

# Automated Negotiation

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Ongoing collaboration with: Tim Baarslag and Reyhan Aydogan

# Contents of these slides

- Recap: Formalizing Negotiations
  - Domain models
  - Preferences and preference elicitation
  - Analysing results
- Protocols
  - bilateral
  - Multi-lateral
- Negotiation strategies
  - BOA framework
  - An overview of important strategies
- Analysis of Negotiation Dynamics
- Using the BOA framework
- Prepare for Tutorial and Test

# Why negotiation is difficult for humans?

- Leaving money on the table
  - Sub-optimal outcomes for both sides.
- Bounded rationality
  - Outcome space might be too big.
- Emotions
  - May have negative effect on acting rationally
  - Some people are too shy to ask what they want.



# Automated Negotiation

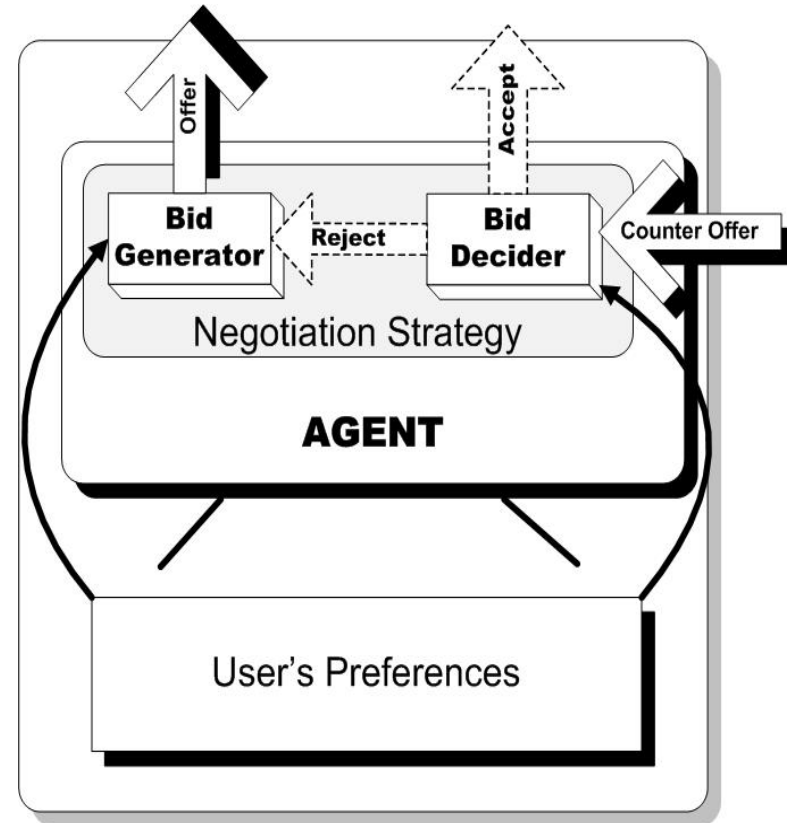


- Intelligent software agents negotiate on behalf of their users.
- Possible application domains: e-commerce, politics, cloud-computing, crisis management system, task allocation, etc.



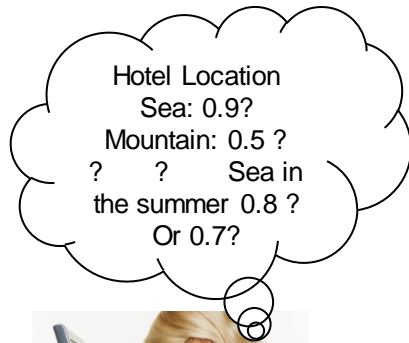
# How can a software agent negotiate its user's behalf?

- Evaluating bids
  - Reasoning on its user's **preferences**
- Employing a **negotiation strategy**
  - Which action the agent will take
  - How the agent will generate its offer
  - When the agent will accept the opponent's counter offer
- Communicating with other agent (s) based on predefined rules (**negotiation protocol**)



# Preferences:

## Utility Functions



### Holiday Domain

- Hotel Location: Sea, Historical Places, Mountain.
- Season: Winter, Summer.
- Duration: One week, Two weeks, Three weeks.

Hotel Location	Season	Duration	Utility
Sea	Summer	1- week	0.95
Historical Places	Summer	1- week	0.87
Mountain	Summer	1-week	0.36
Sea	Summer	2- weeks	0.76
...	...	...	...

**Most of the negotiation approaches use utility functions.**

# Preferences

## Additive Utility Functions

- **Assumption:** Issues are preferentially independent.
- **Utility** is determined as a weighted sum of the evaluation values of each issue.

$$U(X_1, X_2, \dots, X_n) = \sum_{i=1}^n w_i * U_i(X_i)$$

- The utility of <Sea, Summer, One-week> =  
 $0.5 * U_1(\text{Sea}) + 0.3 * U_2(\text{Summer}) + 0.2 * U_3(\text{One-Week})$   
where  $w_1(\text{Location}) = 0.5$ ,  $w_2(\text{Season}) = 0.3$ ,  $w_3(\text{Duration}) = 0.2$

- clouddomain.xml
- laptop\_domain.xml
- party\_domain.xml
- son\_domain.xml
- son\_domain\_with\_discount\_factor.xml
- ampo\_vs\_city\_template.xml
- thompson\_employment.xml
- car\_domain.xml
  - car\_buyer.xml
  - car\_dealer.xml

laptop\_domain laptop\_buyer\_utility laptop\_seller\_utility car\_domain car\_buyer

Name	Type	Value	Weight
Car	OBJECTIVE	This == Objective	
CD player	DISCRETE	), fairly good (80), standard (75), meager (70)	<input type="text" value="0,31"/>
Extra speakers	DISCRETE	), fairly good (95), standard (90), meager (20)	<input type="text" value="0,31"/>
Airconditioning	DISCRETE	. fairly good (98), standard (99), meager (100)	<input type="text" value="0,08"/>
Tow hedge	DISCRETE	. fairly good (98), standard (99), meager (100)	<input type="text" value="0,12"/>
Price	REAL	Min: 13000.0Max: 22666.0	<input type="text" value="0,18"/>

Specifying weight of each issue.



GENIUS 4.0

Start Help

Scenarios Agents

clouddomain.xml  
laptop\_domain.xml  
party\_domain.xml  
son\_domain.xml  
son\_domain\_with\_discount\_factor.xml  
ampo\_vs\_city\_template.xml  
thompson\_employment.xml  
car\_domain.xml  
    car\_buyer.xml  
    car\_dealer.xml

laptop\_domain laptop\_buyer\_utility laptop\_seller\_utility car\_domain car\_buyer

Name	Type	Value	Weight
Car	OBJECTIVE	This == Objective	
CD player	DISCRETE	), fairly good (80), standard (75), meager (70)	
Extra speakers	DISCRETE		
Airconditioning	DISCRETE		
Tow hedge	DISCRETE		
Price	REAL		

Basic Properties  
Name: Extra speakers

Issue Properties  
Discrete

Edit the discrete values below.

	Evaluation values.
good	100
fairly good	95
standard	90
meager	20
none	0

Assigning evaluation value for each issue value.

Ok Cancel

# Reflection on last week:

## Normalization

- You need first to normalize all evaluation functions (also named valuation functions in last week's slides). I discuss it here for discrete domains:
  - Pick the item of the issue's range that has maximum value, the normalized evaluation function for that issue maps that item to 1.
  - For all other items in the range normalize in proportion to the maximum value to determine it's normalized value.

## Normalization (2/3)

- Formally: Given issue  $j$  with range  $D_j$ , and valuation function  $v_j$
- Let  $m = \max(\{v_j(x) \mid x \in D_j\})$ ,
- We define the *normalized evaluation* function  $e_j : D_j \rightarrow [0,1]$  by:  $e_j(x) = v_j(x)/m$
- Then to determine the normalized utility of a bid:
  - Multiply the normalized evaluation of the issue wrt the bid with the weight of that issue
  - Do this for all issues
  - Add it all up

# Normalization (3/3)

- Formally:
  - Let  $D = D_1 \times D_2 \times \dots \times D_n$  be the cartesian product of the ranges of all issues.  $D$  is also the bid space.
  - Let  $w_j$  be the weight of issue  $j$ , for all  $j$ :  $1 \leq j \leq n$ .
  - Let  $e_j$  be the normalized evaluation function of issue  $j$ .
  - The *normalized utility* function  $u: D \rightarrow [0,1]$  is defined by:  $u(b) = \sum_{1 \leq j \leq n} (w_j * e_j(b_j))$ , where  $b_j$  is the projection of  $b$  on issue  $j$ .

# NEGOTIATION PROTOCOLS

# Negotiation Protocol

- A negotiation protocol governs the interaction between negotiating parties by determining
  - how the parties interact/exchange information
    - " **who can say what and when they can say it** "
  - when the negotiation ends
- Bilateral Negotiation
  - Alternating Offers Protocol (Rubinstein 1982)
- Multiparty Negotiation
  - Mediated Single Text Protocol

# Alternating Offers Protocol (Rubinstein 1982)

- One of the agents initiates negotiation with an offer.

- The agent receiving an offer can

- accept that offer
- make a counteroffer
- end negotiation



**Offer [10days, 100\$]**

**Counter Offer [15 days, 80 \$]**

**Offer [11days, 99\$]**

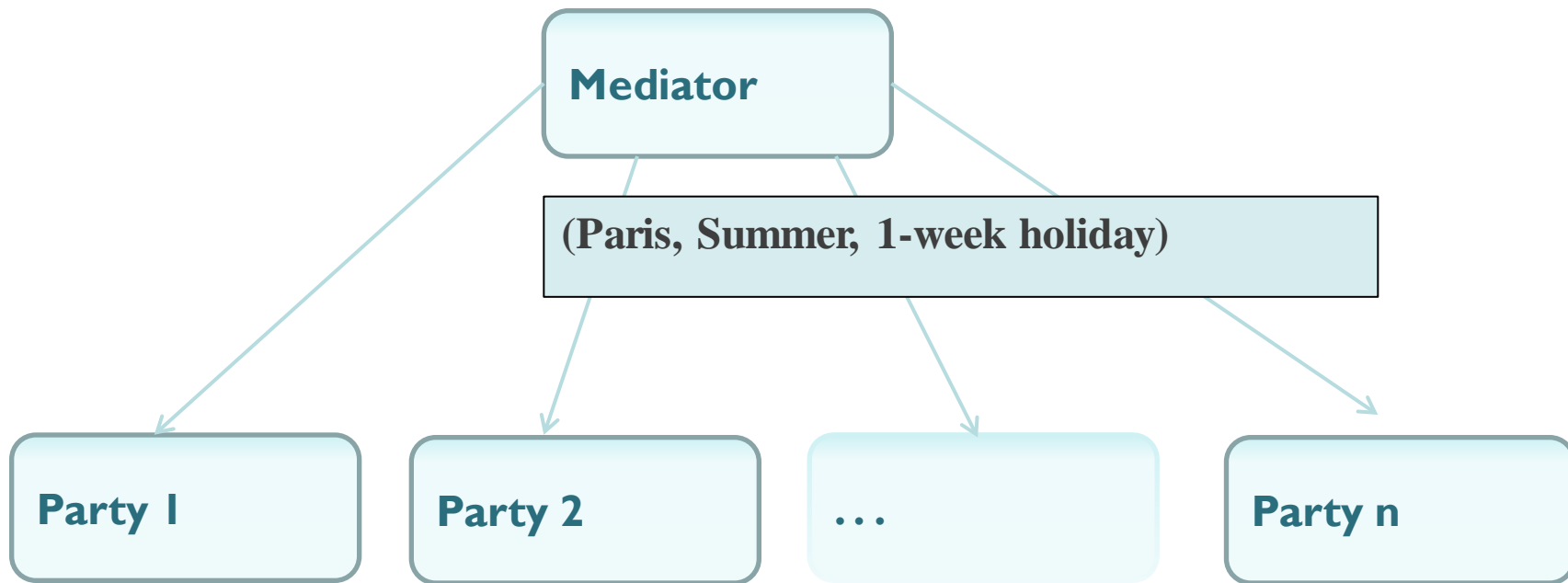
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- This process continues in a turn-taking fashion until having a consensus or reaching a termination condition such as a deadline.

# Mediated Single Text Negotiation Protocol

(based on Raiffa 1982)

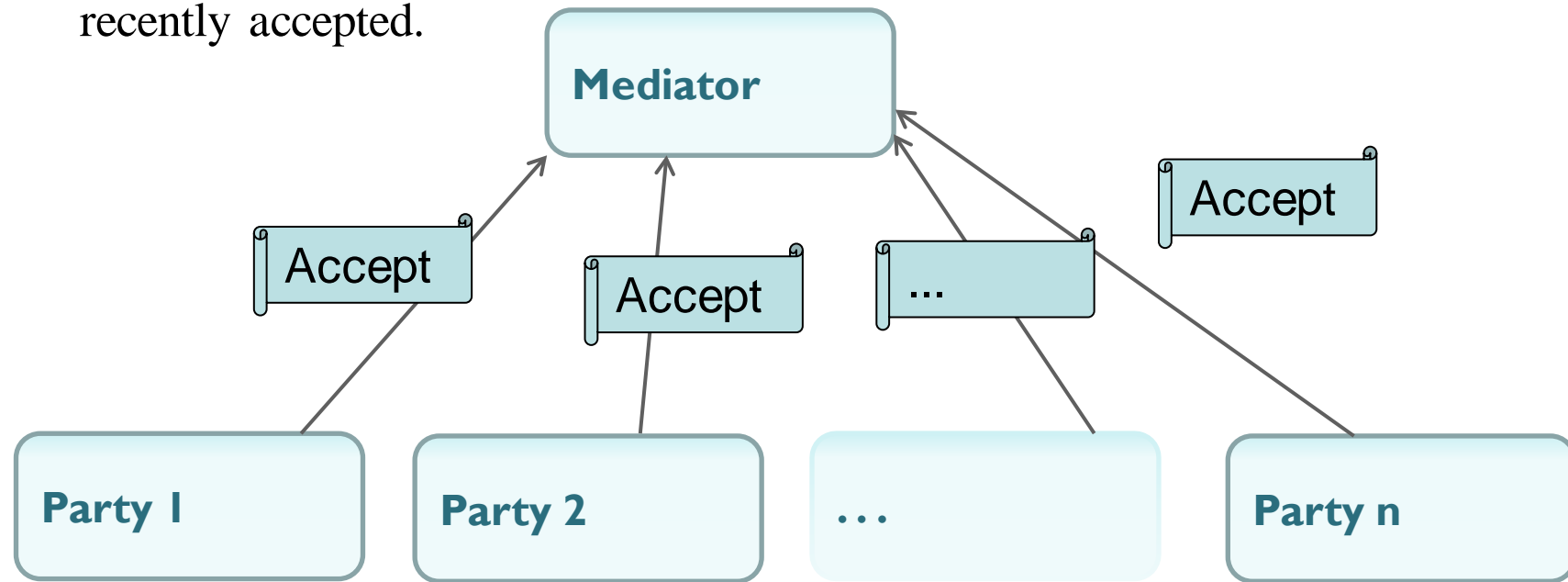
Mediator generates an offer and asks negotiating agents for their votes either to accept or to reject this offer.





