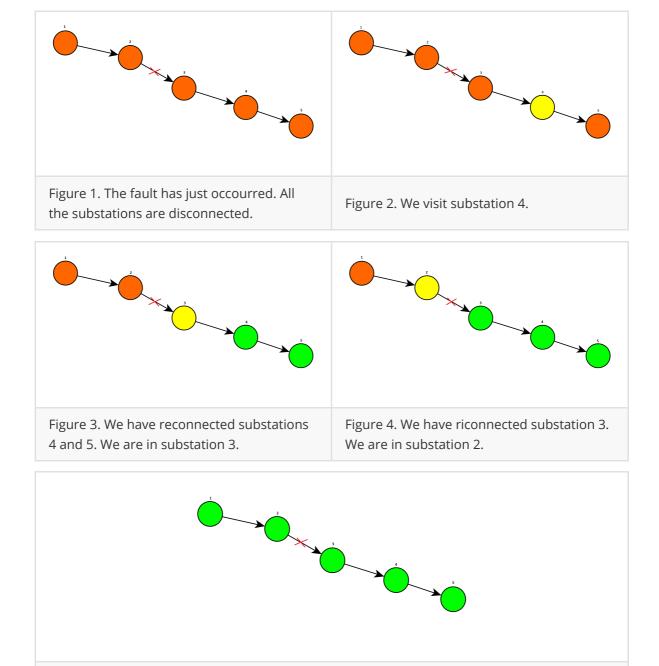
Example

In a graph with 4/5 nodes do the gradient descend. Use the defined transition probabilities and the random policy, then compute Q and η . Then compute the gradient and go on.



Let's use as our example the MDP in Figures 1-5 but pretending that substation 5 doesn't exist (too many computations otherwise). So we have that N=4.

Figure 5. We reconnected substations 1 and 2. All the subsations are reconnected.

We estimated that the number of states is $|\mathcal{S}|\sim O(N\cdot N^2)=O(N^3)$, so in our case we have that $|\mathcal{S}|\sim N^3=4^3=64$. Instead $|\mathcal{A}|\sim O(N)$ so in our case $|\mathcal{A}|\sim 4$.

We have that the fault is $x_g=2-3$ (a branch is identified by an ID or its ends).

So we have that the initial parameters are heta=0, so the policy is:

$$\pi\Big(a \mid s = (x_g, y = (v_k, \{v\}))\Big) = rac{e^{ heta y}}{\sum_{b \in |A|} e^{ heta y}} = rac{e^{ heta y}}{e^{ heta y} \sum_{b \in \{v\}} 1} = rac{1}{|\{v\}|} \,.$$

The equations are:

$$egin{aligned} Q_\pi\Big(s = (x_g, v_k, \{v\}), a\Big) &= d_{v_k, a} \cdot n_{k+1} + \sum_{a' \in \{v'\}} rac{1}{|\{v'\}|} Q\Big(\sigma(s, a), a'\Big) \ \\ \eta_\pi\Big(s' = (x_g, v_{k+1}, \{v'\})\Big) &= rac{1}{N^2} \mathbb{I}ig(\{v'\} = \mathcal{C}ig) + \sum_s rac{1}{|\{v\}|} \eta_\pi\Big(s = (x_g, v_k, \{v\})ig) \end{aligned}$$

Let's suppose we have this time matrix (in seconds) for the values of $d_{v_k,v_{k+1}}$ (for now it is symmetric, but it can also not be symmetric, for example if there are one way streets or if we consider traffic):

and these values for the number of users under each substation:

$$u_1$$
 u_2 u_3 u_4 102 45 256 168

Computation of Q

The initial state is $s_0=(x_g,0,\mathcal{C}=\{1,2,3,4\})$. We have 4 possible actions: $a\in\{1,2,3,4\}$ and we have that $\pi(a|s_0)=\frac{1}{|\{1,2,3,4\}|}=\frac{1}{4}$.

