text{newtemp}(); \\ \text{gen}(E.\text{addr} = 'minus' E_1.\text{addr}); \}$
- ④ $E \rightarrow (E_1) \{ E.\text{addr} = E_1.\text{addr}; \}$
- ⑤ $E \rightarrow id \{ E.\text{addr} = \text{lookup}(id.\text{lexeme}); \text{if } !E.\text{addr} \text{ then error; } \}$

- Input

$$x = (a + b) + c$$

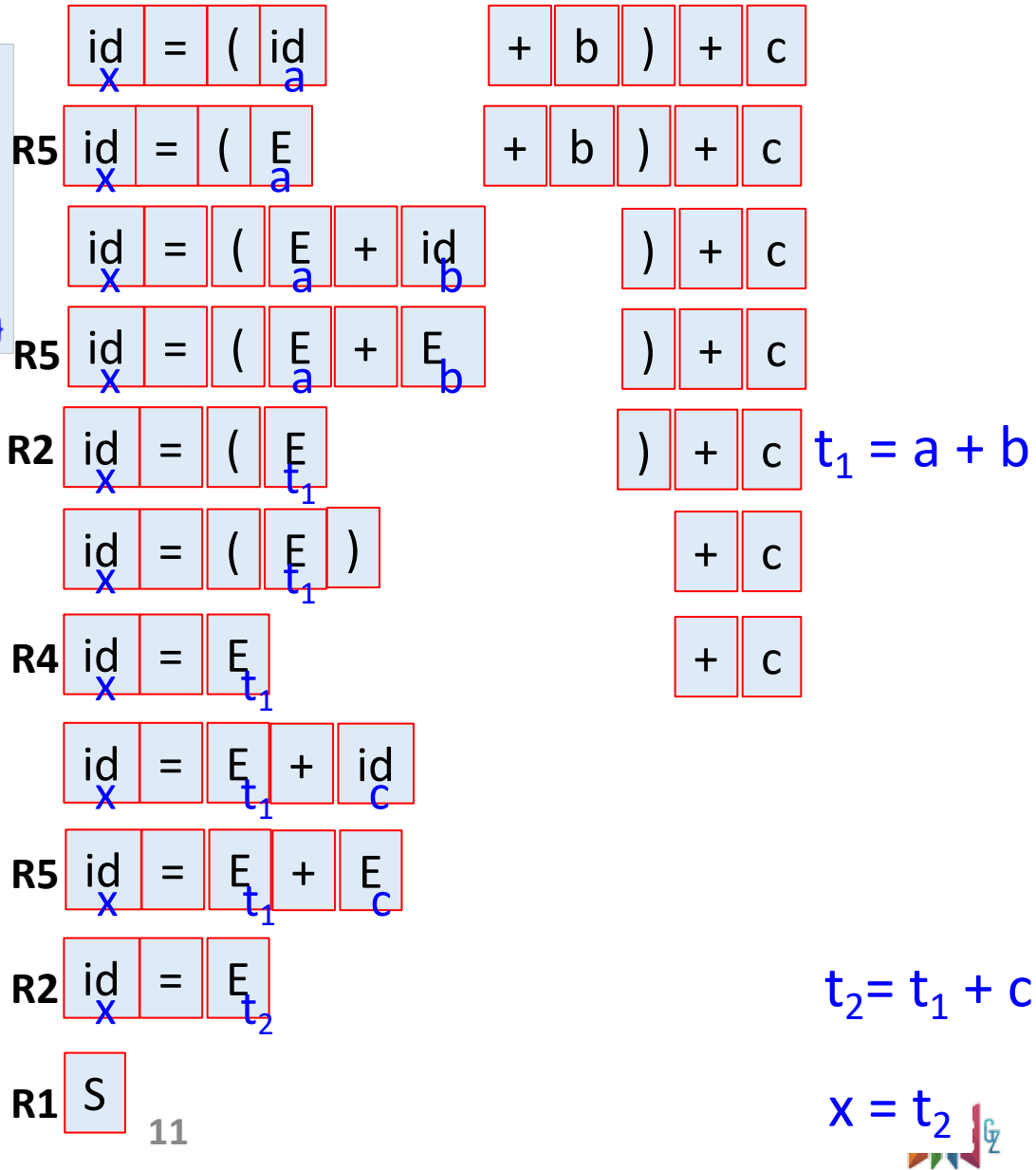


- Translated TAC

$$t_1 = a + b$$

$$t_2 = t_1 + c$$

$$x = t_2$$



CodeGen: Array Reference[数组引用]

