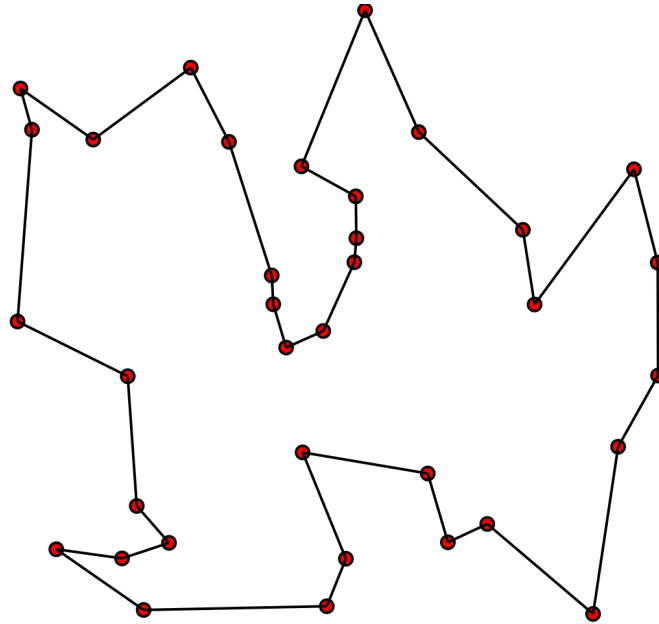


Optimization Algorithms for Traveling Salesman Problem: A Comparison of Basic Ant System and Ant Colony Optimization-Genetic Algorithm Hybrid

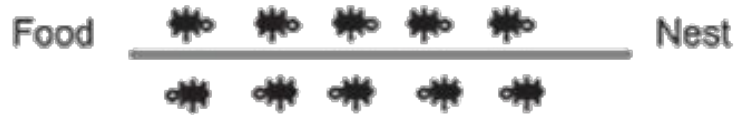
Michael Webber, Andy Stoneman, and Alex Clark