NB: Let's name the states with $s_{abc...}$ where the letters denotes the sequence of visited substations

• if a=1, we can reconnect only substation 1, so the next state is $s_{01}=(x_g,1,\{2,3,4\})$, thus $n_0=\sum_{v\in\mathcal{C}}u_v=\sum_{v\in\{1,2,3,4\}}u_v=102+45+256+168=571$ and we have that

$$Q_{\pi}(s_{0}, 1) = d_{0,1} \cdot n_{0} + \sum_{a' \in \{2,3,4\}} \frac{1}{3} Q(s_{01}, a')$$

$$= 213 \cdot 571 + \frac{1}{3} Q(s_{01}, 2) + \frac{1}{3} Q(s_{01}, 3) + \frac{1}{3} Q(s_{01}, 4)$$

$$Q_{\pi}(s_{0}, 1) - \frac{1}{3} Q(s_{01}, 2) - \frac{1}{3} Q(s_{01}, 3) - \frac{1}{3} Q(s_{01}, 4) = 121623$$

$$(1.1)$$

From here we have these possible actions:

 \circ if a=2, we can reconnect only substation 2, so the next state is $s_{012}=(x_g,2,\{3,4\})$, thus $n_{01}=\sum_{v\in\{2,3,4\}}u_v=45+256+168=469$ and we have that

$$Q_{\pi}(s_{01},2) = d_{1,2} \cdot n_{01} + \sum_{a' \in \{3,4\}} rac{1}{2} Q\Big(s_{012},a'\Big)$$

$$= 633 \cdot 469 + \frac{1}{2}Q(s_{012}, 3) + \frac{1}{2}Q(s_{012}, 4)$$

$$Q_{\pi}(s_{01}, 2) - \frac{1}{2}Q(s_{012}, 3) - \frac{1}{2}Q(s_{012}, 4) = 296877$$
(1.2)

From here we have these possible actions:

• if a=3, we can reconnect substations 3 and 4, so the next state is $s_{0123}=(x_g,3,\varnothing)$, thus $n_{012}=\sum_{v\in\{3,4\}}=256+168=424$ and we have that

$$Q(s_{012}, 3) = d_{2,3} \cdot n_{012} = 359 \cdot 424 = 152216 \tag{1.3}$$

if a=4, we can reconnect only substation 4, so the next state is $s_{0124}=(x_g,4,\{3\})$, thus $n_{012}=\sum_{v\in\{3,4\}}u_v=256+168=424$ and we have that

$$egin{align} Q_{\pi}(s_{012},4) &= d_{2,4} \cdot n_{012} + \sum_{a' \in \{3\}} 1 \cdot Q\Big(s_{0124},a'\Big) \ &= 568 \cdot 424 + Q(s_{0124},3) \ Q_{\pi}(s_{012},4) - Q(s_{0124},3) = 240832 \ \end{align}$$

• then a=3 and we reconnect all the substations, so the next state is $s_{01243}=(x_g,3,\varnothing)$, thus $n_{0124}=\sum_{v\in\{3\}}u_v=256$ and we have that

$$Q(s_{0124}, 3) = d_{4.3} \cdot n_{0124} = 614 \cdot 256 = 157184 \tag{1.5}$$

 \circ if a=3, we can reconnect substations 3 and 4, so the next state is $s_{013}=(x_g,3,\{2\})$, thus $n_{01}=\sum_{v\in\{2,3,4\}}u_v=45+256+168=469$ and we have that

$$egin{aligned} Q_{\pi}(s_{01},3) &= d_{1,3} \cdot n_{01} + \sum_{a' \in \{2\}} 1 \cdot Q\Big(s_{013},a'\Big) \ &= 426 \cdot 469 + Q(s_{013},2) \ Q_{\pi}(s_{01},3) - Q(s_{013},2) = 199794 \end{aligned}$$

