

# mortality\_analysis

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## Evaluation procedure

1. calculate the ratio between mae/rmse of reconciled forecasts and mae/rmse of base forecasts
2. mae/rmse of the total, mean, max and min mae/rmse of bottom series
3. summarised over specific domains

## mint and wlsv vs ols and wlss

OLS and structural scaling are more likely to produce more extreme results.

robustness: wlsv > mint > wlss > ols

```
ratio %>% group_by(rf_method, accuracy_method) %>%  
  summarise(total= mean(total), bottom_max=mean(bottom_max),  
            bottom_min=mean(bottom_min), bottom_mean=mean(bottom_mean)) %>%  
  arrange(accuracy_method)
```

```
## `summarise()` has grouped output by 'rf_method'. You can override using the  
## `.groups` argument.
```

```
## # A tibble: 8 x 6  
## # Groups:   rf_method [4]  
##   rf_method accuracy_method total bottom_max bottom_min bottom_mean  
##   <chr>      <chr>      <dbl>    <dbl>    <dbl>    <dbl>  
## 1 mint      mae          0.857      1.63    0.740    1.01  
## 2 ols       mae          0.956     27.9    0.589    2.20  
## 3 wlss      mae          0.862     13.4    0.642    1.48  
## 4 wlsv      mae          0.846      1.41    0.818    1.00  
## 5 mint      rmse          0.945      1.51    0.764    1.00  
## 6 ols       rmse          0.976     22.9    0.627    2.01  
## 7 wlss      rmse          0.940     11.1    0.675    1.40  
## 8 wlsv      rmse          0.944      1.36    0.844    1.00
```

In general, the improvement of some series comes with the cost of some other series. It's very unlikely that reconciliation improves all the series.

```
ratio %>% filter(bottom_max <= 1.01) %>% select(representator, rf_method, distance, cluster, total, bot  
  arrange(bottom_max)
```

```
## # A tibble: 26 x 9  
##   representator rf_method distance cluster total bottom_mean bottom_max  
##   <chr>         <chr>    <chr>    <chr>    <dbl>    <dbl>    <dbl>  
## 1 ""          wlsv      ""      ""      1.04     0.999    1.00  
## 2 "forecast"  wlsv      "uncorrelati~ "kmedo~ 1.04     0.998    1.00
```

```
## 3 "forecast"      wlsv      "uncorrelati~ "kmedo~ 1.04      0.998      1.00
## 4 "forecast"      wlsv      "uncorrelati~ "kmedo~ 1.04      0.999      1.00
## 5 ""              wlsv      ""              ""        1.03      1.00      1.00
## 6 "forecast"      wlsv      "uncorrelati~ "kmedo~ 1.03      0.998      1.00
## 7 "error.features" wlsv      "dtw"          "kmedo~ 1.46      0.992      1.00
## 8 "error.features" wlsv      "dtw"          "kmedo~ 1.46      0.991      1.00
## 9 "forecast"      wlsv      "uncorrelati~ "kmedo~ 1.03      0.999      1.00
## 10 "error.features" wlsv      "dtw"          "kmedo~ 1.45      0.991      1.00
## # i 16 more rows
## # i 2 more variables: bottom_min <dbl>, batch <int>
```

## K-medoids (only mint, rmse)

```
tmp <- ratio %>% filter(startsWith(cluster, "kmedoids"), rf_method == "mint", accuracy_method == "rmse")
  rowwise() %>%
  mutate(n_middle = NROW(other$S)) %>%
  select(representator, distance, cluster, total, bottom_mean, bottom_max, bottom_min, n_middle, batch)
  ungroup()
```

## distance

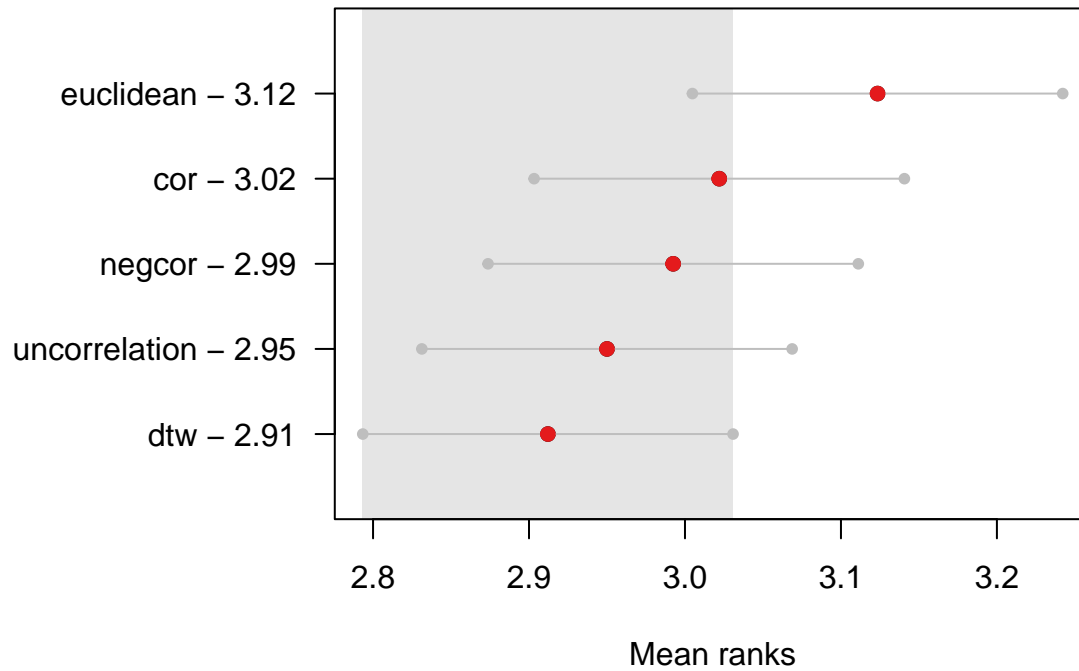
```
tmp %>% group_by(distance) %>% summarise_at(c("total", "bottom_mean", "bottom_max", "bottom_min"), c(me
```

```
## # A tibble: 5 x 5
##   distance      total_mean bottom_mean_mean bottom_max_mean bottom_min_mean
##   <chr>          <dbl>          <dbl>          <dbl>          <dbl>
## 1 cor           0.956          0.998          1.46          0.767
## 2 dtw           0.952          1.00          1.55          0.776
## 3 euclidean     0.959          0.999          1.49          0.768
## 4 negcor        0.946          1.00          1.60          0.757
## 5 uncorrelation 0.951          1.01          1.52          0.760
```

```
mcb <- function(x) {
  tsutils::nemenyi(x, plottype = "vmcb")
}
```

```
## total
tmp %>% select(representator, cluster, batch, distance, total) %>%
  tidyr::pivot_wider(names_from = "distance", values_from = "total") %>%
  select(-representator, -cluster, -batch) %>%
  mcb()
```

