

## INFO20003 Database System Assignment 3

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### Question 1

1.(a) Page-oriented Nested Loops Join.

$$\begin{aligned}\text{NPages}(\text{Parts}) &= \text{NTuples}(\text{Parts}) / \text{NTuplesPerPage}(\text{Parts}) \\ &= 60,000 / 50 = 1200 \text{ pages}\end{aligned}$$

$$\begin{aligned}\text{NPages}(\text{Supply}) &= \text{NTuples}(\text{Supply}) / \text{NTuplesPerPage}(\text{Supply}) \\ &= 150,000 / 50 = 3000 \text{ pages}\end{aligned}$$

$$\begin{aligned}\text{Cost} &= \text{NPages}(\text{Parts}) + \text{NPages}(\text{Parts}) \times \text{NPages}(\text{Supply}) \\ &= 1200 + 1200 \times 3000 = \mathbf{3601200} \text{ (I/O)}\end{aligned}$$

1.(b) Block-oriented Nested Loops Join.

$$\begin{aligned}\text{NBlock}(\text{Parts}) &= \text{NPages}(\text{Parts}) / (B - 2) \\ &= 1200 / (202 - 2) = 6\end{aligned}$$

$$\begin{aligned}\text{Cost} &= \text{NPages}(\text{Parts}) + \text{NBlocks}(\text{Parts}) \times \text{NPages}(\text{Supply}) \\ &= 1200 + 6 \times 3000 = \mathbf{19200} \text{ (I/O)}\end{aligned}$$

1.(c) Sort-Merge Join.

$$\begin{aligned}\text{Cost} &= \text{Sort}(\text{Parts}) + \text{Sort}(\text{Supply}) + \text{Merge} \\ &= 2 \times \text{NumPasses} \times \text{NPages}(\text{Parts}) + 2 \times \text{NumPasses} \times \text{NPages}(\text{Supply}) \\ &\quad + \text{NPages}(\text{Parts}) + \text{NPages}(\text{Supply}) \\ &= 2 \times 2 \times 1200 + 2 \times 2 \times 3000 + 1200 + 3000 \\ &= 5 \times (1200 + 3000) = \mathbf{21000} \text{ (I/O)}\end{aligned}$$

1.(d) Hash Join.

$$\begin{aligned}\text{Cost} &= 3 \times \text{NPages}(\text{Parts}) + 3 \times \text{NPages}(\text{Supply}) \\ &= 3 \times 1200 + 3 \times 3000 = \mathbf{12600} \text{ (I/O)}\end{aligned}$$

1.(e)

Block Nested Loops Join with B chosen so that the smaller table fits into memory as a single block.

Due to  $\text{NPages}(\text{Parts}) / (B - 2) = 1 \rightarrow B = 1202$  pages

$$\text{Cost} = 1200 + 3000 = 4200 \text{ (I/O)}$$

Therefore, the minimum buffer size is **1202** pages, the cost is **4200** (I/O).

## Question 2

2.(a)

$$RF_{Salary > 300,000} = [ High(Salary) - Value ] / [ High(Salary) - Low(Salary) ] \\ = ( 500,000 - 300,000 ) / ( 500,000 - 100,000 ) = 0.5$$

$$RF_{department = "Market"} = 1 / NKeys(department) \\ = 1 / 6$$

$$Result\ size = NTuples(Employee) \times \Pi\ RF \\ = NPages(Employee) \times NTuplesPerPage(Employee) \times RF_{Salary > 300,000} \times RF_{department = "Market"} \\ = 1200 \times 120 \times 0.5 \times (1/6) = 12000\ tuples$$

2.(b)

Plan 1:

Using clustered B+ tree on (department, salary):

$$Cost = RF_{Salary > 300,000} \times RF_{department = "Market"} \times [ NPages(I) + NPages(Employee) ] \\ = (1/6) \times 0.5 \times ( 300 + 1200 ) = 125\ (I/O)$$

Plan 2:

Using Heap Scan:

$$Cost = NPages(Employee) = 1200\ (I/O)$$

$$125 < 1200$$

Therefore, the best plan is the **clustered B+ tree** on (department, salary) with a cost of **125** (I/O).