• then a=2 and we reconnect all the substations, so the next state is $s_{0132}=(x_q,2,\varnothing)$, thus $n_{013}=\sum_{v\in\{2\}}u_v=45$ and we have that

$$Q(s_{013}, 2) = d_{3,2} \cdot n_{013} = 359 \cdot 45 = 16155 \tag{1.7}$$

 \circ if a=4, we can reconnect only substation 4, so the next state is $s_{014}=(x_g,4,\{2,3\})$, and since $n_{01}=469$ and we have that

$$Q_{\pi}(s_{01}, 4) = d_{1,4} \cdot n_{01} + \sum_{a' \in \{2,3\}} \frac{1}{2} \cdot Q(s_{014}, a')$$

$$= 212 \cdot 469 + \frac{1}{2}Q(s_{014}, 2) + \frac{1}{2}Q(s_{014}, 3)$$

$$Q_{\pi}(s_{01}, 4) - \frac{1}{2}Q(s_{014}, 2) - \frac{1}{2}Q(s_{014}, 3) = 99428$$

$$(1.8)$$

From here we have these possible actions:

• if a=2, we can reconnect only substation 2, so the next state is $s_{0142}=(x_g,2,\{3\})$, thus $n_{014}=\sum_{v\in\{2,3\}}u_v=45+256=301$ and we have that

$$egin{aligned} Q_{\pi}(s_{014},2) &= d_{4,2} \cdot n_{014} + \sum_{a' \in \{3\}} 1 \cdot Q\Big(s_{0142},a'\Big) \ &= 568 \cdot 301 + Q(s_{0142},3) \end{aligned}$$

$$Q_{\pi}(s_{014}, 2) - Q(s_{0142}, 3) = 170968 \tag{1.9}$$

lacktriangledown then a=3 and we reconnect all the substations, so the next state is $s_{01423}=(x_g,3,arnothing)$, thus $n_{0142}=u_3=256$ and we have that

$$Q(s_{0142}, 3) = d_{2,3} \cdot n_{0142} = 359 \cdot 256 = 91904 \tag{1.10}$$

ullet if a=3, we can reconnect only substation 3, so the next state is $s_{0143}=(x_g,3,\{2\})$, thus $n_{014}=\sum_{v\in\{2,3\}}u_v=45+256=301$ and we have that

$$egin{aligned} Q_{\pi}(s_{014},3) &= d_{4,3} \cdot n_{014} + \sum_{a' \in \{2\}} 1 \cdot Q\Big(s_{0143},a'\Big) \ &= 614 \cdot 301 + Q(s_{0143},2) \ Q_{\pi}(s_{014},3) - Q(s_{0143},2) &= 184814 \end{aligned}$$

• then a=2 and we reconnect all the substations, so the next state is $s_{01432}=(x_q,2,\varnothing)$, thus $n_{0143}=u_2=45$ and we have that

$$Q(s_{0143}, 2) = d_{3.2} \cdot n_{0143} = 359 \cdot 45 = 16155 \tag{1.12}$$

• if a=2, we can reconnect substations 1 and 2, so the next state is $s_{02}=(x_g,2,\{3,4\})$, thus $n_0=\sum_{v\in\mathcal{C}}u_v=\sum_{v\in\{1,2,3,4\}}u_v=102+45+256+168=571$ and we have that

$$Q_{\pi}(s_{0}, 2) = d_{0,2} \cdot n_{0} + \sum_{a' \in \{3,4\}} \frac{1}{2} Q(s_{02}, a')$$

$$= 514 \cdot 571 + \frac{1}{2} Q(s_{02}, 3) + \frac{1}{2} Q(s_{02}, 4)$$

$$Q_{\pi}(s_{0}, 2) - \frac{1}{2} Q(s_{02}, 3) - \frac{1}{2} Q(s_{02}, 4) = 293494$$

$$(1.13)$$

From here we have these possible actions:

o if a=3, we can reconnect substations 3 and 4, so the next state is $s_{023}=(x_g,3,\varnothing)$, thus $n_{02}=n_{012}=\sum_{v\in\{3,4\}}u_v=256+168=424$ and we have that

$$Q(s_{02}, 3) = d_{2.3} \cdot n_{23} = 359 \cdot 424 = 152216 \tag{1.14}$$

 \circ if a=4, we can reconnect only substation 4, so the next state is $s_{024}=(x_g,4,\{3\})$, thus $n_{02}=\sum_{v\in\{3,4\}}u_v=256+168=424$ and we have that

$$egin{align} Q_{\pi}(s_{02},4) &= d_{2,4} \cdot n_2 + \sum_{a' \in \{3\}} 1 \cdot Q\Big(s_{024},a'\Big) \ &= 568 \cdot 424 + Q(s_{024},3) \ Q_{\pi}(s_{02},4) - Q(s_{024},3) = 240832 \end{align}$$