# Mediated Single Text Negotiation Protocol

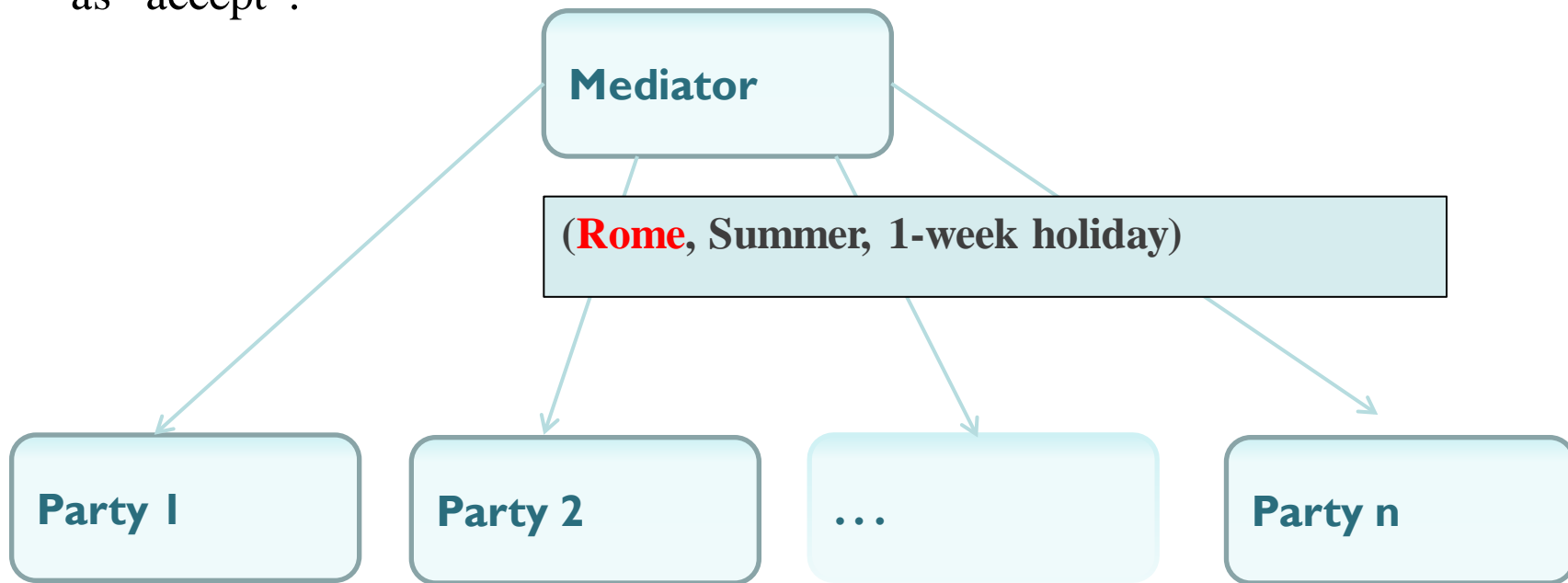
- Negotiating agents send their votes for the current bid according to their acceptance strategy.
- If all negotiating agents vote “accept”, the bid is labeled as the most recently accepted.



E.g. MRA Bid: (Paris, Summer, 1-week holiday)

# Mediated Single Text Negotiation Protocol

- Mediator modifies the most recently accepted bid by exchanging one value arbitrary and asks negotiating agents' votes again.
- It updates the most recently accepted bid if all negotiating agents vote as “accept”.



This process continues iteratively until reaching a predefined number of bids.

# How does a mediator find a solution acceptable to all?

- The role of the mediator is to propose new ideas that are acceptable to all.
- How to find these?
- Trusted mediator might know all profiles (partially)
- What if mediator doesn't know the profiles?
  - Mediated Hill-Climber Agent
  - Mediated Annealer Agent

# Mediated Single Text Negotiation

## Hill-Climber Agent (Klein et al., 2003)

- Accept a bid if its utility is higher than the utility of the most recently accepted bid
  - MRA Bid = (Antalya, Summer, 1-week),
  - Bid<sub>6</sub> = (Antalya, Summer, 2-week),
  - $U(\text{Bid}_6) = 0.95 > U(\text{MRA Bid}) = 0.87 \rightarrow \text{ACCEPT}$

Note: If the utility of initial bid is quite high for one of the agents, that agent may not accept other bids even though those bids might be better for the majority.

# Mediated Single Text Negotiation: Annealer Agent (Klein et al., 2003)

- Calculates the probability of acceptance for the current bid:

$$P(\text{accept}) = \min(1, e^{-\Delta U/T})$$

T: Virtual temperature gradually declines over time

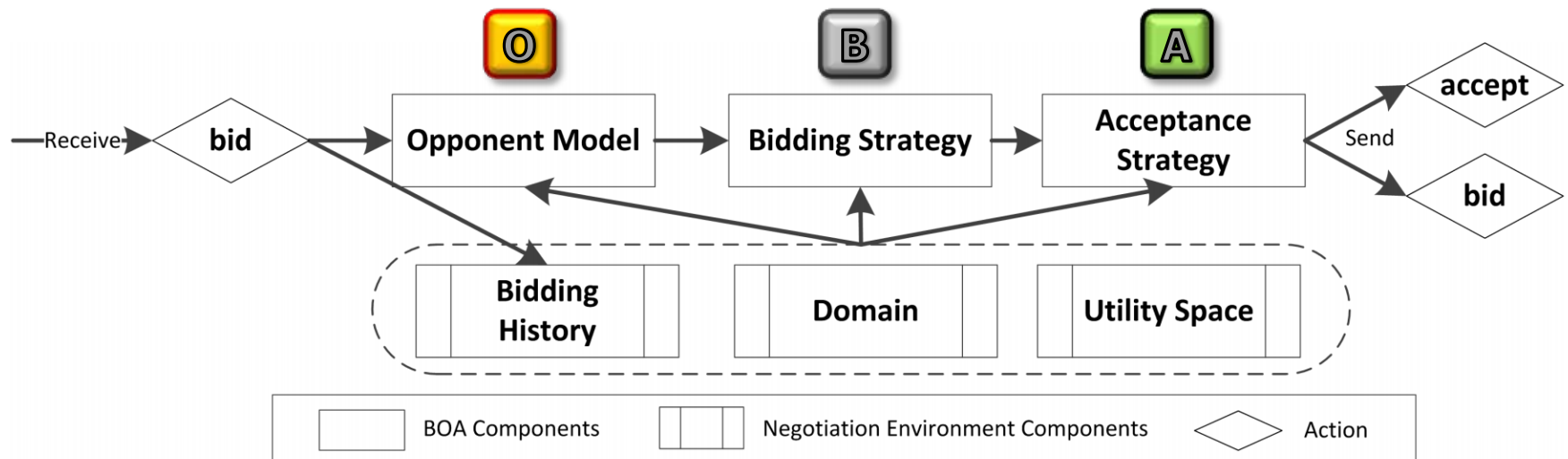
- Higher probability for acceptance
  - The utility difference is small & virtual temperature is high
- Tendency to accept individually worse bids earlier so the agents find win-win bids later

Baarslag et al., for more information see phd thesis

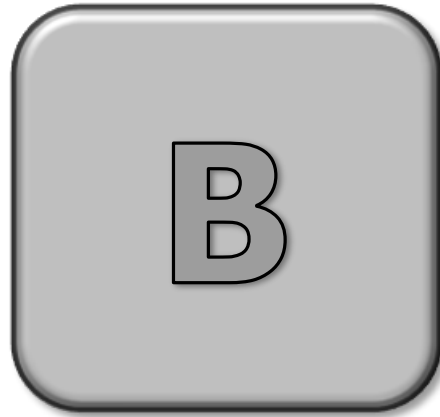
# NEGOTIATION STRATEGIES

# Negotiation Strategy

- Determines
  - which action the agent will take
  - how the agent will generate its offers
  - how the agent decide whether the opponent's counter-offer is acceptable



# Bidding strategies





# Random Walker

- It generates an offer randomly as follows:
  - Selects values of issues randomly
  - Proposes only those bids whose own utility greater than its reservation utility ( $RU=0.6$ ).

# Time-dependent Concession Strategy

## [Faratin, Sierra & Jennings, 1998]

- Each agent has a deadline and the agent's behavior changes with respect to the time.
- An offer which is not acceptable at the beginning, may become acceptable over time (conceding while approaching the deadline).
- A function determines how much the agent will concede
  - Remaining negotiation time
  - Parameter related to concession speed ( $\beta$ )
- **Conceder Tactic:**
  - $\beta > 1$  concedes fast and goes to its reservation value quickly.
- **Boulware Tactic:**
  - $\beta < 1$  hardly concedes until the deadline

# Trade-Off Strategy (1)

- Not only considers its own utility but also take its opponent's utility into account.
- The importance of the issues may be different for the negotiating agents.
  - E.g. delivery time might be more important for the consumer
- The agent may demand more on some issues while concedes on other issues without changing its overall utility as if possible.
  - E.g. higher price in order to have an earlier delivery

# Trade-Off Strategy (2)

## [Faratin, Sierra, Jennings, AIJ 2002]

- Selects a subset of bids having the same utility with its previous offer (iso-curve)
  - If not possible, it makes minimal concession such as 0.05.
- Among those bids, choose the bids which might be more preferred by its opponent
  - Heuristic: the most similar one to opponent's last bid

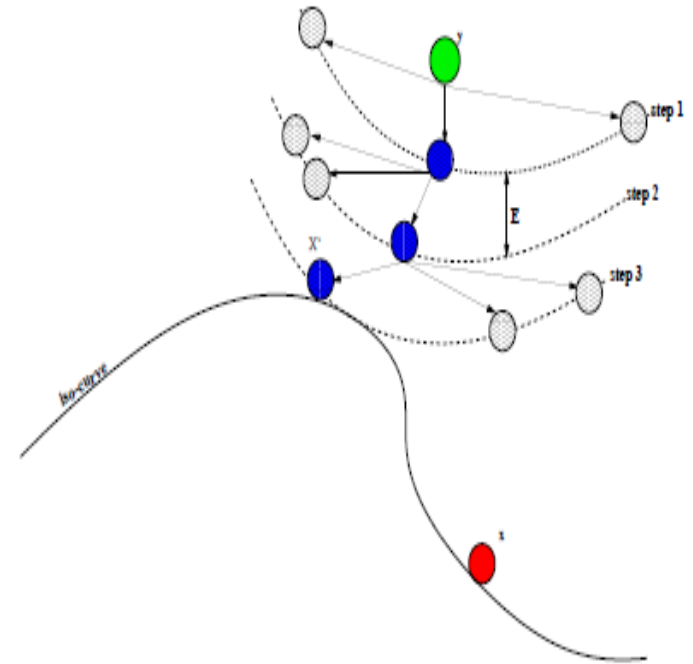


Figure 4.8: Schema of the trade-off algorithm with  $N = 3$  and  $S = 3$ .

This figure is taken from Faratin's PhD Thesis.

# Behaviour Dependent Strategies:

[Faratin, Sierra & Jennings, 1998]

- The agent imitates its opponent's behaviour.
- The degree of imitation may vary
  - Absolute Tit-For-Tat:
    - E.g. The opponent increases the price by 50 units then the agent will decrease the price by 50 units.
  - Relative (proportionally) Tit-For-Tat:
    - Taking into account the changes of its opponent's behaviour in a number of previous steps.
  - Averaged Tit-For-Tat
    - Taking into account the average changes within a window of size of its opponent history

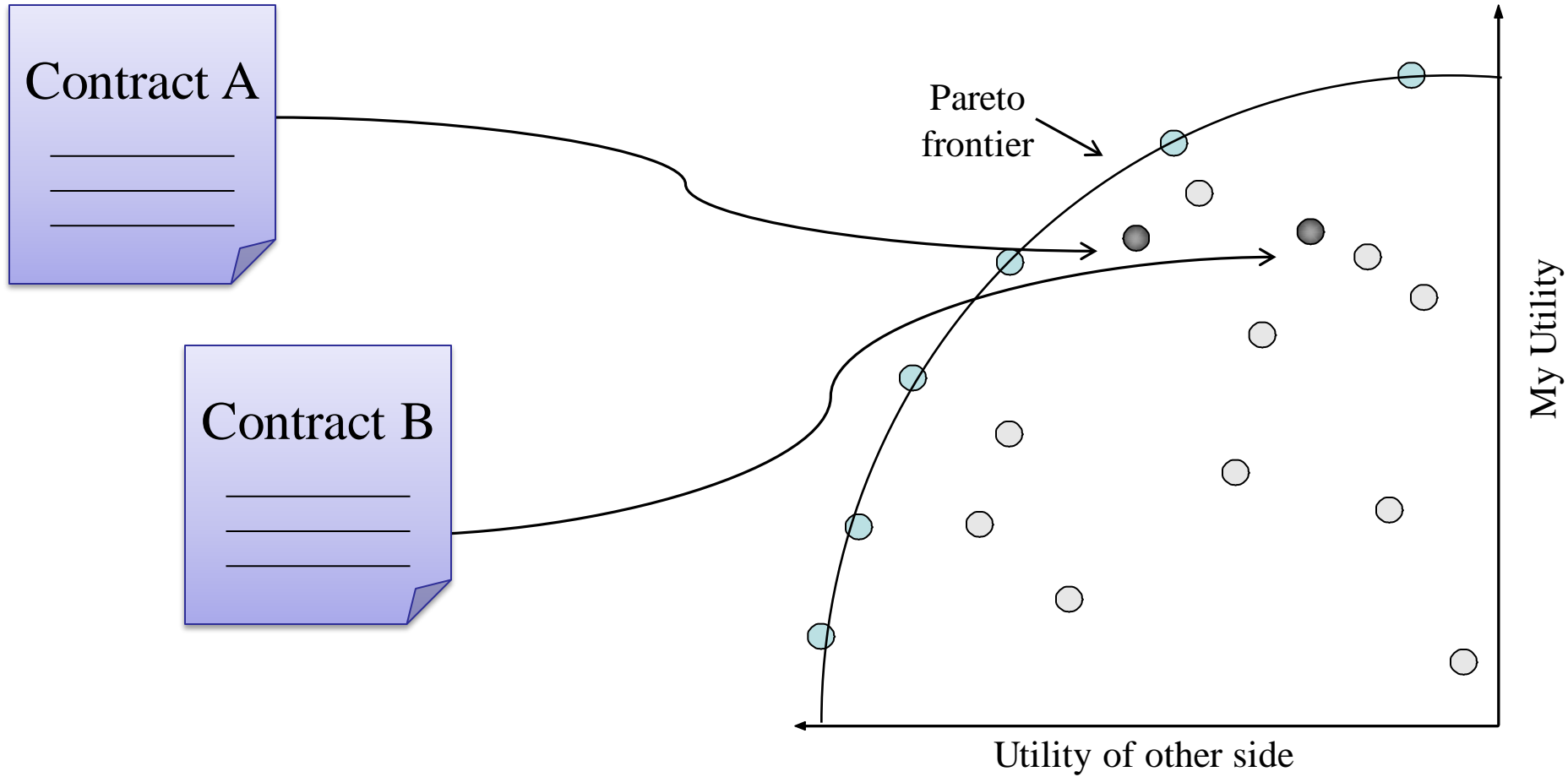
# Opponent modelling strategies



# Opponent Modelling (1) Why?

- Exploit the opponent
- Maximize chance of reaching an agreement
  - Requiring outcome with acceptable utility for opponent, i.e. resolving the conflict of interest.
- Increase the efficiency of a negotiated agreement
  - Searching through the outcome space for outcomes that are mutually beneficial
  - Reaching better/optimal agreements
- Avoid unfortunate moves
  - which is worse for both agents
- Make trade-offs and maximize social welfare
- Reach agreements early
  - Reducing communication cost

# Opponent Modeling





# Opponent Modelling (2) What?

- Learning which issues are important for the opponent
  - Issue weights
- Learning opponent's preferences
  - Evaluation of issue values
  - Preference ordering of issue values
- Learning about opponent's strategy
  - Predicting the utility of its next offer
- Learning what kind of offers are not acceptable
  - Reservation value
  - Constraints

# Some Examples (1):

- Kernel density estimation for estimating the opponent's **issue weights** [Coehoorn and Jennings 2004]
  - Intuition: The opponent has a tendency to concede slowly on important issues.
  - Assumption: Weighted scoring function & Concession based strategy
- Bayesian Learning for predicting **evaluation functions and weights** [Hindriks and Tykhonov, 2008]
  - Hypothesis for evaluation functions: uphill, downhill, triangular
  - Assumption: Linear additive functions & Concession based strategy

## Some Examples (2)

- A guessing heuristic for predicting the opponent's **unknown weights** [Jonker, Robu & Treur, 2007]
  - Some of the weights are revealed by the opponent
  - Requiring domain knowledge
- Concept-based Learning (RCEA) for classifying offers regarding **their acceptability** [Aydogan & Yolum 2012]
  - Assumption: Conjunctive & Disjunctive Constraints
  - Intuition: Avoid offering unacceptable offers to opponent

# A Simple Example:

## Frequency Analysis Heuristic

- A heuristic adopted by some of the agents in ANAC competition such as *HardHeaded Agent*
- Based on **how often the value of an issue changed** and **the frequency of appearance of values in offers**
- Learning issue weights: importance of issues
  - Heuristic: If the value is often changed, then the issue gets a low weight.
- Learning issue value weights: evaluations of the issue values
  - Heuristic: A preferred value will appeared more often in agent's offers than a less preferred value.

