# INFO20003 Database Systems

Week 5

# Relational Algebra

 a collection of operators, which take instance(s) of a relation as operand(s), and returns a relation instance as an output

An operator can be either unary or binary

# Fundamental Operations

## 5 basic operators for Relational Algebra:

- Selection  $(\sigma)$
- Projection  $(\pi)$
- Set-difference (-)
- Union (∪)
- Cross Product (x)

# Removal Operators

• Projection: removes columns

• Selection: removes rows

# Projection

$$\pi_{A1, A2, ..., An}(R)$$

- R: input relation
- A1, A2, ..., An: attributes that are projected

Output: create a new relation with the projected attributes

# Projection

LastName	]	Phone	Email
Snow	(	551-999-210	knowsnothing@hotmail.com
Targaryen	(	569-988-112	bendtheknee@gmail.com
Lannister	(	)531-987-654	handsfree@gmail.com
King	(	)566-123-456	killerstare@gmail.com
	Snow Targaryen Lannister	Snow (Targaryen (Lannister (	Snow         0551-999-210           Targaryen         0569-988-112           Lannister         0531-987-654

The expression  $\pi_{\text{FirstName, LastName}}$  (Person) will result in:

FirstName	LastName
Jon	Snow
Daenerys	Targaryen
Jamie	Lannister
Night	King

## Selection

## $\sigma_C(\mathbf{R})$

- R: input relation
- C: condition used to filter rows

 Output: creates a new relation consisting of the rows for which C is true

# Selection

FirstName	LastName	Phone	Email
Jon	Snow	0551-999-210	knowsnothing@hotmail.com
Daenerys	Targaryen	0569-988-112	bendtheknee@gmail.com
Jamie	Lannister	0531-987-654	handsfree@gmail.com
Night	King	0566-123-456	killerstare@gmail.com

$$\sigma$$
FirstName = 'Jon'  $\vee$  LastName = 'King' (Person)

FirstName	LastName	Phone	Email
Jon	Snow	0551-999-210	knowsnothing@hotmail.com
Night	King	0566-123-456	killerstare@gmail.com

# Combine expressions

 $\pi$ FirstName, LastName ( $\sigma$ FirstName = 'Jon'  $\vee$  LastName = 'King' (Person))

FirstName	LastName
Jon	Snow
Night	King

# Set Operators

- Set-difference
- Union

 Input relations R and S must have the same attributes with the same domains, in the same order

## Set-Difference

## R - S

• R & S: 2 relations with the same attributes

 Output: every row which is in R but not in S

#### RandomCombo1

FirstName	LastName
Jon	Snow
Daenerys	Targaryen
Jamie	Lannister
Night	King

#### RandomCombo2

FirstName	LastName
Night	King
Arya	Stark
Cersei	Lannister
Daenerys	Targaryen

#### RandomCombo1 – RandomCombo2 will result in:

FirstName	LastName
Jon	Snow
Jamie	Lannister

## Union

## $\mathbf{R} \cup \mathbf{S}$

• R&S: 2 relations with the same attributes

 Output: every row which is in either R or S

#### GoodGuys

FirstName	LastName
Jon	Snow
Daenerys	Targaryen

#### BadGuys

FirstName	LastName
Cersei	Lannister
Night	King

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#### GoodGuys ∪ BadGuys will result in:

FirstName	LastName
Jon	Snow
Daenerys	Targaryen
Cersei	Lannister
Night	King

## Cross Product

#### $R \times S$

- Each row of R pairs with each row of S
- The resulting schema has all the attributes from both relations
- If some attributes have **same name**, **rename** them by using renaming operator

## Cross Product

#### Person

# FirstNameLastNameEmailJonSnowknowsnothing@hotmail.comNightKingkillerstare@gmail.com

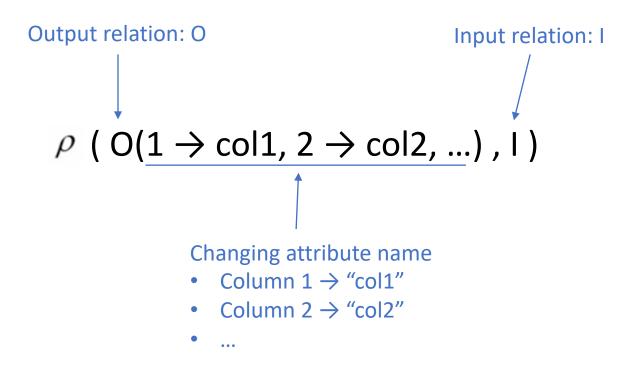
#### Weapon

Weapon	Metal
Sword	Valyrian steel
Dagger	Dragon glass

#### Person × Weapon will result in:

FirstName	LastName	Email	Weapon	Metal
Jon	Snow	knowsnothing@hotmail.com	Sword	Valyrian steel
Jon	Snow	knowsnothing@hotmail.com	Dagger	Dragon glass
Night	King	killerstare@gmail.com	Sword	Valyrian steel
Night	King	killerstare@gmail.com	Dagger	Dragon glass

