Lab 3 (Bhuvnesh Sharma, Weixin Wu)

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Introduction

Crime is huge menace in the society, there have been many attempts in past to reduce crime rates within communities in North Carolina. Traditional politicians and conventional approach has assumed that tough on crime is an effective tool to curb crime. Being tough on crime is regularly misunderstood as longer and mandatory prison sentences. This misguided strategy can lead to state's higher investment on prison infrastructure and also make laws which can promote mandatory prison sentences appear as effective crime fighting tool. The goal of this study is to uncover the real facts around the crime rates within North Carolina to develop effective state policy around to reduce crime rates. Key motivation of the report discover the real drivers and instruments which the policy makers can use and have meaningful impact on crime. Study intends to empower the state politicians, key legislative leaders with key facts which have been based on data and not on conventional empirical narratives. Study intends to discover key variables which have major impact on crime rates in North Carolina. This information would be critical for voters to understand so that they can make an informed decision on a important election issue.

Data Cleansing

```
crimeData <- read.csv("crime_v2.csv")
summary(crimeData)</pre>
```

```
##
         county
                                                              prbarr
                           year
                                         crmrte
##
    Min.
            : 1.0
                      Min.
                              :87
                                    Min.
                                            :0.005533
                                                         Min.
                                                                 :0.09277
##
    1st Qu.: 52.0
                      1st Qu.:87
                                    1st Qu.:0.020927
                                                         1st Qu.:0.20568
##
    Median :105.0
                      Median:87
                                    Median: 0.029986
                                                         Median: 0.27095
##
    Mean
            :101.6
                      Mean
                              :87
                                            :0.033400
                                                                 :0.29492
                                    Mean
                                                         Mean
##
    3rd Qu.:152.0
                      3rd Qu.:87
                                    3rd Qu.:0.039642
                                                         3rd Qu.:0.34438
            :197.0
##
    Max.
                      Max.
                              :87
                                    Max.
                                            :0.098966
                                                         Max.
                                                                 :1.09091
    NA's
                      NA's
                              :6
##
            :6
                                    NA's
                                                         NA's
                          prbpris
##
            prbconv
                                              avgsen
                                                                 polpc
##
                : 5
                       Min.
                               :0.1500
                                          Min.
                                                  : 5.380
                                                             Min.
                                                                     :0.000746
    0.588859022: 2
                                          1st Qu.: 7.340
##
                       1st Qu.:0.3648
                                                             1st Qu.:0.001231
##
                  1
                       Median : 0.4234
                                          Median: 9.100
                                                             Median: 0.001485
##
    0.068376102: 1
                               :0.4108
                                                  : 9.647
                                                                     :0.001702
                       Mean
                                          Mean
                                                             Mean
##
    0.140350997: 1
                       3rd Qu.:0.4568
                                          3rd Qu.:11.420
                                                             3rd Qu.:0.001877
    0.154451996: 1
                               :0.6000
                                                                     :0.009054
##
                       Max.
                                          Max.
                                                  :20.700
                                                             Max.
    (Other)
##
                :86
                       NA's
                               :6
                                          NA's
                                                  :6
                                                             NA's
                                                                     :6
##
       density
                             taxpc
                                                west
                                                                 central
##
    Min.
            :0.00002
                        Min.
                                : 25.69
                                           Min.
                                                   :0.0000
                                                              Min.
                                                                      :0.0000
##
    1st Qu.:0.54741
                        1st Qu.: 30.66
                                           1st Qu.:0.0000
                                                              1st Qu.:0.0000
##
    Median : 0.96226
                        Median : 34.87
                                           Median :0.0000
                                                              Median :0.0000
##
    Mean
            :1.42884
                        Mean
                                : 38.06
                                                   :0.2527
                                                                      :0.3736
                                           Mean
                                                              Mean
                        3rd Qu.: 40.95
##
    3rd Qu.:1.56824
                                           3rd Qu.:0.5000
                                                              3rd Qu.:1.0000
    Max.
            :8.82765
                        Max.
                                :119.76
                                           Max.
                                                   :1.0000
                                                              Max.
                                                                      :1.0000
    NA's
                        NA's
                                           NA's
                                                   :6
                                                              NA's
                                                                      :6
            :6
                                :6
```

```
##
                           pctmin80
        urban
                                                wcon
                                                                  wtuc
##
    Min.
            :0.00000
                                : 1.284
                                                   :193.6
                                                                     :187.6
                        \mathtt{Min}.
                                           Min.
                                                             Min.
                        1st Qu.: 9.845
##
    1st Qu.:0.00000
                                           1st Qu.:250.8
                                                             1st Qu.:374.6
    Median :0.00000
                        Median :24.312
                                           Median :281.4
                                                             Median :406.5
##
##
    Mean
            :0.08791
                        Mean
                                :25.495
                                           Mean
                                                   :285.4
                                                             Mean
                                                                     :411.7
##
    3rd Qu.:0.00000
                        3rd Qu.:38.142
                                           3rd Qu.:314.8
                                                             3rd Qu.:443.4
##
    Max.
            :1.00000
                        Max.
                                :64.348
                                           Max.
                                                   :436.8
                                                             Max.
                                                                     :613.2
##
    NA's
            :6
                        NA's
                                :6
                                           NA's
                                                   :6
                                                             NA's
                                                                     :6
##
          wtrd
                           wfir
                                             wser
                                                                wmfg
##
    Min.
            :154.2
                      Min.
                              :170.9
                                       Min.
                                               : 133.0
                                                          Min.
                                                                  :157.4
    1st Qu.:190.9
                      1st Qu.:286.5
                                        1st Qu.: 229.7
                                                          1st Qu.:288.9
    Median :203.0
                      Median :317.3
                                       Median : 253.2
                                                          Median :320.2
##
            :211.6
                                               : 275.6
##
    Mean
                              :322.1
                                                                  :335.6
                      Mean
                                       Mean
                                                          Mean
    3rd Qu.:225.1
                      3rd Qu.:345.4
                                                          3rd Qu.:359.6
##
                                        3rd Qu.: 280.5
            :354.7
                              :509.5
                                               :2177.1
                                                          Max.
##
    Max.
                      Max.
                                        Max.
                                                                  :646.9
##
    NA's
            :6
                      NA's
                              :6
                                        NA's
                                               :6
                                                          NA's
                                                                  :6
##
          wfed
                                             wloc
                           wsta
                                                               mix
##
            :326.1
                              :258.3
                                                                 :0.01961
    Min.
                      Min.
                                       Min.
                                               :239.2
                                                         Min.
##
    1st Qu.:400.2
                      1st Qu.:329.3
                                        1st Qu.:297.3
                                                         1st Qu.:0.08074
##
    Median :449.8
                      Median :357.7
                                       Median :308.1
                                                         Median: 0.10186
##
    Mean
            :442.9
                      Mean
                              :357.5
                                       Mean
                                               :312.7
                                                         Mean
                                                                 :0.12884
    3rd Qu.:478.0
                      3rd Qu.:382.6
                                        3rd Qu.:329.2
##
                                                         3rd Qu.:0.15175
            :598.0
##
    Max.
                              :499.6
                                               :388.1
                                                                 :0.46512
                      {\tt Max.}
                                       Max.
                                                         Max.
##
    NA's
            :6
                      NA's
                             :6
                                       NA's
                                               :6
                                                         NA's
                                                                 :6
##
       pctymle
##
    Min.
            :0.06216
    1st Qu.:0.07443
##
##
    Median :0.07771
##
    Mean
            :0.08396
    3rd Qu.:0.08350
##
    Max.
            :0.24871
##
    NA's
            :6
```