• then a=3 and we reconnect all the substations, so the next state is $s_{0243}=(x_q,3,\varnothing)$, thus $n_{024}=u_3=256$ and we have that

$$Q(s_{024},3) = d_{4,3} \cdot n_{024} = 614 \cdot 256 = 157184 \tag{1.16}$$

• if a=3, we can reconnect substations 3 and 4, so the next state is $s_{03}=(x_g,3,\{1,2\})$, thus $n_0=\sum_{v\in\mathcal{C}}u_v=\sum_{v\in\{1,2,3,4\}}u_v=102+45+256+168=571$ and we have that

$$Q_{\pi}(s_0,3) = d_{0,3} \cdot n_0 + \sum_{a' \in \{1,2\}} rac{1}{2} Q\Big(s_{03},a'\Big)$$

$$=421 \cdot 571 + \frac{1}{2}Q(s_{03}, 1) + \frac{1}{2}Q(s_{03}, 2)$$

$$Q_{\pi}(s_0, 3) - \frac{1}{2}Q(s_{03}, 1) - \frac{1}{2}Q(s_{03}, 2) = 240391$$
(1.17)

From here we have these possible actions:

o if a=1, we can reconnect only substation 1, so the next state is $s_{031}=(x_g,1,\{2\})$, thus $n_{03}=\sum_{v\in\{1,2\}}u_v=102+45=147$ and we have that

$$egin{align} Q_{\pi}(s_{03},1) &= d_{3,1} \cdot n_{31} + \sum_{a' \in \{2\}} 1 \cdot Q\Big(s_{031},a'\Big) \ &= 426 \cdot 147 + Q(s_{031},2) \ Q_{\pi}(s_{03},1) - Q_{\pi}(s_{031},2) = 62622 \end{align}$$

lacktriangledown then a=2 and we reconnect all the substations, so the next state is $s_{0312}=(x_g,2,arnothing)$, thus $n_{031}=u_2=45$ and we have that

$$Q(s_{031}, 2) = d_{1,2} \cdot n_{132} = 633 \cdot 45 = 28485 \tag{1.19}$$

 \circ if a=2, we can reconnect substations 1 and 2, so the next state is $s_{032}=(x_g,2,\varnothing)$, thus $n_{03}=\sum_{v\in\{1,2\}}u_v=102+45=147$ and we have that

$$Q(s_{03}, 2) = d_{3.2} \cdot n_{32} = 359 \cdot 147 = 52773 \tag{1.20}$$

• if a=4, we can reconnect only substation 4, so the next state is $s_{04}=(x_g,4,\{1,2,3\})$, thus $n_0=\sum_{v\in\mathcal{C}}u_v=\sum_{v\in\{1,2,3,4\}}u_v=102+45+256+168=571$ and we have that

$$Q_{\pi}(s_{0}, 4) = d_{0,4} \cdot n_{0} + \sum_{a' \in \{1, 2, 3\}} \frac{1}{3} Q(s_{04}, a')$$

$$= 346 \cdot 571 + \frac{1}{3} Q(s_{04}, 1) + \frac{1}{3} Q(s_{04}, 2) + \frac{1}{3} Q(s_{04}, 3)$$

$$Q_{\pi}(s_{0}, 4) - \frac{1}{3} Q(s_{04}, 1) - \frac{1}{3} Q(s_{04}, 2) - \frac{1}{3} Q(s_{04}, 3) = 197566 \qquad (1.21)$$