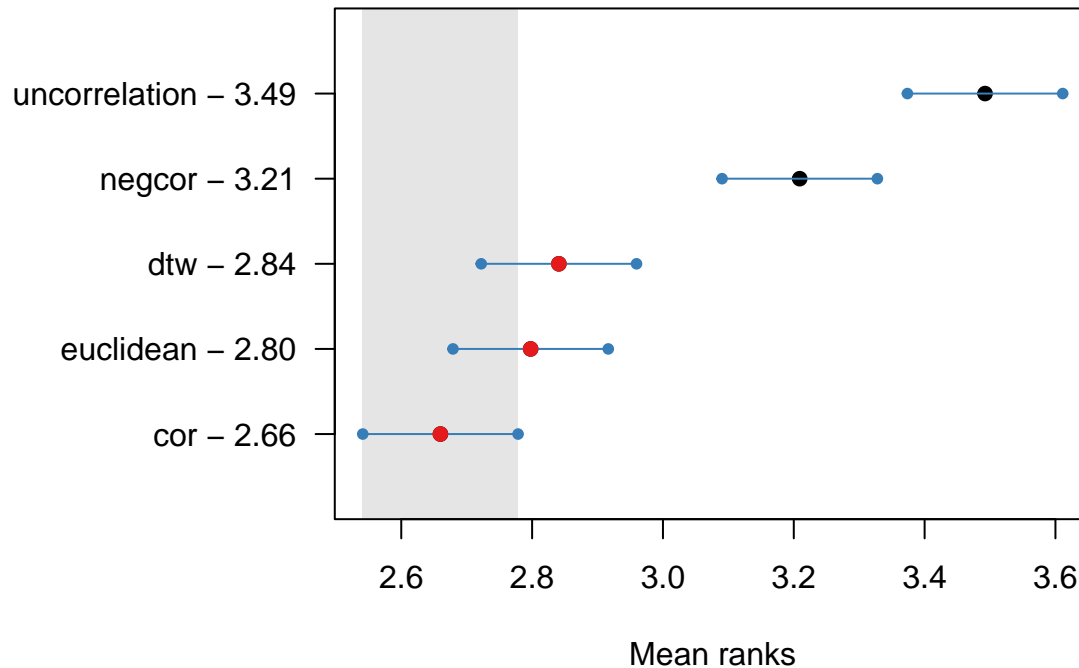
**Friedman: 0.139 (H0: Identical)**  
**Critical distance: 0.237**



```
## Friedman and Nemenyi Tests
## The confidence level is 5%
## Number of observations is 660 and number of methods is 5
## Friedman test p-value: 0.1394 - H0: Identical
## Critical distance: 0.2374

tmp %>% select(representator, cluster, batch, distance, bottom_mean) %>%
  tidyr::pivot_wider(names_from = "distance", values_from = "bottom_mean") %>%
  select(-representator, -cluster, -batch) %>%
  mcb()
```

**Friedman: 0.000 (Ha: Different)**  
**Critical distance: 0.237**



```
## Friedman and Nemenyi Tests
## The confidence level is 5%
## Number of observations is 660 and number of methods is 5
## Friedman test p-value: 0.0000 - Ha: Different
## Critical distance: 0.2374
```

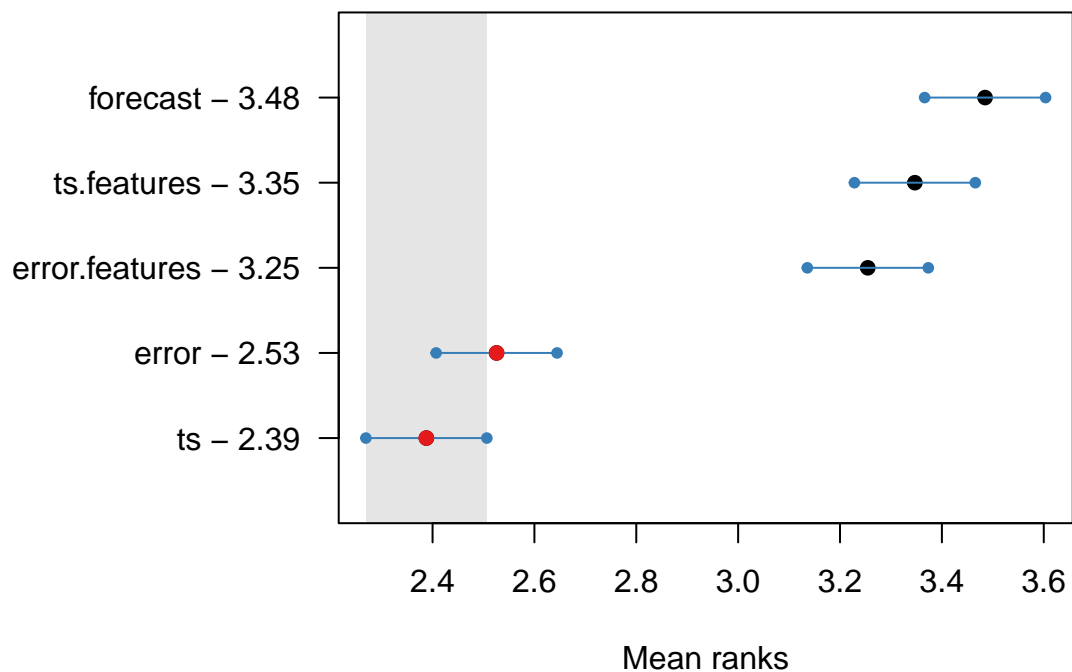
representator

```
tmp %>% group_by(representator) %>% summarise_at(c("total", "bottom_mean", "bottom_max", "bottom_min"),
```

```
## # A tibble: 5 x 5
##   representator total_mean bottom_mean_mean bottom_max_mean bottom_min_mean
##   <chr>          <dbl>          <dbl>          <dbl>          <dbl>
## 1 error          0.931          0.996          1.54          0.758
## 2 error.features 0.966          1.01          1.54          0.755
## 3 forecast       0.975          1.00          1.53          0.789
## 4 ts             0.924          1.00          1.47          0.779
## 5 ts.features    0.968          1.01          1.55          0.747
```

```
tmp %>% select(representator, cluster, batch, distance, total) %>%
  tidyr::pivot_wider(names_from = "representator", values_from = "total") %>%
  select(-distance, -cluster, -batch) %>%
  mcb()
```