As shown in the summary table, there are 6 NA's in every variable. After reviewing the data, we found that all NA's are in 6 rows, so we removed those rows as they did not provide any information.

```
crimeData2 <- crimeData[complete.cases(crimeData),]</pre>
```

Variable 'prbcony' was incorrectly displayed as a text field. We converted it to numermic.

```
crimeData2 <- transform(crimeData2, prbconv = as.numeric(as.character(prbconv)))
summary(crimeData2$prbconv)</pre>
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.06838 0.34541 0.45283 0.55128 0.58886 2.12121
```

Usually the probability variable should be bound between 0 and 1. However, there is one observation with 'prbarr' (probability of arrest) higher than 1, and 10 observations with 'prbconv' (probability of conviction) higher than 1.

```
nrow(crimeData2[which(crimeData2$prbarr>1),])
## [1] 1
nrow(crimeData2[which(crimeData2$prbconv>1),])
```

[1] 10

Variable 'prbarr' is defined as the ratio of arrests to offenses. One possible explanation for 'prbarr' being greater than 1 is that multiple people who convicted a single crime together is counted as one conviction but multiple arrests.

Variable 'prbconv' is defined as the ratio of convictions to arrests. One possible explanation for 'prbconv' being greater than 1 is that one person who is convicted of multiple crimes but only arrested once.

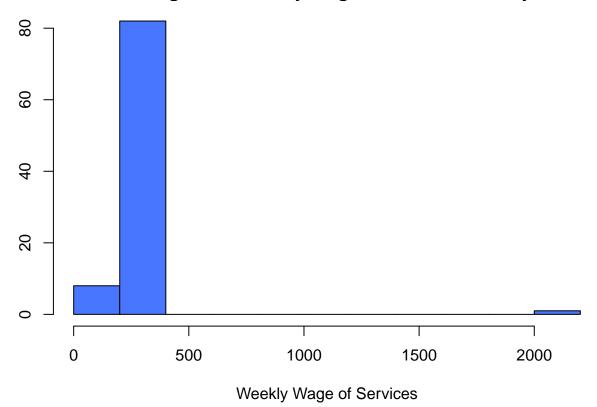
Without further information on the variables, we could not conclude whether these values are invalid. So we left those observations in the data.

Variable 'pctmin80' (percent of minority in 1980) is expressed as percentages. We converted it into decimals to be consistent with variable 'pctymle' (percent of young male).

```
crimeData2$pctmin80_2 <- crimeData2$pctmin80/100</pre>
```

The max value of variable 'wser' (weekly wage of service industry) is significantly higher than its third quartile. The histogram below shows that the max value (2177.068) is significantly higher than the rest of values.

Histogram of Weekly Wage in Service Industry



crimeData2[which(crimeData2\$wser>2000),]

```
##
      county year
                               prbarr prbconv prbpris avgsen
                      crmrte
                                                                   polpc
## 84
               87 0.0108703 0.195266 2.12121 0.442857
         185
                                                          5.38 0.0012221
##
        density
                   taxpc west central urban pctmin80
                                                           wcon
                                                                    wtuc
## 84 0.3887588 40.82454
                                              64.3482 226.8245 331.565
                                     1
##
                   wfir
                                           wfed
                                                   wsta
          wtrd
                             wser
                                    wmfg
## 84 167.3726 264.4231 2177.068 247.72 381.33 367.25 300.13 0.04968944
```

```
## pctymle pctmin80_2
## 84 0.07008217 0.643482
```

We examined County 185, whose wser is 2177.068. We noticed that most other weekly wage variables for County 185 are below the means. You would expect that a richer county would have weekly wage in multiple industries to be higher than the average. So it's very unlikely for a county to have lower than average weekly wage on constructure, transportation, retail, finance, etc. but extremely high weekly wage on the service industry. In addition, an average weekly wage of 2177.068 in 1987 is an unreasonable value. So we believed 2177.068 is erroneous. We removed this observation from the data.

```
crimeData2 <- crimeData2[which(crimeData2$wser<2000),]</pre>
```

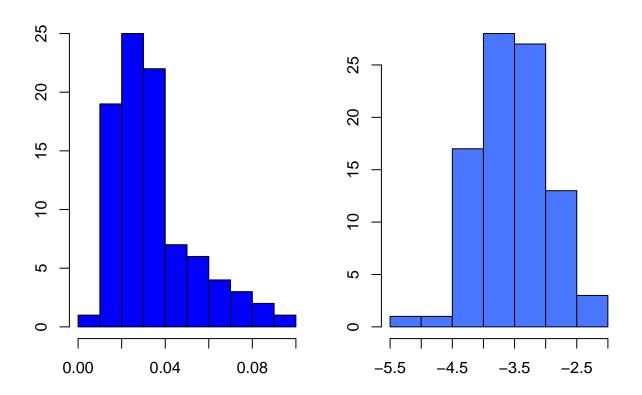
Exploratory Data Analysis

Crimes committed per person (crmrte)

The distribution of crime rate is skewed to the right, so we considered taking the log of crime rate. After the log transformation, the distribution of crmrte_log is closer to normal. Semilogarithmic form is interpretable later in modeling: it tells us what's the percentage change in crime rate in response to a unit change in explantory variables. Our target variable is crmrte_log.

```
par(mfrow=c(1,2), oma=c(0, 0, 2, 0))
par(mar=c(2, 2, 2, 2))
hist(crimeData2$crmrte, main="",xlab = "Crime Rate", col = "blue")
crimeData2$crmrte_log = log(crimeData2$crmrte)
hist(crimeData2$crmrte_log, main="", xlab = "Log of Crime Rate", col = "royalblue1")
mtext("Distributions of Crime Rate and Log Crime Rate", outer=TRUE, cex = 1.2, font=2)
```

Distributions of Crime Rate and Log Crime Rate



Probability of arrest (prbarr)

The scatter plot of crmrte vs. prbarr on the left shows an exponential decay trend. In addition, the variation of crmrte decreases substantially as prbarr increases. We took the log of crime rate, and then re-graph the scatter plot (shown on the right). The scatter plot of crmrte_log vs. prbarr indicates a more linear relationship and the variation of crmrte_log does not vary as much with prbarr. The correlation coefficient further supports the transformation.