## Rename



## Rename example

$$\rho(S1(1 \rightarrow sid1, 2 \rightarrow sname1, 3 \rightarrow rating1, 4 \rightarrow age1), Sailors)$$

# Compound Operations

- Intersection
- Natural Join
- Condition join (Theta/Inner join)

## Intersection

$$R \cap S = R - (R - S)$$

 Output: a relation containing all the tuples which are present in both relations

RandomCombo1

FirstName	LastName
Jon	Snow
Daenerys	Targaryen
Jamie	Lannister
Night	King

RandomCombo2

FirstName	LastName
Night	King
Arya	Stark
Cersei	Lannister
Daenerys	Targaryen

RandomCombo1 \cap RandomCombo2 will result in:

FirstName	LastName
Daenerys	Targaryen
Night	King

# Compound Operations

- Intersection
- Natural Join
- Condition join (Theta/Inner join)

## Natural Join

# $R \bowtie S$

 Create a new relation, pairing each tuple from R and S where the common attributes are equal

A natural join can be broken down into following steps:

- $\diamond$  Compute  $R \times S$
- Select rows where attributes that appear in both relations have equal values.
- Project all unique attributes and one copy of each of the common ones.

# Natural Join example

Person				
FirstName	LastName	Email		
Jon	Snow	knowsnothing@hotmail.com		
Daenerys	Targaryen	bendtheknee@gmail.com		
Tyrion	Lannister	idrinkandiknow@gmail.com		
Night	King	killerstare@gmail.com		

WeaponOwner					
Weapon	LastName	Metal			
Sword	Snow	Valyrian steel			
Dagger	Lannister	Dragon glass			

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Common attribute = LastName

# Natural Join example

#### **Person** $\times$ **Weapon** (intermediate result):

FirstName	LastName	Email	Weapon	LastName	Metal
Jon	Snow	knowsnothing@hotmail.com	Sword	Snow	Valyrian steel
Jon	Snow	knowsnothing@hotmail.com	Dagger	Lannister	Dragon glass
Daenerys	Targaryen	bendtheknee@gmail.com	Sword	Snow	Valyrian steel
Daenerys	Targaryen	bendtheknee@gmail.com	Dagger	Lannister	Dragon glass
Tyrion	Lannister	idrinkandiknow@gmail.com	Sword	Snow	Valyrian steel
Tyrion	Lannister	idrinkandiknow@gmail.com	Dagger	Lannister	Dragon glass
Night	King	killerstare@gmail.com	Sword	Snow	Valyrian steel
Night	King	killerstare@gmail.com	Dagger	Lannister	Dragon glass

# Natural Join example

#### **Person** ⋈ **Weapon** will result in:

FirstName	LastName	Email	Weapon	Metal
Jon	Snow	knowsnothing@hotmail.com	Sword	Valyrian steel
Tyrion	Lannister	idrinkandiknow@gmail.com	Dagger	Dragon glass

# Compound Operations

- Intersection
- Natural Join
- Condition join (Theta/Inner join)

# Conditional Join

## $R \bowtie_{\mathbb{C}} S$

 joins rows from relation R and S such that the Boolean condition C is true

•  $R \bowtie_C S = \sigma_C(R \times S)$ 

# Conditional Join example

Person				
FirstName	LastName	Email		
Jon	Snow	knowsnothing@hotmail.com		
Daenerys	Targaryen	bendtheknee@gmail.com		
Tyrion	Lannister	idrinkandiknow@gmail.com		
Night	King	killerstare@gmail.com		

WeaponOwner					
Weapon Name Metal					
Sword	Snow	Valyrian steel			
Dagger Lannister Dragon glass					

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Person ⋈<sub>LastName = Name</sub> Weapon Owner