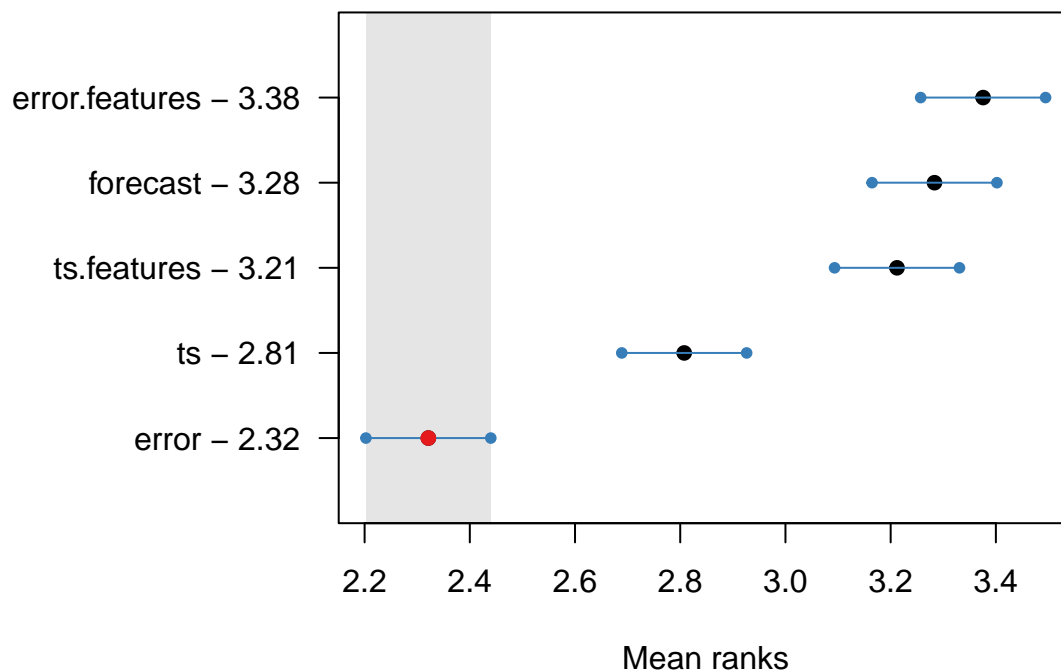
**Friedman: 0.000 (Ha: Different)**  
**Critical distance: 0.237**



```
## Friedman and Nemenyi Tests
## The confidence level is 5%
## Number of observations is 660 and number of methods is 5
## Friedman test p-value: 0.0000 - Ha: Different
## Critical distance: 0.2374
```

```
# bottom
tmp %>% select(representator, cluster, batch, distance, bottom_mean) %>%
  tidyr::pivot_wider(names_from = "representator", values_from = "bottom_mean") %>%
  select(-distance, -cluster, -batch) %>%
  mcb()
```

**Friedman: 0.000 (Ha: Different)**  
**Critical distance: 0.237**

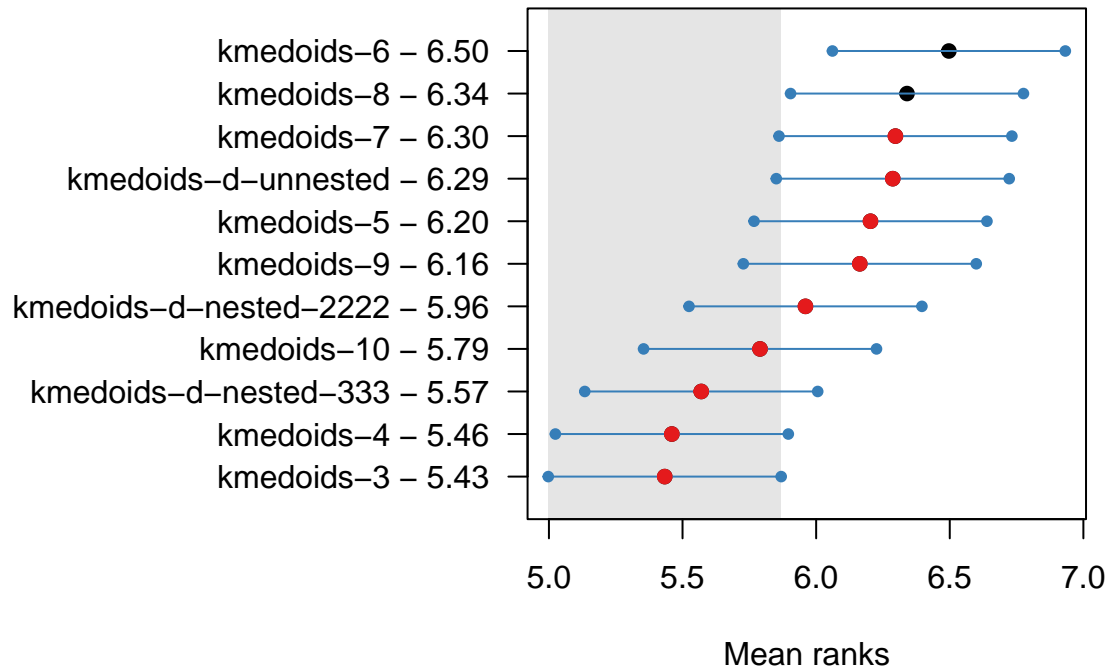


```
## Friedman and Nemenyi Tests
## The confidence level is 5%
## Number of observations is 660 and number of methods is 5
## Friedman test p-value: 0.0000 - Ha: Different
## Critical distance: 0.2374
```

cluster

```
tmp %>% select(representator, cluster, batch, distance, total) %>%
  tidyr::pivot_wider(names_from = "cluster", values_from = "total") %>%
  select(-representator, -distance, -batch) %>%
  mcb()
```