From here we have these possible actions:

o if a=1, we can reconnect only substation 1, so the next state is $s_{041}=(x_g,1,\{2,3\})$, thus $n_{04}=\sum_{v\in\{1,2,3\}}u_v=102+45+256=403$ and we have that

$$Q_{\pi}(s_{04}, 1) = d_{4,1} \cdot n_{41} + \sum_{a' \in \{2,3\}} \frac{1}{2} Q(s_{041}, a')$$

$$= 212 \cdot 403 + \frac{1}{2} Q(s_{041}, 2) + \frac{1}{2} Q(s_{041}, 3)$$

$$Q_{\pi}(s_{04}, 1) - \frac{1}{2} Q(s_{041}, 2) - \frac{1}{2} Q(s_{041}, 3) = 85436$$

$$(1.22)$$

From here we have these possible actions:

if a=2, we can reconnect only substation 2, so the next state is $s_{0412}=(x_g,2,\{3\})$, thus $n_{041}=\sum_{v\in\{2,3\}}u_v=45+256=301$ and we have that

$$egin{aligned} Q_{\pi}(s_{041},2) &= d_{1,2} \cdot n_{412} + \sum_{a' \in \{3\}} 1 \cdot Q\Big(s_{0412},a'\Big) \ &= 633 \cdot 301 + Q(s_{0412},3) \ Q_{\pi}(s_{041},2) - Q(s_{0412},3) = 162048 \end{aligned}$$

• then a=3 and we reconnect all the substations, so the next state is $s_{04123}=(x_q,3,\varnothing)$, thus $n_{0412}=u_3=256$ and we have that

$$Q(s_{0412}, 3) = d_{2.3} \cdot n_{0412} = 359 \cdot 256 = 91904 \tag{1.24}$$

lacksquare if a=3, we can reconnect only substation 3, so the next state is $s_{0413}=(x_g,3,\{2\})$, thus $n_{041}=\sum_{v\in\{2,3\}}u_v=45+256=301$ and we have that

$$egin{aligned} Q_{\pi}(s_{041},3) &= d_{1,3} \cdot n_{413} + \sum_{a' \in \{2\}} 1 \cdot Q\Big(s_{0413},a'\Big) \ &= 426 \cdot 301 + Q(s_{0413},2) \ Q_{\pi}(s_{041},3) - Q(s_{0413},2) = 128226 \end{aligned}$$

 $lack then \ a=2$ and we reconnect all the substations, so the next state is $s_{04132}=(x_g,2,arnothing)$, thus $n_{0413}=u_2=45$ and we have that

$$Q(s_{0413}, 2) = d_{3,2} \cdot n_{4132} = 359 \cdot 45 = 16155 \tag{1.26}$$

 \circ if a=2, we can reconnect substations 1 and 2, so the next state is $s_{042}=(x_g,2,\{3\})$, thus $n_{04}=\sum_{v\in\{1,2,3\}}u_v=102+45+256=403$ and we have that

$$Q_{\pi}(s_{04}, 2) = d_{4,2} \cdot n_{04} + \sum_{a' \in \{3\}} 1 \cdot Q(s_{042}, a')$$

$$= 568 \cdot 403 + Q(s_{042}, 3)$$

$$Q_{\pi}(s_{04}, 2) - Q(s_{042}, 3) = 228904 \tag{1.27}$$

• then a=3 and we reconnect all the substations, so the next state is $s_{0423}=(x_g,3,\varnothing)$, thus $n_{042}=u_3=256$ and we have that

$$Q(s_{042}, 3) = d_{2.3} \cdot n_{042} = 359 \cdot 256 = 91904 \tag{1.28}$$

 \circ if a=3, we can reconnect only substation 3, so the next state is $s_{043}=(x_g,3,\{1,2\})$, thus $n_{04}=\sum_{v\in\{1,2,3\}}u_v=102+45+256=403$ and we have that

$$Q_{\pi}(s_{04},3) = d_{4,3} \cdot n_{04} + \sum_{a' \in \{1,2\}} \frac{1}{2} Q(s_{043}, a')$$

$$= 614 \cdot 403 + \frac{1}{2} Q(s_{043}, 1) + \frac{1}{2} Q(s_{043}, 2)$$

$$Q_{\pi}(s_{04}, 3) - \frac{1}{2} Q(s_{043}, 1) - \frac{1}{2} Q(s_{043}, 2) = 247442$$

$$(1.29)$$

From here we have these possible actions:

• if a=1, we can reconnect only substation 1, so the next state is $s_{0431}=(x_g,1,\{2\})$, thus $n_{043}=\sum_{v\in\{1,2\}}u_v=102+45=147$ and we have that

$$Q_{\pi}(s_{043}, 1) = d_{3,1} \cdot n_{043} + \sum_{a' \in \{2\}} 1 \cdot Q\Big(s_{0431}, a'\Big)$$

$$= 426 \cdot 147 + Q(s_{0431}, 2)$$

$$Q_{\pi}(s_{043}, 1) - Q(s_{0431}, 2) = 62622 \tag{1.30}$$

 $lack \$ then a=2 and we reconnect all the substations, so the next state is $s_{04312}=(x_g,2,arnothing)$, thus $n_{0431}=u_2=45$ and we have that

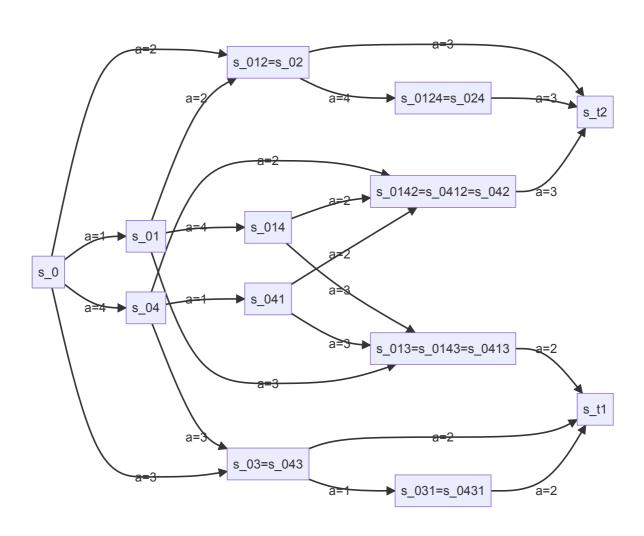
$$Q(s_{0431}, 2) = d_{1,2} \cdot n_{0431} = 633 \cdot 45 = 28485 \tag{1.31}$$

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lack if a=2, we can reconnect substations 1 and 2, so the next state is $s_{0432}=(x_g,2,\varnothing)$, thus $n_{043}=\sum_{v\in\{1,2\}}u_v=102+45=147$ and we have that

$$Q(s_{043}, 2) = d_{3,2} \cdot n_{043} = 359 \cdot 147 = 52773 \tag{1.32}$$

States schema



There are 33 states, instead of the 64 we estimated. The terminal states are $s=(x_g,v_k,\varnothing)$, but we have that v_k must be one of the two substations near the fault, or the substation in which we have the fault. So there are at most two terminal states. In this example, they are $s_{t_1}=(x_g,2,\varnothing)$ and $s_{t_2}=(x_g,3,\varnothing)$. Besides, there are some states that are equal, so they are actually less than 33.

Q-table

$$egin{aligned} s_{0143} &= s_{013} \Rightarrow Q(s_{0143},2) = Q(s_{0143},2) \Rightarrow (1.12) = (1.7). \ s_{02} &= s_{012} \Rightarrow Q(_{02},3) = Q(_{012},3) \Rightarrow (1.14) = (1.3), Q(_{02},4) = Q(_{012},4) \Rightarrow (1.15) = (1.4) \ . \ . \ s_{024} &= s_{0124} \Rightarrow Q(s_{024},3) = Q(s_{0124},3) \Rightarrow (1.16) = (1.5). \end{aligned}$$