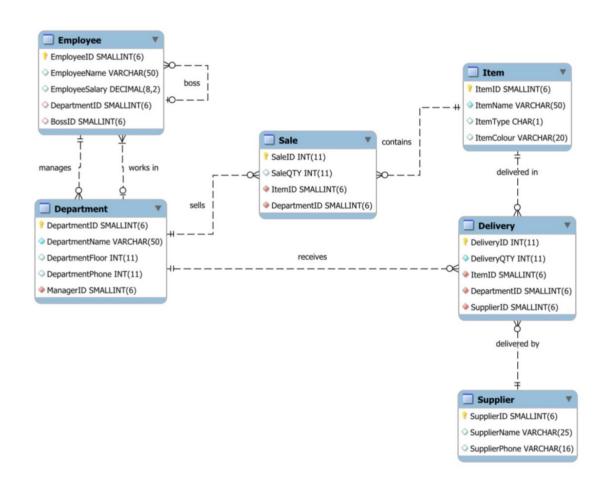
# Conditional Join example

#### **Person** $\times$ **Weapon** (intermediate result):

FirstName	LastName	Email	Weapon	Name	Metal
Jon	Snow	knowsnothing@hotmail.com	Sword	Snow	Valyrian steel
Jon	Snow	knowsnothing@hotmail.com	Dagger	Lannister	Dragon glass
Daenerys	Targaryen	bendtheknee@gmail.com	Sword	Snow	Valyrian steel
Daenerys	Targaryen	bendtheknee@gmail.com	Dagger	Lannister	Dragon glass
Tyrion	Lannister	idrinkandiknow@gmail.com	Sword	Snow	Valyrian steel
Tyrion	Lannister	idrinkandiknow@gmail.com	Dagger	Lannister	Dragon glass
Night	King	killerstare@gmail.com	Sword	Snow	Valyrian steel
Night	King	killerstare@gmail.com	Dagger	Lannister	Dragon glass

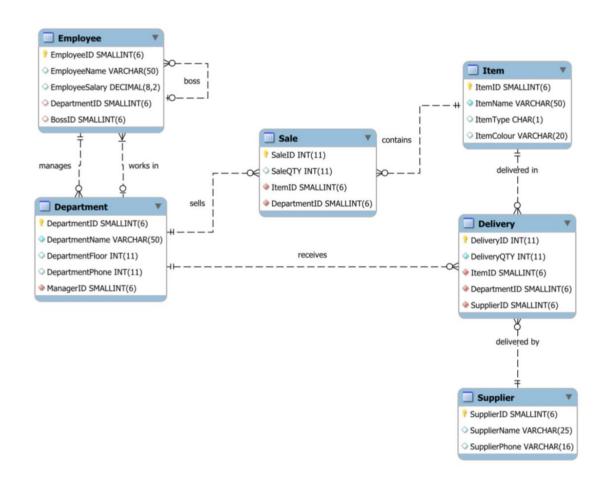
#### Person ⋈LastName = Name Weapon

FirstName	LastName	Email	Weapon	Name	Metal
Jon	Snow	knowsnothing@hotmail.com	Sword	Snow	Valyrian steel
Tyrion	Lannister	idrinkandiknow@gmail.com	Dagger	Lannister	Dragon glass



Solve the following problems using relational algebra (RA) and translate to SQL statements:

- a) Find the names of all employees.
- b) Find the names of all employees in department with id of 1.
- c) List the names of green items of type C.
- d) Find the items sold by the departments on the second floor (only show ItemID)
- e) Find the names of brown items sold by the Recreation department.
- f) Find the employees whose salary is less than half that of their boss



Solve the following problems using relational algebra (RA) and translate to SQL statements:

- a) Find the names of all employees.
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- f) Find the employees whose salary is less than half that of their boss

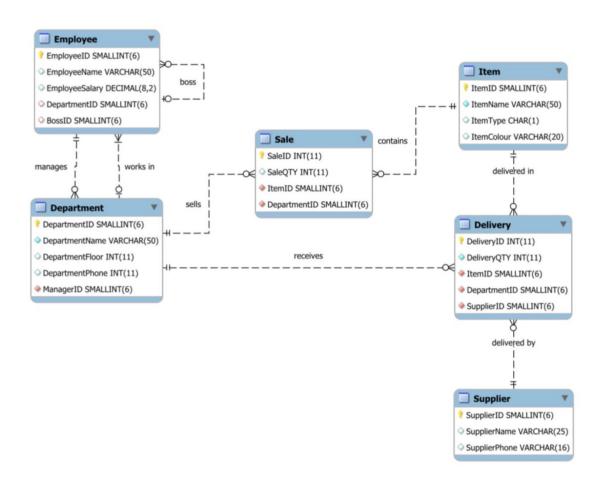
# Q2a)

a. Find the names of all employees.