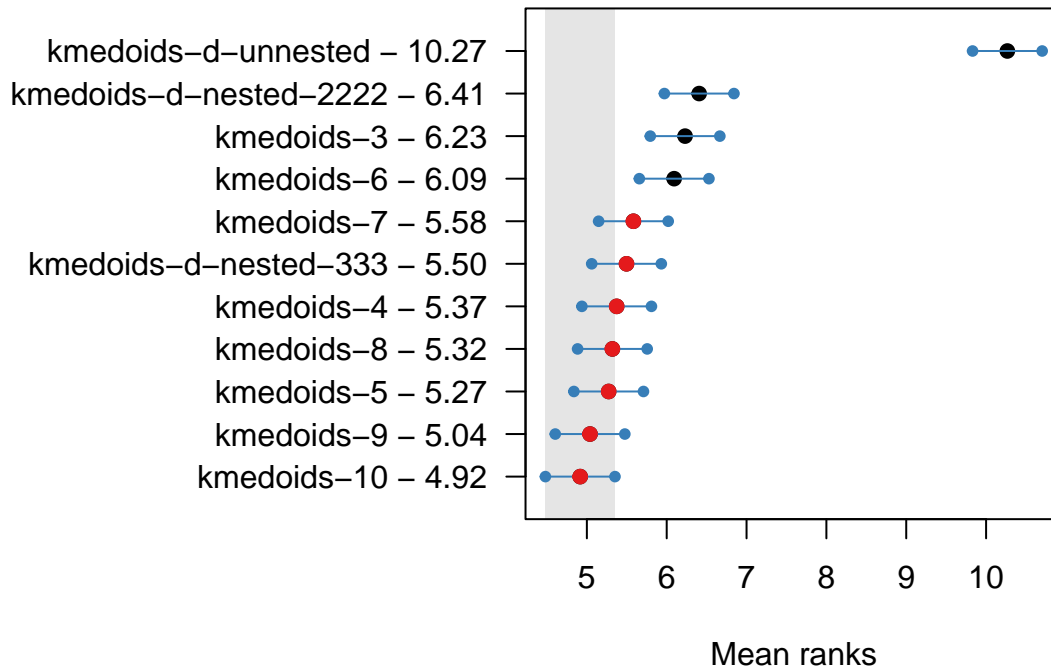
**Friedman: 0.000 (Ha: Different)**  
**Critical distance: 0.872**



```
## Friedman and Nemenyi Tests
## The confidence level is 5%
## Number of observations is 300 and number of methods is 11
## Friedman test p-value: 0.0000 - Ha: Different
## Critical distance: 0.8716

tmp %>% select(representator, cluster, batch, distance, bottom_mean) %>%
  tidyr::pivot_wider(names_from = "cluster", values_from = "bottom_mean") %>%
  select(-representator, -distance, -batch) %>%
  mcb()
```

**Friedman: 0.000 (Ha: Different)**  
**Critical distance: 0.872**



```
## Friedman and Nemenyi Tests
## The confidence level is 5%
## Number of observations is 300 and number of methods is 11
## Friedman test p-value: 0.0000 - Ha: Different
## Critical distance: 0.8716
```

## HCluster

```
tmp <- ratio %>% filter(startsWith(cluster, "hcluster"), rf_method == "mint", accuracy_method == "rmse")
  rowwise() %>%
  mutate(n_middle = NROW(other$S)) %>%
  select(representator, distance, cluster, total, bottom_mean, bottom_max, bottom_min, n_middle, batch)
  ungroup()
```

## representator

```
tmp %>% group_by(distance) %>% summarise_at(c("total", "bottom_mean", "bottom_max", "bottom_min"), c(measurements))
```

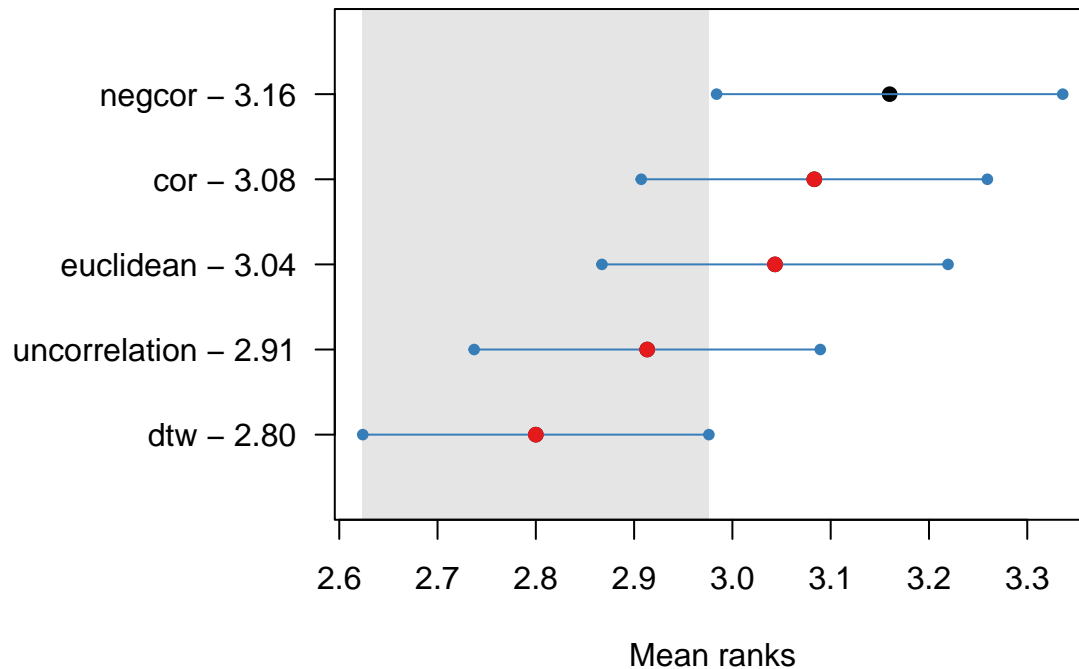
```
## # A tibble: 5 x 5
##   distance      total_mean bottom_mean_mean bottom_max_mean bottom_min_mean
##   <chr>          <dbl>          <dbl>          <dbl>          <dbl>
## 1 cor           0.958            1.02            1.98            0.569
## 2 dtw           0.944            1.02            2.00            0.575
## 3 euclidean     0.965            1.02            1.97            0.569
## 4 negcor        0.956            1.02            1.96            0.566
## 5 uncorrelation 0.950            1.02            1.89            0.583
```

```
## total
tmp %>% select(representator, cluster, batch, distance, total) %>%
```



```
tidyr::pivot_wider(names_from = "distance", values_from = "total") %>%
select(-representator, -cluster, -batch) %>%
mcb()
```

