

# Spring 2023 Data C100/C200 Midterm Reference Sheet

## Pandas

Suppose `df` is a DataFrame; `s` is a Series. `import pandas as pd`

Function	Description
<code>df[col]</code>	Returns the column labeled <code>col</code> from <code>df</code> as a Series.
<code>df[[col1, col2]]</code>	Returns a DataFrame containing the columns labeled <code>col1</code> and <code>col2</code> .
<code>s.loc[rows] / df.loc[rows, cols]</code>	Returns a Series/DataFrame with rows (and columns) selected by their index values.
<code>s.iloc[rows] / df.iloc[rows, cols]</code>	Returns a Series/DataFrame with rows (and columns) selected by their positions.
<code>s.isnull() / df.isnull()</code>	Returns boolean Series/DataFrame identifying missing values
<code>s.fillna(value) / df.fillna(value)</code>	Returns a Series/DataFrame where missing values are replaced by <code>value</code>
<code>df.drop(labels, axis)</code>	Returns a DataFrame without the rows or columns named <code>labels</code> along <code>axis</code> (either 0 or 1)
<code>df.rename(index=None, columns=None)</code>	Returns a DataFrame with renamed columns from a dictionary <code>index</code> and/or <code>columns</code>
<code>df.sort_values(by, ascending=True)</code>	Returns a DataFrame where rows are sorted by the values in columns <code>by</code>
<code>s.sort_values(ascending=True)</code>	Returns a sorted Series.
<code>s.unique()</code>	Returns a NumPy array of the unique values
<code>s.value_counts()</code>	Returns the number of times each unique value appears in a Series
<code>pd.merge(left, right, how='inner', on='a')</code>	Returns a DataFrame joining DataFrames <code>left</code> and <code>right</code> on the column labeled <code>a</code> ; the join is of type <code>inner</code>
<code>left.merge(right, left_on=col1, right_on=col2)</code>	Returns a DataFrame joining DataFrames <code>left</code> and <code>right</code> on columns labeled <code>col1</code> and <code>col2</code> .
<code>df.pivot_table(index, columns, values=None, aggfunc='mean')</code>	Returns a DataFrame pivot table where columns are unique values from <code>columns</code> (column name or list), and rows are unique values from <code>index</code> (column name or list); cells are collected <code>values</code> using <code>aggfunc</code> . If <code>values</code> is not provided, cells are collected for each remaining column with multi-level column indexing.
<code>df.set_index(col)</code>	Returns a DataFrame that uses the values in the column labeled <code>col</code> as the row index.
<code>df.reset_index()</code>	Returns a DataFrame that has row index 0, 1, etc., and adds the current index as a column.

Let `grouped = df.groupby(by)` where `by` can be a column label or a list of labels.

Function	Description
<code>grouped.count()</code>	Return a Series containing the size of each group, excluding missing values
<code>grouped.size()</code>	Return a Series containing size of each group, including missing values
<code>grouped.mean()/grouped.min()/grouped.max()</code>	Return a Series/DataFrame containing mean/min/max of each group for each column, excluding missing values
<code>grouped.filter(f)</code> <code>grouped.agg(f)</code>	Filters or aggregates using the given function <code>f</code>

Function	Description
<code>s.str.len()</code>	Returns a Series containing length of each string
<code>s.str.lower()/s.str.upper()</code>	Returns a Series containing lowercase/uppercase version of each string
<code>s.str.replace(pat, repl)</code>	Returns a Series after replacing occurrences of substrings matching regular expression <code>pat</code> with string <code>repl</code>
<code>s.str.contains(pat)</code>	Returns a boolean Series indicating whether a substring matching the regular expression <code>pat</code> is contained in each string
<code>s.str.extract(pat)</code>	Returns a Series of the first subsequence of each string that matches the regular expression <code>pat</code> . If <code>pat</code> contains one group, then only the substring matching the group is extracted

Visualization

Matplotlib: **x** and **y** are sequences of values.

Function	Description
<code>plt.plot(x, y)</code>	Creates a line plot of <b>x</b> against <b>y</b>
<code>plt.scatter(x, y)</code>	Creates a scatter plot of <b>x</b> against <b>y</b>
<code>plt.hist(x, bins=None)</code>	Creates a histogram of <b>x</b> ; <b>bins</b> can be an integer or a sequence
<code>plt.bar(x, height)</code>	Creates a bar plot of categories <b>x</b> and corresponding heights <b>height</b>

Tukey-Mosteller Bulge Diagram.

Seaborn: **x** and **y** are column names in a DataFrame **data**. `import seaborn as sns`

Function	Description
<code>sns.countplot(data, x)</code>	Create a barplot of value counts of variable <b>x</b> from <b>data</b>
<code>sns.histplot(data, x, kde=False)</code> <code>sns.displot(x, data, rug=True, kde=True)</code>	Creates a histogram of <b>x</b> from <b>data</b> ; optionally overlay a kernel density estimator. <b>displot</b> is similar but can optionally overlay a rug plot.
<code>sns.boxplot(data, x=None, y)</code> <code>sns.violinplot(data, x=None, y)</code>	Create a boxplot of <b>y</b> , optionally factoring by categorical <b>x</b> , from <b>data</b> . <b>violinplot</b> is similar but also draws a kernel density estimator of <b>y</b> .
<code>sns.scatterplot(data, x, y)</code>	Create a scatterplot of <b>x</b> versus <b>y</b> from <b>data</b>
<code>sns.lmplot(x, y, data, fit_reg=True)</code>	Create a scatterplot of <b>x</b> versus <b>y</b> from <b>data</b> , and by default overlay a least-squares regression line
<code>sns.jointplot(x, y, data, kind)</code>	Combine a bivariate scatterplot of <b>x</b> versus <b>y</b> from <b>data</b> , with univariate density plots of each variable overlaid on the axes; <b>kind</b> determines the visualization type for the distribution plot, can be <b>scatter</b> , <b>kde</b> or <b>hist</b>