- * The correlation between crmrte and prbarr is -0.41
- * The correlation between crmrte log and prbarr is -0.50

In addition, we noticed a leveraged data point in the graph, that's County 115. County 115 has significantly higher probability of arrest than all other counties. If we removed County 115 from the data, the correlation coefficient reduced from -0.50 to -0.39. This indicates that County 115 could be an infludential observation. Later when building the model, we will calculate Cook's distance to confirm that County 15 is an influential observation and also address the impact of influential observations to parameter estimates.

[1] -0.4076239

```
cor(crimeData2$prbarr, crimeData2$crmrte_log)
## [1] -0.4964904
plot(crimeData2$prbarr, crimeData2$crmrte,main = "Prob of arrest & Log crime rate" ,
     xlab = "Prob of Arrest",ylab = "Log of Crime Rate",col="royalblue1")
text(crimeData2$prbarr, crimeData2$crmrte, labels = crimeData2$county, cex=0.7, pos=3,col = "red")
   Prob of arrest & Crime rate
                                   Prob of arrest & Log crime rate  Prob of arrest & Log crime rate
                                  -2.5
      0
0.08
                                                                    0.08
      0
90.0
                                                                    90.0
9.0
                                                                    9.0
                                                                    0.02
                                  -5.0
               0.6
                    8.0
                         1.0
                                             0.4
                                                  0.6
                                                      8.0
                                                           1.0
                                                                          0.2
                                                                               0.4
                                                                                    0.6
                                                                                         8.0
                                                                                              1.0
      0.2
           0.4
                                        0.2
           Prob of Arrest
                                              Prob of Arrest
                                                                                Prob of Arrest
crimeData3 <- crimeData2[which(crimeData2$county!=115),]</pre>
cor(crimeData3$prbarr, crimeData3$crmrte_log)
```

[1] -0.3949839

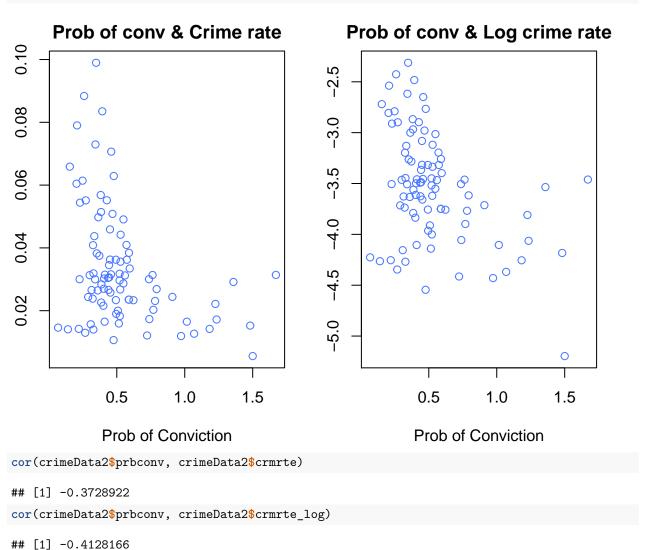
Probability of conviction (prbconv)

Similar to probar, the scatter plot of crmrte vs. proconv on the left shows an exponential decay trend. In addition, the variation of crmrte decreases substantially as proconv increases. We took the log of crime rate, and then re-graph the scatter plot (shown on the right). The scatter plot of crmrte_log vs. prbconv indicates a more linear relationship and the variation of crmrte_log does not vary as much with prbconv The correlation coefficient further supports the transformation.

```
par(mfrow=c(1,2))
par(mar=c(4, 2, 2, 2))
plot(crimeData2$prbconv, crimeData2$crmrte,main = "Prob of conv & Crime rate" ,
```

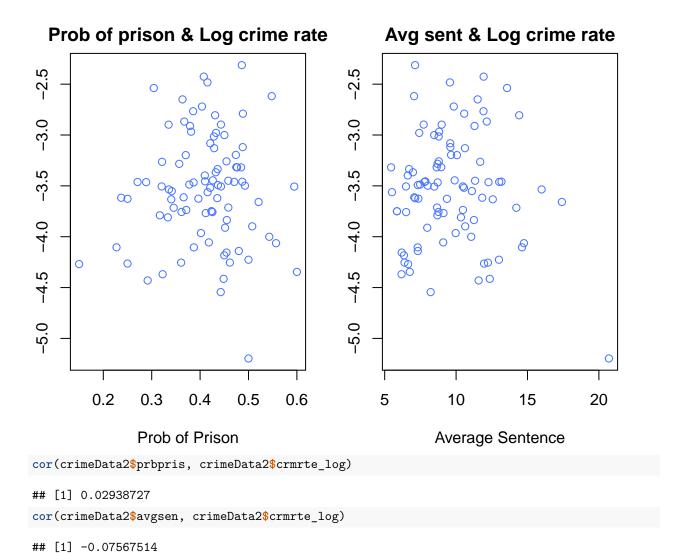
^{*} The correlation between crmrte and prbarr is -0.37

^{*} The correlation between crmrte log and prbarr is -0.41



Probability of prison (prbpris) | Average sentence days (avgsen)

Neither scatter plots below (prbpris vs. crmrte_log, avgsen vs. crmrte_log) shows obvious relationships. The correlation coefficients are only 0.03 and -0.08 respectively.



Police per capita (polpc)

Similar to probabilities of arrest and conviction, we observed a linear relationship between crime rate and policy per capita in the scatter plot below. The scatter plot also shows that County 115 has significantly higher police per capital than any other counties, County 115 is a highly leveraged observation. In addition, the variation of crmrte increases as proconv increases, which justifies taking the log of crmrte. The correlation between crmrte_log and polpc (after removing County 115) is 0.45.