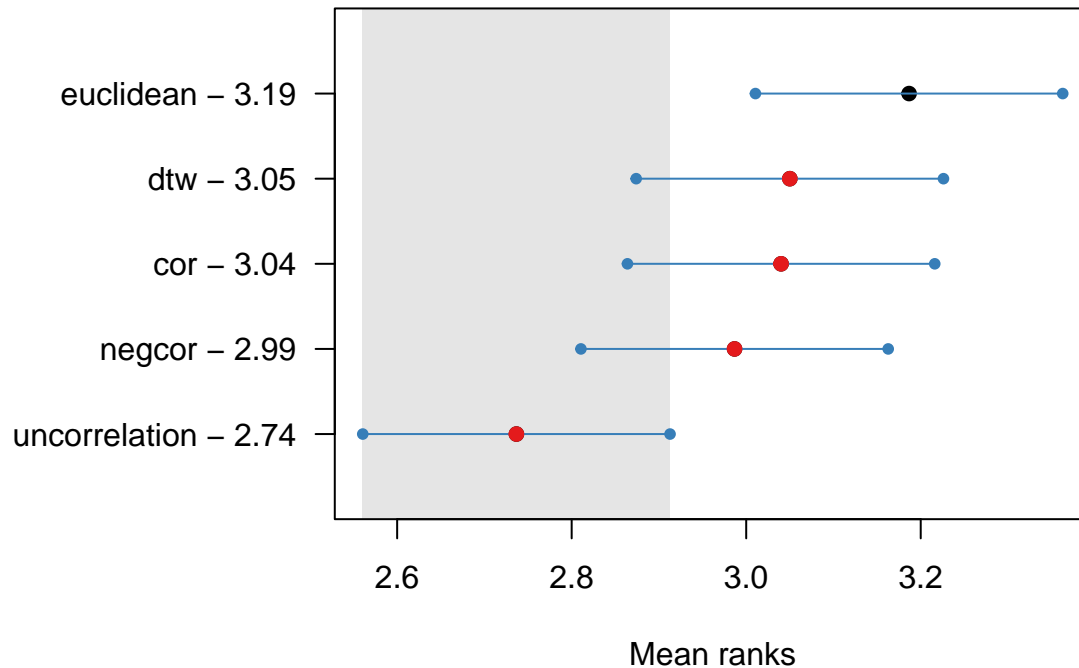
**Friedman: 0.038 (Ha: Different)**  
**Critical distance: 0.352**



```
## Friedman and Nemenyi Tests
## The confidence level is 5%
## Number of observations is 300 and number of methods is 5
## Friedman test p-value: 0.0382 - Ha: Different
## Critical distance: 0.3522
```

```
tmp %>% select(representator, cluster, batch, distance, bottom_mean) %>%
  tidyr::pivot_wider(names_from = "distance", values_from = "bottom_mean") %>%
  select(-representator, -cluster, -batch) %>%
  mcb()
```

**Friedman: 0.009 (Ha: Different)**  
**Critical distance: 0.352**



```
## Friedman and Nemenyi Tests
## The confidence level is 5%
## Number of observations is 300 and number of methods is 5
## Friedman test p-value: 0.0094 - Ha: Different
## Critical distance: 0.3522
```