# Frequency Analysis Heuristic (2)

## Estimation of issue weights

- Assume that we have two issues (X, Y) and opponent 's first offer is  $[x1, y1]$ .
  - Take the predicted weights 0.5 and 0.5 for X, Y respectively
- Second offer  $[x1, y2]$ 
  - $W1=0.5 + n$  since opponent didn't change the value of X
  - $W2=0.5$
  - If  $n= 0.1$  then new weights will be 0.6, 0.5 respectively
    - $W1_{new}= 0.55$   $W2_{new}= 0.45$

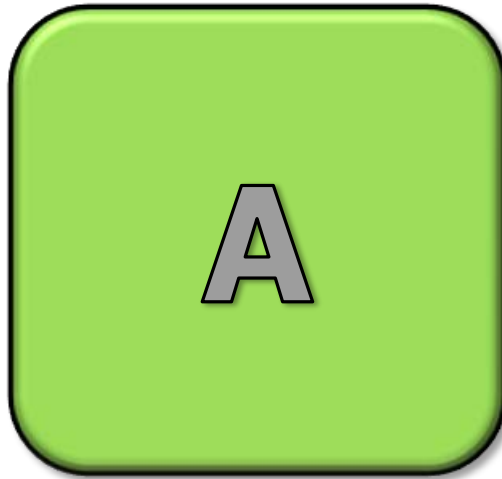
# Frequency Analysis Heuristic (3)

## Estimation of evaluation values for issues

- Assume negotiation round=45 and our opponent's offer history
  - “Brand” issue in Laptop domain

Issue Values:	Dell	Mac	HP
# of times appeared in offers	20	15	10
Estimated Evaluation	1.0 (20/20)	0.75 (15/20)	0.5 (10/20)

# Acceptance Conditions



# Introduction

Why and when should we accept?

- In every negotiation with a deadline, one of the negotiating parties has to accept an offer to avoid a break off.
- A break off is usually an undesirable outcome; therefore, it is important to consider under which conditions to accept.



# Introduction

## The Acceptance Dilemma

- When designing such conditions one is faced with the acceptance dilemma:
  - Accepting too early may result in suboptimal agreements
  - On the other hand, accepting too late may result in a break off
- We have to find a balance:

$$\text{Total average utility} = \text{Agreement percentage} \times \text{Average utility of agreements.}$$

# Acceptance Conditions

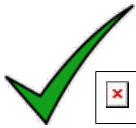
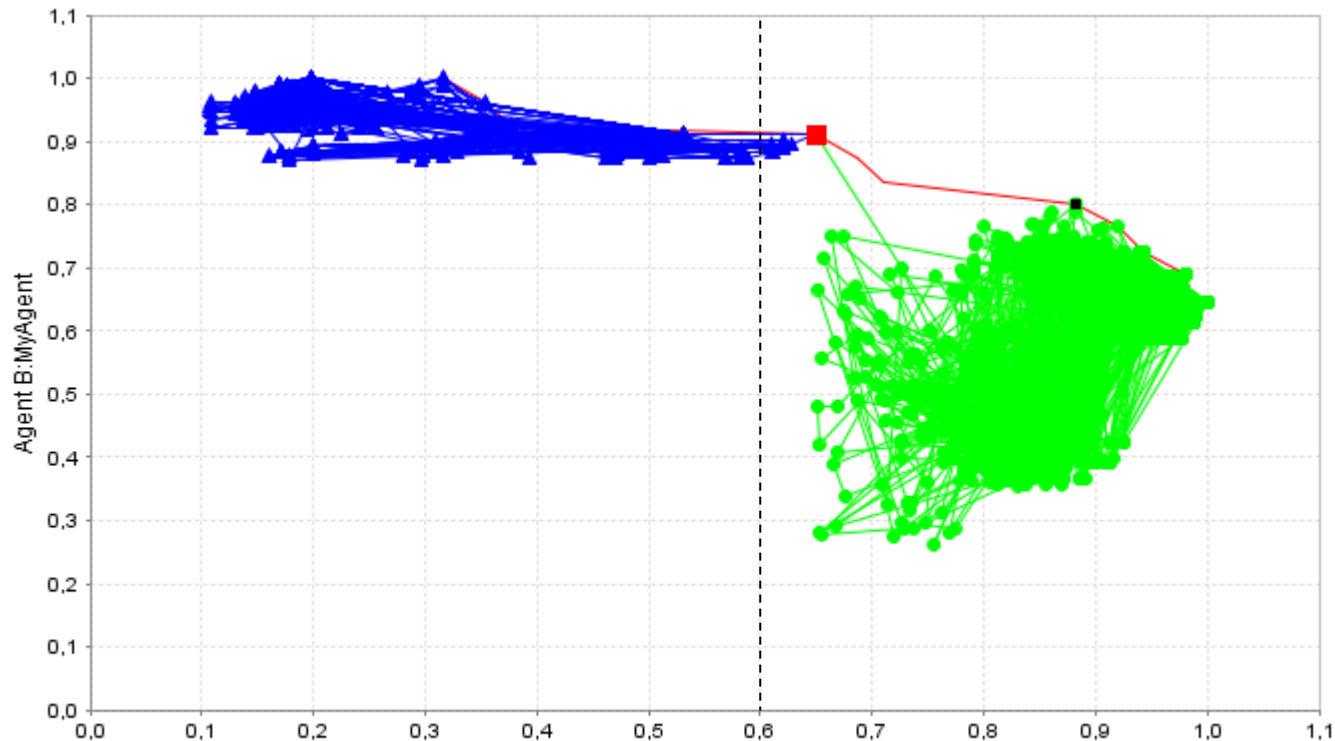
## Selection of Existing Acceptance Conditions

- In literature and current agent implementations, we see the following recurring acceptance conditions:
- $\mathbf{AC}_{\text{const}}(\alpha)$     Accept when the opponent's bid is better than  $\alpha$
- $\mathbf{AC}_{\text{next}}$     Accept when the opponent's bid is better than our upcoming bid
- $\mathbf{AC}_{\text{time}}(T)$     Accept when time  $T \in [0, 1]$  has passed

# Acceptance Conditions

## Example

$t = 0.7$



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AC<sub>next</sub>

# Acceptance Conditions

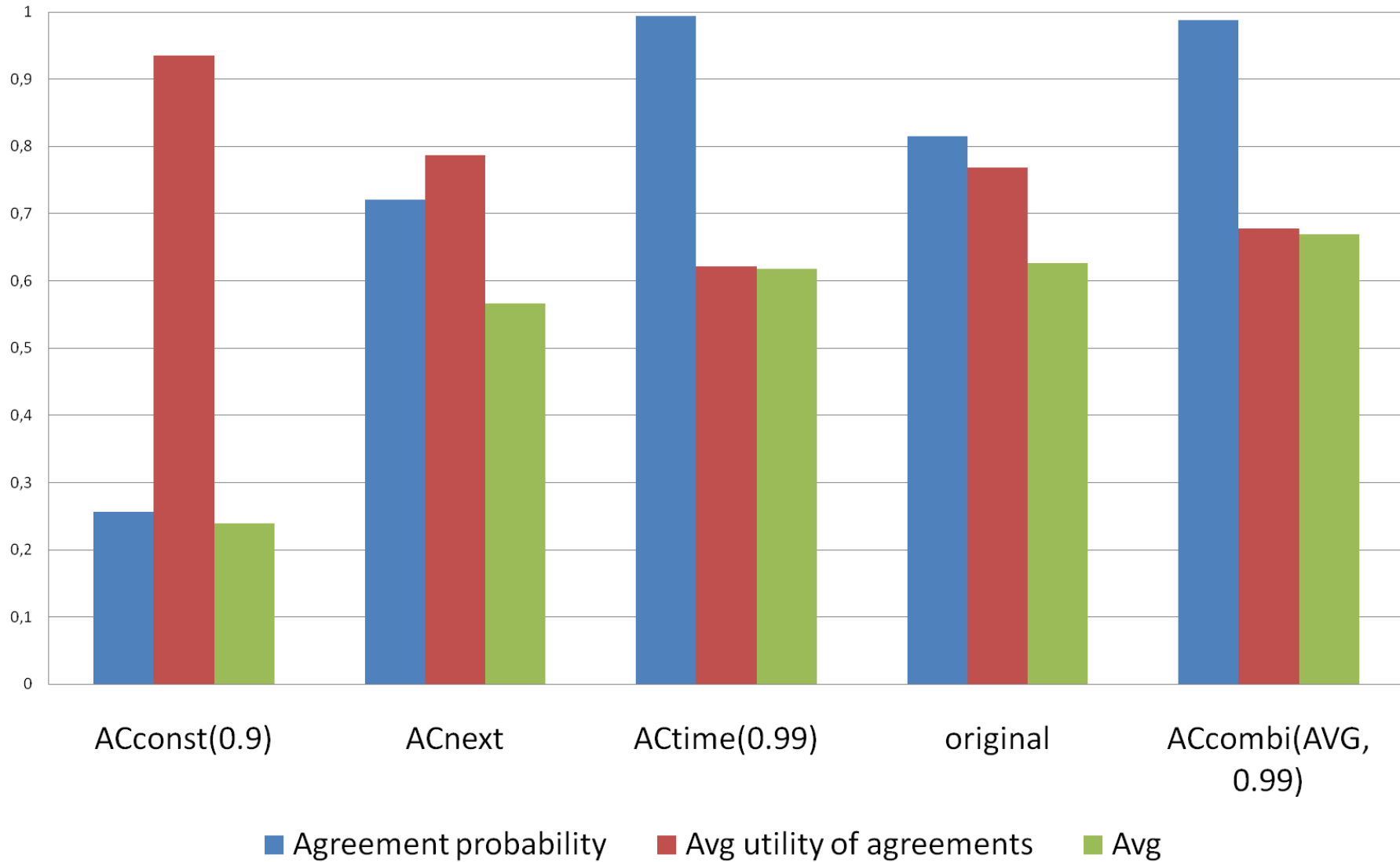
## Combining Acceptance Conditions

- We can also combine acceptance conditions, e.g.:

$$\begin{aligned} & \mathbf{AC}_{\text{combi}}(T, \alpha) \\ & \quad \stackrel{\text{def}}{\iff} \\ & \mathbf{AC}_{\text{next}} \vee \mathbf{AC}_{\text{time}}(T) \wedge \mathbf{AC}_{\text{const}}(\alpha). \end{aligned}$$

- $\mathbf{AC}_{\text{combi}}(T, \alpha)$  splits the negotiation time into two phases:  $[0, T)$  and  $[T, 1]$
- We can also choose non-constant values for  $\alpha$  such as average utility so far received (AVG), or maximum utility (MAX).

## Experimental results: utility scores of acceptance conditions



# Conclusion

- $AC_{next}$  is often used, but does not always give the best results.
- $AC_{const}(\alpha)$  performs worst of all AC's, as a good value for  $\alpha$  is highly domain-dependent.
- $AC_{time}(T)$  always reaches an agreement, but of relatively low utility.
- We need combinations of different approaches.