We also noticed that the distribution of polpc is highly skewed to the right, so we took the log of polpc. The correlation coefficient (after removing County 115) increased from 0.45 to 0.54.

```
xlab = "Police per capita",ylab = "Log of Crime Rate",col="royalblue1")
cor(crimeData3$polpc, crimeData3$crmrte_log)
## [1] 0.453951
hist(crimeData2$polpc, main="Histogram of Police per Capita",
     xlab = "Police per capita" , col = "royalblue1")
            Polpc & Crime Rate
                                                             Polpc & Crime Rate
0.10
                                                0.10
                                                                    55
                   O
90.0
                                                90.0
                                                                     195
                     0
0.02
                                                0.02
         0.002
                 0.004
                          0.006
                                   0.008
                                                                          0.006
                                                         0.002
                                                                  0.004
                                                                                   0.008
                Police per capita
                                                                 Police per capita
          Polpc & Log Crime Rate
                                                      Histogram of Police per Capita
                                                 9
                                                 4
S
                                         O
                                                20
                            0
                0.002
                                   0.004
                                                    0.000
      0.001
                         0.003
                                                           0.002
                                                                  0.004
                                                                         0.006
                                                                                0.008
                                                                                       0.010
                Police per capita
                                                                 Police per capita
crimeData2$polpc_log <- log(crimeData2$polpc)</pre>
crimeData3 <- crimeData2[which(crimeData2$county!=115),]</pre>
cor(crimeData3$polpc_log, crimeData3$crmrte_log)
```

[1] 0.541829

People per square mile (density) | If in SMSA (urban)

The histogram shows the distribution of density is highly skewed to the right, so we took the log of density. The scatter plot shows County 173 is highly leveraged as it has much lower population density than other counties. Removing County 173 significantly increases correlation coefficient from 0.49 to 0.68. The correlation between density and crmrte_log (without County 173) is 0.63, which is lower than the correlation between density_log and crmrte_log (without County 173) of 0.68. This further confirms that log of density has a stronger linear relationship with log of crime rate than density does.

Urban is a binary variable. The box plot shows that the mean and interquartile range of density is significantly different depending on whether county is in urban area or not. Log of density is highly correlated with urban with a correlation coefficient of 0.66. When building the model, we should avoid putting both variables in the model for two reasons:

- 1. Adding the second variable doesn't explain much additional variation of the response variable
- 2. High correlation can greatly increase the standard errors of parameter estimates

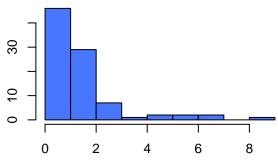
```
par(mfrow=c(2,2))
par(mar=c(4, 2, 2, 2))
hist(crimeData2$density, main="Histogram of People per Square Mile",
     xlab = "People per Square Mile / Density " , col = "royalblue1")
crimeData2$density_log <- log(crimeData2$density)</pre>
plot(crimeData2$density_log, crimeData2$crmrte_log,main = "Log Density & Crime Rate" ,
     xlab = "Log of Density",ylab = "Log of Crime Rate",col="royalblue1")
plot(crimeData2$density_log, crimeData2$crmrte_log,main = "Log Density & Crime Rate" ,
     xlab = "Log of Density",ylab = "Log of Crime Rate",col="royalblue1")
text(crimeData2$density_log, crimeData2$crmrte_log, labels = crimeData2$county, cex=0.7, pos=3 , col =
crimeData4 <- crimeData2[which(crimeData2$county!=173),]</pre>
cor(crimeData2$density_log, crimeData2$crmrte_log)
## [1] 0.4909562
cor(crimeData4$density_log, crimeData4$crmrte_log)
## [1] 0.677355
```

[1] 0.6281475

boxplot(density~urban, data=crimeData2, main = "Box plot of crime rate")

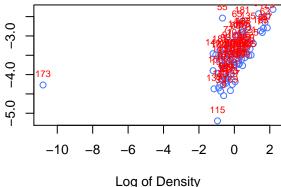
Histogram of People per Square Mile

cor(crimeData4\$density, crimeData4\$crmrte_log)

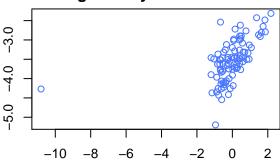


People per Square Mile / Density

Log Density & Crime Rate

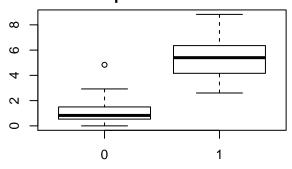


Log Density & Crime Rate



Log of Density

Box plot of crime rate



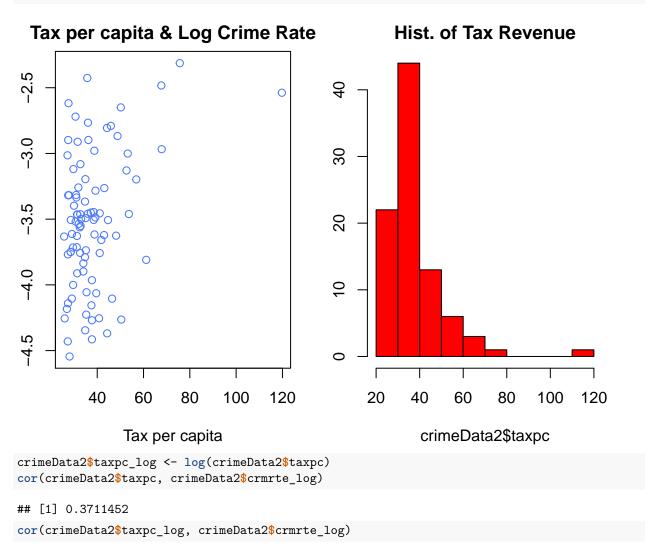
```
cor(crimeData4$urban, crimeData4$density_log)
```

[1] 0.660531

[1] 0.3570773

Tax revenue per capita (taxpc)

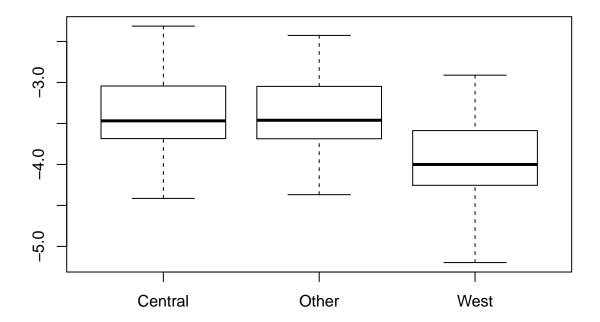
The scatter plot indicates there may be a weak linear relationship between taxpc and crmrte_log. The histogram of taxpc is skewed to the right, so we considered taking the log of taxpc. However, the correlation between taxpc and crmrte_log (0.37) is slightly higher than the correlation between taxpc_log and crmrte_log (0.36).



If in western/central North Carolina

We created a variable, area, to categorize the area counties reside in. Area takes three values: West, Central, and Other. The box plot shows that the mean and interquartile range of crmrte_log is very similar between Central and Other. The crmrte_log for West area is lower than other areas. In modeling, we can group "Central" and "Other" together and only add the variable "West" to the model.

```
crimeData2$area <- ifelse(crimeData2$west==1, "West", ifelse(crimeData2$central==1, "Central", "Other")
boxplot(crmrte_log~area, data=crimeData2)</pre>
```



Percent of minority in 1980 (pctmin80)

The scatter plot shows a weak linear relationship between log of crime rate and percent of minority. Low correlation coefficient (0.3) also confirms that.