Regular Expressions

Operator	Description	Operator	Description
<code>.</code>	Matches any character except <code>\n</code>	<code>*</code>	Matches preceding character/group zero or more times
<code>\\</code>	Escapes metacharacters	<code>?</code>	Matches preceding character/group zero or one times
<code> </code>	Matches expression on either side of expression; has lowest priority of any operator	<code>+</code>	Matches preceding character/group one or more times
<code>\d, \w, \s</code>	Predefined character group of digits (0-9), <code>^</code> , <code>\$</code> alphanumerics (a-z, A-Z, 0-9, and underscore), or whitespace, respectively		Matches the beginning and end of the line, respectively
<code>\D, \W, \S</code>	Inverse sets of <code>\d, \w, \s</code> , respectively	<code>( )</code>	Capturing group used to create a sub-expression
<code>{m}</code>	Matches preceding character/group exactly <b>m</b> times	<code>[ ]</code>	Character class used to match any of the specified characters or range (e.g. <code>[abcde]</code> is equivalent to <code>[a-e]</code> )
<code>{m, n}</code>	Matches preceding character/group at least <b>m</b> times and at most <b>n</b> times if either <b>m</b> or <b>n</b> are omitted, set lower/upper bounds to 0 and $\infty$ , respectively	<code>[^ ]</code>	Invert character class; e.g. <code>[^a-c]</code> matches all characters except <b>a</b> , <b>b</b> , <b>c</b>
Function	Description		
<code>re.match(pattern, string)</code>	Returns a match if zero or more characters at beginning of <b>string</b> matches <b>pattern</b> , else None		
<code>re.search(pattern, string)</code>	Returns a match if zero or more characters anywhere in <b>string</b> matches <b>pattern</b> , else None		
<code>re.findall(pattern, string)</code>	Returns a list of all non-overlapping matches of <b>pattern</b> in <b>string</b> (if none, returns empty list)		

Function	Description
<code>re.sub(pattern, repl, string)</code>	Returns <code>string</code> after replacing all occurrences of <code>pattern</code> with <code>repl</code>

Modified lecture example for a single capturing group:

```
lines = '169.237.46.168 - - [26/Jan/2014:10:47:58 -0800] "GET ... HTTP/1.1"'
re.findall(r'\[\d+\/(\w+)\/\d+:\d+:\d+:\d+ .+\]', line) # returns ['Jan']
```

## Modeling

Concept	Formula	Concept	Formula
Variance, $\sigma_x^2$	$\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$	Correlation $r$	$r = \frac{1}{n} \sum_{i=1}^n \frac{x_i - \bar{x}}{\sigma_x} \frac{y_i - \bar{y}}{\sigma_y}$
$L_1$ loss	$L_1(y, \hat{y}) =  y - \hat{y} $	Linear regression estimate of $y$	$\hat{y} = \theta_0 + \theta_1 x$
$L_2$ loss	$L_2(y, \hat{y}) = (y - \hat{y})^2$	Least squares linear regression	$\hat{\theta}_0 = \bar{y} - \hat{\theta}_1 \bar{x} \qquad \hat{\theta}_1 = r \frac{\sigma_y}{\sigma_x}$
Empirical risk with loss $L$	$R(\theta) = \frac{1}{n} \sum_{i=1}^n L(y_i, \hat{y}_i)$		

## Ordinary Least Squares

Multiple Linear Regression Model:  $\hat{\mathbb{Y}} = \mathbb{X}\theta$  with design matrix  $\mathbb{X}$ , response vector  $\mathbb{Y}$ , and predicted vector  $\hat{\mathbb{Y}}$ . If there are  $p$  features plus a bias/intercept, then the vector of parameters  $\theta = [\theta_0, \theta_1, \dots, \theta_p]^T \in \mathbb{R}^{p+1}$ . The vector of estimates  $\hat{\theta}$  is obtained from fitting the model to the sample  $(\mathbb{X}, \mathbb{Y})$ .

Concept	Formula	Concept	Formula
Mean squared error	$R(\theta) = \frac{1}{n}   \mathbb{Y} - \mathbb{X}\theta  _2^2$	Normal equation	$\mathbb{X}^T \mathbb{X} \hat{\theta} = \mathbb{X}^T \mathbb{Y}$
		Least squares estimate, if $\mathbb{X}$ is full rank	$\hat{\theta} = (\mathbb{X}^T \mathbb{X})^{-1} \mathbb{X}^T \mathbb{Y}$
Residual vector, $e$	$e = \mathbb{Y} - \hat{\mathbb{Y}}$	Multiple $R^2$ (coefficient of determination)	$R^2 = \frac{\text{variance of fitted values}}{\text{variance of } y}$