

BASIC PROBABILITY QUESTIONS

1. Basic Probability - Coin Toss

Q: A coin is tossed once. What is the probability of getting a head?

A: $1/2 = 0.5$

2. Basic Probability - Dice Roll

Q: A die is rolled once. What is the probability of getting a number greater than 4?

A: Favorable outcomes = {5, 6} $\Rightarrow P = 2/6 = 1/3 \approx 0.333$

3. Conditional Probability - Coin Toss

Q: A coin is tossed twice. What is the probability of getting heads on the first toss given that the second toss is a tail?

A: $P(\text{First H} \mid \text{Second T}) = 1/2 = 0.5$

4. Conditional Probability - Card Draw

Q: A card is drawn from a standard deck. Given that the card is red, what is the probability that it is a heart?

A: $P(\text{Heart} \mid \text{Red}) = 13/26 = 0.5$

5. Conditional Probability - Dice Roll

Q: A die is rolled. Given that the number is even, what is the probability it is a 2?

A: $P(2 \mid \text{Even}) = 1/3 \approx 0.333$

6. Bayes' Theorem - Coin Bag Example

Q: One bag with a fair coin, one with a double-headed coin. A head is observed. Probability it came from double-headed coin?

A: $P(\text{Bag2} \mid \text{Head}) = 2/3 \approx 0.667$

7. Bayes' Theorem - Medical Test

Q: Disease rate = 0.001, test accuracy = 99%. Test is positive. What's $P(\text{Disease} \mid \text{Positive})$?

A: $P = 0.00099 / (0.00099 + 0.00999) \approx 0.09$ or 9%

8. Bayes' Theorem - Weather Prediction

Q: $P(\text{Rain}) = 0.7$, $P(\text{Correct forecast} \mid \text{Rain}) = 0.9$

A: Directly given: $P(\text{Correct} \mid \text{Rain}) = 0.9$ or 90%

9. Bayes' Theorem - Student Test Result

Q: 70% prepare. $P(\text{Pass} \mid \text{Prepared}) = 0.9$, $P(\text{Pass} \mid \text{Unprepared}) = 0.3$. Student passed.

A: $P(\text{Prepared} \mid \text{Passed}) = 0.875$ or 87.5%

10. Conditional Probability from Joint Probability

Q: 60% boys (70% like math), 40% girls (50% like math). Given likes math, $P(\text{student is boy})$?

A: $P(\text{Boy} \mid \text{Likes Math}) = 0.42 / 0.62 \approx 0.677$ or 67.7%