# Conclusion:

## Challenges in Automated Negotiation

- Designing negotiation protocols & strategy
- Representing and Reasoning on Preferences in Negotiation
- Predicting Other Agent's Preferences during Negotiation
- Acceptance Strategies

Hindriks, Jonker, Tykhonov, 2011

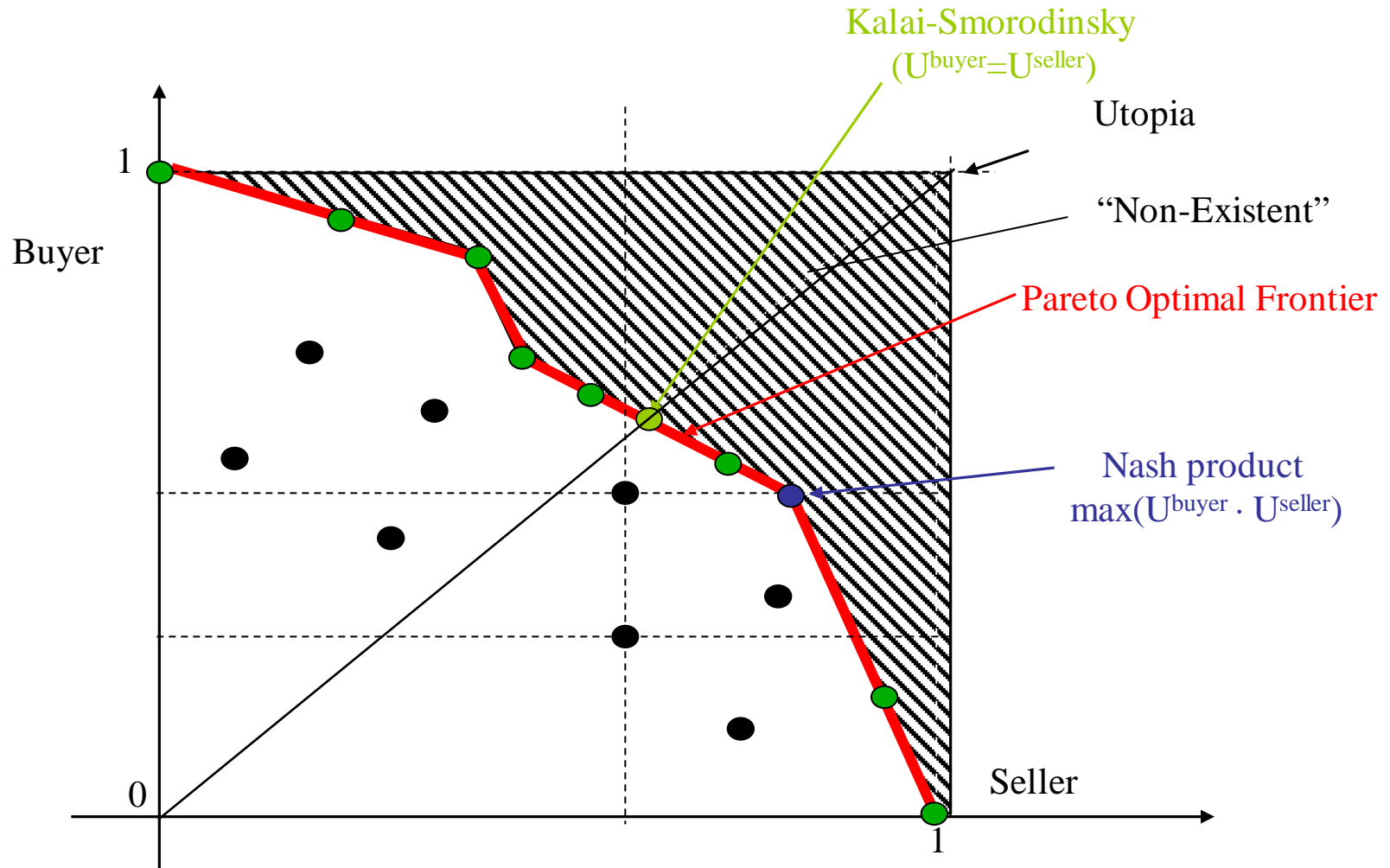
# ANALYSIS OF NEGOTIATION DYNAMICS



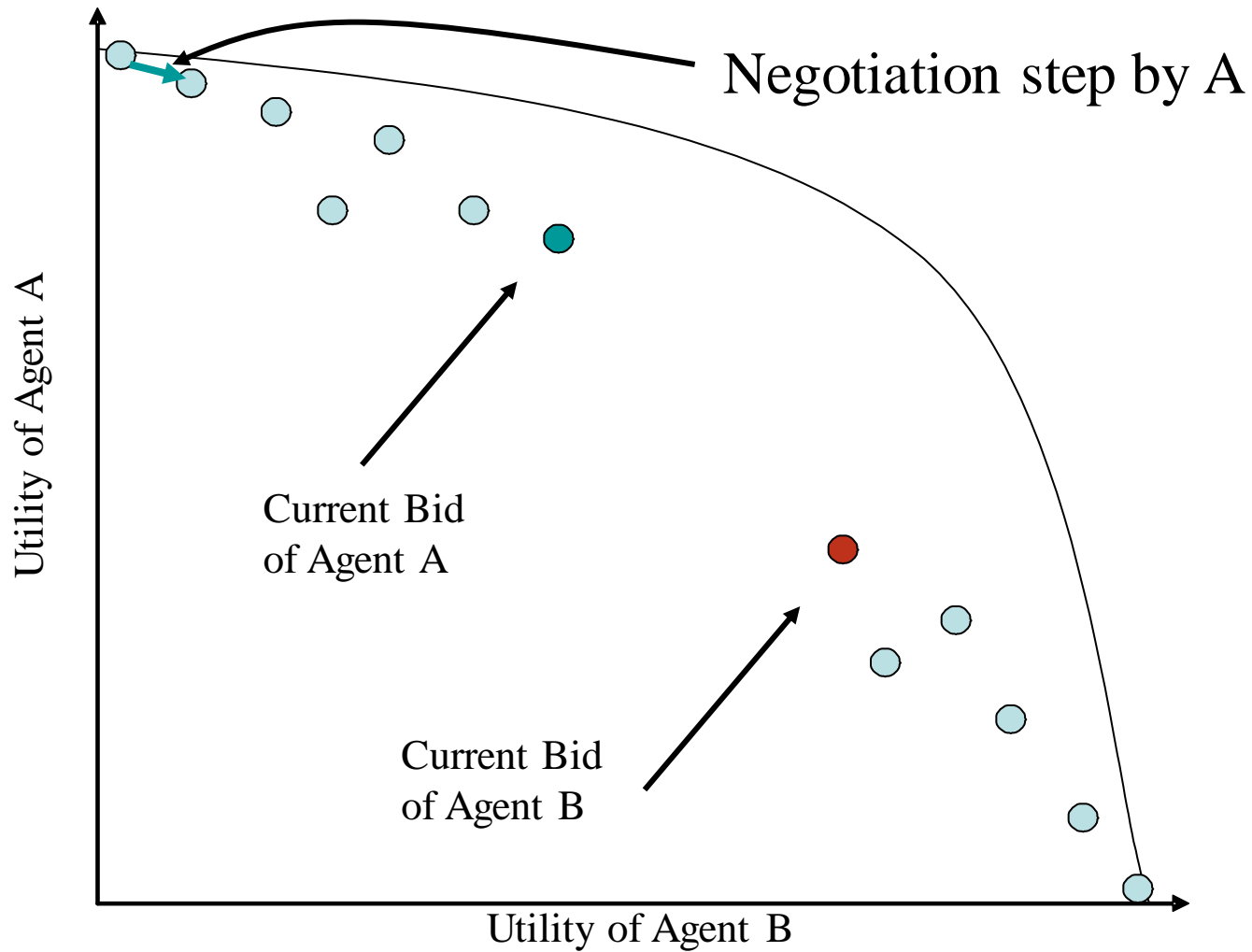
# Analysis of negotiation strategies

- What kind of bids to **make**:
- Process analysis
  - Step analysis
  - Dynamic properties
- What kind of bids to **accept**:
- Outcome analysis
  - Nash product
  - Kalai-Smorodinsky
  - Pareto-optimal

# Outcome Analysis



# Negotiation traces

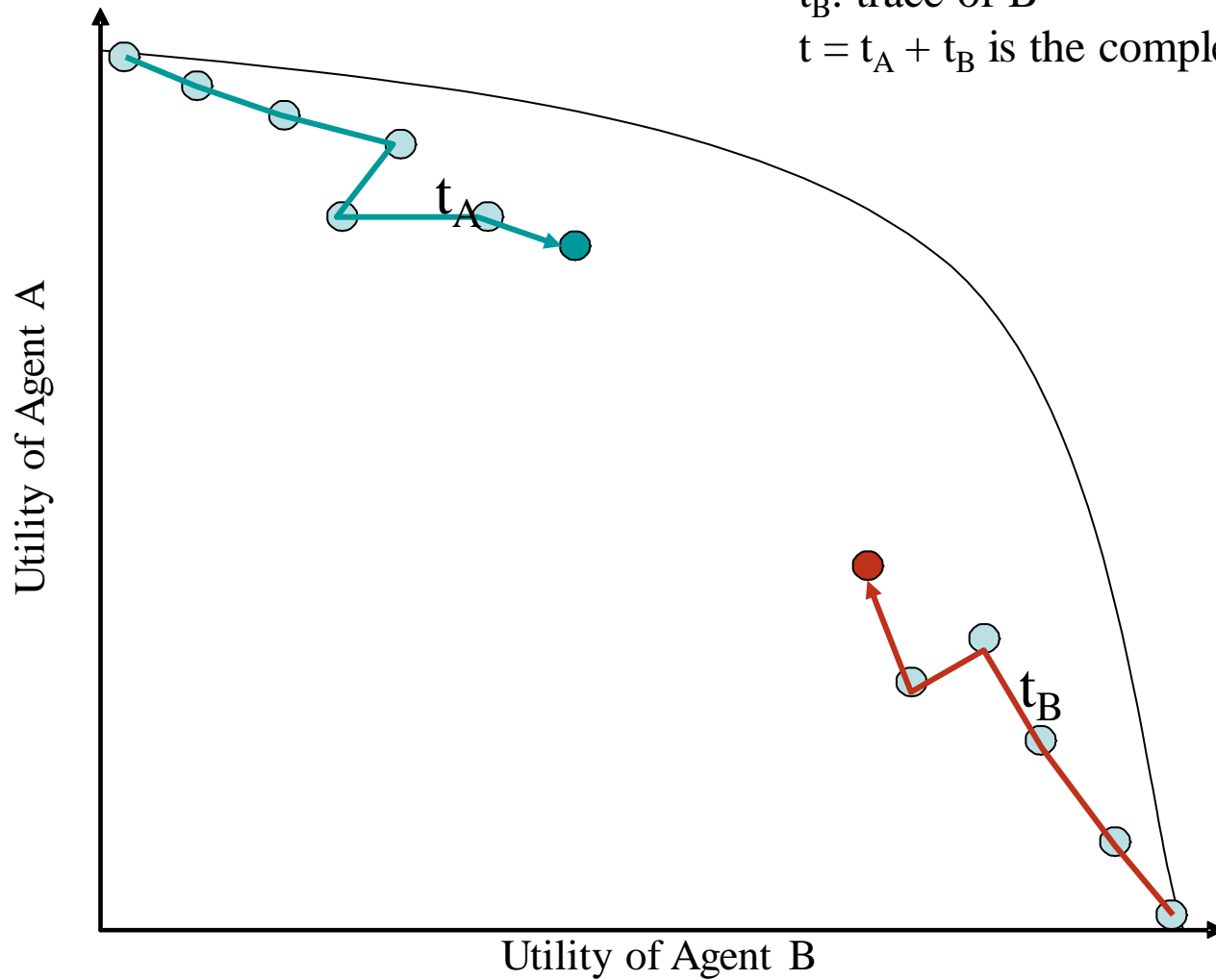


# Negotiation traces

$t_A$ : trace of A

$t_B$ : trace of B

$t = t_A + t_B$  is the complete nego trace



# Utility, negotiation steps, and traces

$U_S(b)$ : utility of "Self" for bid  $b$

$U_O(b)$ : utility of "Other" for  $b$

$\Delta_a(b, b') = U_a(b') - U_a(b)$ ,  $a \in \{S, O\}$

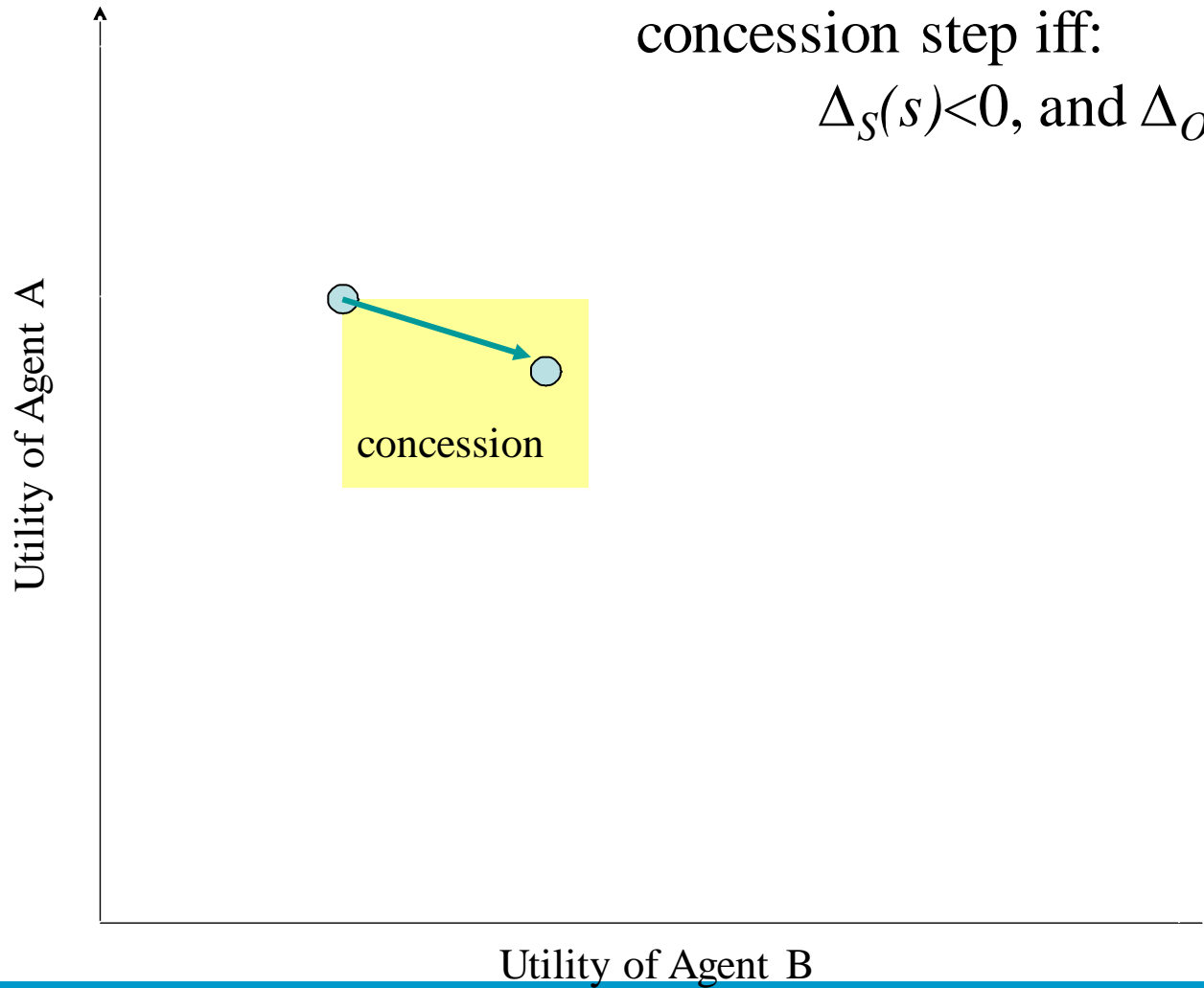
$\Delta_a(s)$ :  $\Delta_a(b, b')$  for a step  $s = b \rightarrow b'$ .

A trace  $t$  is a series of negotiation steps, i.e., transitions  $b \rightarrow b'$  with  $b, b'$  offers.