- Primary problem in generating code for array references is to determine the address of element

- 1D array

```
int A[N];
```

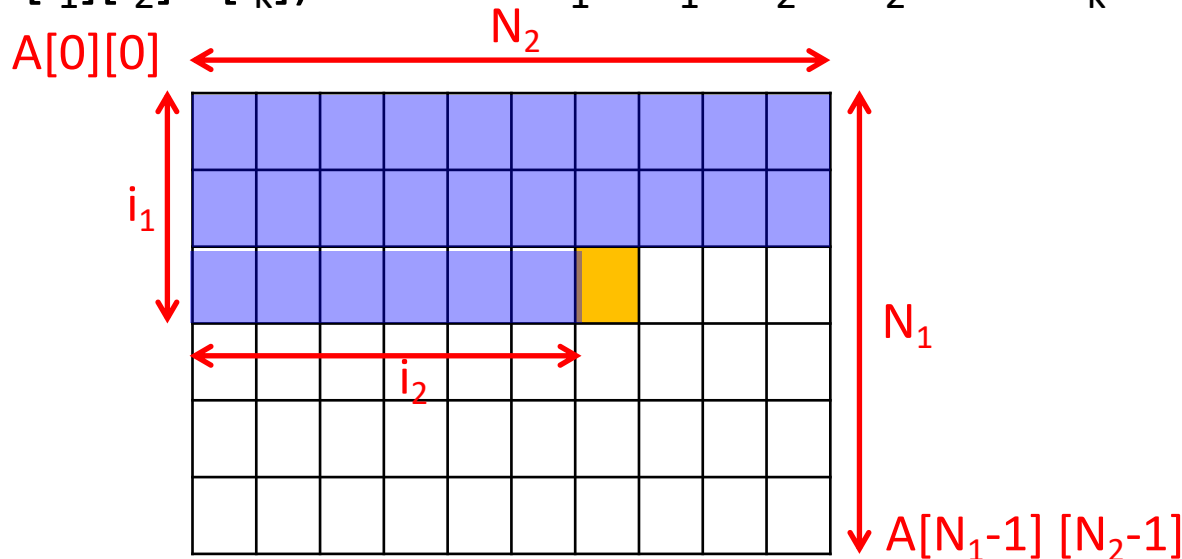
```
A[i] ++;
```



- *Base*: address of the first element
 - *Width*: width of each element
 - $i \times \text{width}$ is the offset
- Addressing an array element
 - $\text{addr}(A[i]) = \text{base} + i \times \text{width}$

N-dimensional Array

- Laying out 2D array in 1D memory
 - `int A[N1][N2]; /* int A[0..N1][0..N2] */`
 - `A[i1][i2] ++;`
- The organization can be row-major or column-major
 - C language uses row major (i.e., stored row by row)
 - Row-major: $\text{addr}(A[i_1, i_2]) = \text{base} + (i_1 \times \underbrace{N_2}_{w_1} \times \text{width} + i_2 \times \underbrace{\text{width}}_{w_2})$
- *k*-dimensional array
 - $\text{addr}(A[i_1][i_2] \dots [i_k]) = \text{base} + i_1 \times w_1 + i_2 \times w_2 + \dots + i_k \times w_k$