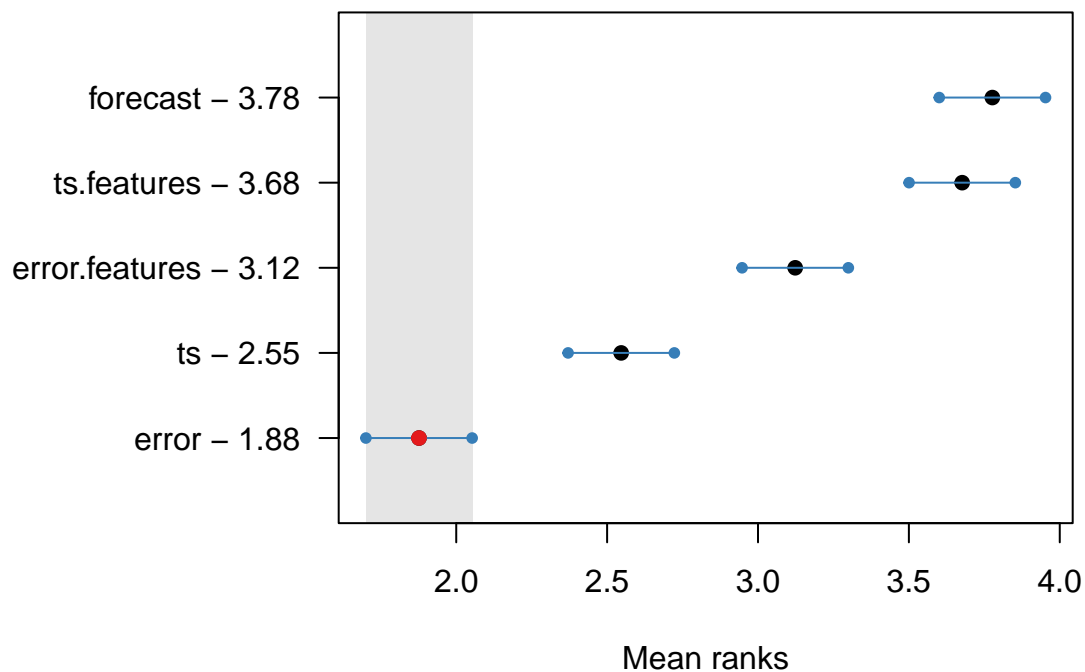
representator

```
tmp %>% group_by(representator) %>% summarise_at(c("total", "bottom_mean", "bottom_max", "bottom_min"),
```

```
## # A tibble: 5 x 5
##   representator total_mean bottom_mean_mean bottom_max_mean bottom_min_mean
##   <chr>          <dbl>          <dbl>          <dbl>          <dbl>
## 1 error          0.841          1.01          2.03          0.565
## 2 error.features 0.971          1.03          2.01          0.590
## 3 forecast       1.04          1.03          1.93          0.518
## 4 ts             0.906          1.01          1.89          0.596
## 5 ts.features    1.01          1.02          1.94          0.592
```

```
tmp %>% select(representator, cluster, batch, distance, total) %>%
  tidyr::pivot_wider(names_from = "representator", values_from = "total") %>%
  select(-distance, -cluster, -batch) %>%
  mcb()
```

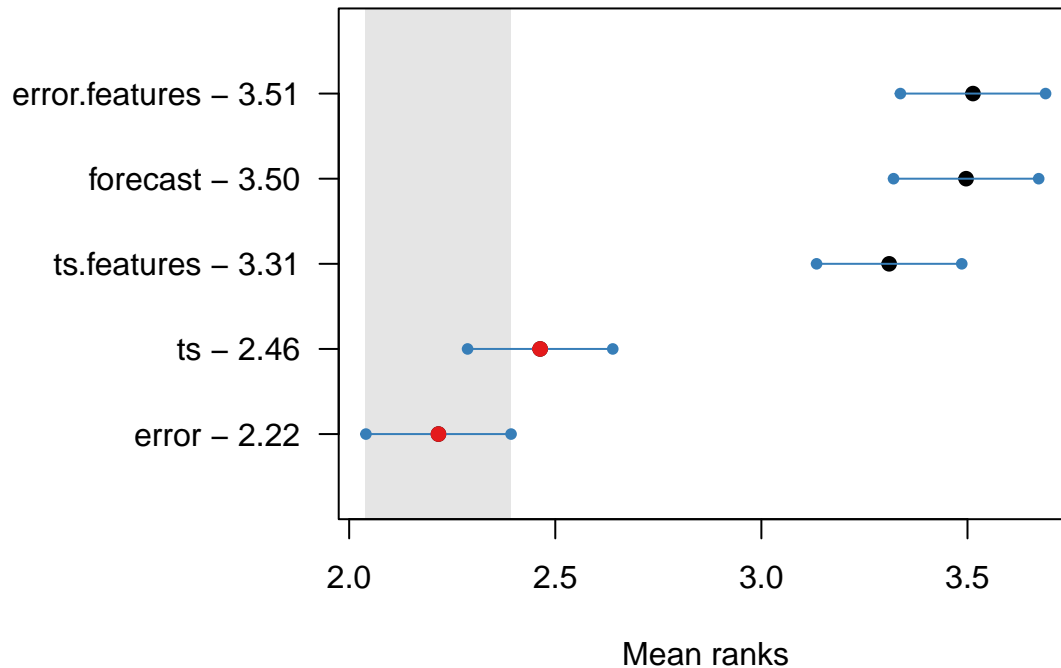
**Friedman: 0.000 (Ha: Different)**  
**Critical distance: 0.352**



```
## Friedman and Nemenyi Tests
## The confidence level is 5%
## Number of observations is 300 and number of methods is 5
## Friedman test p-value: 0.0000 - Ha: Different
## Critical distance: 0.3522
```

```
# bottom
tmp %>% select(representator, cluster, batch, distance, bottom_mean) %>%
  tidyr::pivot_wider(names_from = "representator", values_from = "bottom_mean") %>%
  select(-distance, -cluster, -batch) %>%
  mcb()
```

**Friedman: 0.000 (Ha: Different)**  
**Critical distance: 0.352**



```
## Friedman and Nemenyi Tests
## The confidence level is 5%
## Number of observations is 300 and number of methods is 5
## Friedman test p-value: 0.0000 - Ha: Different
## Critical distance: 0.3522
```