% Minority & Log crime rate



cor(crimeData2\$pctmin80, crimeData2\$crmrte_log)

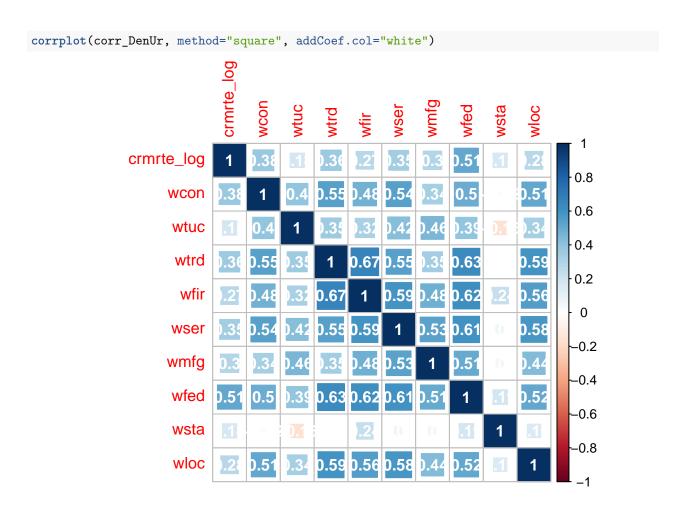
[1] 0.2957882

Weekly wages

There are nine variables related to weekly wages in the data. They represent weekly wages in different industries. As the correlation matrix shows, most of the weekly wages variables are highly correlated except for wsta. When building the model, we should avoid putting all the correlated variables in the model for the same reason pointed out in the density/urban section of the EDA. We also noticed that log of crime rate has the strongest linear relationship with wfed with correlation coefficient of 0.51.

```
crimeData_temp1 <- crimeData2[,c("crmrte_log","wcon", "wtuc", "wtrd", "wfir", "wser", "wmfg", "wfed", "
corr_DenUr <- cor(crimeData_temp1, use="pairwise")
library(corrplot)</pre>
```

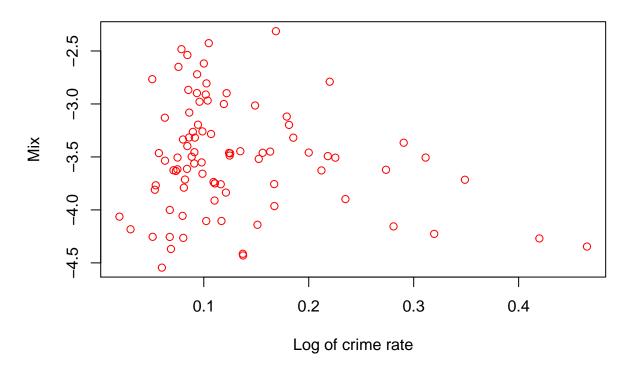
```
## Warning: package 'corrplot' was built under R version 3.4.4
## corrplot 0.84 loaded
```



Offense mix: face-to-face/other (mix)

The scatter plot doesn't indicate a strong relationship between mix and log of crime rate. The weak correlation coefficient (-0.15) also confirms that.

Mix & Log crime rate



```
cor(crimeData2$mix, crimeData2$crmrte_log)
```

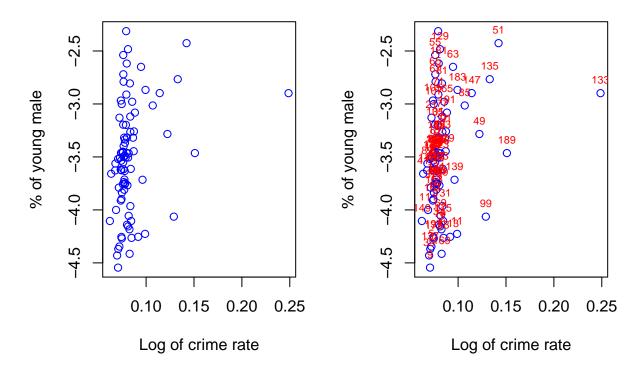
[1] -0.1466527

Percent young male (pctymle)

The scatter plot shows that the majority of counties have 5%-10% of young male. County 133 has significantly higher male percentage than the rest of counties. Log of crime rate doesn't seem to vary by the percent of young male based on the scatter plot, which is also evidented by 0.27 correlation coefficient.

% young M & Log crime rate

% young M & Log crime rate



```
cor(crimeData2$pctymle, crimeData2$crmrte_log)
```

[1] 0.2723973

Model Building 1

In the first model, we only include the four key variables we are interested in. They are probability of arrest, probability of conviction, probability of prison, average sentences. Based on the EDA above, we take the log of crime rate as our response variable and didn't find any transformation to be necessary for the four explanatory variables.

```
\log (\text{Crime Rate}) = \beta_0 + \beta_1 \cdot (\text{prbarr}) + \beta_2 \cdot (\text{prbconv}) + \beta_3 \cdot (\text{prbpris}) + \beta_4 \cdot (\text{avgsen})
```

```
model1 <- lm(crmrte_log ~ prbarr+prbconv+prbpris+avgsen, data=crimeData2)
model1$coefficients

## (Intercept) prbarr prbconv prbpris avgsen
## -2.92426013 -2.09740014 -0.79654556 0.42628304 0.02705387

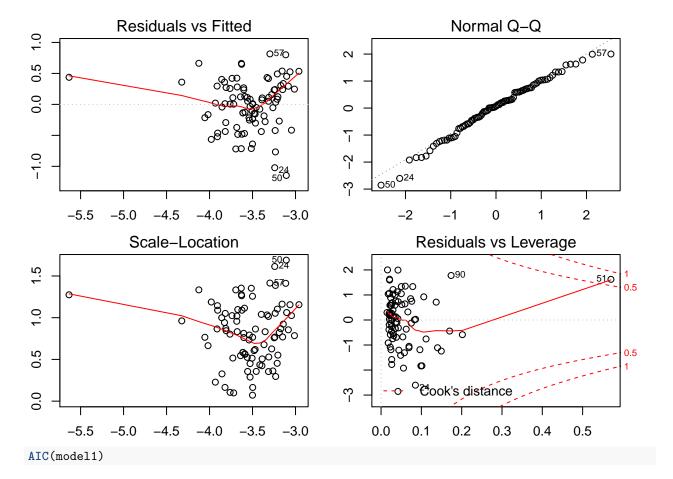
library(lmtest)

## Warning: package 'lmtest' was built under R version 3.4.4

## Loading required package: zoo

##
## Attaching package: 'zoo'</pre>
```

```
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
library(sandwich)
## Warning: package 'sandwich' was built under R version 3.4.3
coeftest(model1, vcov = vcovHC)
##
## t test of coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -2.924260
                          0.441535 -6.6229 3.024e-09 ***
## prbarr
               -2.097400
                          0.531077 -3.9493 0.0001611 ***
                          0.198873 -4.0053 0.0001322 ***
               -0.796546
## prbconv
## prbpris
                0.426283
                           0.652947 0.6529 0.5156084
## avgsen
                0.027054
                           0.019351 1.3980 0.1657380
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
par(mfrow=c(2,2))
par(mar=c(2, 2, 2, 2))
plot(model1)
```



[1] 101.9591

Cook's distance for Observation 51, which is County 115, is close to 1.