2.(c)

Plan 1:

Using unclustered B+ tree on (salary):

$$Cost = RF_{Salary > 300,000} \times [ NPages(I) + NTuples(Employee) ] \\ = 0.5 \times ( 200 + 1200 \times 120 ) = 72100\ (I/O)$$

Plan 2:

Using Heap Scan:

$$Cost = NPages(Employee) = 1200\ (I/O)$$

$$1200 < 72100$$

Therefore, the best plan is the **Heap Scan** with a cost of **1200** (I/O).

2.(d)

Plan 1:

Using unclustered Hash index on (department):

$$Cost = RF_{department = "Market"} \times 2.2 \times NTuples(Employee) \\ = (1/6) \times 2.2 \times 1200 \times 120 = 52800\ (I/O)$$

Plan 2:

Using Heap Scan:

Cost = NPAGES(Employee) = **1200** (I/O)

$1200 < 52800$

Therefore, the best plan is the **Heap Scan** with a cost of **1200** (I/O).

2.(e)

Hash index **cannot be** used for range queries.

The only available plan is the **Heap Scan** with a cost of **1200** (I/O).

### Question 3

3.(a)

$$RF_{eid} = 1/NKeys(eid) = 1/NTuples(Employee) = 1 / 5000$$

$$RF_{projid} = 1/NKeys(projid) = 1/NTuples(Project) = 1/60,000$$

$$RF_{salary < 300,000} = [ \text{Value} - \text{Low}(\text{Salary}) ] / [ \text{High}(\text{Salary}) - \text{Low}(\text{Salary}) ] \\ = ( 300,000 - 100,000 ) / ( 500,000 - 100,000 ) = 0.5$$

$$RF_{code = \text{"alpha 340"}} = 1 / NKeys(code) = 1/1000$$

$$\begin{aligned} \text{Result size} &= NTuples(Employee) \times NTuples(projid) \times NTuples(department) \\ &\quad \times RF_{eid} \times RF_{projid} \times RF_{salary < 300,000} \times RF_{code = \text{"alpha 340"}} \\ &= 5000 \times 60000 \times 20000 \times (1/5000) \times (1/60000) \times 0.5 \times (1/1000) \\ &= 10 \text{ tuples} \end{aligned}$$

3.(b)

**Plan [1]:**

$$NPages(Employee) = 5000/100 = 50 \text{ pages}$$

$$NPages(Project) = 60000/100 = 600 \text{ pages}$$

$$NPages(Department) = 20000/100 = 200 \text{ pages}$$

$$\begin{aligned} \text{Cost to join Employee} \bowtie \text{Project} &= NPages(Employee) + NPages(Employee) \times NPages(Project) \\ &= 50 + 50 \times 600 = 30050 \text{ (I/O)} \end{aligned}$$

$$\begin{aligned} \text{Result size of Employee} \bowtie \text{Project} &= NTuples(Employee) \times NTuples(Project) \times (1/NKeys(eid)) \\ &= 5000 \times 60000 \times (1/5000) = 6000 \text{ tuples} \end{aligned}$$

$$NPages( \text{Employee} \bowtie \text{Project} ) = 6000/100 = 60 \text{ pages}$$

$$\begin{aligned} \text{Cost to join with Department} &= NPages(\text{Employee} \bowtie \text{Project}) + NPages(\text{Employee} \bowtie \text{Project}) \\ &\quad \times NPages(Department) - Npages(\text{Employee} \bowtie \text{Project}) \\ &= 60 \times 200 = 12000 \text{ (I/O)} \quad \text{\#due to pipelining} \end{aligned}$$

$$\text{Overall cost} = 30050 + 12000 = 150050 \text{ (I/O)}$$

**Plan [2]:**

$$\begin{aligned} \text{Cost to join Porject} \bowtie \text{Department} &= 3 \times NPages(Project) + 3 \times NPages(Department) \\ &= 3 \times (600 + 200) = 2400 \text{ (I/O)} \end{aligned}$$

$$\begin{aligned} \text{Result size of Porject} \bowtie \text{Department} &= NTuples(Project) \times NTuples(Department) \times (1/NKeys(projid)) \\ &= 60000 \times 20000 \times (1/60000) = 20000 \text{ tuples} \end{aligned}$$

$$NPages( \text{Porject} \bowtie \text{Department} ) = 20000/100 = 200 \text{ pages}$$

$$\begin{aligned} \text{Cost to join with Employee} &= 2 \times \text{NumPasses} \times NPages(\text{Porject} \bowtie \text{Department}) \\ &\quad + 2 \times \text{NumPasses} \times NPages(Employee) + NPages(\text{Porject} \bowtie \text{Department}) \\ &\quad + NPages(Employee) - Npages(\text{Porject} \bowtie \text{Department}) \\ &= 4 \times 200 + 5 \times 50 = 1050 \text{ (I/O)} \quad \text{\#due to pipelining} \end{aligned}$$