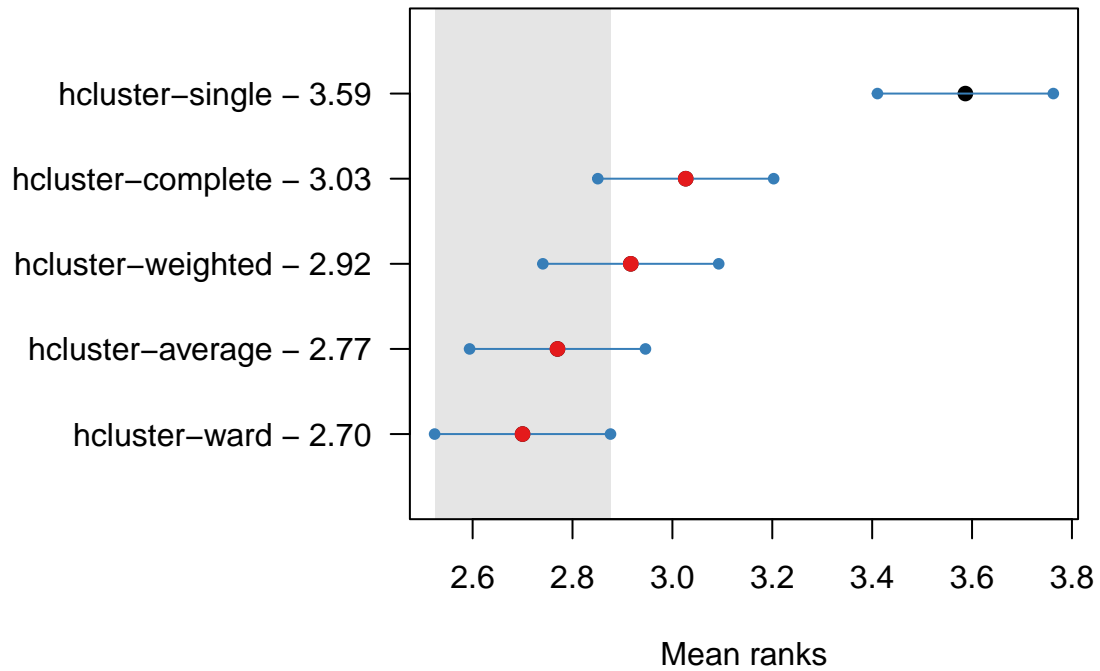
cluster

```
tmp %>% group_by(cluster) %>% summarise_at(c("total", "bottom_mean", "bottom_max", "bottom_min"), c(mean, min, max, min))
```

```
## # A tibble: 5 x 5
##   cluster      total_mean bottom_mean_mean bottom_max_mean bottom_min_mean
##   <chr>          <dbl>          <dbl>          <dbl>          <dbl>
## 1 hcluster-average 0.940          1.02          1.94          0.572
## 2 hcluster-complete 0.951          1.02          1.96          0.571
## 3 hcluster-single  1.00           1.03          1.97          0.576
## 4 hcluster-ward    0.934          1.02          1.93          0.574
## 5 hcluster-weighted 0.947          1.02          2.00          0.569
```

```
tmp %>% select(representator, cluster, batch, distance, total) %>%
  tidyr::pivot_wider(names_from = "cluster", values_from = "total") %>%
  select(-representator, -distance, -batch) %>%
  mcb()
```

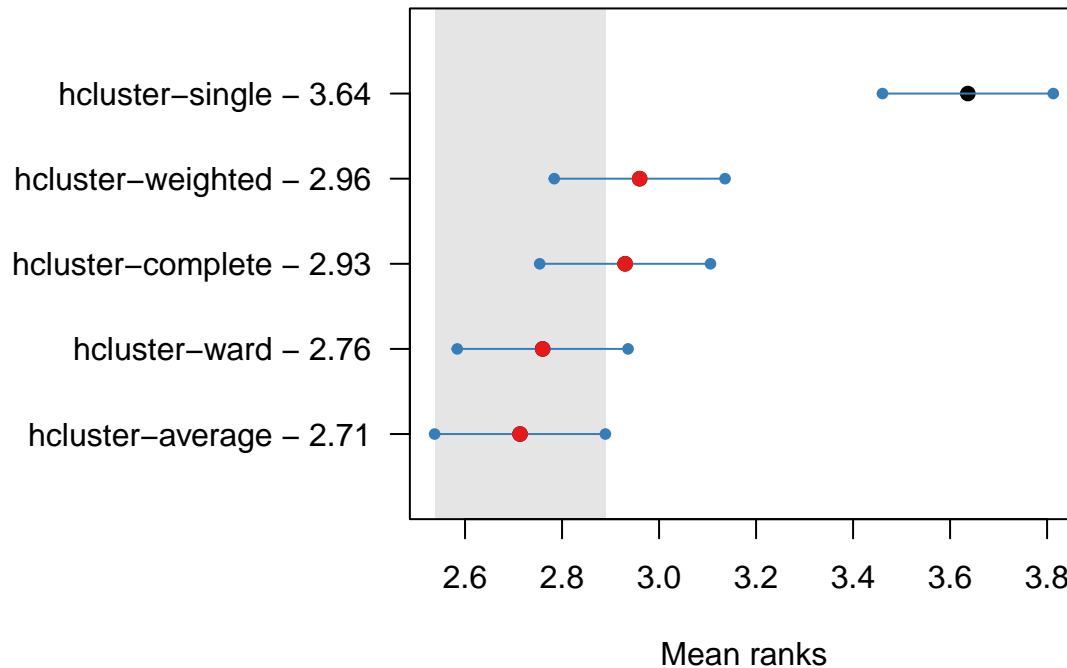
**Friedman: 0.000 (Ha: Different)**  
**Critical distance: 0.352**



```
## Friedman and Nemenyi Tests
## The confidence level is 5%
## Number of observations is 300 and number of methods is 5
## Friedman test p-value: 0.0000 - Ha: Different
## Critical distance: 0.3522
```

```
tmp %>% select(representator, cluster, batch, distance, bottom_mean) %>%
  tidyr::pivot_wider(names_from = "cluster", values_from = "bottom_mean") %>%
  select(-representator, -distance, -batch) %>%
  mcb()
```