# Concession step

denoted by  $(S-, O\geq)$ ,  $s$  is a concession step iff:

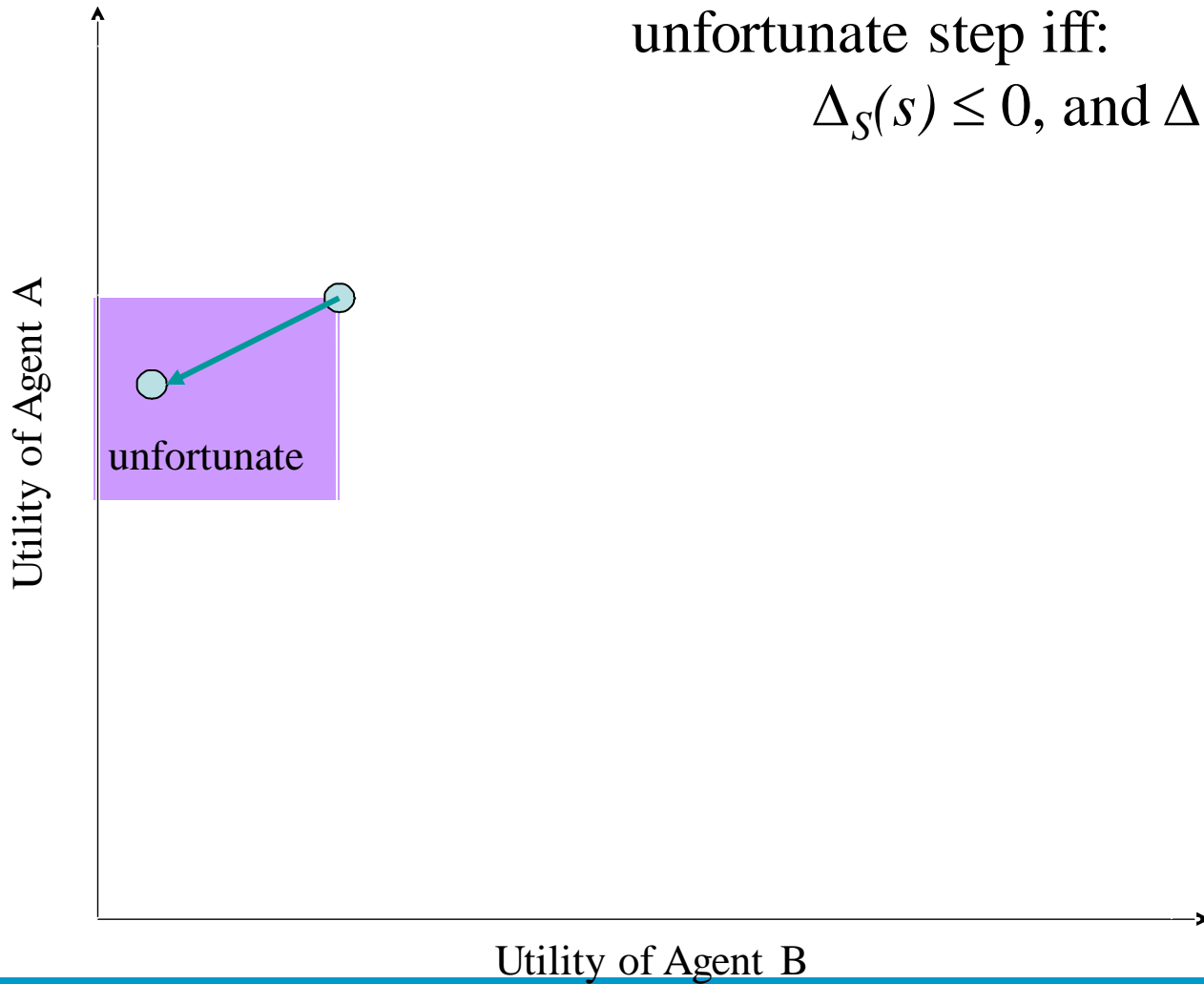
$$\Delta_S(s) < 0, \text{ and } \Delta_O(s) \geq 0.$$



# Unfortunate step

denoted by  $(S \leq, O-)$ ,  $s$  is an unfortunate step iff:

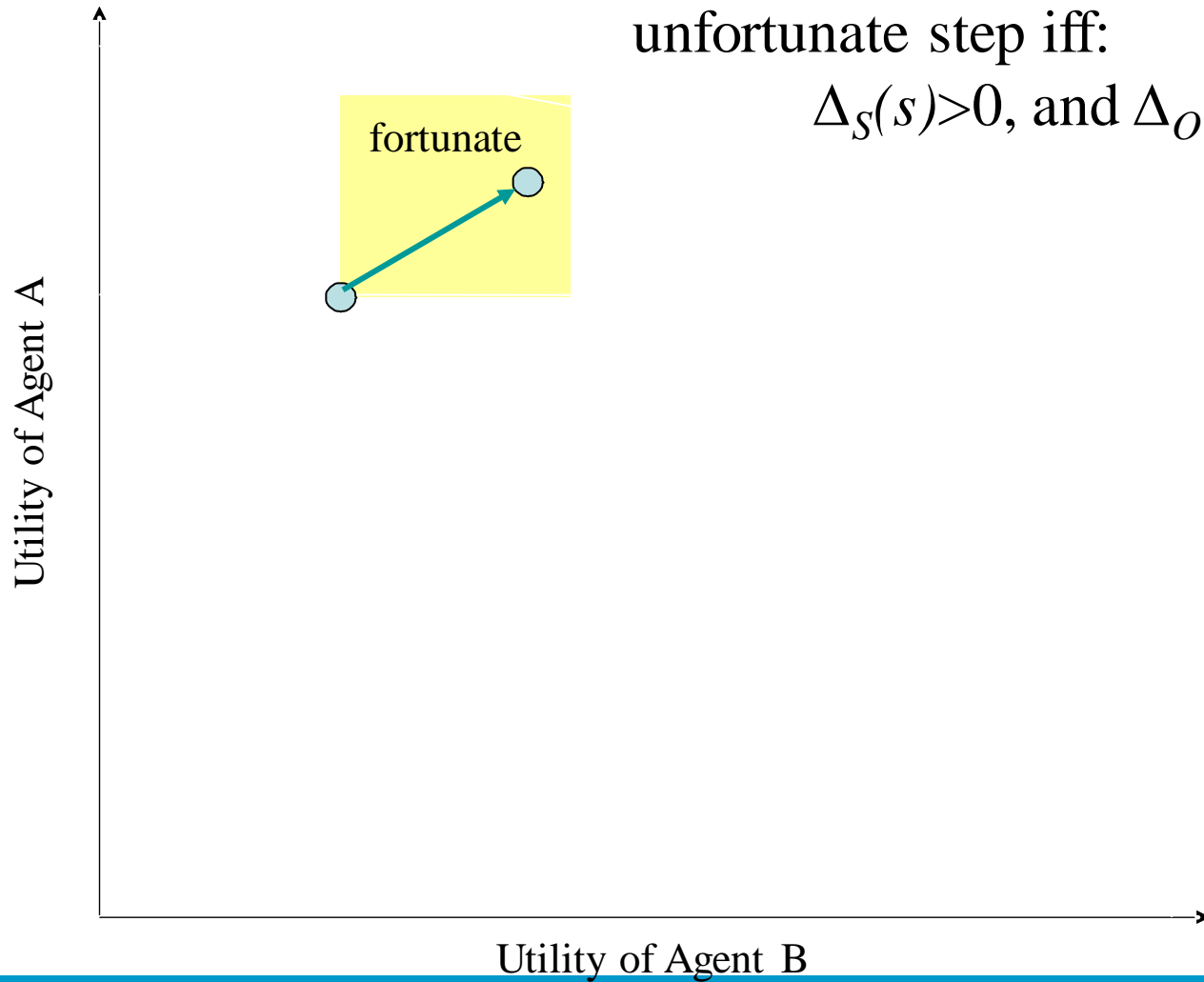
$$\Delta_S(s) \leq 0, \text{ and } \Delta_O(s) < 0.$$



# Fortunate step

denoted by  $(S+, O+)$ ,  $s$  is an unfortunate step iff:

$$\Delta_S(s) > 0, \text{ and } \Delta_O(s) > 0.$$

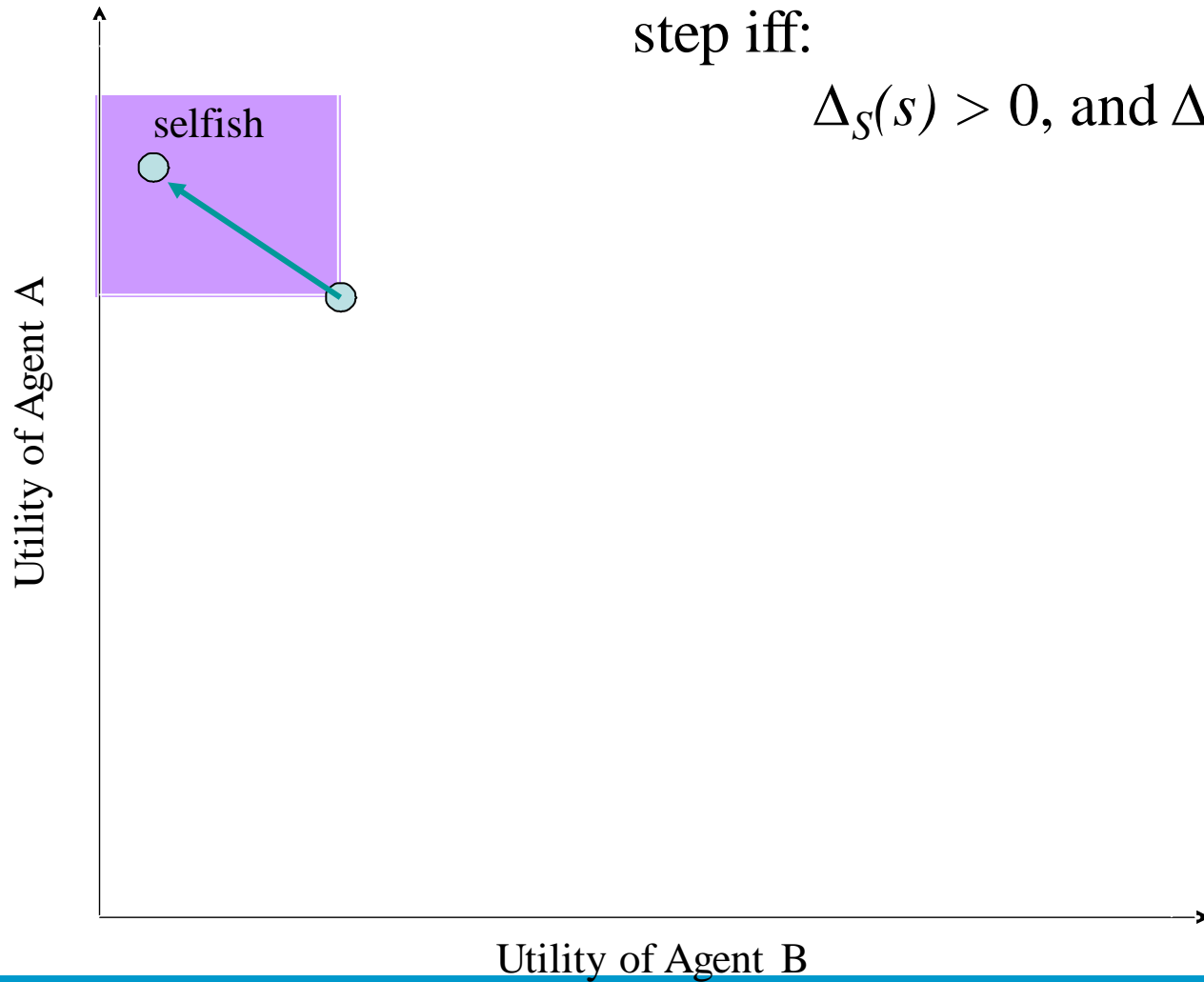




# Selfish step

denoted by  $(S+, O\leq)$ ,  $s$  is a selfish step iff:

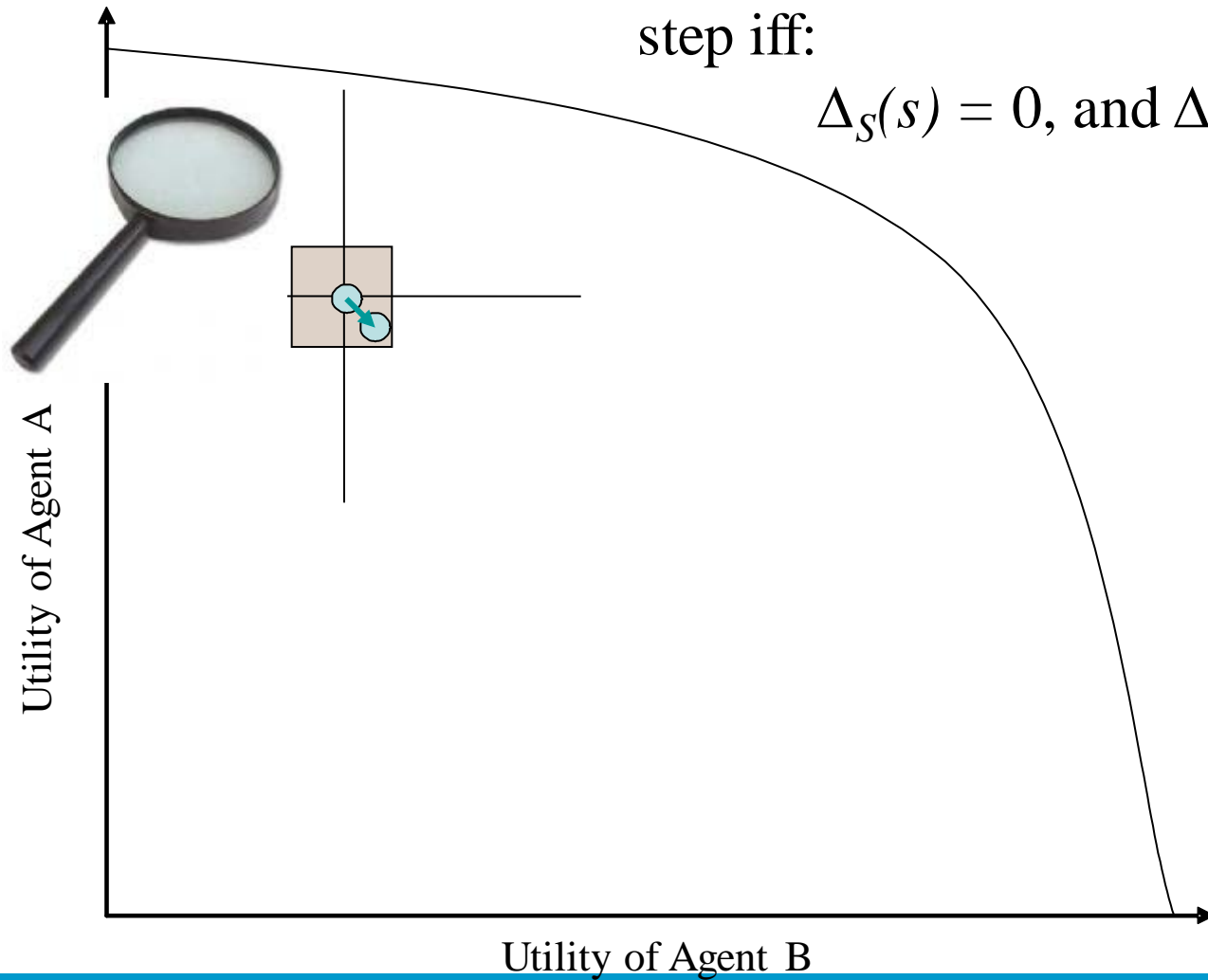
$$\Delta_S(s) > 0, \text{ and } \Delta_O(s) \leq 0.$$



# Silent step

denoted by  $(S=, O=)$ ,  $s$  is a silent step iff:

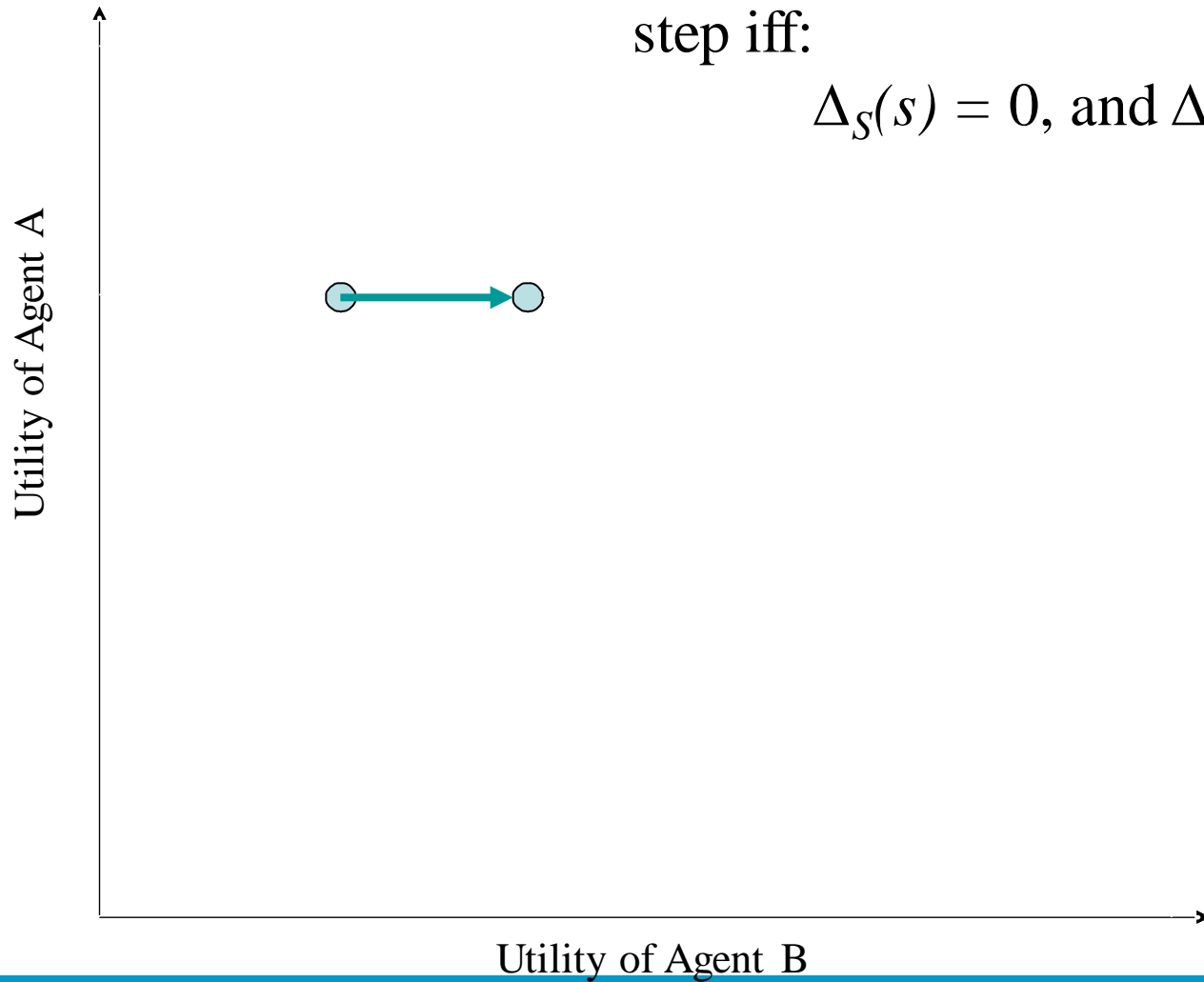
$$\Delta_S(s) = 0, \text{ and } \Delta_O(s) = 0.$$



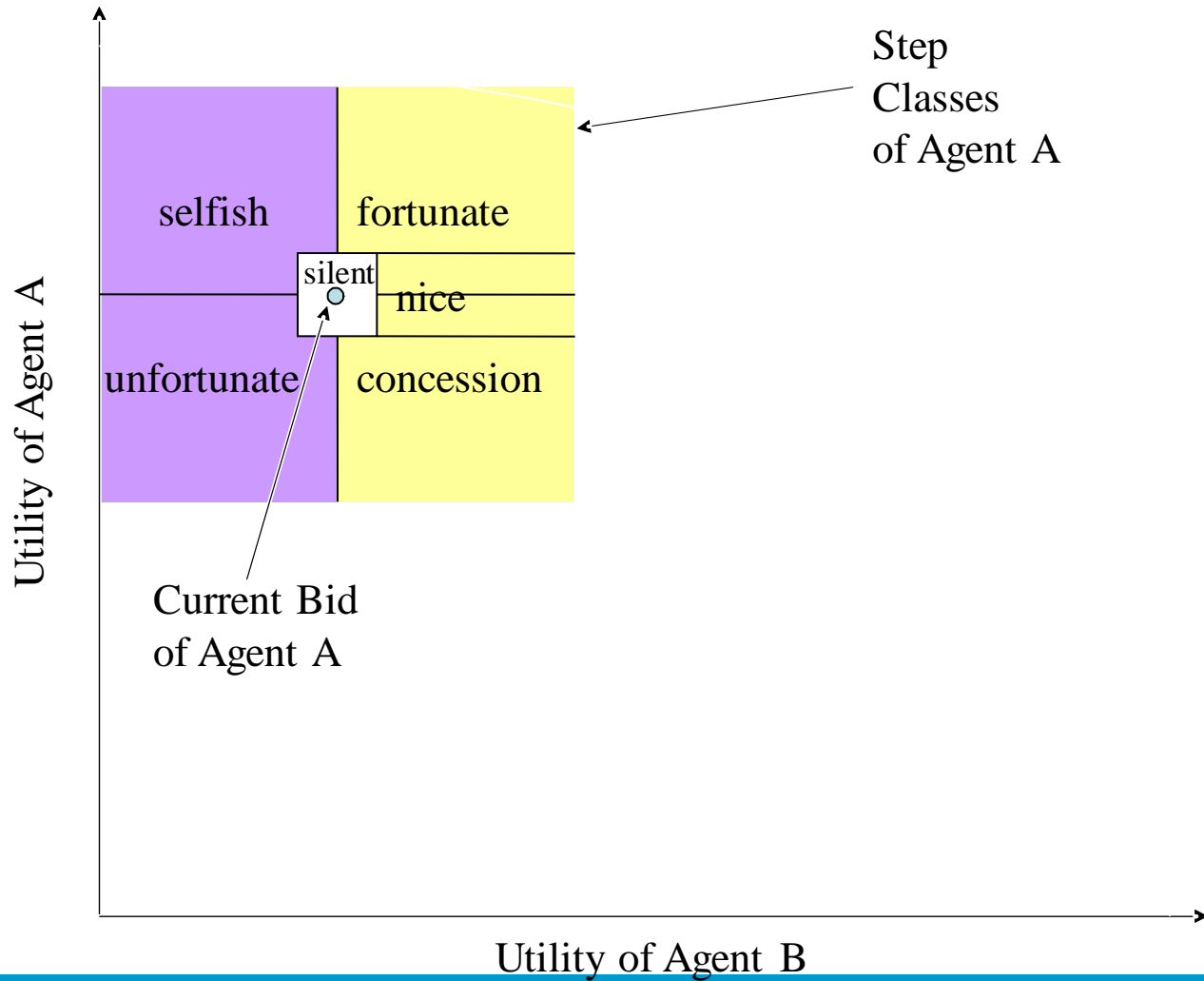
# Nice step

denoted by  $(S=, O+)$ ,  $s$  is a nice step iff:

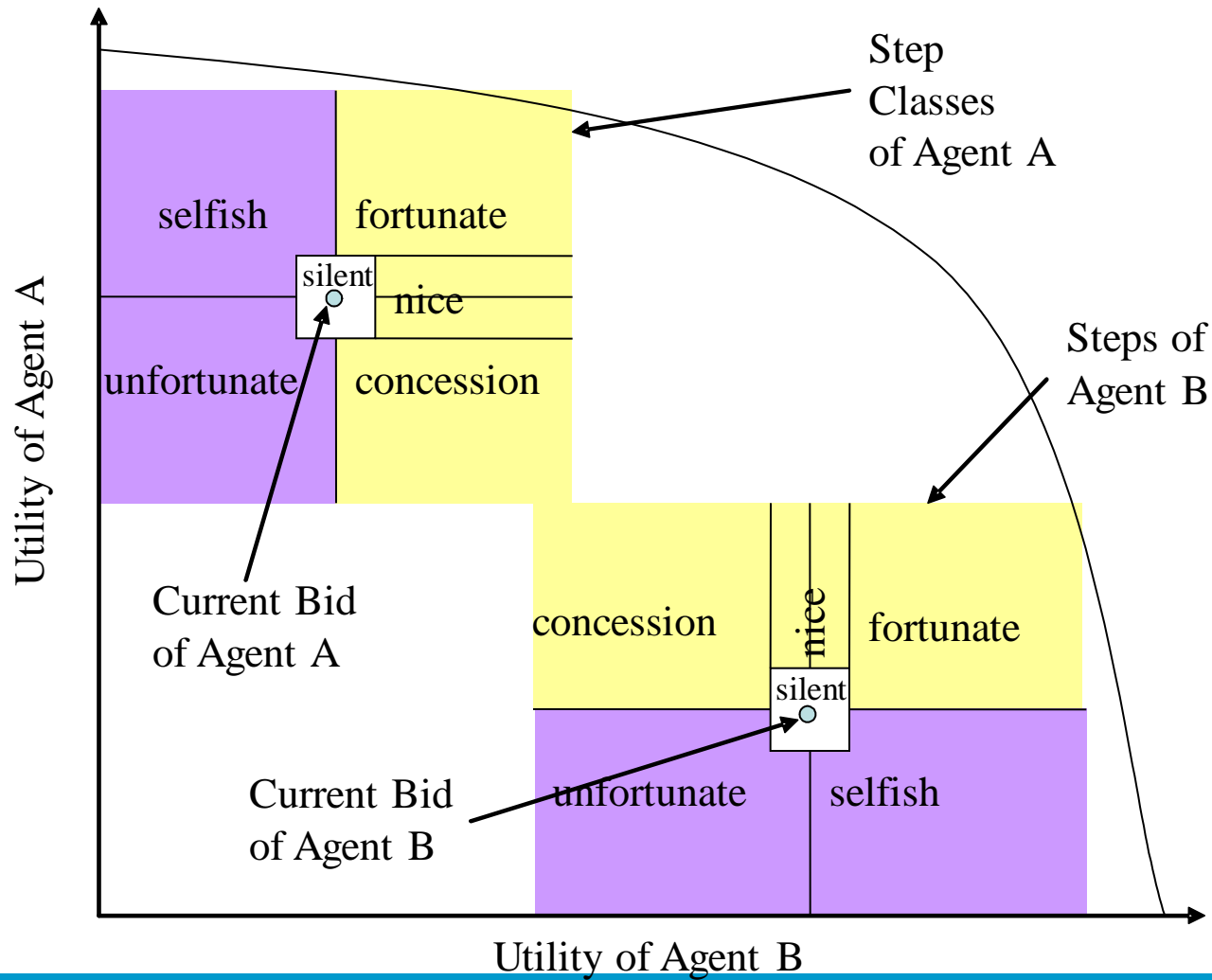
$$\Delta_S(s) = 0, \text{ and } \Delta_O(s) > 0.$$



# Classification of negotiation steps



# Classification of negotiation steps



# Sensitivity to Opponent Preferences

A rational negotiator would try to make *fortunate, nice, or concession steps*.

$$\text{sensitivity}_a(t) = \frac{\%_{Fortunate}(t_a) + \%_{Nice}(t_a) + \%_{Concession}(t_a)}{\%_{Selfish}(t_a) + \%_{Unfortunate}(t_a) + \%_{Silent}(t_a)}$$

- In case no selfish, unfortunate or silent steps are made we stipulate that  $\text{sensitivity}_a(t) = \infty$ .
- If  $\text{sensitivity}_a(t) < 1$ , then an agent is more or less insensitive to opponent preferences;
- If  $\text{sensitivity}_a(t) > 1$ , then an agent is more or less sensitive to the opponent's preferences, with complete sensitivity for  $\text{sensitivity}_a(t) = \infty$ .

# The Three Strategies

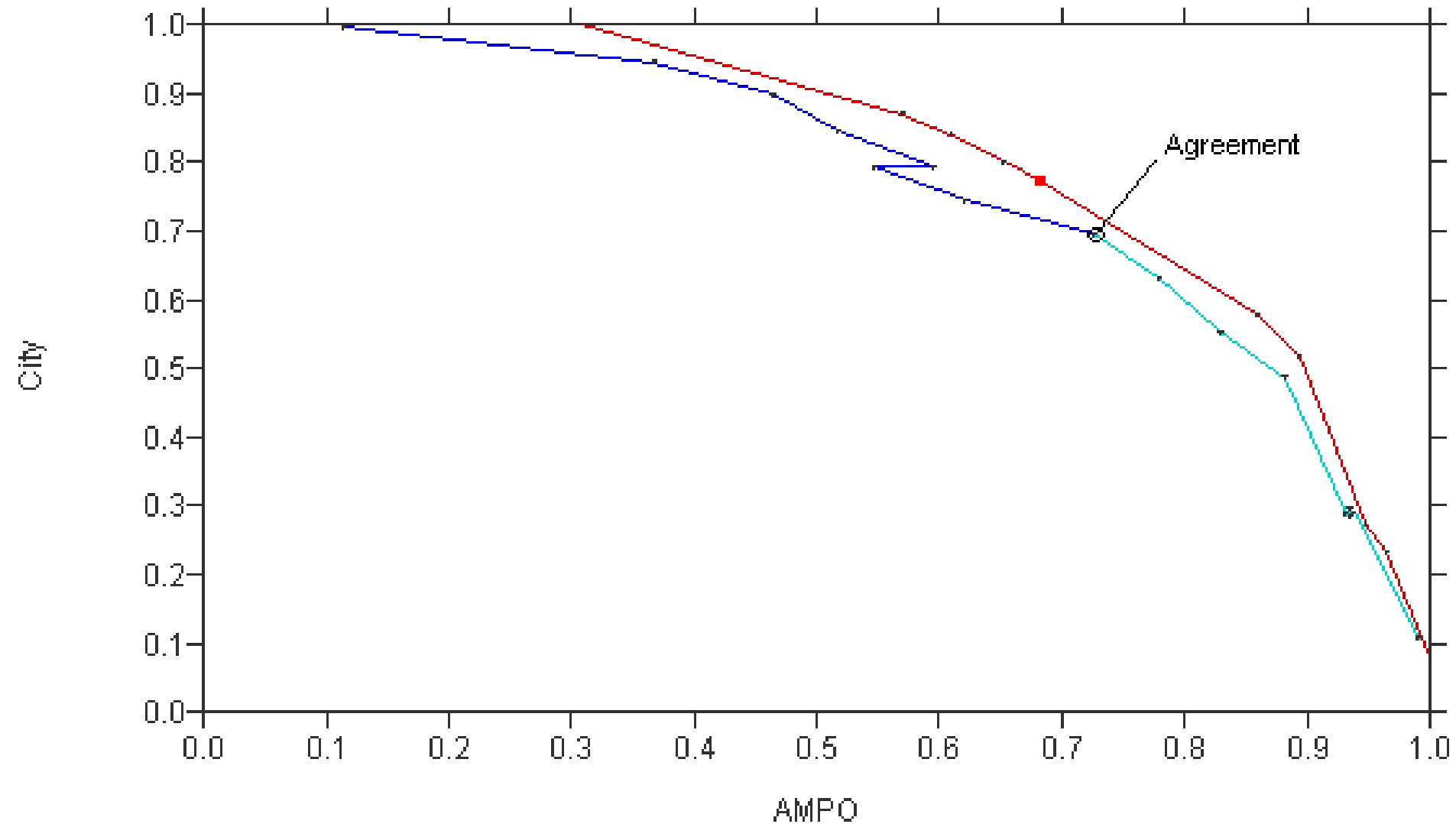
- **ABMP** [Jonker, Treur, 2001]
  - does not use any knowledge about opponent;
  - calculates concession step on every round of negotiation;
  - always make concession on every issue;
- **Trade-off** [Faratin, Sierra, Jennings, AIJ 2002]
  - uses domain knowledge;
  - tries to find bids on the same iso-level of own utility function that is closer to the current opponent's bid, makes concession of 0.05 if stuck;
  - uses opponent's bid to make trade-offs;
- **Random-Walker** [Hindriks, Jonker, Tykhonov, IAT 2007]
  - Selects values of issues randomly
  - Proposes only those bids that have own utility  $>0.6$