Relational Algebra: π<sub>EmployeeName</sub> (Employee)

SQL: SELECT EmployeeName

FROM Employee;



Solve the following problems using relational algebra (RA) and translate to SQL statements:

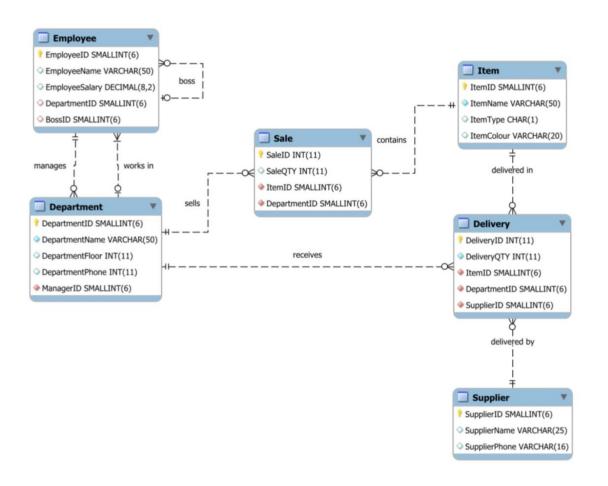
- a) Find the names of all employees.
- b) Find the names of all employees in department with id of 1.
- c) List the names of green items of type C.
- d) Find the items sold by the departments on the second floor (only show ItemID)
- e) Find the names of brown items sold by the Recreation department.
- f) Find the employees whose salary is less than half that of their boss

# Q2b)

b. Find the names of all employees in department number 1.

```
Relational Algebra: π<sub>EmployeeName</sub> (σ<sub>DepartmentID</sub> = 1 (Employee))

SQL: SELECT EmployeeName
FROM Employee
WHERE DepartmentID = 1;
```



Solve the following problems using relational algebra (RA) and translate to SQL statements:

- a) Find the names of all employees.
- b) Find the names of all employees in department with id of 1.
- c) List the names of green items of type C.
- d) Find the items sold by the departments on the second floor (only show ItemID)
- e) Find the names of brown items sold by the Recreation department.
- f) Find the employees whose salary is less than half that of their boss

# Q2c)

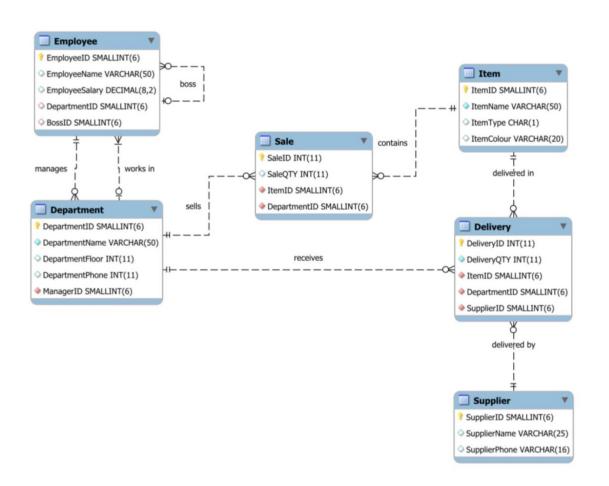
c. List the names of green items of type C.

```
Relational Algebra: \pi_{\text{ItemName}}(\sigma_{\text{ItemColour} = 'Green' \land \text{ItemType} = 'C'}(\text{Item}))

SQL: SELECT ItemName

FROM Item

WHERE ItemType = 'C' AND ItemColour = 'Green';
```



Solve the following problems using relational algebra (RA) and translate to SQL statements:

- a) Find the names of all employees.
- b) Find the names of all employees in department with id of 1.
- c) List the names of green items of type C.
- d) Find the items sold by the departments on the second floor (only show ItemID)
- e) Find the names of brown items sold by the Recreation department.
- f) Find the employees whose salary is less than half that of their boss

# Q2d)

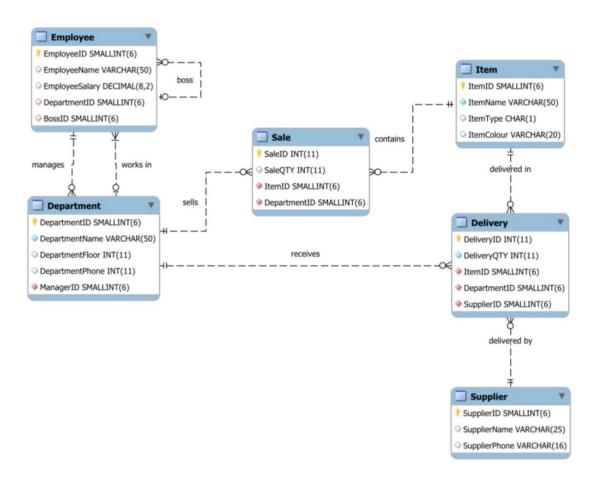
d. Find the items sold by the departments on the second floor (only show ItemID).