**Friedman: 0.000 (Ha: Different)**  
**Critical distance: 0.352**



```
## Friedman and Nemenyi Tests
## The confidence level is 5%
## Number of observations is 300 and number of methods is 5
## Friedman test p-value: 0.0000 - Ha: Different
## Critical distance: 0.3522
```

natural hierarchy, random

```
tmp <- ratio %>% filter((cluster == "natural") | (startsWith(cluster, "random-average") | (startsWith(c(
  filter(rf_method == "mint", accuracy_method == "mae") %>%
  select(-representator, -distance) %>%
  select(batch, cluster, total, bottom_mean)

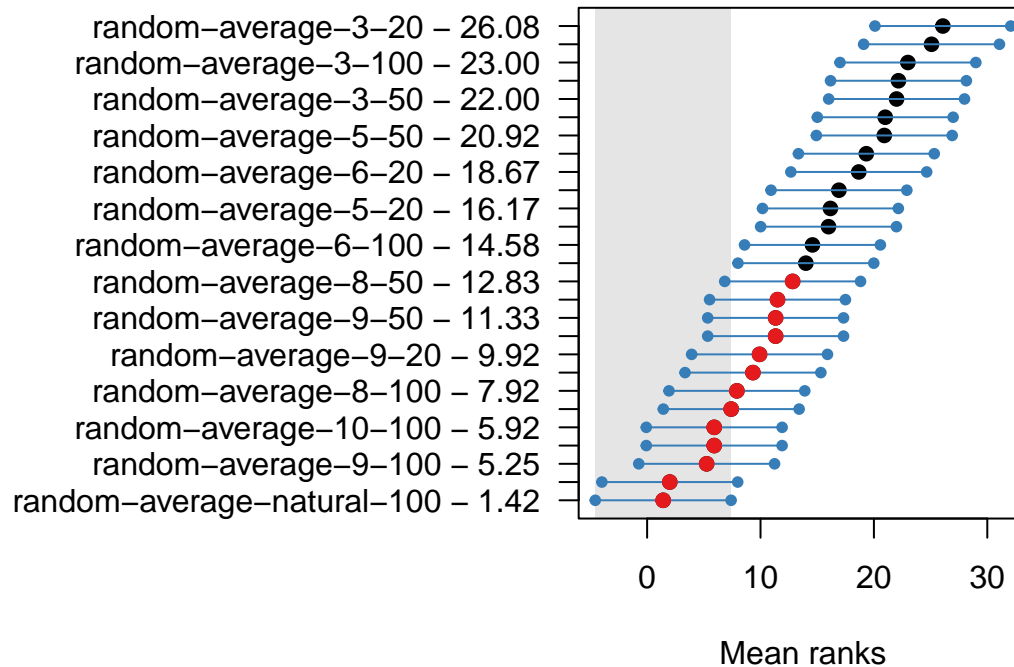
tmp %>% group_by(cluster) %>% summarise_at(c("total", "bottom_mean"), c(mean=function(x){mean(x)})) %>%
  arrange(bottom_mean_mean)
```

```
## # A tibble: 27 x 3
##   cluster                total_mean bottom_mean_mean
##   <chr>                  <dbl>          <dbl>
## 1 random-average-natural-100 0.850          0.983
## 2 random-average-natural-20 0.857          0.984
## 3 random-average-9-100      0.844          0.989
## 4 random-average-10-100     0.831          0.990
## 5 natural                  0.847          0.990
## 6 random-average-10-20      0.819          0.990
## 7 random-average-10-50      0.831          0.990
## 8 random-average-8-100      0.840          0.991
## 9 random-average-7-20       0.831          0.992
## 10 random-average-9-50      0.843          0.992
```

```
## # i 17 more rows
```

```
tmp %>% select(-total) %>%
  tidyr::pivot_wider(names_from = "cluster", values_from = "bottom_mean") %>%
  select(-batch) %>%
  mcb()
```

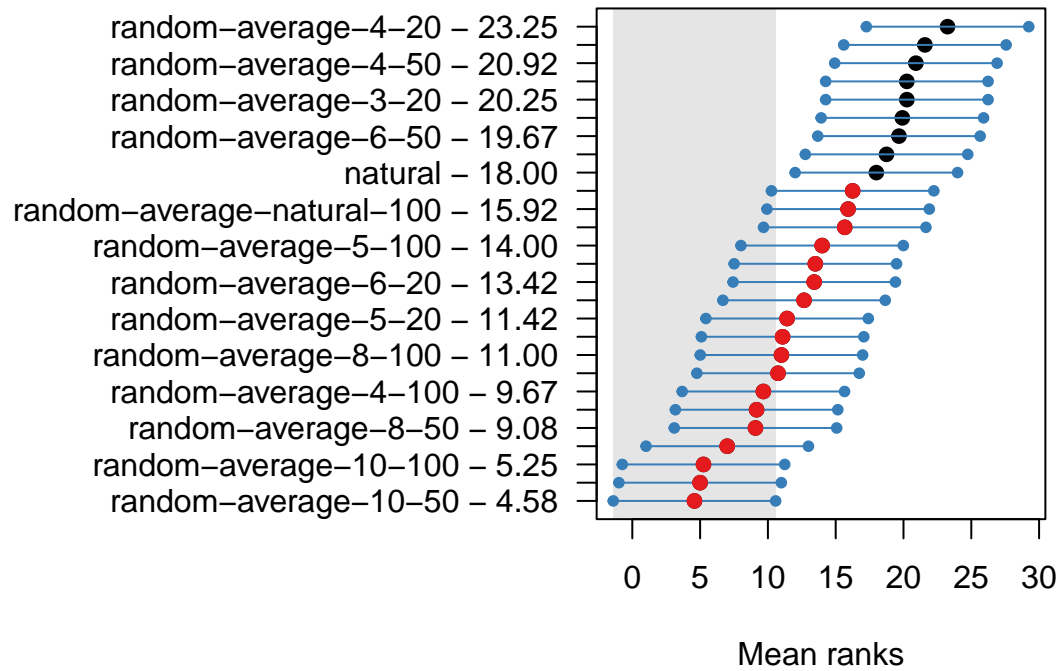
**Friedman: 0.000 (Ha: Different)**  
**Critical distance: 11.978**



```
## Friedman and Nemenyi Tests
## The confidence level is 5%
## Number of observations is 12 and number of methods is 27
## Friedman test p-value: 0.0000 - Ha: Different
## Critical distance: 11.9777
```

```
tmp %>% select(-bottom_mean) %>%
  tidyr::pivot_wider(names_from = "cluster", values_from = "total") %>%
  select(-batch) %>%
  mcb()
```

**Friedman: 0.000 (Ha: Different)**  
**Critical distance: 11.978**



```
## Friedman and Nemenyi Tests
## The confidence level is 5%
## Number of observations is 12 and number of methods is 27
## Friedman test p-value: 0.0000 - Ha: Different
## Critical distance: 11.9777
```