

The following is an attempt to write a denotational semantics for Nu's scripting system, based on <https://www.youtube.com/watch?v=bmKYiUOEo2A>. This presentation uses a more improvised style of syntax than the Conal's, however.

Axiomatic Denotations - When a μ is defined in terms of itself, we consider it axiomatic and irreducible directly in this context.

```
rec  $\mu$ :Value<a> =
|  $\mu$ :Value< $\mu$ :Relation>
|  $\mu$ :Value< $\mu$ :Address>
|  $\mu$ :Value< $\mu$ :Name>
|  $\mu$ :Value< $\mu$ :String>
|  $\mu$ :Value< $\mu$ :Bool>
|  $\mu$ :Value< $\mu$ :Unit>

and  $\mu$ :Stream<a> =
|  $\mu$ :Address ->  $\mu$ :Stream<a>
|  $\mu$ :Name ->  $\mu$ :Relation ->  $\mu$ :Stream<a>
|  $\mu$ :Stream< $\alpha\alpha$  -> a) ->  $\mu$ :Stream<a>
|  $\mu$ :Stream< $\alpha\mu$ :Stream< $\beta\mu$ :Stream<a when a =  $\alpha$  *  $\beta$ >
|  $\mu$ :Stream< $\alpha\mu$ :Stream< $\beta\mu$ :Stream<a when a =  $\alpha$  |  $\beta$ >
```

μ :Effect = μ :Effect // transforms the environment

μ :Declare a = μ :Name -> μ :Declaration a // augments the environment

Derived Denotations

μ :Get<a> = μ :Name -> μ :Relation -> μ :Value<a>

μ :Set<a> = μ :Name -> μ :Relation -> μ :Value<a> -> μ :Effect

μ :Command<a> = μ :Value<a> -> μ :Effect

μ :Fold<a b> = (μ :Value<a> -> b) -> μ :Stream<a> -> b

μ :Define<a> = μ :Declare< μ :Value<a>>

μ :Variable<a> = μ :Declare< μ :Stream<a>>

μ :Equate<a> = \name -> \rel -> μ :Stream<a> -> μ :Fold (μ :Set<a> name rel)

μ :Handle<a> = μ :Stream<a> -> μ :Fold μ : Command <a>