Model Building 2

Based on EDA, we concludes that the following variables are highly correlated with the response variable, with correlation coefficient greater than 0.3:

prbarr, prbconv, density log, west, and wfed.

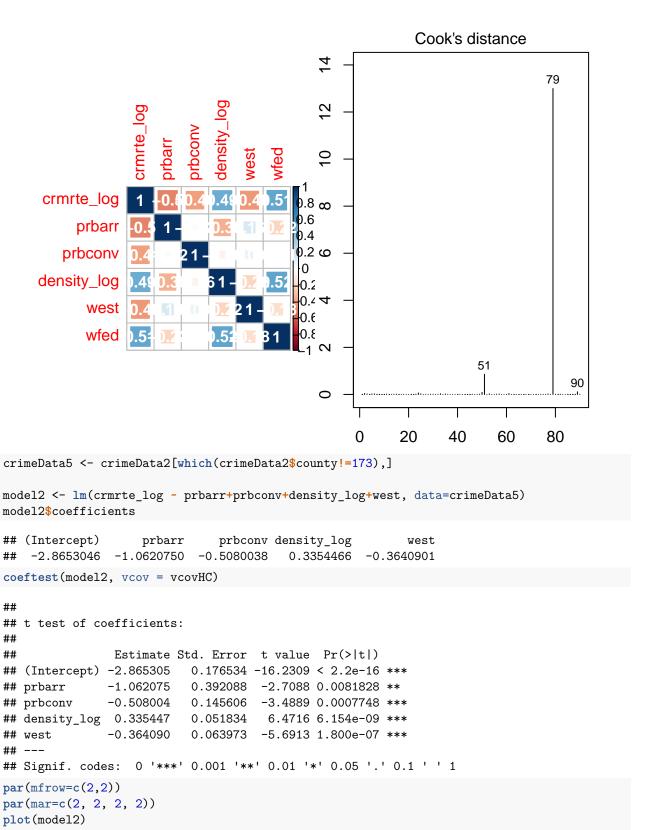
The variable "urban" and a few other weekly wages variables are excluded from the list above due to their higher correlation with other explanatory variables.

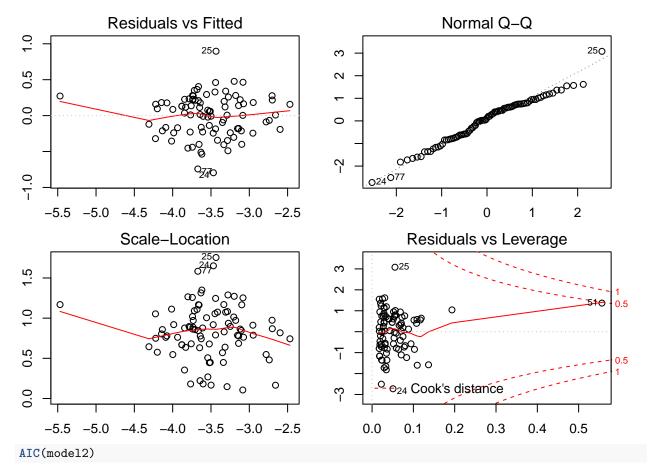
The pairwise correlation table shows that log of density is highly correlated with federal employee wages. Since the proportion of federal employees in a county is small, this variable may not represent the wage characteristics of a county. So we remove federal employee wages from the model.

```
\log (\text{Crime Rate}) = \beta_0 + \beta_1 \cdot (\text{prbarr}) + \beta_2 \cdot (\text{prbconv}) + \beta_3 \cdot (\log \text{density}) + \beta_4 \cdot (\text{west})
```

Since the 79th observation (County 173) has Cook's distance greater than 1, we removed this observation from the model.

```
par(mfrow=c(1,2))
par(mar=c(2, 2, 2, 2))
crimeData_temp2 <- crimeData2[,c("crmrte_log", "prbarr", "prbconv", "density_log", "west", "wfed")]</pre>
corr_Model2 <- cor(crimeData_temp2, use="pairwise")</pre>
corrplot(corr Model2, method="square", addCoef.col="white")
model2 <- lm(crmrte_log ~ prbarr+prbconv+density_log+west, data=crimeData2)</pre>
model2$coefficients
## (Intercept)
                               prbconv density_log
                    prbarr
                                                           west
## -2.6678777 -1.4154097 -0.6540471
                                          0.1094127
                                                    -0.3468193
coeftest(model2, vcov = vcovHC)
##
## t test of coefficients:
##
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.667878
                           0.305360 -8.7368 1.842e-13 ***
                           0.658391 -2.1498 0.0344125 *
## prbarr
               -1.415410
## prbconv
               -0.654047
                           0.233987 -2.7952 0.0064099 **
## density_log 0.109413
                           0.227349 0.4813 0.6315725
## west
               -0.346819
                           0.086012 -4.0322 0.0001201 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
plot(model2, which=4)
```





[1] 44.8252

Assessment of the CLM assumptions

- CLM 1: A linear model
 - The model is specified such that the dependent variable is a linear function of the explanatory variables.
 - This assumption is satisfied.
- CLM 2: Random sampling
 - Each observation represents a county in North Carolina. Only a selection of counties are included in the data. Since we do not have knowledge how counties are selected, we cannot confirm the selection is random.
- CLM 3: Multicollinearity
- CLM 4: Zero-conditional mean
- CLM 5: Homoscedasticity
- CLM 6: Normality of residuals