Traveling Salesman Problem

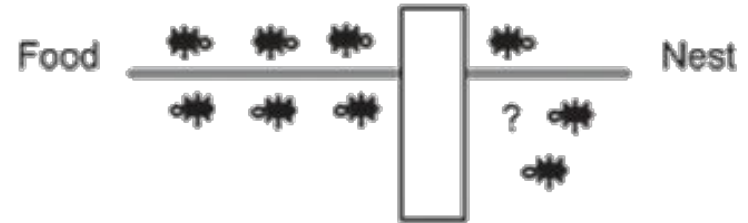


Ant Colony Optimization

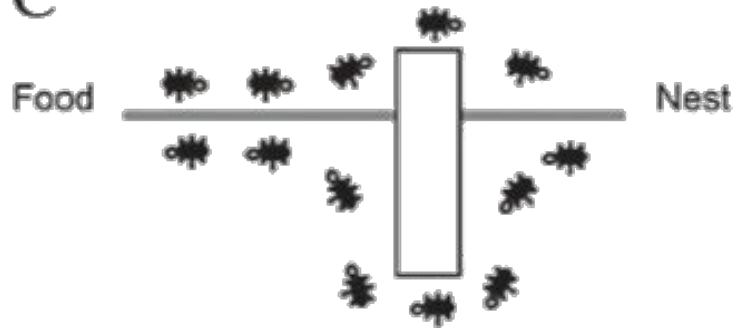
A



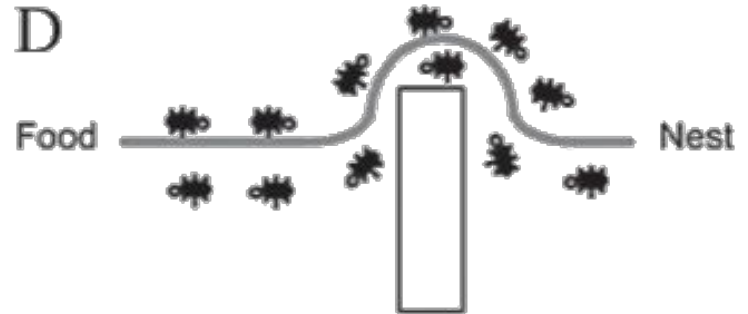
B



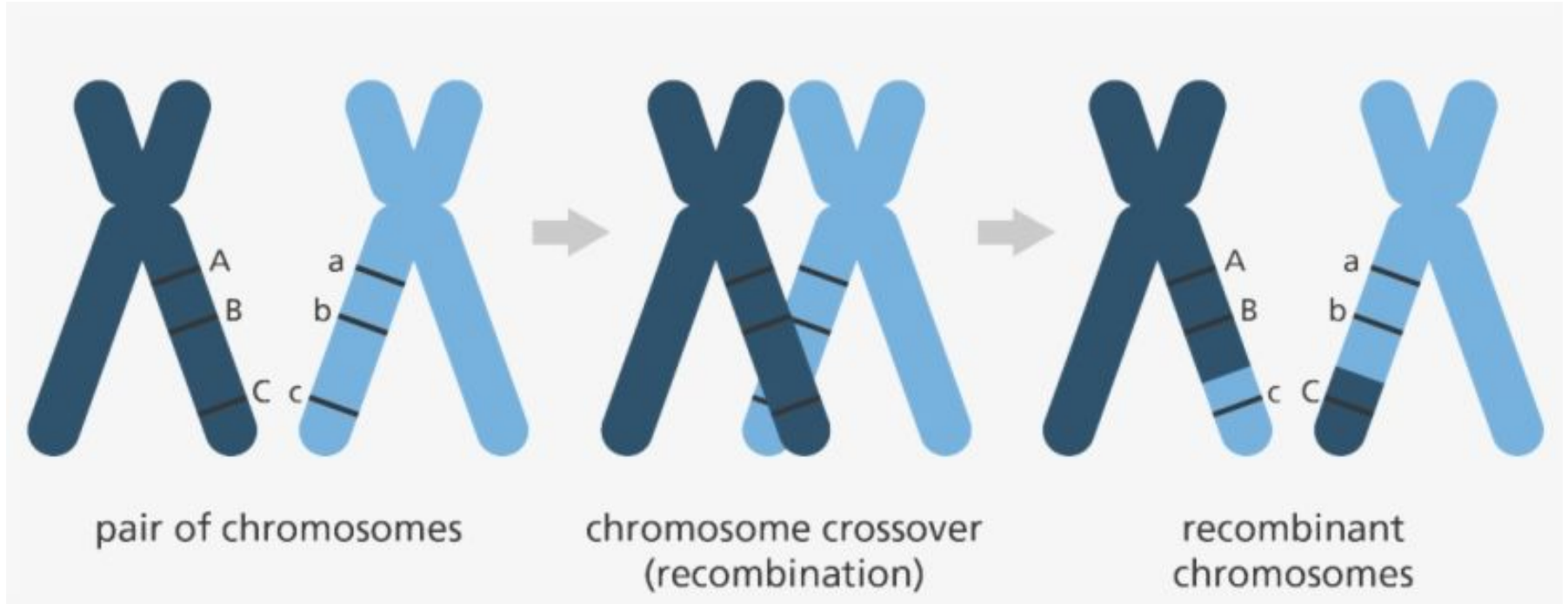
C



D



Genetic Algorithm



Combining ACO and GA



Ant Colony Optimization-Genetic Algorithm Hybrid

- ACO portion is just Basic Ant System
- Candidate solution for GA = single ant's constructed tour
- Genetic Algorithm modified:
 - Tournament Selection–Use top eight
 - Recombination–Order Crossover and Partially Mapped Crossover
 - No mutation–Made things worse
 - Replace bottom eight in initial population

Modified Tournament Selection

```
/**
 * Runs the genetic algorithm portion of the hybrid. Picks half the number of ants using tournament selection
 * and then calls specified crossover operator.
 */
private void gaUpdate() {
    //tournament selection
    Ant[] parentAnts = new Ant[NUM_ANTS];
    Random randomSelect = new Random();

    for (int i = 0; i < 8; i++) {
        //pick two random candidates from the initial population
        Ant candidateOne = antCollection[randomSelect.nextInt(NUM_ANTS)];
        Ant candidateTwo = antCollection[randomSelect.nextInt(NUM_ANTS)];

        //check which one has a higher fitness and add it to the new empty array
        if (candidateOne.getCurDistance() > candidateTwo.getCurDistance()) {
            parentAnts[i] = candidateOne;
        } else {
            parentAnts[i] = candidateTwo;
        }
    }

    //recombination/crossover
    if (crossoverType == "OX") {
        orderCrossover(parentAnts);
    } else if (crossoverType == "PMX") {
        partiallyMappedCrossover(parentAnts);
    }
}
```