# The Three Domains

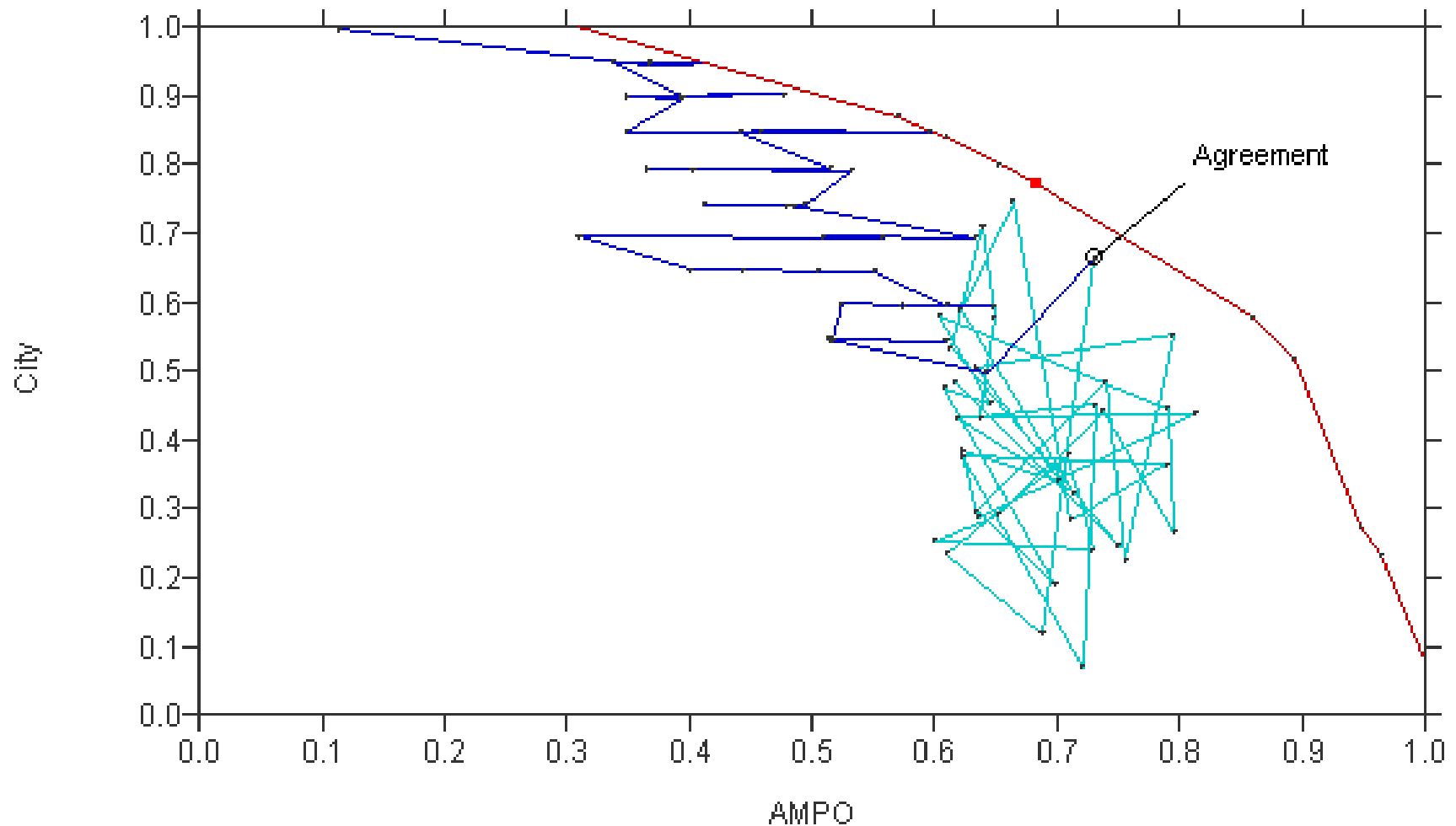
- Second hand car selling domain:
  - 5 issues (4 discrete issues and price issue),
  - only the buyer's preferences and the price issue are predictable
- Service-oriented negotiation (SON):
  - 4 continues issues;
  - all issues are predictable;
- AMPO vs City
  - 10 issues;
  - only 8 issues are predictable;



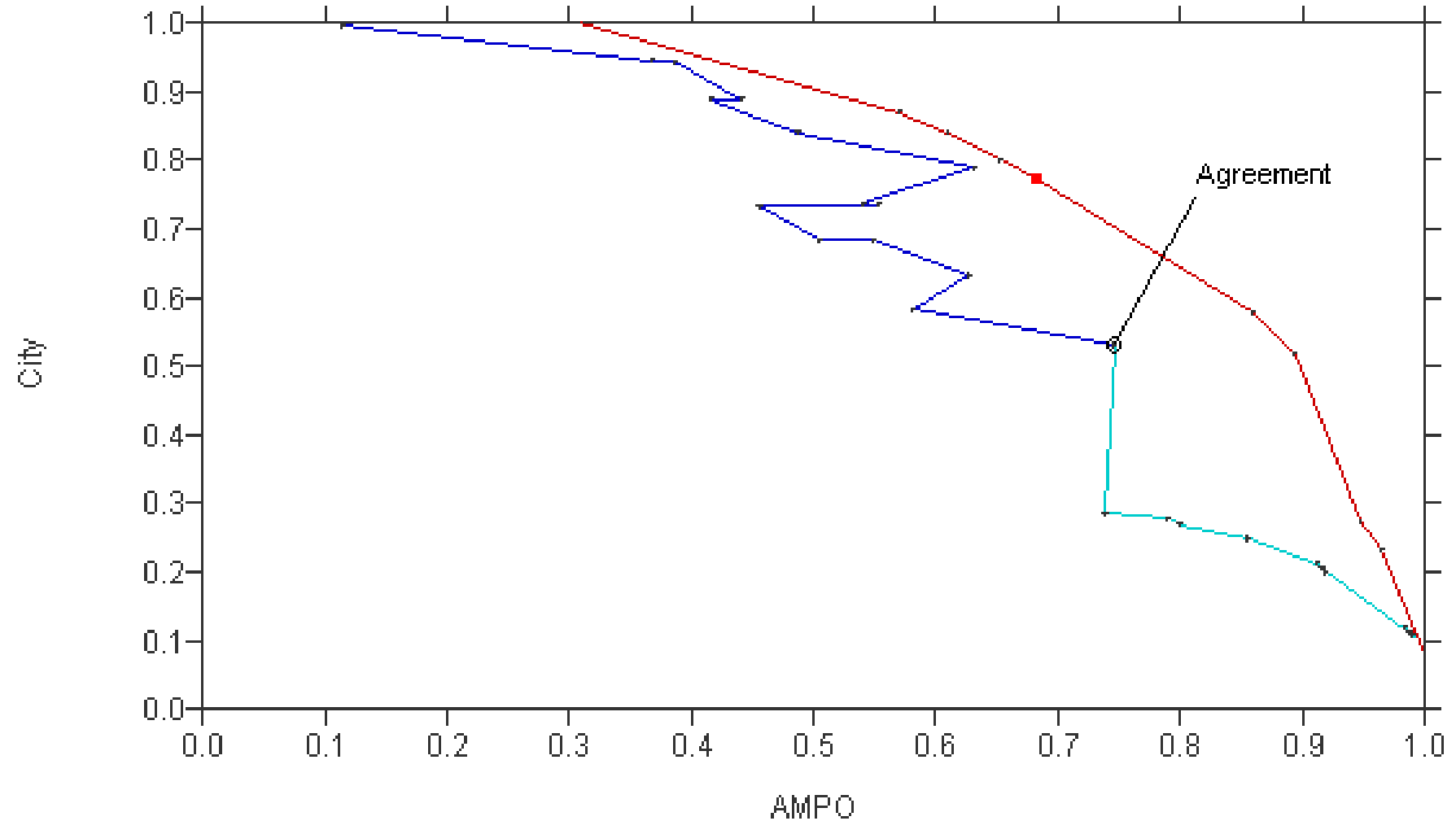
# Trade-Off (City) vs Trade-Off strategy (AMPO)



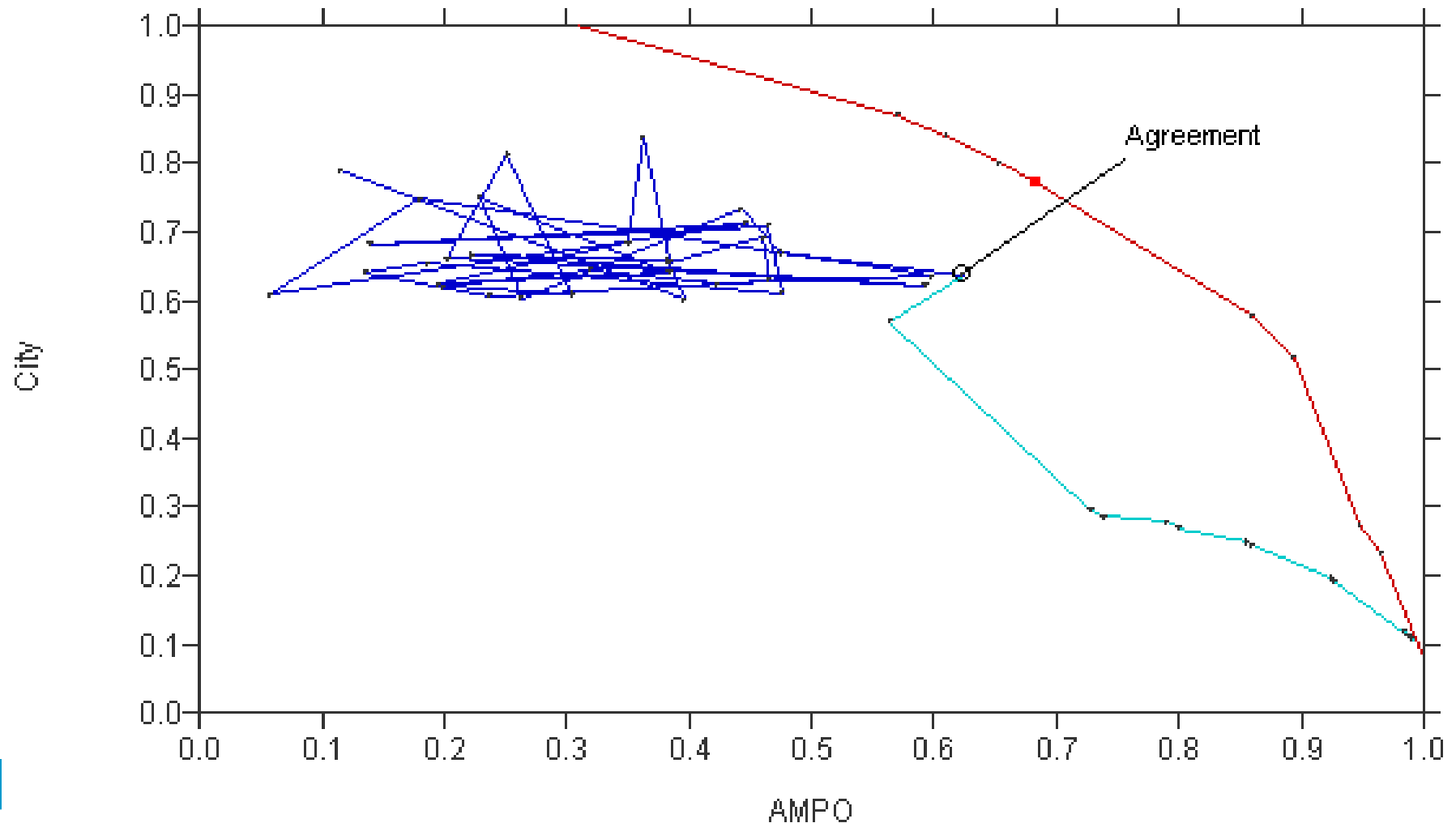
# Trade-Off (City) vs Random Walker (AMPO)



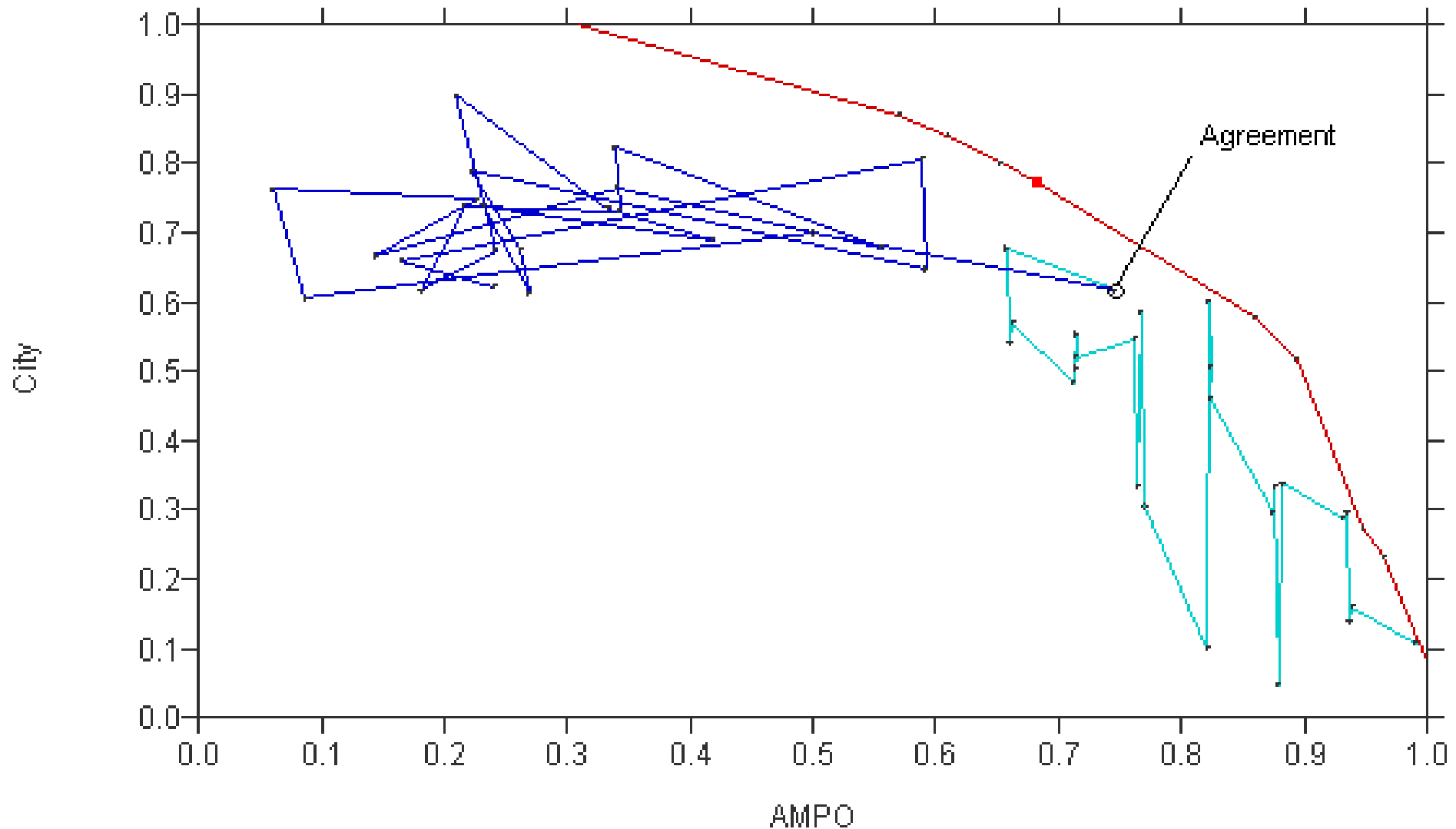
# Trade-Off (City) vs ABMP (AMPO)



# Random Walker (City) vs ABMP (AMPO)



# Random Walker (City) vs Trade-Off strategy (AMPO)



# Outcome Utility

- Overall utility:
  - ABMP 0.72,
  - Trade-Off 0.74, and
  - Random Walker 0.69.
- Trade-Off:
  - Outperforms ABMP on the SON domain with complete information and on the AMPOvsCity domain;
  - Underperforms wrt ABMP on the second hand car domain due to wrong weights and unpredictable issues;
- ABMP:
  - Strong on the second hand car domain;
  - Underperforms on the SON domain.