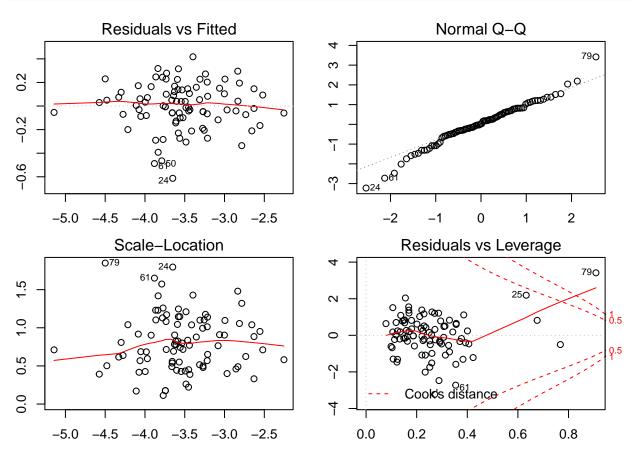
Evaluation of statistical and pratical significance

Model Building 3

```
For this model, we add all the variables to the model.
```

```
model3 <- lm(crmrte_log ~ prbarr+prbconv+prbpris+avgsen+polpc_log+density_log+taxpc+west+</pre>
            central+urban+pctmin80_2+wcon+wtuc+wtrd+wfir+wser+wmfg+wfed+wsta+wloc+mix+
            pctymle, data=crimeData2)
model3$coefficients
##
    (Intercept)
                   prbarr
                              prbconv
                                         prbpris
                                                      avgsen
##
   0.6276444944 \ -1.8190558437 \ -0.5659797104 \ -0.6806825821 \ -0.0270524579
##
     polpc_log
               density_log
                                taxpc
##
   0.6021669897
              ##
         urban
                pctmin80_2
                                 wcon
                                            wtuc
              0.9980385344
##
   0.1513316157
                          0.0003784841
                                     0.0002289608
                                                 0.0017024817
##
         wfir
                     wser
                                wmfg
                                            wfed
                                                        wsta
  -0.0009627851 -0.0020813035 -0.0003396119
                                     0.0017579658 -0.0006933810
##
##
         wloc
                      mix
                              pctymle
  0.0016560744 -0.0504661995
                          2.0567468321
coeftest(model3, vcov = vcovHC)
##
## t test of coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 0.62764449 1.70769377 0.3675 0.7143753
## prbarr
            -1.81905584   0.34102505   -5.3341   1.222e-06 ***
## prbconv
            -0.56597971   0.15843282   -3.5724   0.0006609 ***
## prbpris
            ## avgsen
            ## polpc_log
             0.60216699 0.20149853 2.9884 0.0039167 **
## density_log 0.10274766 0.20823129 0.4934 0.6233220
## taxpc
             0.00192305 0.00549983 0.3497 0.7276938
## west
            ## central
            -0.07127277
                      0.09719315 -0.7333 0.4659271
## urban
             0.15133162  0.26447780  0.5722  0.5691081
## pctmin80 2
             0.99803853  0.29650171  3.3660  0.0012661 **
## wcon
             0.00037848 0.00069862 0.5418 0.5897814
## wtuc
             0.00022896 0.00060391 0.3791 0.7057912
## wtrd
             ## wfir
## wser
            -0.00033961 0.00042854 -0.7925 0.4308740
## wmfg
## wfed
            0.00175797  0.00107766  1.6313  0.1075235
## wsta
            0.00165607 0.00200238 0.8271 0.4111430
## wloc
## mix
            2.05674683 1.62341958 1.2669 0.2095693
## pctymle
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
par(mfrow=c(2,2))
par(mar=c(2, 2, 2, 2))
plot(model3)
```



Model Display

```
#se.model1 = sqrt(diag(vcovHC(model1)))#se.model2 = sqrt(diag(vcovHC(model2)))#se.model3 = sqrt(diag(vcovHC(model3)) #sqrt(diag(vcovHC(model3)))#se.model3 = sqrt(diag(vcovHC(model3)))#se.model3 = sqrt(diag(vcovHC(model3)))#se.model3 = sqrt(diag(vcovHC(model3)))#se.model3 = sqrt(diag(vcovHC(model3)))#se.model3 = sqrt(diag(vcovHC(model3)))#se.model3 = sqrt(diag(vcovHC(model2)))#se.model3 = sqrt(diag(vcovHC(model3)))#se.model3 = sqrt(diag(vcovHC(model3))#se.model3 = sqrt(diag(vcovHC(model3))#se.mo
```

% Table created by stargazer v.5.2 by Marek Hlavac, Harvard University. E-mail: hlavac at fas.harvard.edu % Date and time: Sat, Apr 14, 2018 - 7:34:29 PM

	(1)	(2)	(3)
prbarr	-2.097^{***} (0.323)	-1.062^{***} (0.256)	-1.819^{***} (0.232)
prbconv	-0.797^{***} (0.145)	-0.508*** (0.105)	-0.566^{***} (0.098)
prbpris	0.426 (0.543)		-0.681 (0.362)
avgsen	0.027 (0.016)		-0.027^* (0.011)
polpc_log			0.602*** (0.106)
density_log		$0.335^{***} (0.047)$	0.103*** (0.030)
taxpc			0.002 (0.003)
west		-0.364^{***} (0.075)	-0.068 (0.109)
central			-0.071 (0.074)
urban			0.151 (0.116)
pctmin80_2			0.998*** (0.258)
wcon			0.0004 (0.001)
wtuc			0.0002 (0.0004)
wtrd			0.002 (0.001)
wfir			-0.001 (0.001)
wser			-0.002^* (0.001)
wmfg			-0.0003 (0.0004)
wfed		24	0.002* (0.001)
wsta			-0.001

Omitted Variables

We are interested in the relationship between prbarr and prbconv and our "omitted" variables mentioned below. 1.) Education 2.) Percentage of people using drug 3.) Percentage of people are married with kids 4.) Percentage of people who own guns 5.) Percentage of smart mobile penetration

Suppose our estimation model is represented by below equation , where A is prbarr and B is prbconv. $\beta_0, \beta_1, \beta_2$ is the intercepts and coefficients of A (prbarr) and B (prbconv) respectively. We can represent the Population regression as

$$Y(Population) = \beta_0 + \beta_1 A + \beta_2 B$$

$$Y(Estimated) = \alpha_0 + \alpha_1 A + \alpha_2 B$$

$$Y(EstModel1) = -2.92426013 - 2.09740014 * prbarr - 0.79654556 * prbconv$$

Omitted variable 1: Education

Crime rate and Education are negatively correlated (NEGATIVE).

