Scheme Notes 02

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Mantra Review

- Every expression has a value (exceptions: errors, infinite loops and define)
- ▶ To find the value of a combination.
 - ► Find the values of all of the subexpressions, in any order
 - Apply the value of the first to the values of the rest
- ► The value of a lambda expression is a procedure

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$$(+23)$$

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- x is the only parameter in the parameter list (x)
- What is the body?
- (* x x) is the body of the lambda expression.

```
(define absolute-value (lambda (n) (if (< n 0) (- n) n) (absolute-value (+ 3 -8))
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       -5 0)
(if
(if
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```

Computing the Euclidean distance between two points

```
(define square
   (lambda (x) (* x x)))
(define sum-squares
   (lambda (x y) (+ (square x) (square y))))
(define dist-between-pts
   (lambda (x1 y1 x2 y2)
      (sqrt (sum-squares (- x1 x2) (- y1 y2)))))
Use the substitution model to evaluate (dist-between-pts 1 1 4 5):
```

- ► Applicative Order: Evaluate the arguments and then apply the value of the first to the value of the rest.
 - ▶ Everything is evaluated, whether or not we use it.
 - This is the method Scheme uses and is the reason that we need special forms.
- ▶ Normal Order: Fully expand, then reduce. Don't evaluate operands until they are needed.

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Normal order is not as efficient as applicative order. We needed to evaluate (+ 5 1) and (* 6 2) twice each using normal order, instead of once each with applicative order.

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(sum-squares (+ 5 1) (* 6 2))
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- ▶ Normal order is not as efficient as applicative order. We needed to evaluate (+ 5 1) and (* 6 2) twice each using normal order, instead of once each with applicative order.
- How can we test if Scheme is applicative or normal order?



```
(define p (lambda () (p)))
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What does this function do?

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- What does this function do?
- ▶ It calls itself repeatedly, causing an infinite loop.

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- What does this function do?
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- (test 0 (p))
 - What happens with applicative order?
 - ▶ We get an infinite loop.

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- We get an infinite loop.
- What happens with normal order?

```
(define p (lambda () (p)))
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- What does this function do?
- It calls itself repeatedly, causing an infinite loop.

- ► What happens with applicative order?
- We get an infinite loop.
- What happens with normal order?
- ► It returns 0.

Writing our own if

No real problems so far.

```
What if if were not a special form?
(define new-if
   (lambda (predicate consequent alternative)
       (cond (predicate consequent)
             (else alternative))))
What happens when we evaluate (new-if (> 3 2) 0 2)?
(\text{new-if} (> 3 2) 0 2)
(new-if (> 3 2) 0
(\text{new-if } (> 3 \ 2) |0||2|)
(new-if | (> 3 2)
(new-if | #t|
              0
(cond (|#t||0|) (else |2|))
0
```

Writing our own if

▶ What if we use new-if instead of the special form if?

Writing our own if

- ▶ What if we use new-if instead of the special form if?
- ▶ We'll get an infinite loop, since (* n (fact (- n 1))) will be evaluated every time, even if we have hit the base case.