Ordered Crossover

$$P_1 = (8 \ 3 \ 4 \mid 1 \ 2 \ 7 \mid 5 \ 6)$$

$$P_2 = (5 \ 4 \ 2 \mid 8 \ 1 \ 6 \mid 3 \ 7)$$

Keep portion
of the
corresponding
parent.

$$C_1 = (x \ x \ x \mid 1 \ 2 \ 7 \mid x \ x)$$

$$C_2 = (x \ x \ x \mid 8 \ 1 \ 6 \mid x \ x)$$

Insert
ordering of the
opposite
parent's values
after the cutoff
and remove
the values that
are already in
the child.

$$C_1 = (4 \ 8 \ 6 \mid 1 \ 2 \ 7 \mid 3 \ 5)$$

$$C_2 = (4 \ 2 \ 7 \mid 8 \ 1 \ 6 \mid 5 \ 3)$$

Partially Mapped Crossover

Make maps
between cuts.

$$P_1 = (8 \ 3 \ 4 \mid 1 \ 2 \ 7 \mid 5 \ 6)$$

$$P_2 = (5 \ 4 \ 2 \mid 8 \ 1 \ 6 \mid 3 \ 7)$$

Maintain the middle portion of
the opposite parent.

$$C_1 = (x \ x \ x \mid 8 \ 1 \ 6 \mid x \ x)$$

$$C_2 = (x \ x \ x \mid 1 \ 2 \ 7 \mid x \ x)$$

Pieces with no conflict are filled in.

$$C_1 = (x \ 3 \ 4 \mid 8 \ 1 \ 6 \mid 5 \ x)$$

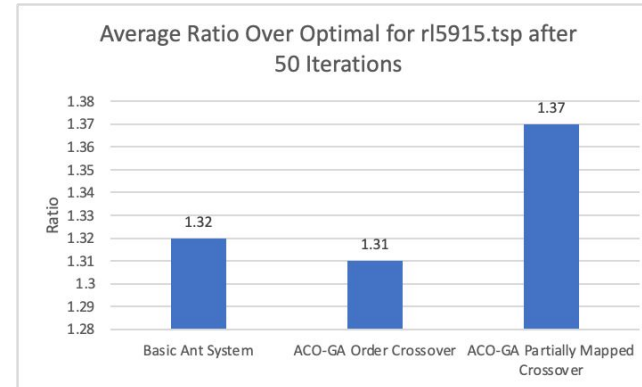
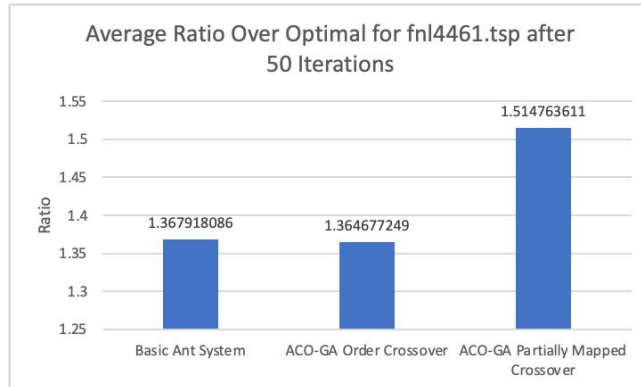
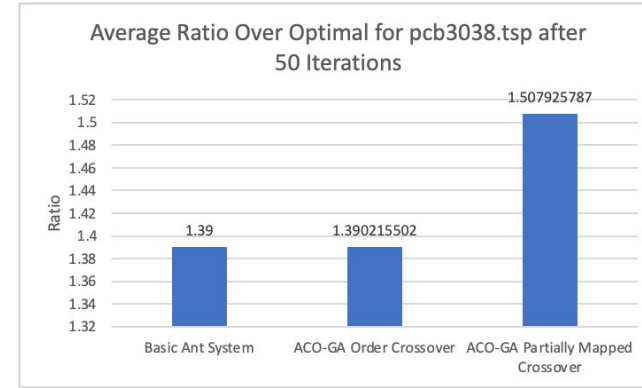
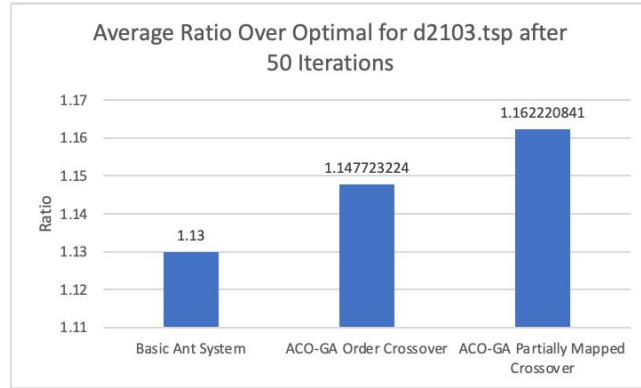
$$C_2 = (5 \ 4 \ x \mid 1 \ 2 \ 7 \mid x \ 3)$$