Overall cost = 2400 + 1050 = **3450** (I/O)

**Plan [3]:**

Cost to select from Employee =  $RF_{\text{salary} < 300,000} \times (\text{NPages}(\text{Index on salary}) + \text{NPages}(\text{Employee}))$   
 $= 0.5 \times (10 + 50) = 30$  (I/O)

Result size of  $\sigma_{\text{salary} < 300,000}(\text{Employee}) = \text{NTuples}(\text{Employee}) \times RF_{\text{salary} < 300,000}$   
 $= 5000 \times 0.5 = 2500$  tuples

$\text{NPages}(\sigma_{\text{salary} < 300,000}(\text{Employee})) = 2500/100 = 25$  pages

Cost to join  $\sigma_{\text{salary} < 300,000}(\text{Employee}) \bowtie \text{Project} = \text{NPages}(\sigma_{\text{salary} < 300,000}(\text{Employee}))$   
 $+ \text{NPages}(\sigma_{\text{salary} < 300,000}(\text{Employee})) \times \text{NPages}(\text{Project})$   
 $- \text{Npages}(\sigma_{\text{salary} < 300,000}(\text{Employee}))$   
 $= 25 \times 600 = \mathbf{15000}$  I/O #due to pipelining

Result size of  $\sigma_{\text{salary} < 300,000}(\text{Employee}) \bowtie \text{Project}$   
 $= \text{NTuples}(\sigma_{\text{salary} < 300,000}(\text{Employee})) \times \text{NTuples}(\text{Project})$   
 $\times RF(\sigma_{\text{salary} < 300,000}(\text{Employee}))$   
 $= 2500 \times 60000 \times (1/2500) = 60000$  tuples

$\text{NPages}(\sigma_{\text{salary} < 300,000}(\text{Employee}) \bowtie \text{Project}) = 60000 / 100 = 600$  pages

Cost to join with Department =  $3 \times \text{NPages}(\sigma_{\text{salary} < 300,000}(\text{Employee}) \bowtie \text{Project})$   
 $+ 3 \times \text{NPages}(\text{Department}) - \text{Npages}(\sigma_{\text{salary} < 300,000}(\text{Employee}) \bowtie \text{Project})$   
 $= 2 \times 600 + 3 \times 200 = \mathbf{1800}$  (I/O) #due to pipelining

Overall cost = 30 + 15000 + 1800 = **16830** (I/O)

**Plan [4]:**

# the index on Project.projid is clustered. The data pages of Project are already sorted by projid, so there is no need to sort Project.

Cost to join Porject  $\bowtie$  Department =  $2 \times \text{NumPasses} \times \text{NPages}(\text{Department}) + \text{NPages}(\text{Department})$   
 $+ (\text{NPages}(\text{Index on projid}) + \text{NPages}(\text{Project}))$   
 $= 5 \times 200 + (200 + 600) = \mathbf{1800}$  (I/O)

Result size of Porject  $\bowtie$  Department = 20000 tuples (from Plan [2] )

$\text{NPages}(\text{Porject} \bowtie \text{Department}) = 20000 / 100 = 200$  pages

Cost to join with Employee =  $2 \times \text{NumPasses} \times \text{NPages}(\text{Porject} \bowtie \text{Department})$   
 $+ 2 \times \text{NumPasses} \times \text{NPages}(\text{Employee}) + \text{NPages}(\text{Porject} \bowtie \text{Department})$   
 $+ \text{NPages}(\text{Employee}) - \text{Npages}(\text{Porject} \bowtie \text{Department})$   
 $= 4 \times 200 + 5 \times 50 = \mathbf{1050}$  (I/O)

Overall cost = 1800 + 1050 = **2850** (I/O)