	a = 1	a = 2	a = 3	a = 4
$s_0 = (x_g, 0, \{1, 2, 3, 4\})$	$Q(s_0, 1) = 478819, 167 (1.1)$	$Q(s_0,2) = 568610$ (1.13)	$Q(s_0,3) = 312331 (1.17)$	$Q(s_0, 4) = 505830, 167 (1.21)$
$s_{01}=(x_g,1,\{2,3,4\})$		$Q_{\pi}(s_{01},2) = 524291 (1.2)$	$Q(s_{01},3) = 215949(1.6)$	$Q(s_{01},4) = 331348.5 (1.8)$
$s_{012}=(x_g,2,\{3,4\})=s_{02}$			$Q(s_{012},3) = 152216(1.3)(1.14)$	$Q(s_{012},4) = 398016 (1.4)(1.15)$
$s_{0124}=(x_g,4,\{3\})=s_{024}$			$Q(s_{0124},3) = 157184(1.5)(1.16)$	
$s_{013} = (x_g, 3, \{2\}) = s_{0143} = s_{0413}$		$Q(s_{013},2) = 16155 (1.7)(1.12)$		
$s_{014}=(x_g,4,\{2,3\})$		$Q(s_{014},2) = 262872 (1.9)$	$Q(s_{014},3) = 200969 (1.11)$	
$s_{0142} = (x_g, 2, \{3\}) = s_{0412} = s_{042}$			$Q(s_{0142},3) = 91904 (1.10)(1.24)$	
$s_{03}=(x_g,3,\{1,2\})=s_{043}$	$Q_{\pi}(s_{03},1) = 91107(1.18)$	$Q(s_{03},2) = 52773 (1.20)$		
$s_{031}=(x_g,1,\{2\})=s_{0431}$		$Q(s_{031},2) = 28485(1.19)$		
$s_{04}=(x_g,4,\{1,2,3\})$	$Q_{\pi}(s_{04},1) = 284602, 5 ext{(1.22)}$	$Q_{\pi}(s_{04},2) = 320808 ext{(1.27)}$	$Q_{\pi}(s_{04},3)=319382(1.29)$	
$s_{041}=(x_g,1,\{2,3\})$		$Q_{\pi}(s_{041},2) = 253952(1.23)$	$Q_{\pi}(s_{041},3) = 144381(1.25)$	
$s_{t_1} = (x_g, 2, \varnothing)$				
$s_{t_2} = (x_g, 3, \varnothing)$				

Computation of η

The function $\rho_0(s')$ is the probability of starting in the initial state s'. Since we don't have any prior information of where the fault might be, ρ_0 doesn't depend on it, so ρ_0 will be uniform in x_g (this means that we divide by the number of possible positions of x_g , which is either a substation or an edge, so it is N+(N+1)=2N+1). Instead, the first substation in which to go is the "fake" substation 0 and the set of disconnected substations must be equal to the set of all the substations $\mathcal C$. So ρ_0 must be 1 when $v_k=0$ and the set of the disconnected substations is equal to $\mathcal C$ and must be 0 for every other state. So we have that

$$ho_0\Big(s=(x_g,v_k,\{v\})\Big)=rac{1}{2|\mathcal{C}|+1}\mathbb{I}ig(v_k=0,\{v\}=\mathcal{C}ig)=rac{1}{2N+1}\mathbb{I}ig(\{v\}=\mathcal{C}ig)$$

We have that the initial state is $s_0=(x_g,0,\{1,2,3,4\})$. So

$$\eta_{\pi}(s_0) = rac{1}{2N+1}\mathbb{I}ig(v_k = 0, \{1, 2, 3, 4\} = \mathcal{C}ig) + 0 = rac{1}{2\cdot 4 + 1}\cdot 1 = rac{1}{9}$$