# Conclusions

- Want to negotiate efficiently? Know your partner!
- It is impossible to avoid unfortunate steps without sufficient domain knowledge or opponent knowledge.
- In the analysis of negotiation strategies, not only the outcome of a negotiation is relevant, but also the bidding process itself is important.
- When developing a general negotiation strategy test against many opponents and in many domains.

(Baarslag 2014): Tim Baarslag, Alexander Dirkzwager, Koen Hindriks, and Catholijn Jonker. The significance of bidding, accepting and opponent modeling in automated negotiation. In: 21st European Conference on Artificial Intelligence, 2014.

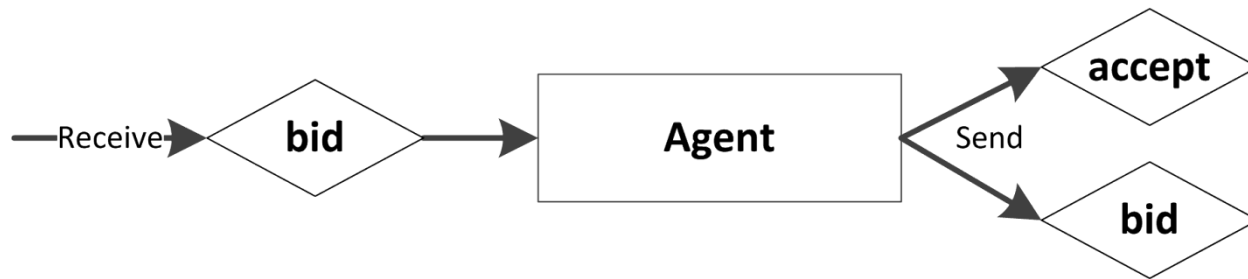
## THE BOA FRAMEWORK



# Introduction

In search of an efficient automated negotiator

- Challenge: from the outside, agent architectures are essentially a 'black box'.



- A negotiation strategy is a result of complex interaction between various components, of which the individual performance may vary significantly.
- Overall performance measures make it hard to pinpoint reasons for success.

# Introduction

## Component-based negotiation

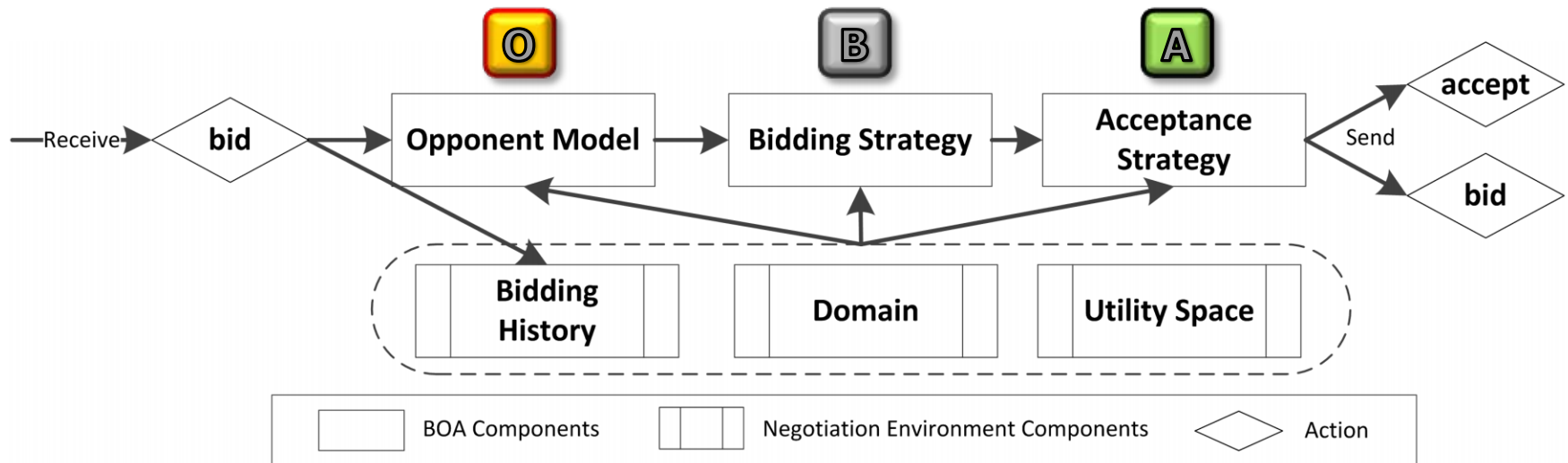
- Many agent strategies are comprised of a fixed set of modules; generally, a distinction is made between three different modules:



- One that decides which set of bids could be proposed next;
- One that tries to guess the opponent's preferences and takes this into account when selecting an offer to send out.
- One module that decides whether the opponent's bid is acceptable;

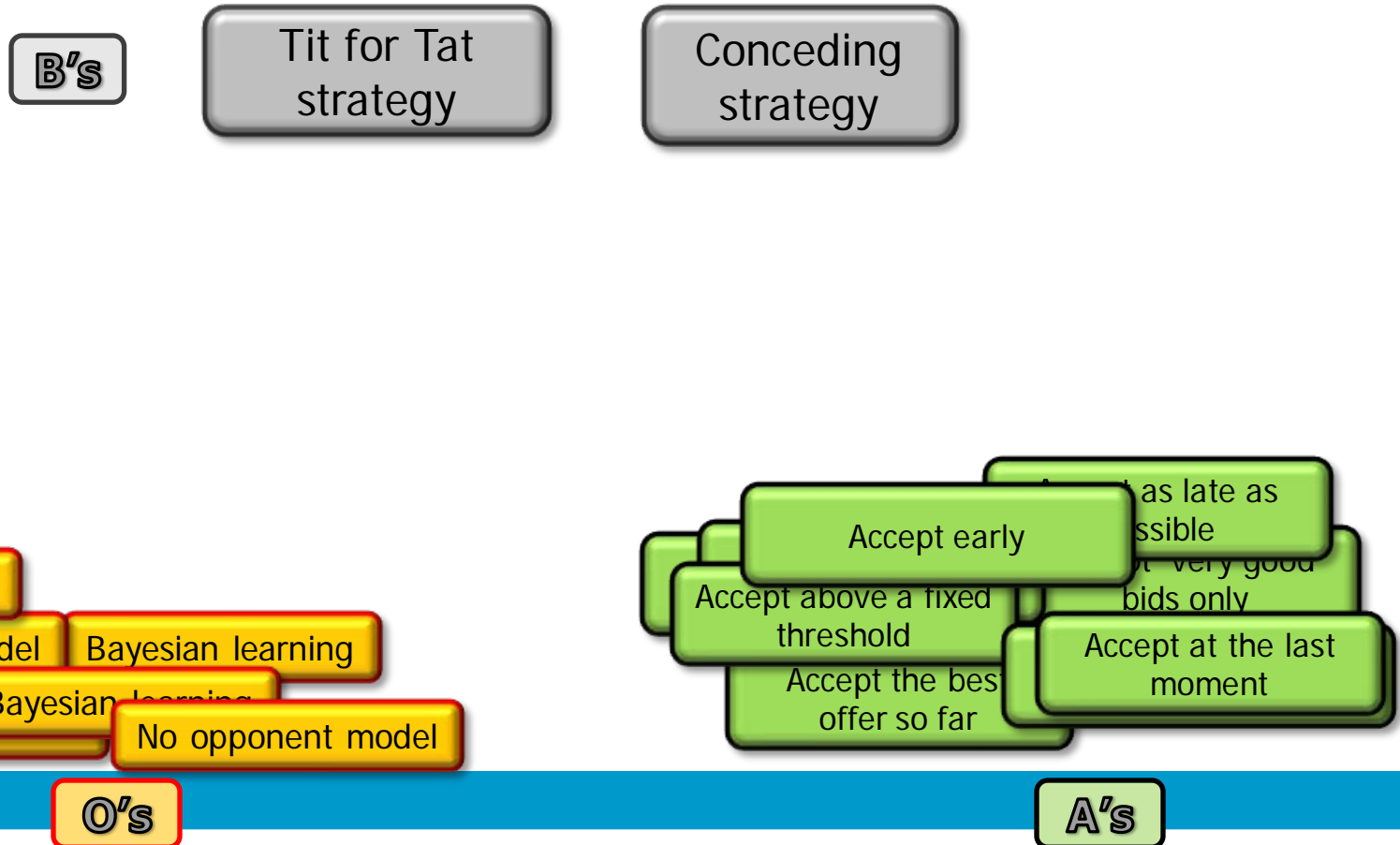
# The BOA framework

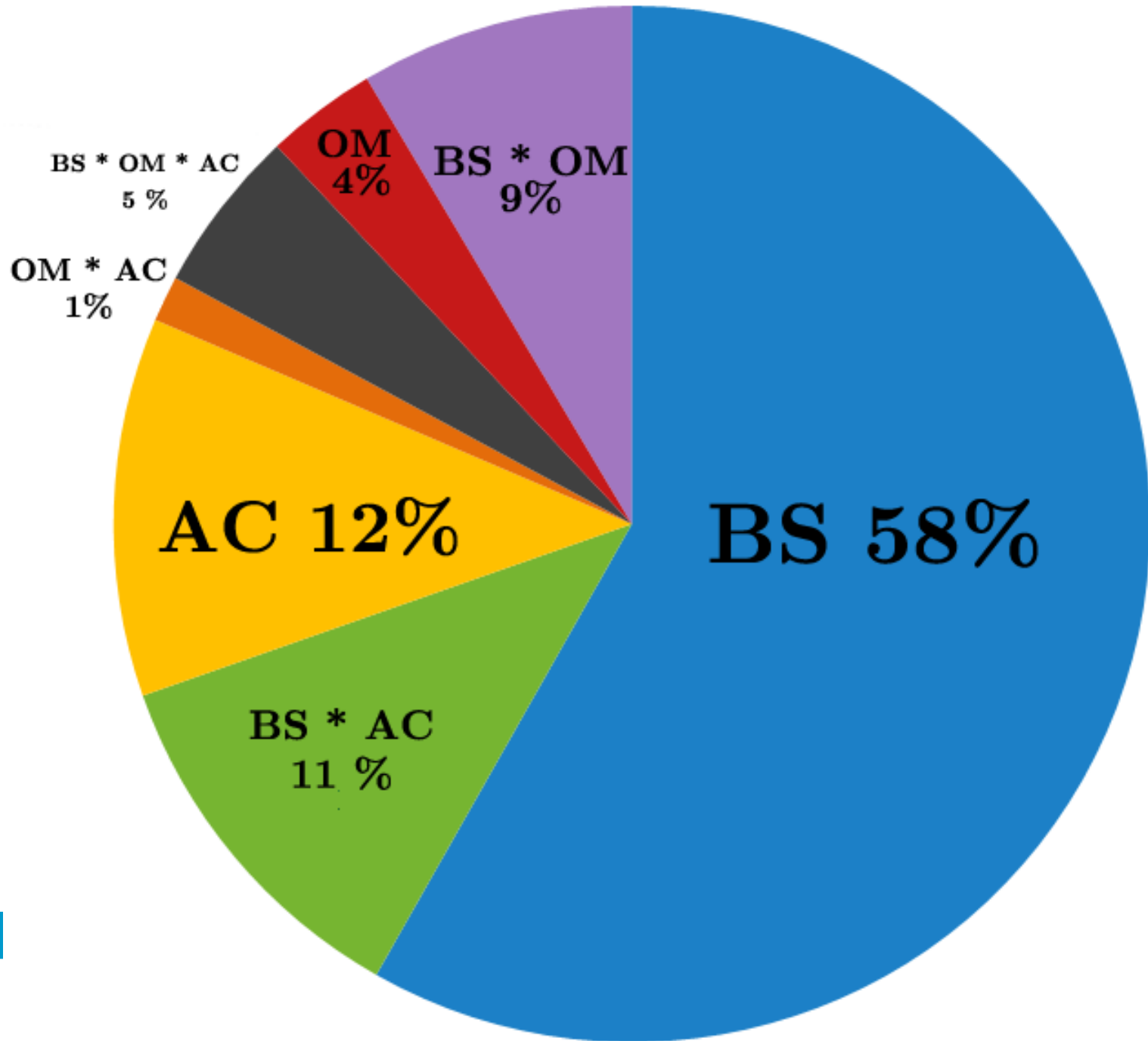
## Negotiation flow



# Applying the BOA Framework

Combining components





# Exam material

- Klein et al., 2003
- Hindriks et al., 2011
- These slides

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[http://ebusiness.mit.edu/research/Briefs/4Klein\\_Negotiation\\_Brief\\_Final.pdf](http://ebusiness.mit.edu/research/Briefs/4Klein_Negotiation_Brief_Final.pdf)

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Raiffa, H., The art and science of negotiation. 1982, Cambridge, Mass.: Belknap Press of Harvard University Press. x, 373.

[Baarslag T.](#) 2014. What to Bid and When to Stop. Delft University of Technology. <http://mmi.tudelft.nl/sites/default/files/thesis.pdf>

Hindriks KV, Jonker CM, Tykhonov D, (2011). Let's dans! An analytic framework of negotiation dynamics and strategies, Web Intelligence and Agent Systems, 9, pages:319-335 (see reading material on blackboard for the paper)