Translation of Array References

- $\text{Type}(a) = \text{array}(10, \text{int})$
– $c = a[i];$

$$\text{addr}(a[i]) = \text{base} + i * 4$$

$$\begin{aligned} t_1 &= i * 4 \\ t_2 &= a[t_1] \\ c &= t_2 \end{aligned}$$

$$\text{addr}(a[i_1][i_2]) = \text{base} + i_1 * 20 + i_2 * 4$$

- $\text{Type}(a) = \text{array}(3, \text{array}(5, \text{int}))$
– $c = a[i_1][i_2];$

$$\begin{aligned} t_1 &= i_1 * 20 \\ t_2 &= i_2 * 4 \\ t_3 &= t_1 + t_2 \\ t_4 &= a[t_3] \\ c &= t_4 \end{aligned}$$

- $\text{Type}(a) = \text{array}(3, \text{array}(5, \text{array}(8, \text{int})))$
– $c = a[i_1][i_2][i_3]$

$$\begin{aligned} \text{addr}(a[i_1][i_2][i_3]) &= \text{base} + i_1 * w_1 + i_2 * w_2 + i_3 * w_3 \\ &= \text{base} + i_1 * 160 + i_2 * 32 + i_3 * 4 \end{aligned}$$

Translation of Array References (cont.)

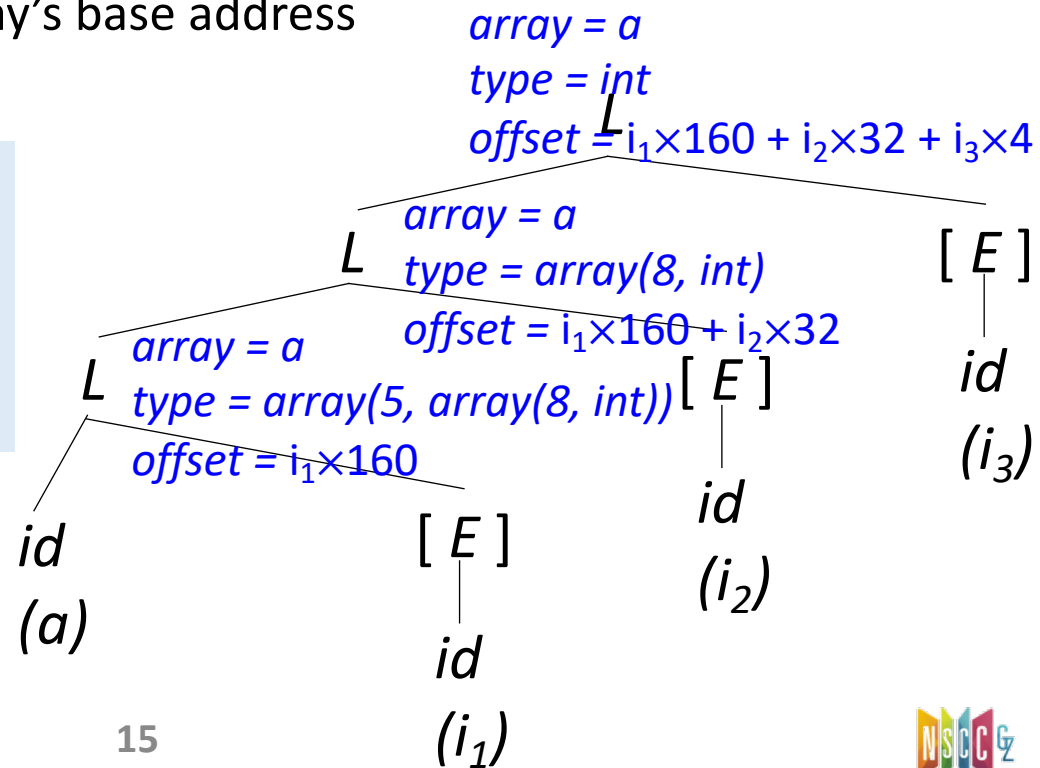
- $A[i_1][i_2][i_3]$, $\text{type}(a) = \text{array}(3, \text{array}(5, \text{array}(8, \text{int})))$
 - $L.\text{type}$: the type of the subarray generated by L
 - $L.\text{addr}$: a temporary that is used while computing the offset for the array reference by summing the terms $i_j \times w_j$
 - $L.\text{array}$: a pointer to the symbol-table entry for the array name
 - $L.\text{array}.\text{base}$ gives the array's base address