Then we have that:

$$\eta_{\pi}(s_{01}) = 0 + \frac{1}{|\{1, 2, 3, 4\}|} \eta_{\pi}(s_{0}) = \frac{1}{4} \cdot \frac{1}{9} = \frac{1}{36}$$
(2.2)

$$\eta_{\pi}(s_{012} = s_{02}) = 0 + \frac{1}{4}\eta_{\pi}(s_0) + \frac{1}{3}\eta_{\pi}(s_{01}) = \frac{1}{4} \cdot \frac{1}{9} + \frac{1}{3} \cdot \frac{1}{36} = \frac{1}{27}$$
(2.3)

$$\eta_{\pi}(s_{0124} = s_{024}) = 0 + \frac{1}{2}\eta_{\pi}(s_{012} = s_{02}) = \frac{1}{2} \cdot \frac{1}{27} = \frac{1}{54}$$
(2.4)

$$\eta_{\pi}(s_{014}) = 0 + \frac{1}{3}\eta_{\pi}(s_{01}) = \frac{1}{3} \cdot \frac{1}{36} = \frac{1}{108}$$
(2.5)

$$\eta_{\pi}(s_{04}) = 0 + \frac{1}{4}\eta_{\pi}(s_0) = \frac{1}{4} \cdot \frac{1}{9} = \frac{1}{36}$$
(2.6)

$$\eta_{\pi}(s_{041}) = 0 + \frac{1}{3}\eta_{\pi}(s_{04}) = \frac{1}{3} \cdot \frac{1}{36} = \frac{1}{108}$$
(2.7)

$$\eta_{\pi}(s_{013} = s_{0143} = s_{0413}) = 0 + \frac{1}{2}\eta_{\pi}(s_{014}) + \frac{1}{2}\eta_{\pi}(s_{041}) + \frac{1}{3}\eta_{\pi}(s_{01})
= \frac{1}{2} \cdot \frac{1}{108} + \frac{1}{2} \cdot \frac{1}{108} + \frac{1}{3} \cdot \frac{1}{36}
= \left(\frac{1}{2} + \frac{1}{2} + 1\right) \frac{1}{108} = \frac{1}{54}$$
(2.8)

$$\eta_{\pi}(s_{0142}=s_{0412}=s_{042})=0+rac{1}{2}\eta_{\pi}(s_{014})+rac{1}{3}\eta_{\pi}(s_{04})+rac{1}{2}\eta_{\pi}(s_{041}) \ 1 \ 1 \ 1 \ 1 \ 1$$

$$= \frac{1}{2} \cdot \frac{1}{108} + \frac{1}{3} \cdot \frac{1}{36} + \frac{1}{2} \cdot \frac{1}{108}$$

$$= \left(\frac{1}{2} + 1 + \frac{1}{2}\right) \frac{1}{108} = \frac{1}{54}$$
(2.9)

$$\eta_{\pi}(s_{03} = s_{043}) = 0 + \frac{1}{4}\eta_{\pi}(s_0) + \frac{1}{3}\eta_{\pi}(s_{04}) = \frac{1}{4} \cdot \frac{1}{9} + \frac{1}{3} \cdot \frac{1}{36} = \frac{1}{27}$$
(2.10)

$$\eta_{\pi}(s_{031} = s_{0431}) = 0 + \frac{1}{2}\eta_{\pi}(s_{03} = s_{043}) = \frac{1}{2} \cdot \frac{1}{27} = \frac{1}{54}$$
(2.11)

$$\eta_{\pi}(s_{t_1}) = 0 + 1 \cdot \eta_{\pi}(s_{013} = s_{0143} = s_{0413}) + \frac{1}{2}\eta_{\pi}(s_{03} = s_{043}) + 1 \cdot \eta_{\pi}(s_{031} = s_{0431})
= \frac{1}{54} + \frac{1}{2} \cdot \frac{1}{27} + \frac{1}{54} = \frac{3}{54} = \frac{1}{18}$$
(2.12)

$$\eta_{\pi}(s_{t_2}) = 0 + \frac{1}{2}\eta_{\pi}(s_{012} = s_{02}) + 1 \cdot \eta_{\pi}(s_{0124} = s_{024}) + 1 \cdot \eta_{\pi}(s_{0142} = s_{0412} = s_{042})
= \frac{1}{2} \cdot \frac{1}{27} + \frac{1}{54} + \frac{1}{54} = \frac{3}{54} = \frac{1}{18}$$
(2.13)

Compute the gradient

$$abla_{ heta}J = \sum_{s,a} \eta_{\pi}(s) Q_{\pi}(s,a)
abla_{ heta}\pi(a|s) \,.$$