Use mapping.

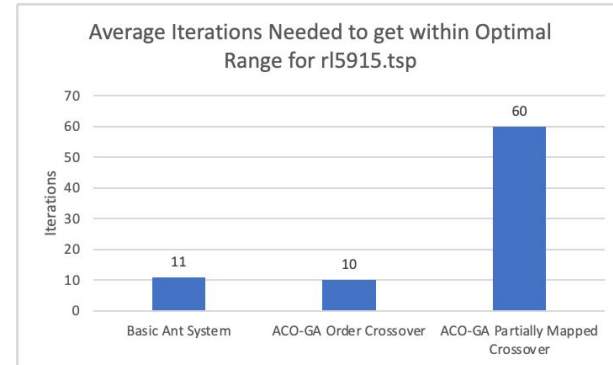
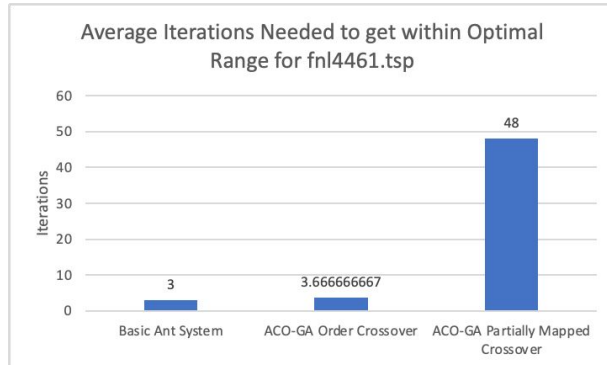
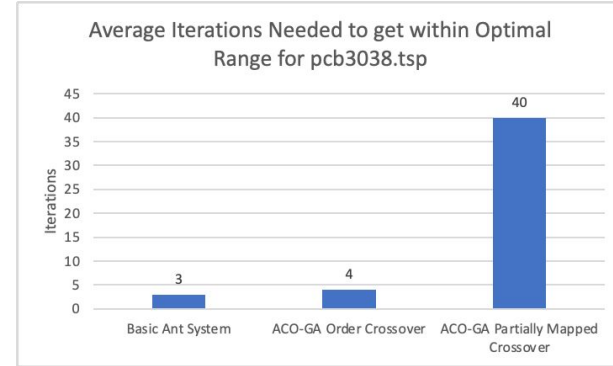
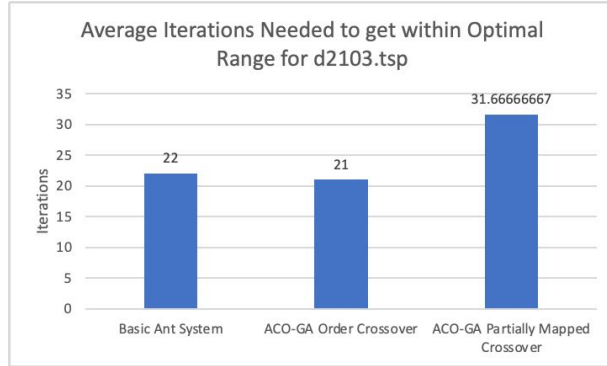
$$C_1 = (2 \ 3 \ 4 \mid 8 \ 1 \ 6 \mid 5 \ 7)$$

$$C_2 = (5 \ 4 \ 8 \mid 1 \ 2 \ 7 \mid 6 \ 3)$$

Experiment 1: Fitness after 50 Iterations



Experiment 2: Iterations to Optimal Range



Further Work

- Implementation of more selection types—vary number of selected ants or increase number of ants total
- Try new mutation implementations that could possibly return better results
- Test on more files—particularly larger files to see if trends continue

Conclusion