① $S \rightarrow \text{id} = E; \mid L = E;$

② $E \rightarrow E_1 + E_2 \mid - E_1 \mid (E_1) \mid \text{id} \mid L$

③ $L \rightarrow \text{id} [E] \mid L_1 [E]$

$\text{base} + i_1 \times w_1 + i_2 \times w_2 + \dots + i_k \times w_k$



Translation of Array References (cont.)

- $A[i_1][i_2][i_3]$, $\text{type}(a) = \text{array}(3, \text{array}(5, \text{array}(8, \text{int})))$

```
①  $S \rightarrow \text{id} = E; \mid L = E; \{ \text{gen}(L.\text{array}.\text{base}['L.\text{addr}'] \text{'=' } E.\text{addr}); \}$   
②  $E \rightarrow E_1 + E_2 \mid - E_1 \mid (E_1) \mid \text{id} \mid L \{ E.\text{addr} = \text{newtemp}();$   
     $\text{gen}(E.\text{addr} \text{'=' } L.\text{array}.\text{base}['L.\text{addr}']); \}$   
③  $L \rightarrow \text{id} [E] \{ L.\text{array} = \text{lookup}(\text{id}.\text{lexeme}); \text{if } !L.\text{array} \text{ then error};$   
     $L.\text{type} = L.\text{array}.\text{type}.\text{elem};$   
     $L.\text{offset} = \text{newtemp}();$   
     $\text{gen}(L.\text{addr} \text{'=' } E.\text{addr} \text{'*'} L.\text{type}.\text{width}); \}$   
 $\mid L_1 [E] \{ L.\text{array} = L_1.\text{array};$   
     $L.\text{type} = L_1.\text{type}.\text{elem};$   
     $t = \text{newtemp}();$   
     $\text{gen}(t \text{'=' } E.\text{addr} \text{'*'} L.\text{type}.\text{width});$   
     $L.\text{addr} = \text{newtemp}();$   
     $\text{gen}(L.\text{addr} \text{'=' } L_1.\text{addr} \text{'+' } t; \}$ 
```

```
 $t_1 = i_1 * 160$   
 $t_2 = i_2 * 32$   
 $t_3 = t_1 + t_2$   
 $t_4 = i_3 * 4$   
 $t_5 = t_3 + t_4$   
 $c = a[t_5]$ 
```


CodeGen: Boolean Expressions

- Boolean expression: *a op b*
 - where op can be <, <=, =, !=, > or >=, &&, ||, ...
- **Short-circuit** evaluation[短路计算]: to skip evaluation of the rest of a boolean expression once a boolean value is known
 - Given following C code: *if (flag || foo()) { bar(); }*
 - If *flag* is true, *foo()* never executes
 - Equivalent to: *if (flag) { bar(); } else if (foo()) { bar(); }*
 - Given following C code: *if (flag && foo()) { bar(); }*
 - If *flag* is false, *foo()* never executes
 - Equivalent to: *if (!flag) { } else if (foo()) { bar(); }*
 - Used to alter control flow, or compute logical values
 - Examples: *if (x < 5) x = 1; x = true; x = a < b*
 - For control flow, boolean operators translate to **jump** statements

Boolean Exprs (w/o Short-Circuiting)

- Computed just like any other arithmetic expression

$E \rightarrow (a < b) \text{ or } (c < d \text{ and } e < f)$

$t_1 = a < b$
 $t_2 = c < d$
 $t_3 = e < f$
 $t_4 = t_2 \ \&\& \ t_3$
 $t_5 = t_1 \ || \ t_4$

- Then, used in control-flow statements

– *S.next*: label for code generated after *S*

$S \rightarrow \text{if } E \text{ } S_1$

if (! t_5) goto *S.next*
*S*₁.code
S.next: ...