**Relational Algebra:**  $\pi_{\text{ItemID}}(\sigma_{\text{DepartmentFloor}=2}(\text{Sale} \bowtie \text{Department}))$ 

**SQL: SELECT DISTINCT** ItemID

FROM Sale NATURAL JOIN Department

WHERE DepartmentFloor = 2;



Solve the following problems using relational algebra (RA) and translate to SQL statements:

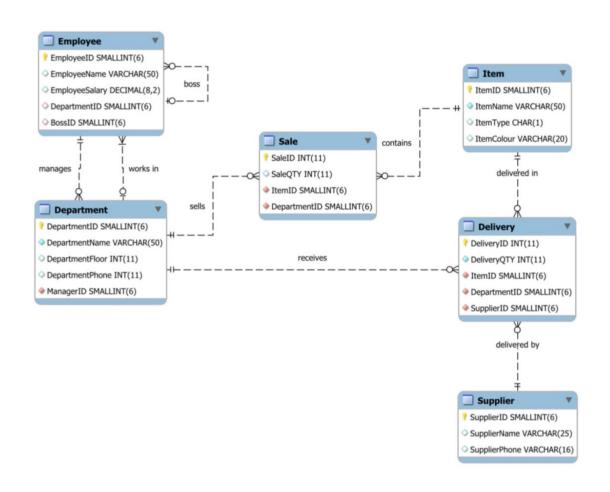
- a) Find the names of all employees.
- b) Find the names of all employees in department with id of 1.
- c) List the names of green items of type C.
- d) Find the items sold by the departments on the second floor (only show ItemID)
- e) Find the names of brown items sold by the Recreation department.
- f) Find the employees whose salary is less than half that of their boss

# Q2e)

e. Find the names of brown items sold by the Recreation department.

```
Relational Algebra: π<sub>ItemName</sub> (σ<sub>DepartmentName = 'Recreation' ∧ ItemColour = 'Brown'</sub> (Item ⋈ Sale ⋈ Department))

SQL: SELECT ItemName
FROM Item NATURAL JOIN Sale NATURAL JOIN Department
WHERE DepartmentName = 'Recreation'
AND ItemColour = 'Brown';
```



Solve the following problems using relational algebra (RA) and translate to SQL statements:

- a) Find the names of all employees.
- b) Find the names of all employees in department with id of 1.
- c) List the names of green items of type C.
- d) Find the items sold by the departments on the second floor (only show ItemID)
- e) Find the names of brown items sold by the Recreation department.
- f) Find the employees whose salary is less than half that of their boss

# Q2f)

f. Find the employees whose salary is less than half that of their managers.

Below are two examples using the rename  $(\rho)$  operator:

```
\rho(\text{Emp(EmployeeName} \rightarrow \text{EmpName}, \text{EmployeeSalary} \rightarrow \\ \text{EmpSalary}, \text{BossID} \rightarrow \text{EmpBossID}), \text{Employee}) \\ \rho(\text{Boss(EmployeeID} \rightarrow \text{BossEmployeeID}, \\ \text{EmployeeSalary} \rightarrow \text{BossSalary}), \text{Employee}) \\ \pi_{\text{EmpName}}(\sigma_{\text{EmpSalary}} < (\text{BossSalary}/2)) \text{(Emp } \bowtie_{\text{EmpBossID}} = \text{BossEmployeeID}) \\ \text{Boss)}) \\ \rho(\text{Boss(BossID} \rightarrow \text{BossBossId}, \\ \text{EmployeeID} \rightarrow \text{BossID}, \text{EmployeeSalary} \rightarrow \\ \text{BossSalary}, \text{DepartmentID} \rightarrow \text{BossDepID}, \\ \text{EmployeeName} \rightarrow \text{BossName}), \text{Employee}) \\ \pi_{\text{EmployeeName}}(\sigma_{\text{EmployeeSalary}} < (\text{BossSalary}/2)) \text{(Employee } \bowtie_{\text{Boss}}))
```

Or you could use an SQL-like notation:

Emp := Employee

Boss := Employee  $\pi_{\text{Emp.EmployeeName}}(\sigma_{\text{Emp.EmployeeSalary}} < (Boss.EmployeeSalary/2) (Emp <math>\bowtie_{\text{Emp.BossID} = Boss.EmployeeID} Boss))$ 

# Q2f)

```
SQL: SELECT Emp.EmployeeName
    FROM Employee AS Emp
    INNER JOIN Employee AS Boss
    ON Emp.BossID = Boss.EmployeeID
    WHERE Emp.EmployeeSalary < (Boss.EmployeeSalary / 2);</pre>
```