We estimate a negative correlation between Crime Rate and Education based on following logic and reasoning. We estimate that higher the education within the population then they are less likely to commit a crime. Another reason could be that educated people tend to understand the law better and are more likely to respect the law and less likely to commit crime.

prbarr and Education are negatively correlated (NEGATIVE)

We estimate that educated people are more likely to be aware of their rights and they are more likely to avoid being wrongfully arrested, hence reduced arrest rates. Also police are less likely to believe an educated person committed the crime. Finally more educated people are more familiar with investigation methods and hence are less likely to leave less clues if they had committed the crime, leading to less likelihood of arrests. Hence we estimate that education and prbarr are negatively correlated.

$$\alpha_1 < 0$$

this is positive bias, alpha1 (estimated) = -2.1 = beta1 (true) + positive

$$\alpha(estimated) = -2.1 = \beta_1(true) + (positive)$$

True Coefficient is even more negative what is estimated and hence increase in statistical significance.

prbconv and Education are negatively correlated (NEGATIVE).

We estimate that higher education people are likely to have have higher income. People with higher income are more likely to afford better lawyers and legal help and are less likely to be convicted. Overall positive bias.

$$\alpha_1 < 0$$

This is positive bias, alpha (estimated) = -0.8 = beta (true) + positive

$$\alpha(estimated) = -0.8 = \beta(true) + (positive)$$

True Coefficient is even more negative what is estimated and hence increase in statistical significance.

Omitted variable 2: % of people using drug

Crime rate and % of people using drug are positively correlated (POSITIVE).

We estimate a positive correlation between Crime Rate and % of people using drug based on following logic and reasoning. We estimate that people under the influence of drugs are more likely to commit a crime.

prbarr and % of people using drug are positively correlated (POSITIVE).

We estimate that drug addicts are easier to be found if they committed the crime leading to likelihood of higher arrests. Another reason could be that police are more likely to believe that drug addicts committed the crime. Finally the people consuming drugs are likely to consume drugs in groups and when police perform arrests they are likely to find other drug consuming people leading to higher arrests. Hence we estimate that % of people using drugs and prbarr are positively correlated.

$$\alpha_1 < 0$$

this is positive bias , alpha1 (estimated) = -2.1 = beta1 (true) + positive

$$\alpha(estimated) = -2.1 = \beta_1(true) + (positive)$$

True Coefficient is even more negative what is estimated and hence increase in STATISTICAL significance.

prbconv and % of people using drug are positively correlated (POSITIVE).

We estimate that % of people using drugs are likely to be spend all their money on drugs leading to poverty. People in poverty are less likely to get best legal help and are likely to have higher convition rates. Overall positive bias.

$$\alpha_1 < 0$$

This is positive bias, alpha (estimated) = -0.8 = beta (true) + positive

$$\alpha(estimated) = -0.8 = \beta(true) + (positive)$$

True Coefficient is even more negative what is estimated and hence increase in STATISTICAL significance.

Omitted variable 3: % of people are married with kids

Crime rate and % of people are married with kids are negatively correlated (NEGATIVE).

We estimate a negative correlation between Crime Rate and % of people are married with kids based on following logic and reasoning. We estimate that married couples with kids to have more considerations for family and thus less likely to commit a crime.

prbarr and % of people are married with kids are negatively correlated (NEG-ATIVE).

We estimate that people married with kids are unlikely to come forward as a witness of a crime (in worry of wellbeing of their family) with any information leading to reduced probability of arrest.

$$\alpha_1 < 0$$

this is positive bias, alpha1 (estimated) = -2.1 = beta1 (true) + positive

$$\alpha(estimated) = -2.1 = \beta_1(true) + (positive)$$

True Coefficient is even more negative what is estimated and hence increase in STATISTICAL significance.

prbconv and % of people are married with kids are negatively correlated (NEG-ATIVE).

We estimate that % of people are married with kids are expected to have less convitions since the judges are likely to keep in consideration impact on the family and kids of the conviction.

$$\alpha_1 < 0$$

This is positive bias, alpha (estimated) = -0.8 = beta (true) + positive

$$\alpha(estimated) = -0.8 = \beta(true) + (positive)$$

True Coefficient is even more negative what is estimated and hence increase in STATISTICAL significance.

Omitted variable 4: % of people who own guns

Crime rate and % of people who own guns are positively correlated (POSITIVE).

We estimate a positive correlation between Crime Rate and % of people who own guns based on following logic and reasoning. With more people owning guns , small alterations / conflicts can lead to gun fight leading to higher rates of crime.

prbarr and % of people who own guns are positively correlated (POSITIVE).

We estimate that people who are gun owners are more likely to involved in shooting related crimes. We estimate that since the guns and gun owners are more likely to easily tracked this can lead to higher probability of arrests.

$$\alpha_1 < 0$$

this is positive bias, alpha1 (estimated) = -2.1 = beta1 (true) + positive

$$\alpha(estimated) = -2.1 = \beta_1(true) + (positive)$$

True Coefficient is even more negative what is estimated and hence increase in STATISTICAL significance.

prbconv and % of people who own guns are negatively correlated (NEGATIVE).

We estimate that % of people who own guns are expected to richer than others and hence more likely to afford better lawyers and legal help. this can lead to less conviction rates.

$$\alpha_1 < 0$$

This is positive bias, alpha (estimated) = -0.8 = beta (true) + negative

$$\alpha(estimated) = -0.8 = \beta(true) + (negative)$$

True Coefficient is less negative what is estimated and hence loose STATISTICAL significance.

Omitted variable 5: % of smart mobile penetration

Crime rate and % of smart mobile penetration are positively correlated (POSI-TIVE).

We estimate a positive correlation between Crime Rate and % of smart mobile penetration based on following logic and reasoning. With higher smart phone users are more likely to use better communication methods via encrypted apps for committing the crime , hence increasing the likelihood of crime rates. Another possible reason can be that smart phones themselves are expensive devices and with higher smart phones in a county can lead to higher theft cases of smart phones itself , hence increasing crime rates.

prbarr and % of smart mobile penetration are negatively correlated (NEGA-TIVE).

We estimate that people using smart phone are more likely to use encrypted apps on the smart phones for communication for committing the crime. Since these encrypted application are extremely difficult to track and hence leading to reduced arrest rates.

$$\alpha_1 < 0$$

this is less negative bias, alpha1 (estimated) = -2.1 = beta1 (true) + negative

$$\alpha(estimated) = -2.1 = \beta_1(true) + (negative)$$

prbarr has less impact on the log of crime rate (lose statistical significance)

prbconv and % of smart mobile penetration are negatively correlated (NEGATIVE).

We estimate that smart phone has higher protection (such as iPhone), which are harder to crack by police , hence reducing the conviction rates. Also we estimate that not all police departments are good at dealing with digital evidence and hence leading to reduced conviction rates.

$$\alpha_1 < 0$$

this is less negative bias, alpha (estimated) = -0.8 = beta (true) + negative

$$\alpha(estimated) = -0.8 = \beta(true) + (negative)$$

prbconv has less impact on the log of crime rate (lose statistical significance).